

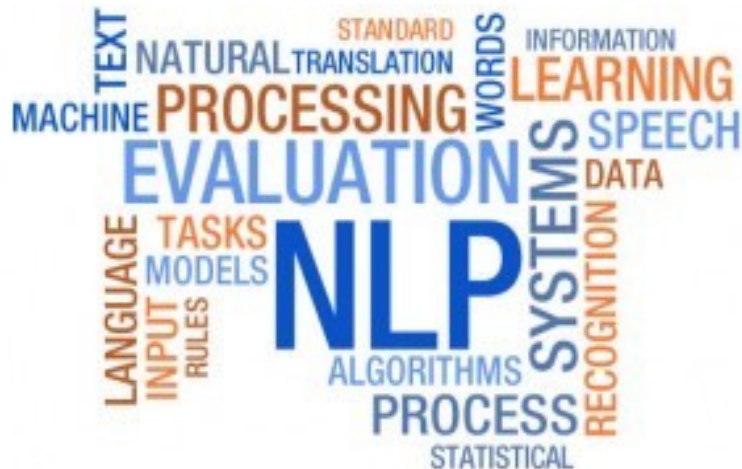
Deep learning

lecture 5, fall 22

NLP basics, Recurrent neural networks

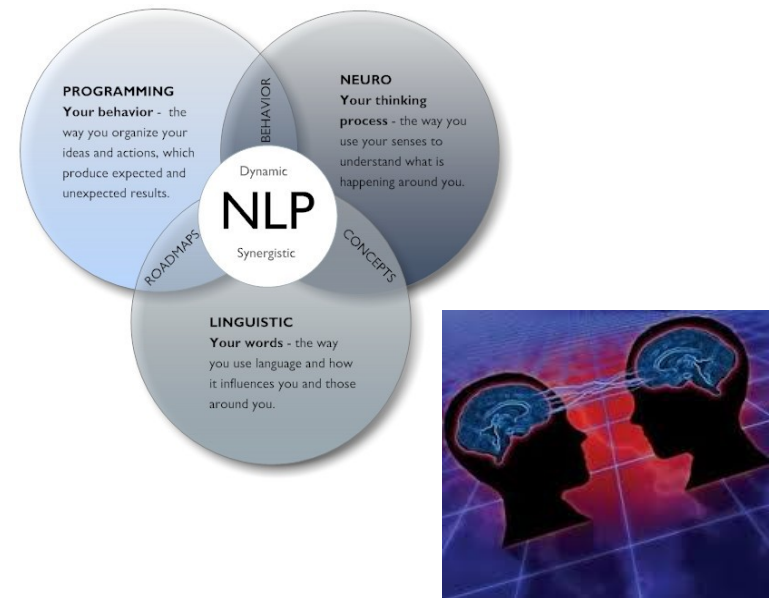


What is NLP?



NLP

Light side of the force



NLP

Dark side of the force₂

Text 101

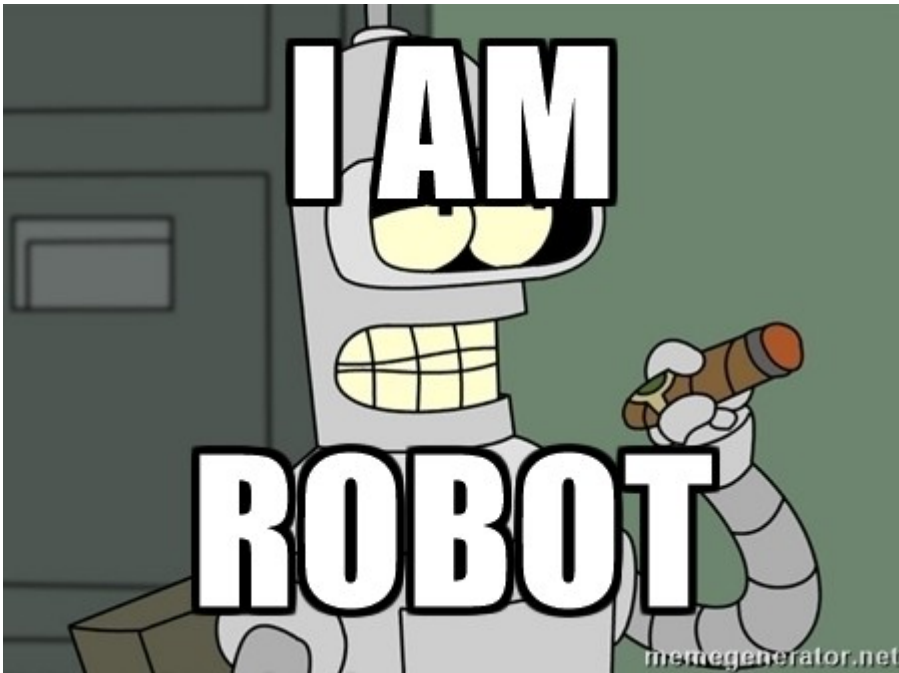
text

/tɛkst/ 

noun

1. a book or other written or printed work, regarded in terms of its content rather than its physical form.
"a text which explores pain and grief"
synonyms: written work, **book**, **work**, printed work, **narrative**
"a text which explores pain and grief"
2. the main body of a book or other piece of writing, as distinct from other material such as notes, appendices, and illustrations.
"the pictures are clear and relate well to the text"
synonyms: words, **wording**; **More**

Text 101: nlp perspective



Text:

A sequence of tokens(words).

Token/word:

A sequence of characters.

Character:

An atomic element of text.

＼_(ツ)_／

Text 101: tokens

Evolution of the hyaluronan synthase (*has*) operon in *Streptococcus zooepidermicus* and other pathogenic streptococci

↓ Filtering

Evolution of the hyaluronan synthase *has* operon in *Streptococcus zooepidermicus* and other pathogenic streptococci

↓ Tokenization

Evolution

of

the

hyaluronan

synthase

has

operon

...

Why bother with texts?

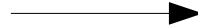
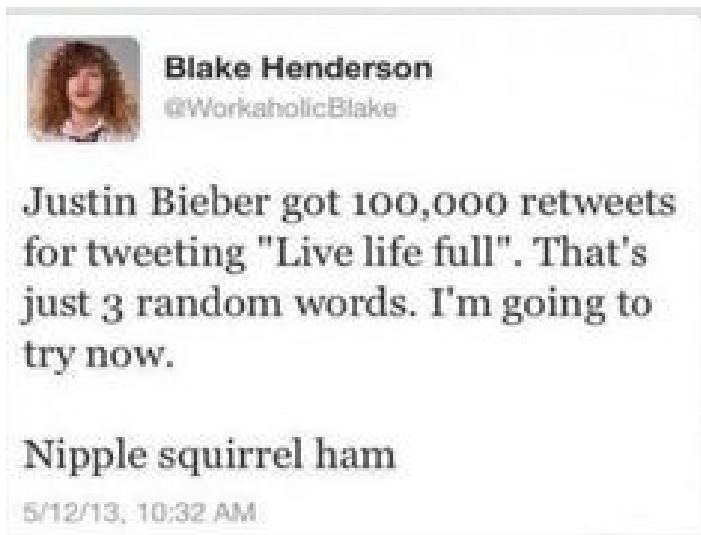
Classification/regression

- Sentiment analysis
- Comment moderation
- Predicting job salary
- Predicting tweet popularity

More complex

- Machine translation
- Information retrieval (web search)
- Conversation systems (chat bots)
- News summarization

Text classification/regression



Applications:

- Adult content filter (safe search)
- Detect age/gender/interests by search queries
- Convert movie review into “stars”
- Survey public opinion for the new iphone Vs old one (SNA)

...

Text classification/regression

text \longrightarrow features \longrightarrow ML model \longrightarrow $P(y|x)$

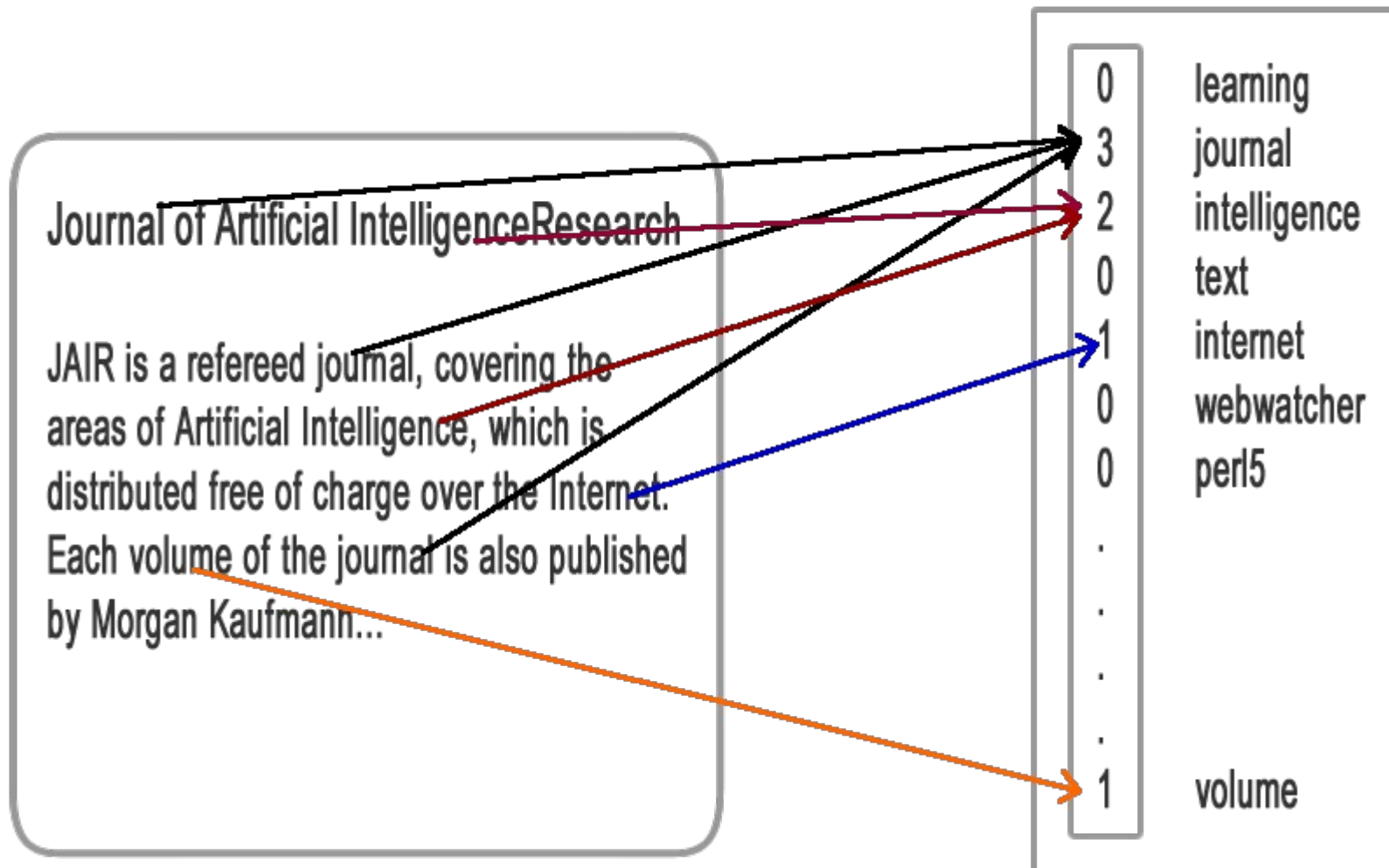
Text classification/regression

text \longrightarrow features \longrightarrow ML model \longrightarrow $P(y|x)$

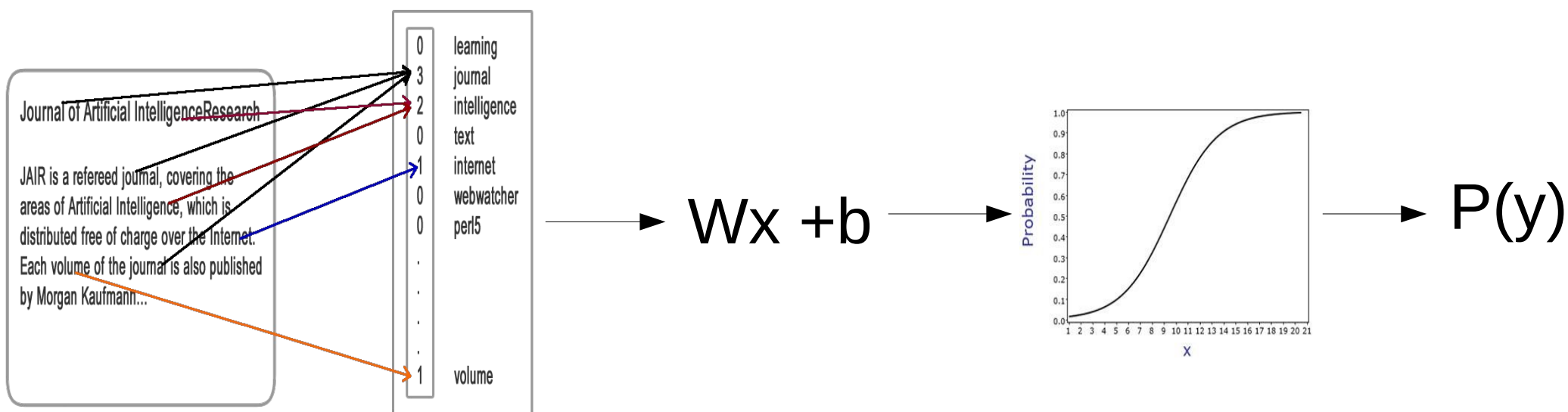


Can we represent text as a
constant-size feature vector?

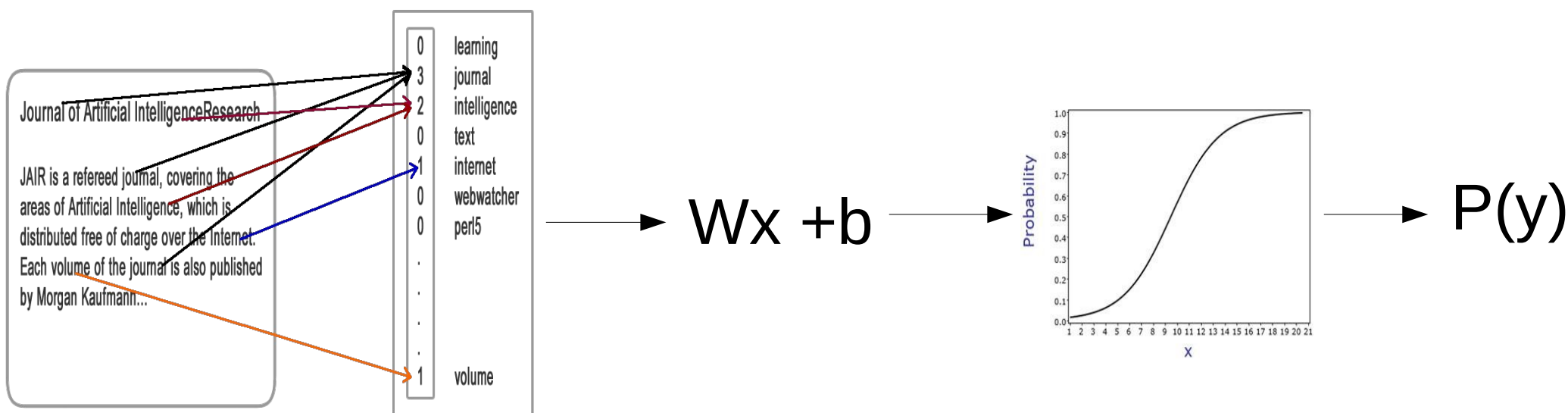
Bag of words



Bag of Words + Linear Model

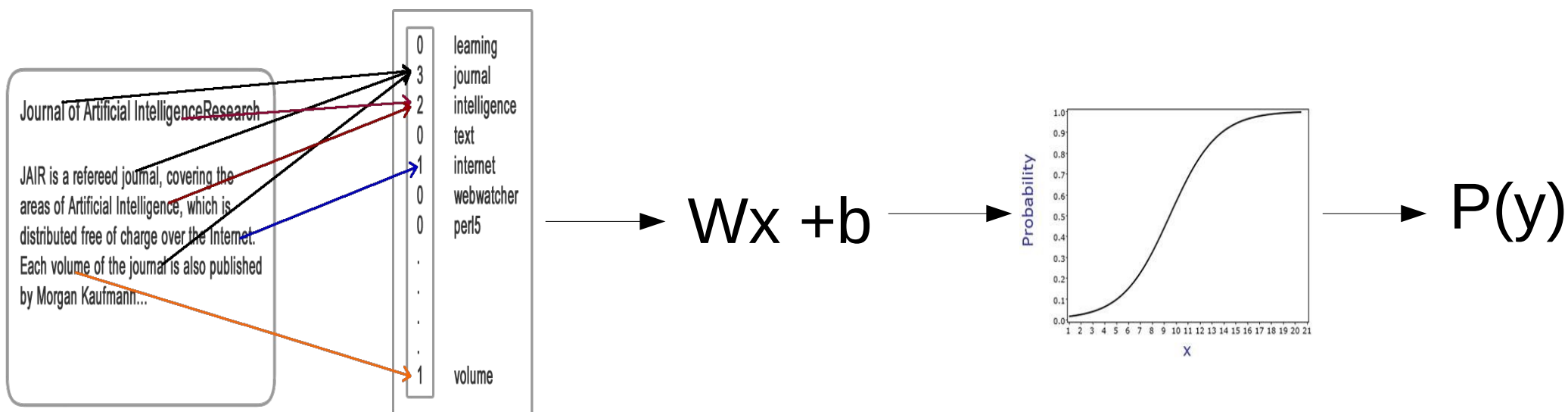


Bag of Words + Linear Model



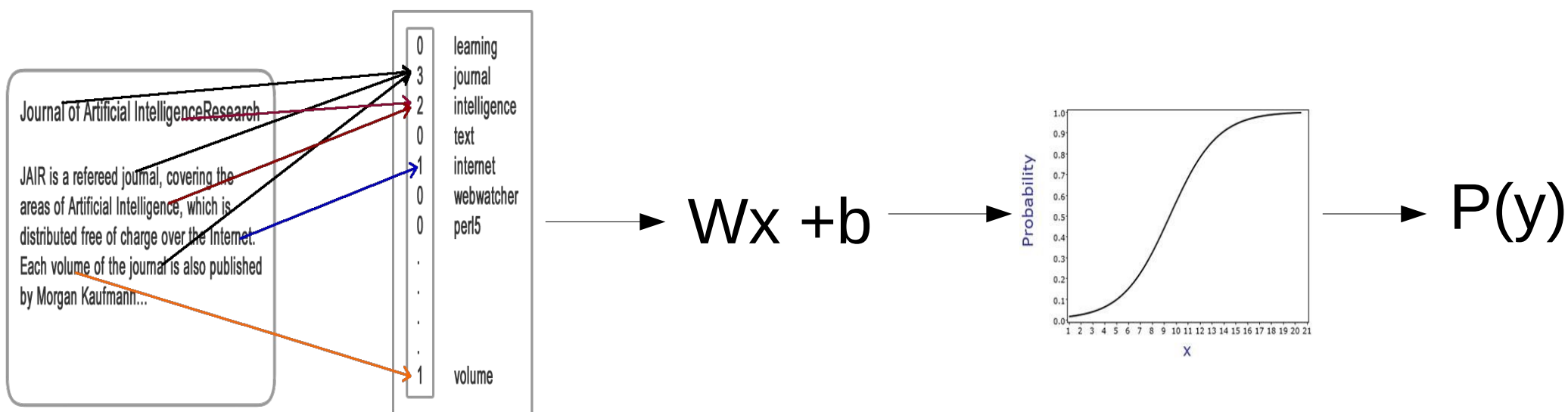
Guess: How many features (approx) will such model have?

Bag of Words + Linear Model



one feature for every token in the vocabulary, total $\sim 10^5$

Bag of Words + Linear Model



one feature for every token in the vocabulary, total $\sim 10^5$

Too many words

- Too many features, easy overfitting
- No information about word order
- Each word is exactly $\sqrt{2}$ away from all others

1
0
0
0

nice

0
1
0
0

beautiful

0
0
1
0

ugly

0
0
0
1

refrigerator

If model hasn't seen the word 'beautiful', that word will be equally close to 'nice' and to 'refrigerator'.

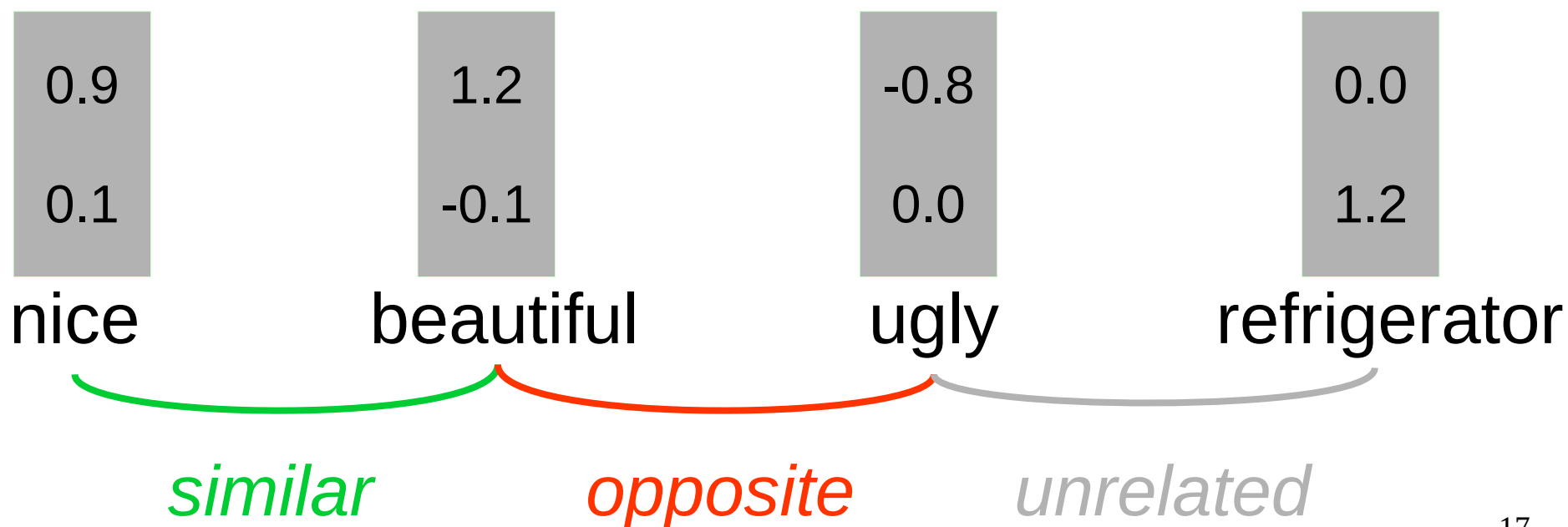
Word embeddings: core idea

Learn word features such that similar words have similar features



Word embeddings: core idea

Learn word features such that similar words have similar features



Distributional hypothesis

You shall know a word by the company it keeps
Firth (1957)

Words that occur in similar contexts
should have similar features

Nameless engineer (year unknown)

Cooccurences

He also found five fish swimming in murky water in an old **bathtub**.

We do abhor dust and dirt, and stains on the **bathtub**, and any kind of filth.

Above At the far end of the garden room a **bathtub** has been planted with herbs for the winter.

They had been drinking Cisco, a fruity, wine-based fluid that smells and tastes like a mixture of cough syrup and **bathtub** gin.

Science finds that a surface tension on the water can draw the boats together, like toy boats in a **bathtub**.

In fact, the godfather of gloom comes up with a plot that takes in Windsor Davies (the ghost of sitcoms past), a **bathtub** and a big box of concentrated jelly.

'I'll tell him,' said the Dean from the bathroom above the sound of bathwater falling from a great height into the ample Edwardian **bathtub**.



the	12
a	9
of	7
and	6
in	5
...	...
like	2
water	2
boat	2
from	2
stain	1
toy	1
god-father	1
Cisco	1
...	...

Cooccurrence matrix



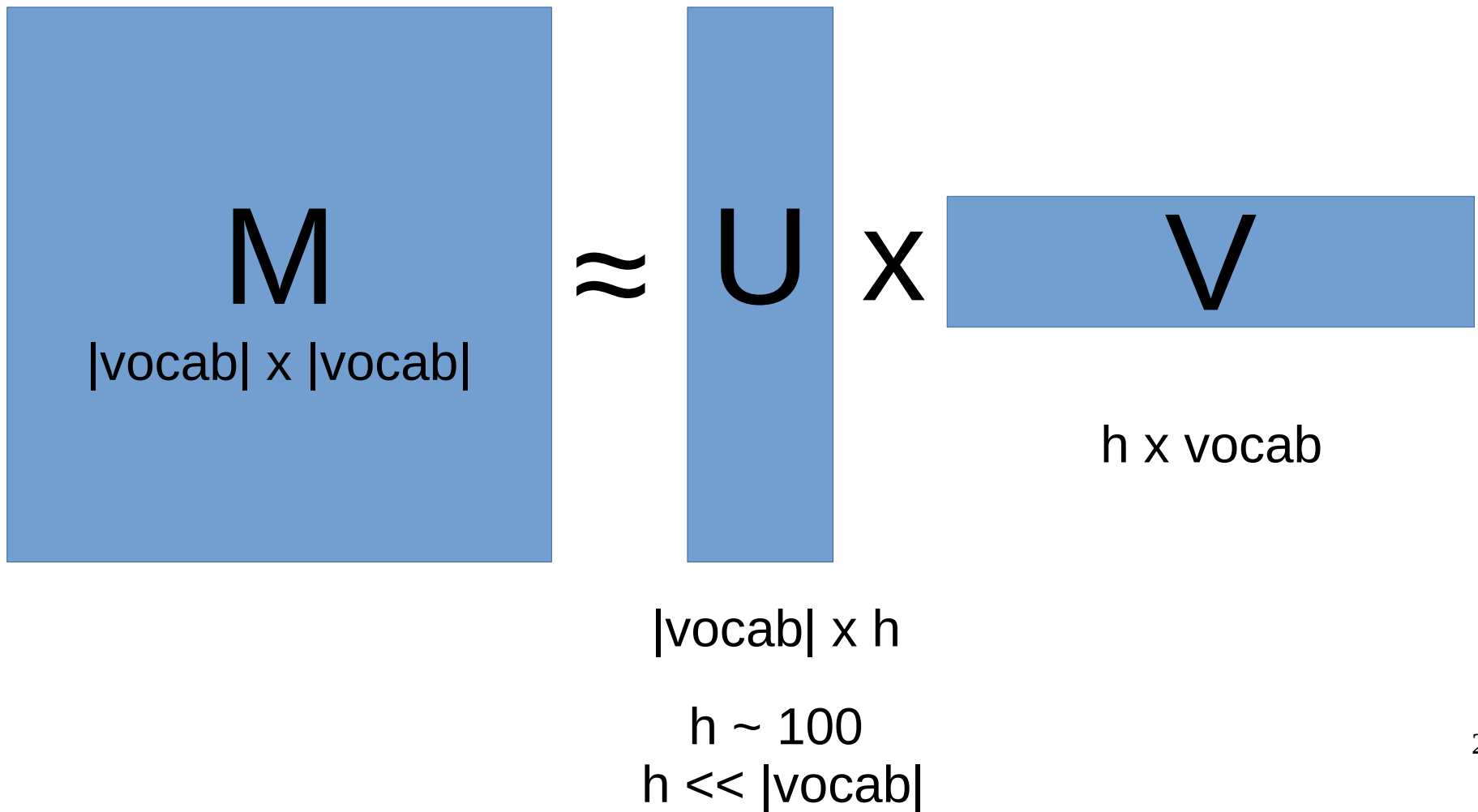
M

$|\text{vocab}| \times |\text{vocab}|$

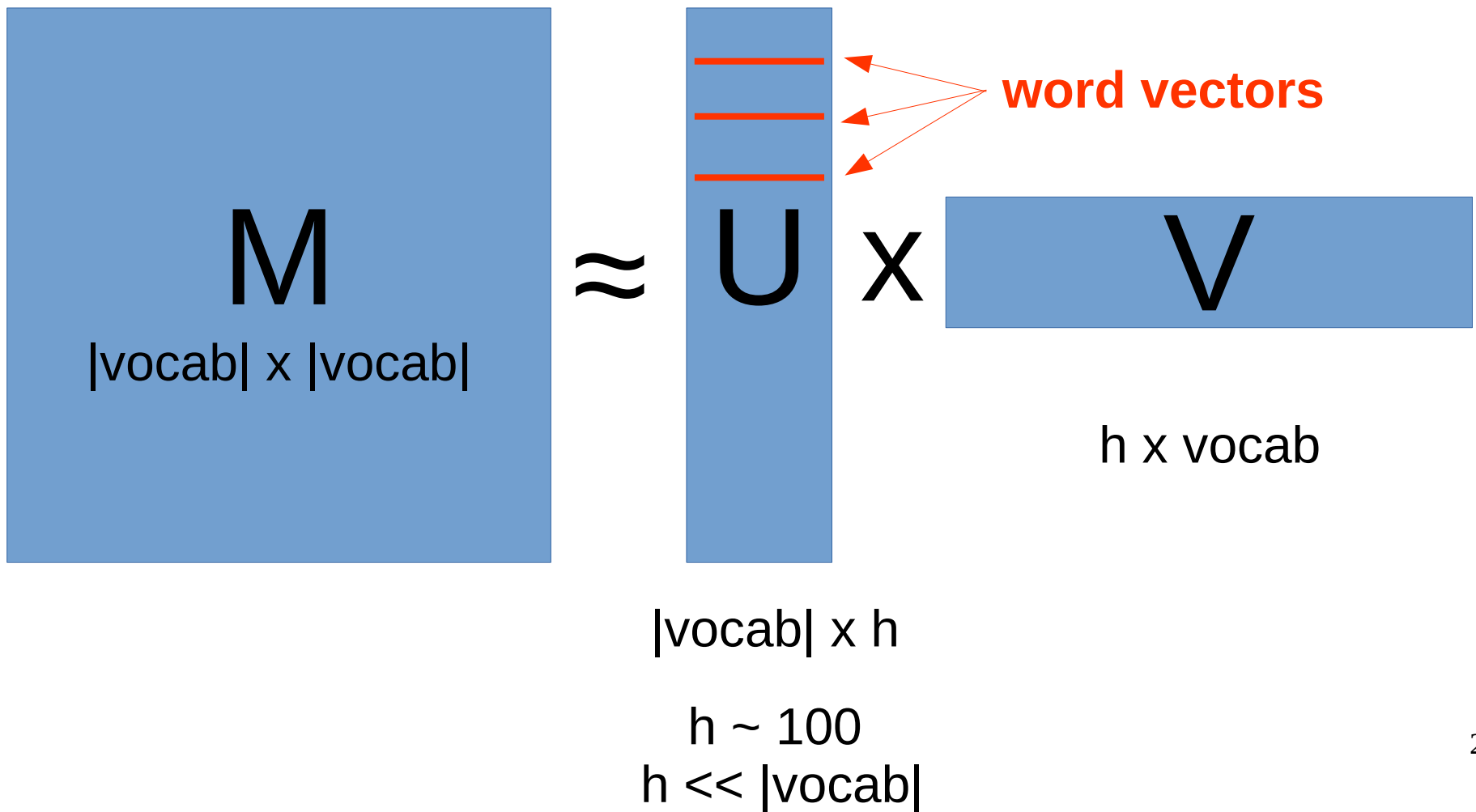
Co-occurrence matrix
i-th row contains co-occurrences of i-th word,
divided by their sum

all rows sum to 1
huge, but sparse

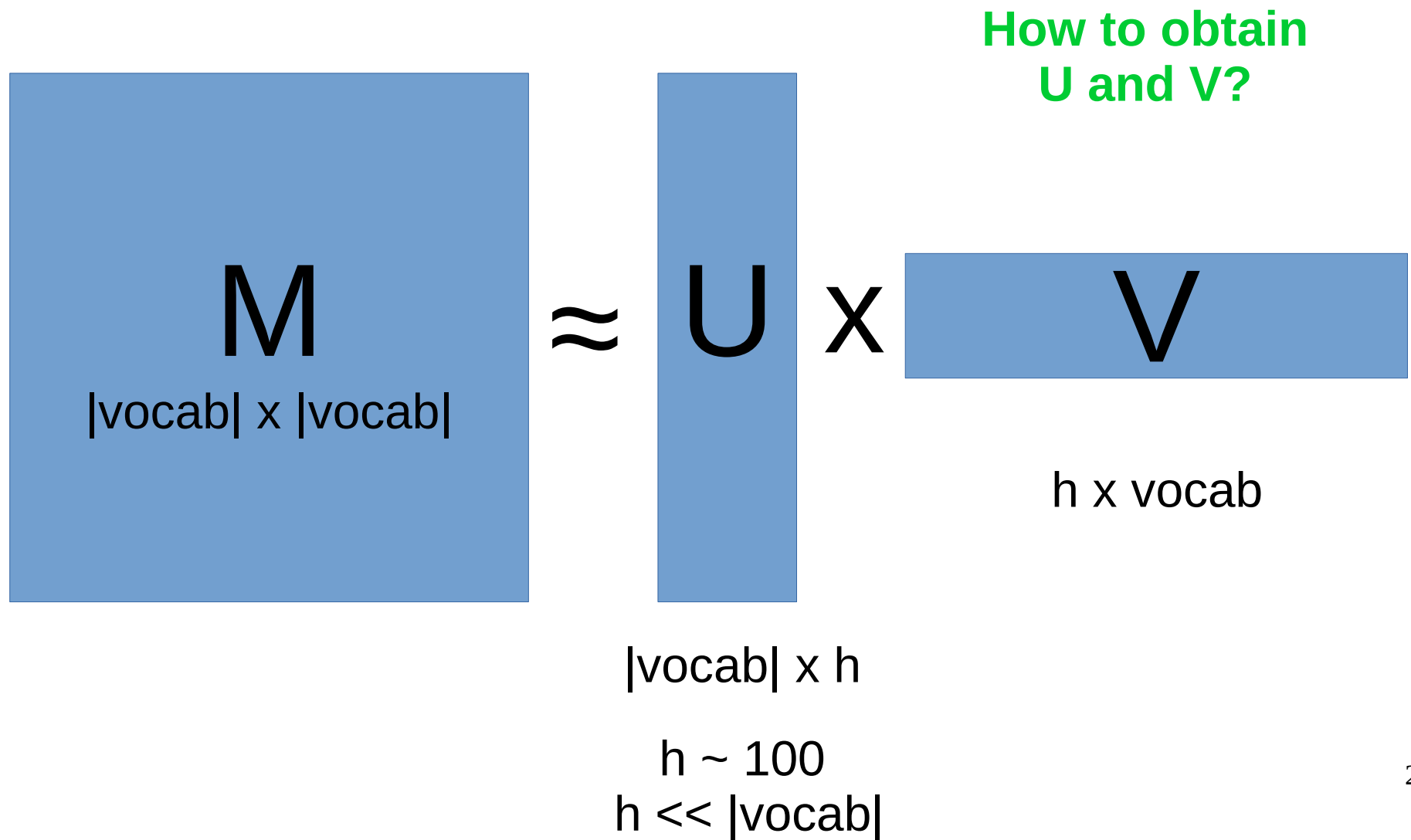
Cooccurrence matrix



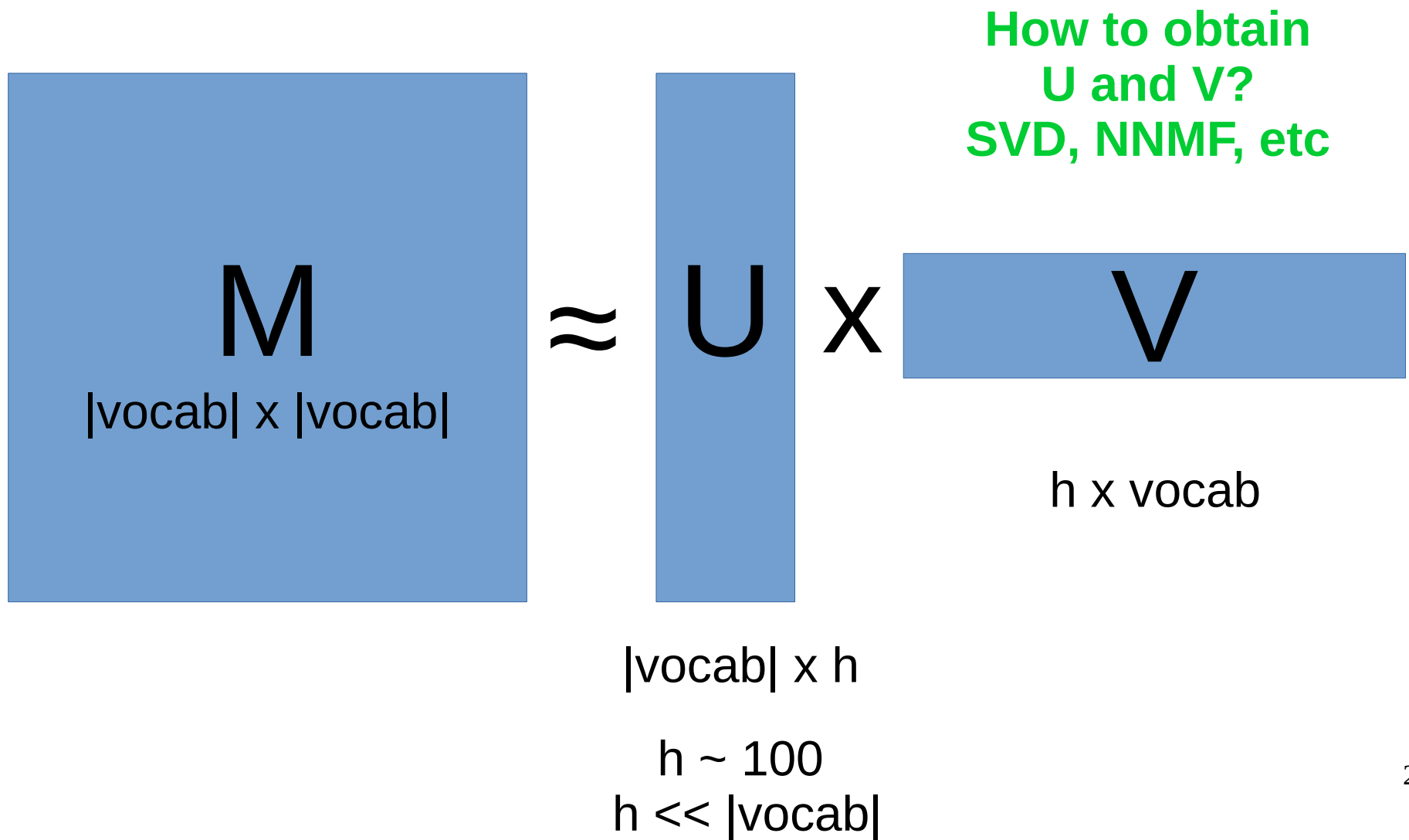
Cooccurrence matrix



Cooccurrence matrix

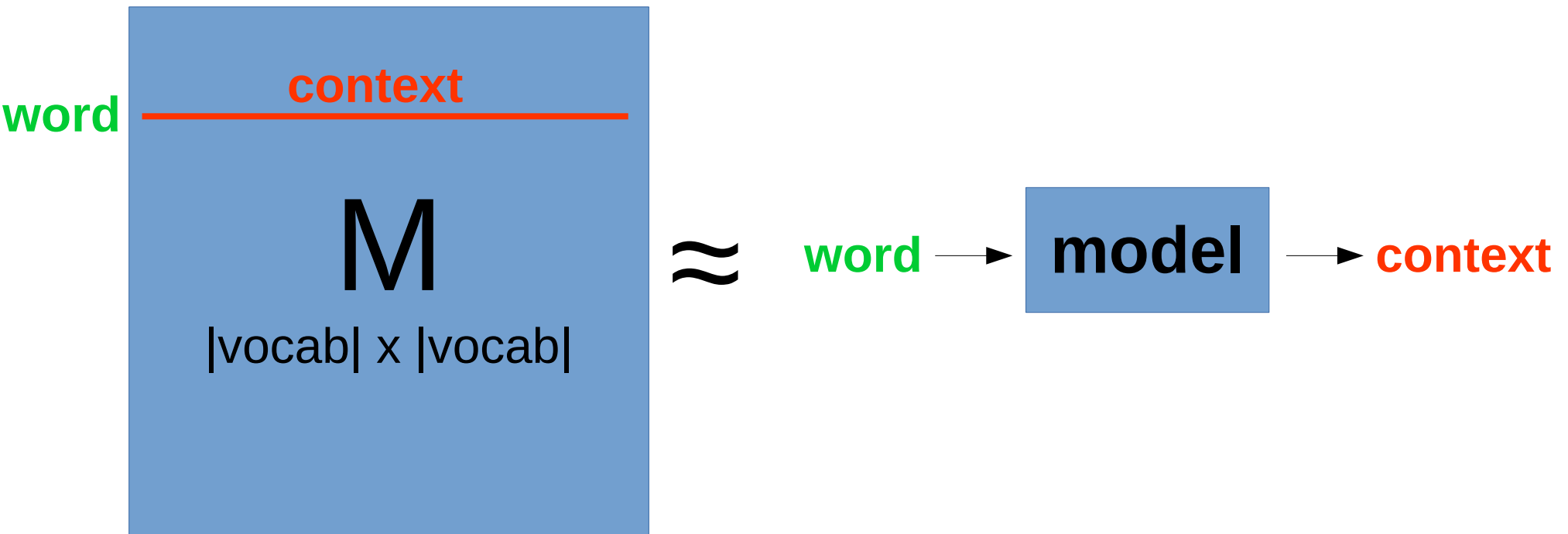


Cooccurrence matrix



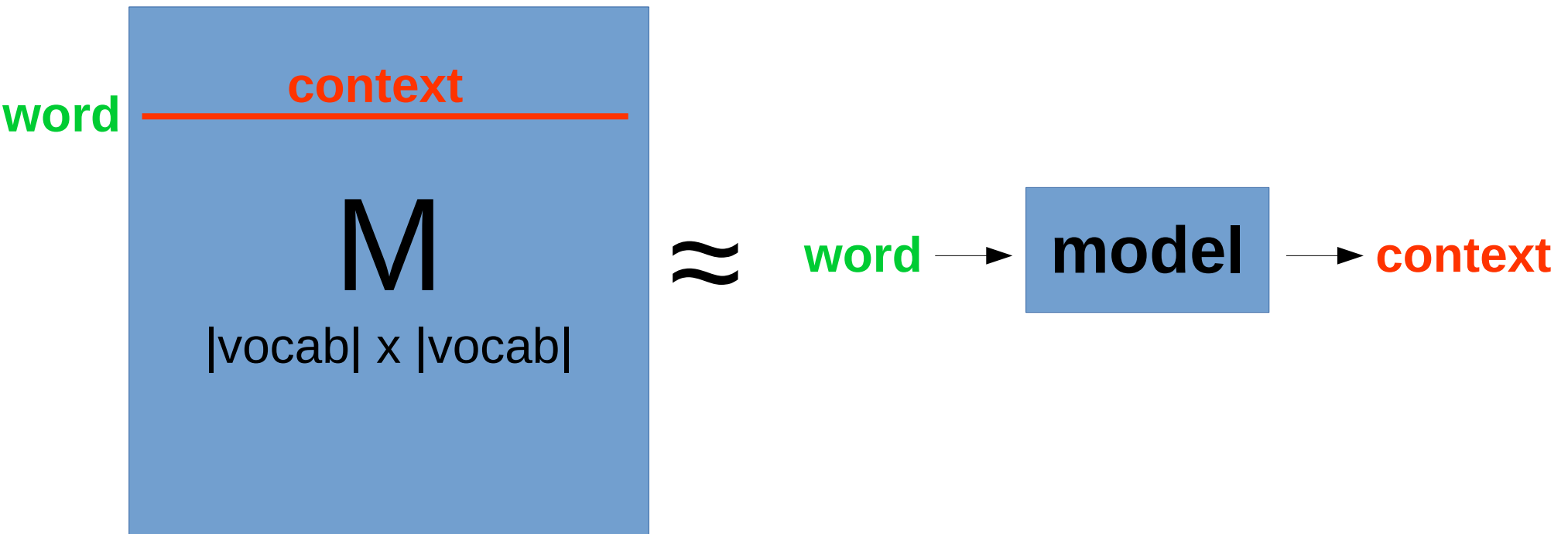
Word2vec

$$P(w_j \text{ is near } | w_i) \approx e^{\langle U_i, V_j \rangle} / \sum_k e^{\langle U_i, V_k \rangle}$$



Word2vec

$$P(w_j \text{ is near } | w_i) \approx e^{\langle U_i, V_j \rangle} / \sum_k e^{\langle U_i, V_k \rangle}$$



Q: how do we train it?

Word2vec

$$P(w_j \text{ is near } | w_i) \approx e^{\langle U_i, V_j \rangle} / \sum_k e^{\langle U_i, V_k \rangle}$$

Crossentropy loss:

$$L = -\frac{1}{N} \sum_{w_i \in \text{vocab}} \sum_{w_j \in \text{vocab}} M_{i,j} \cdot \log P(w_j \text{ is near } | w_i)$$

Word2vec

$$P(w_j \text{ is near} | w_i) \approx e^{\langle U_i, V_j \rangle} / \sum_k e^{\langle U_i, V_k \rangle}$$

Crossentropy loss:

$$L = -\frac{1}{N} \sum_{w_i \in \text{vocab}} \sum_{w_j \in \text{vocab}} M_{i,j} \cdot \log P(w_j \text{ is near} | w_i)$$

Re-write as sum over sentences

$$M_{i,j} = \sum_{w_i \in \text{Text}} \sum_{w_j \in \text{context}(w_i)} + 1$$

$$L = -\frac{1}{N} \sum_{w_i \in \text{Text}} \sum_{w_j \in \text{context}(w_i)} \log P(w_j \text{ is near} | w_i)$$

No need to compute M - train word2vec on sentences!

Embedding: word2vec

“Peace is a lie , there is only passion .”

lie

0
0
0
...
0
0
1
0
0
...
0
0

1-hot
word

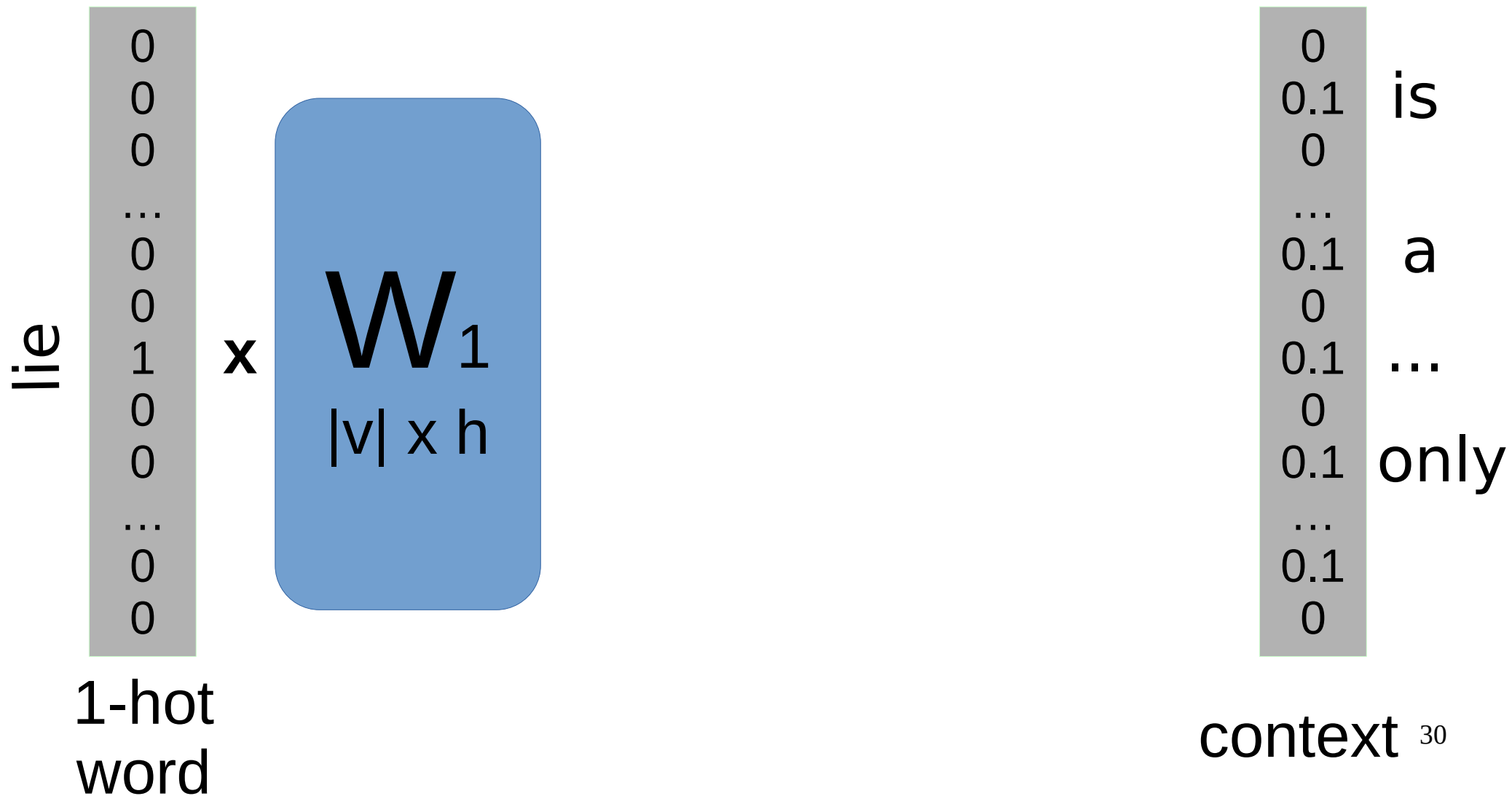
0
0.1
0
...
0.1
0
0.1
0
0.1
...
0.1
0

is
a
...
only

context ²⁹

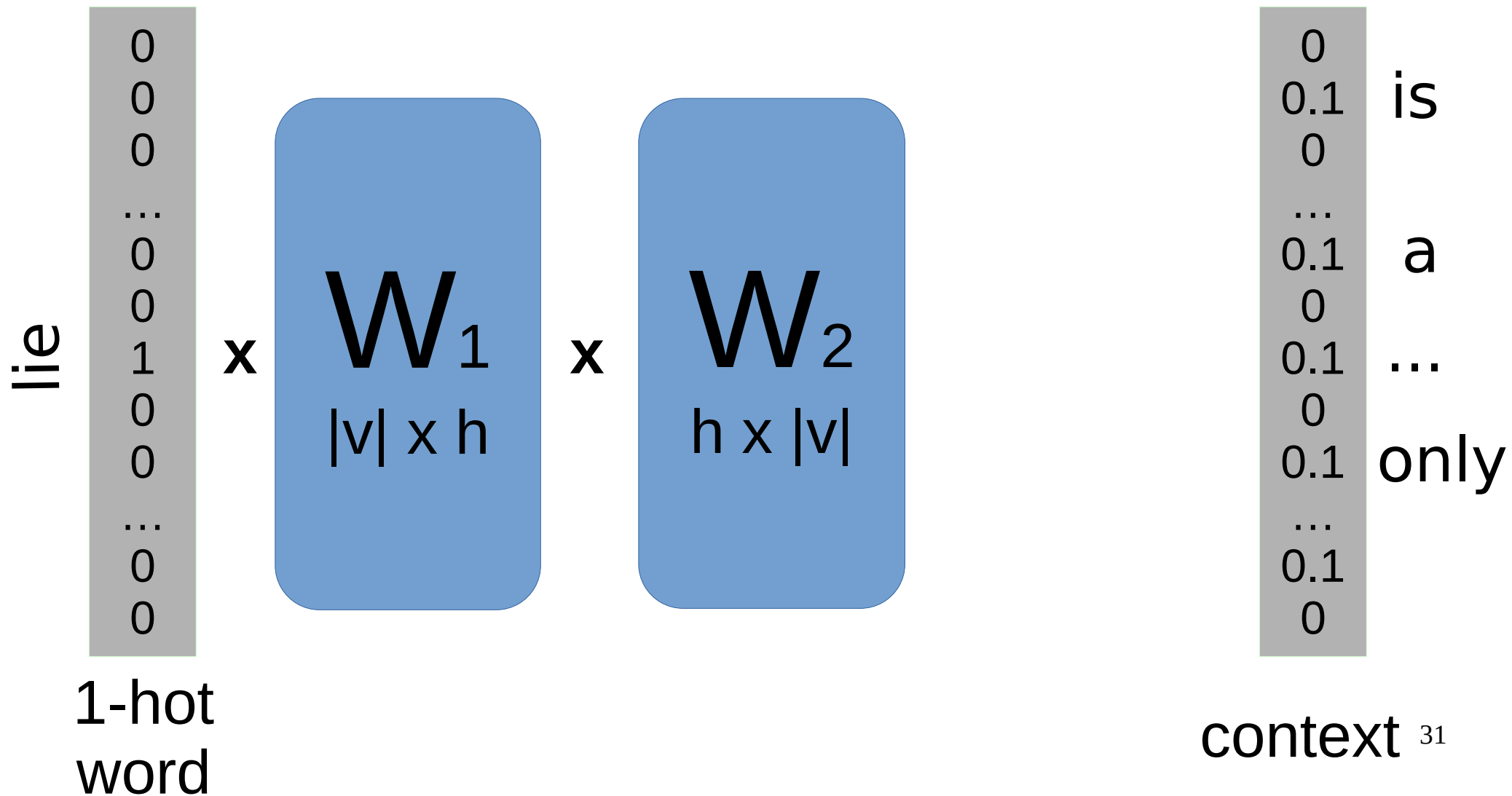
Embedding: word2vec

“Peace is a lie , there is only passion .”



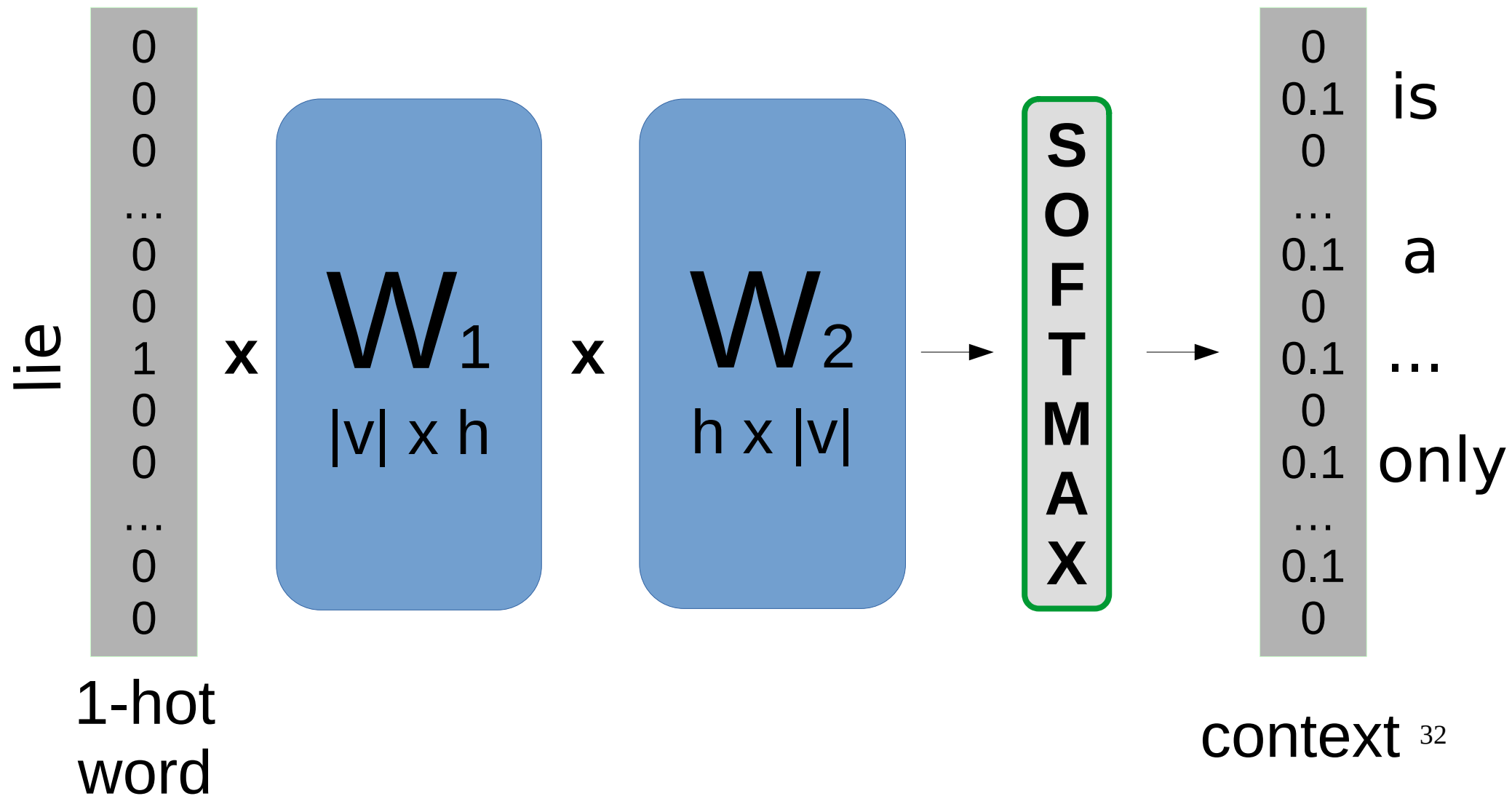
Embedding: word2vec

“Peace is a lie , there is only passion .”



Embedding: word2vec

“Peace is a lie , there is only passion .”



Embedding: word2vec

Side effect: synonyms

“nice” \sim “beautiful”

“hard” \sim “difficult”

Side effect: word algebra

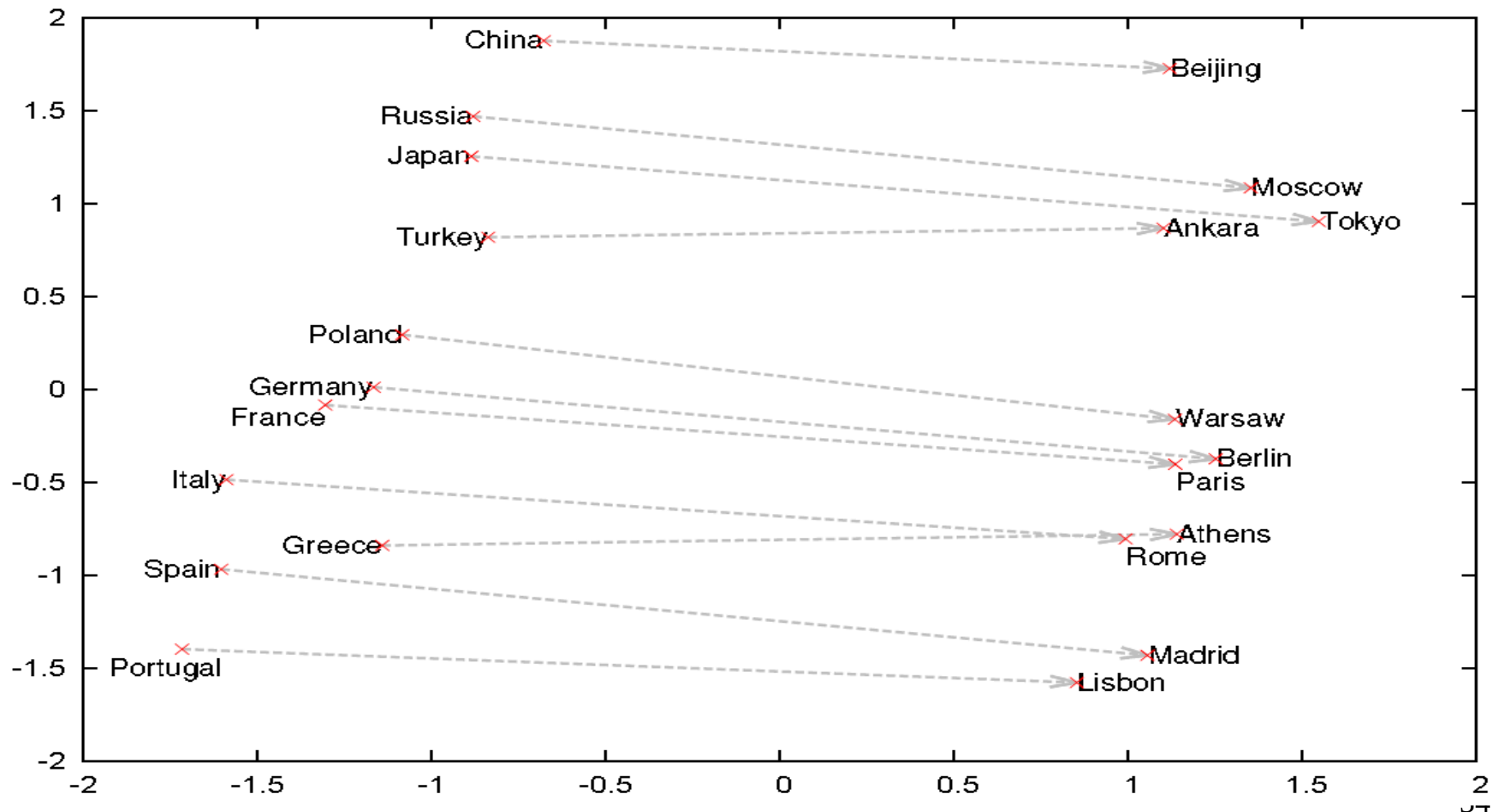
“king” - “man” + “woman” \sim “queen”

“moscow” - “russia” + “france” \sim “paris”

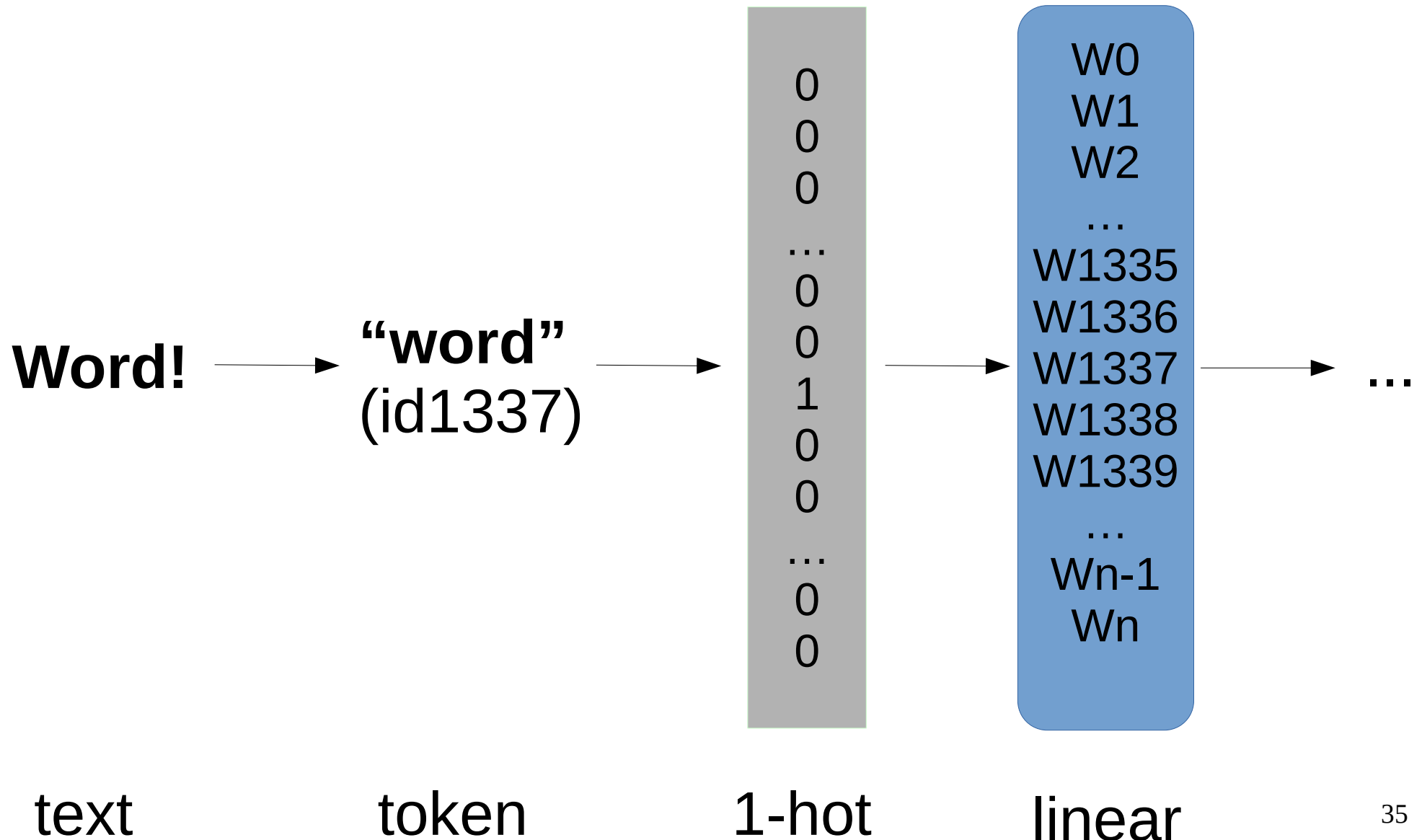
Embedding: word2vec

Side effect: word algebra

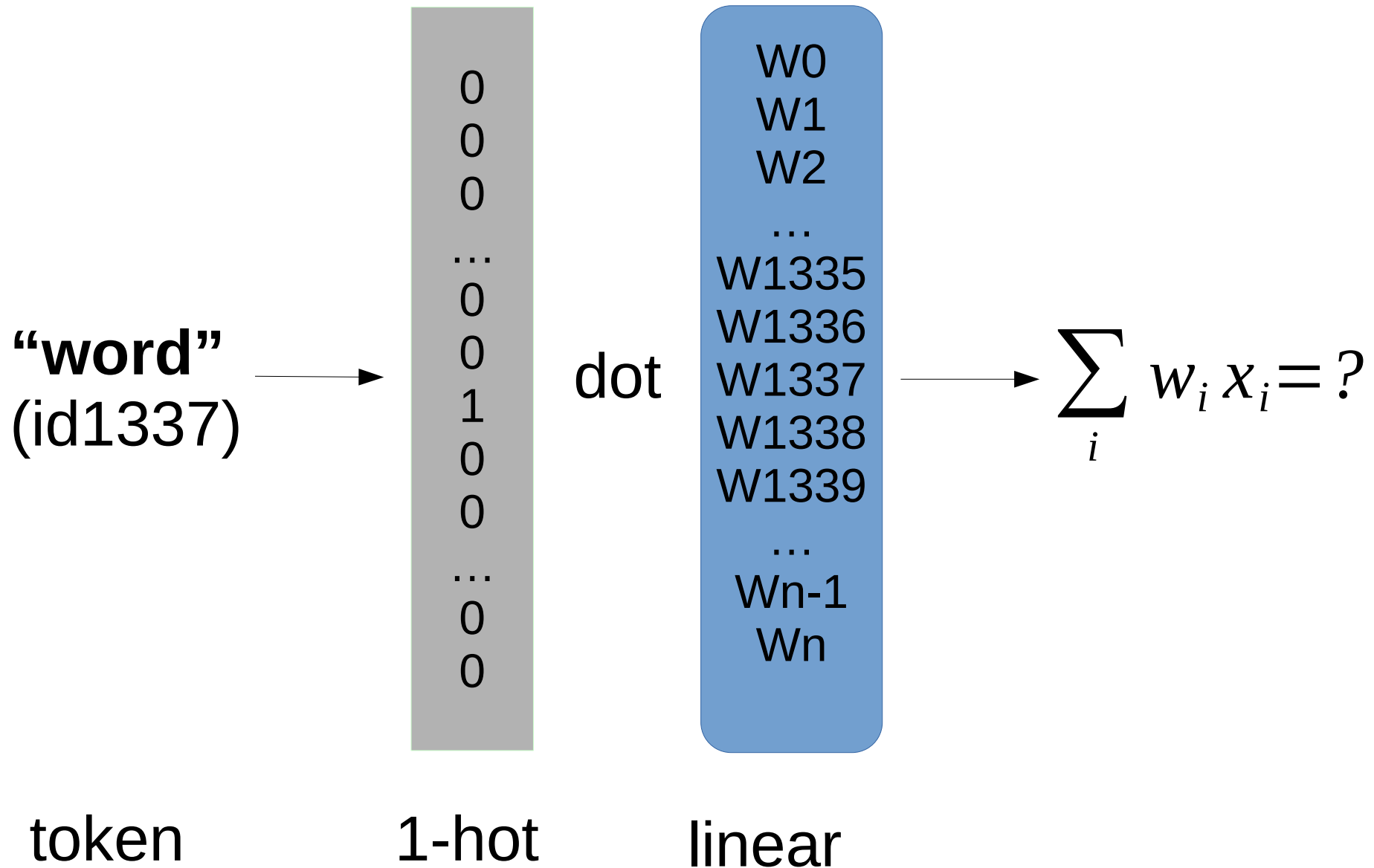
Country and Capital Vectors Projected by PCA



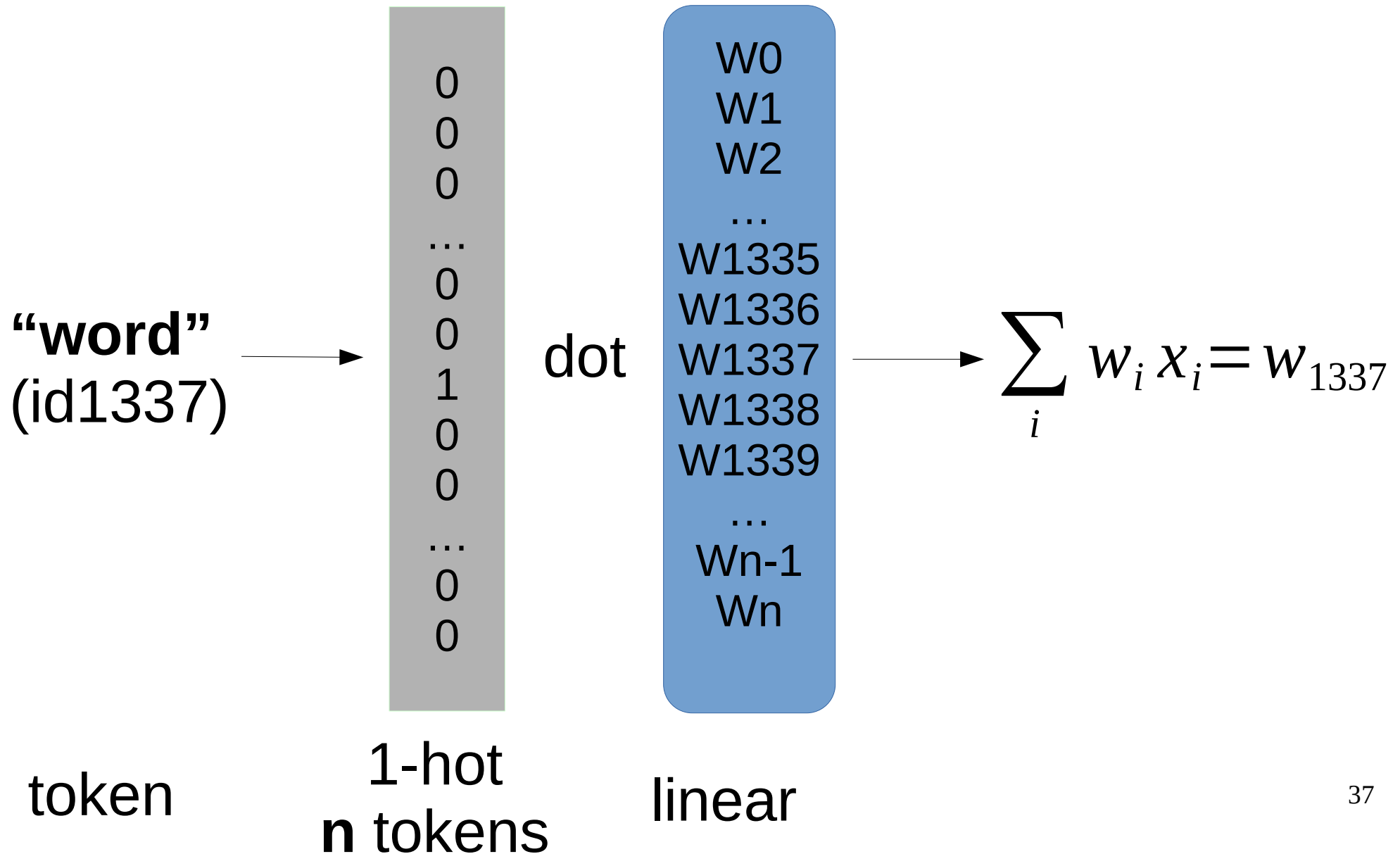
Sparse vector products



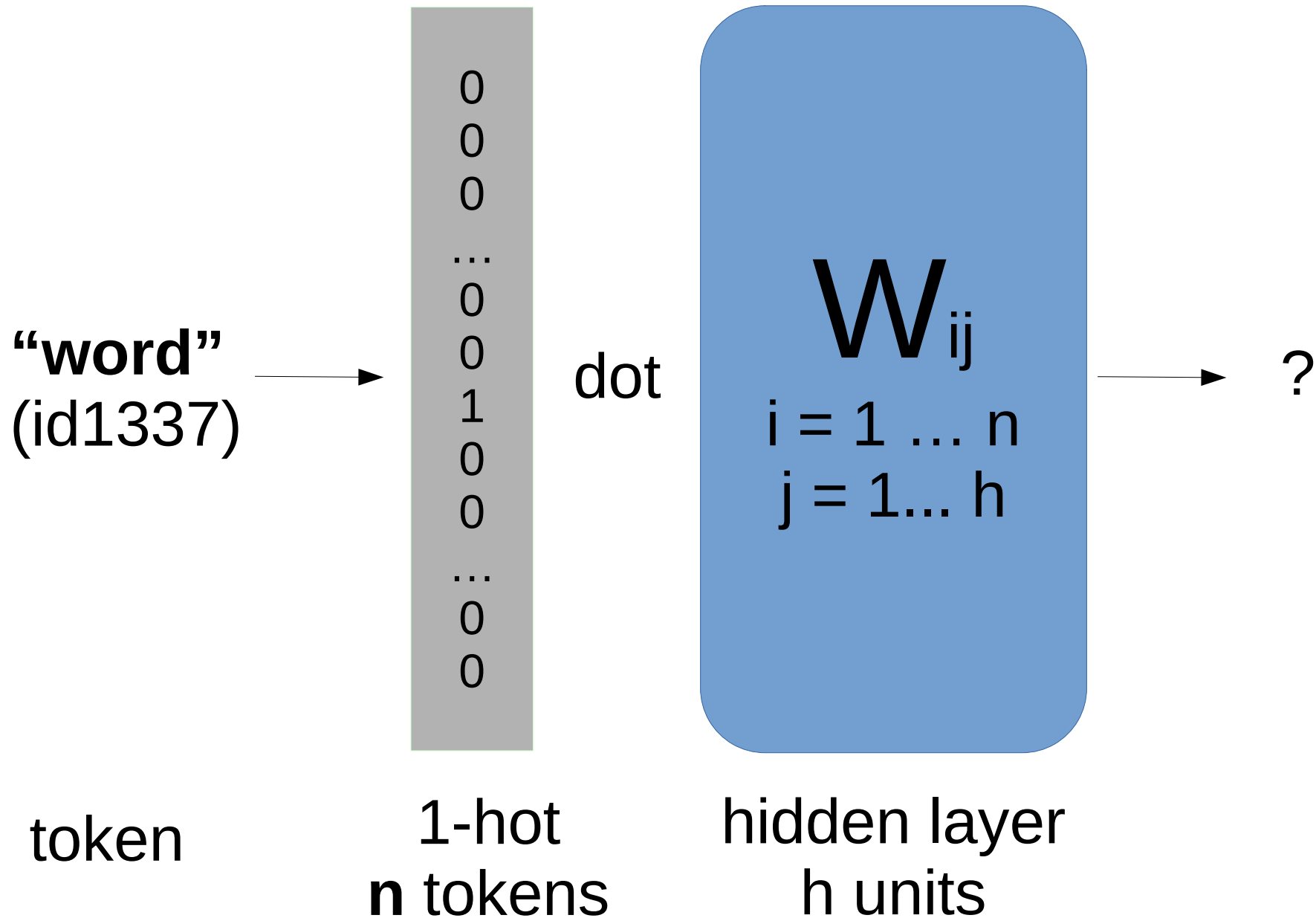
Sparse vector products



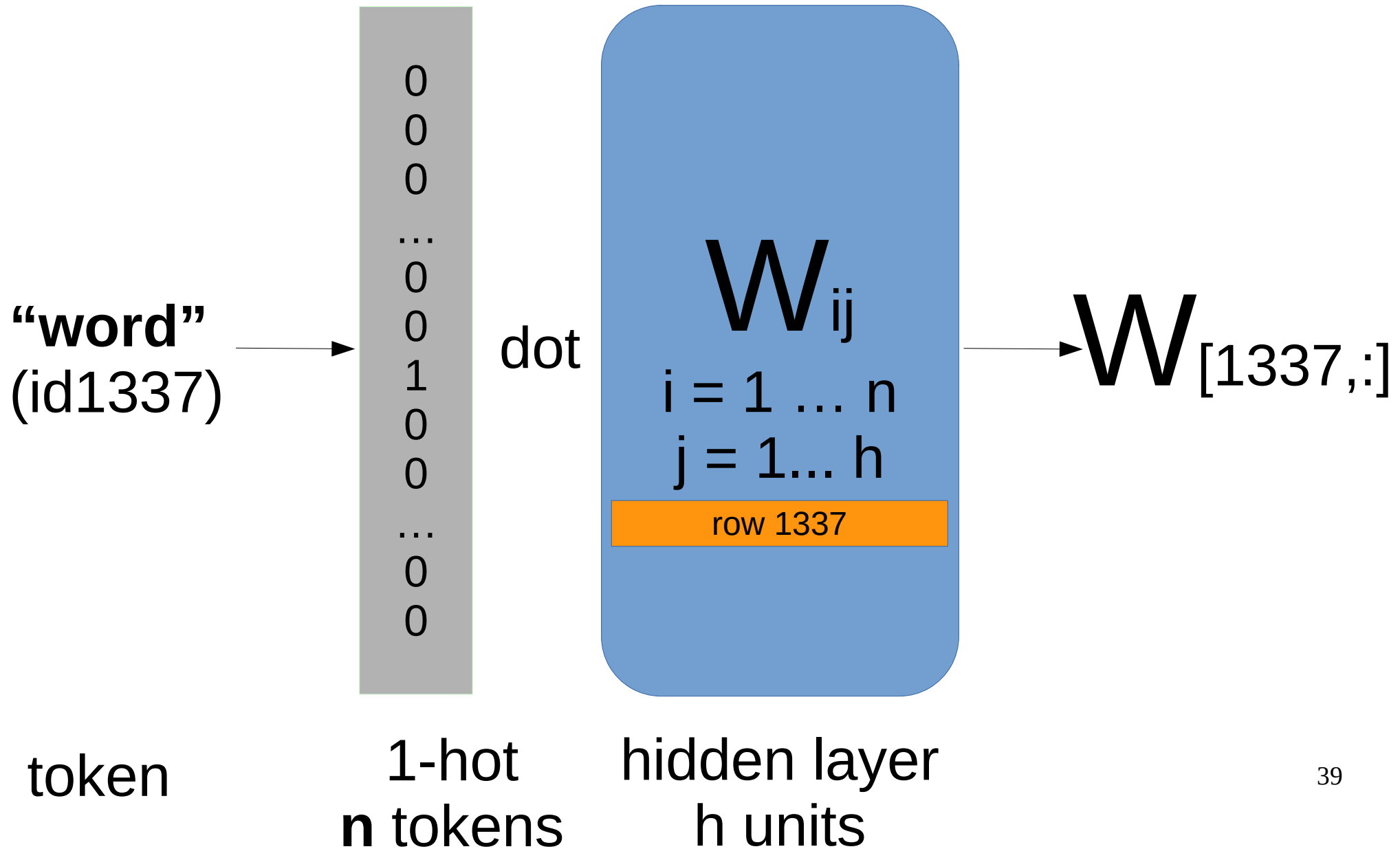
Sparse vector products



Sparse vector products

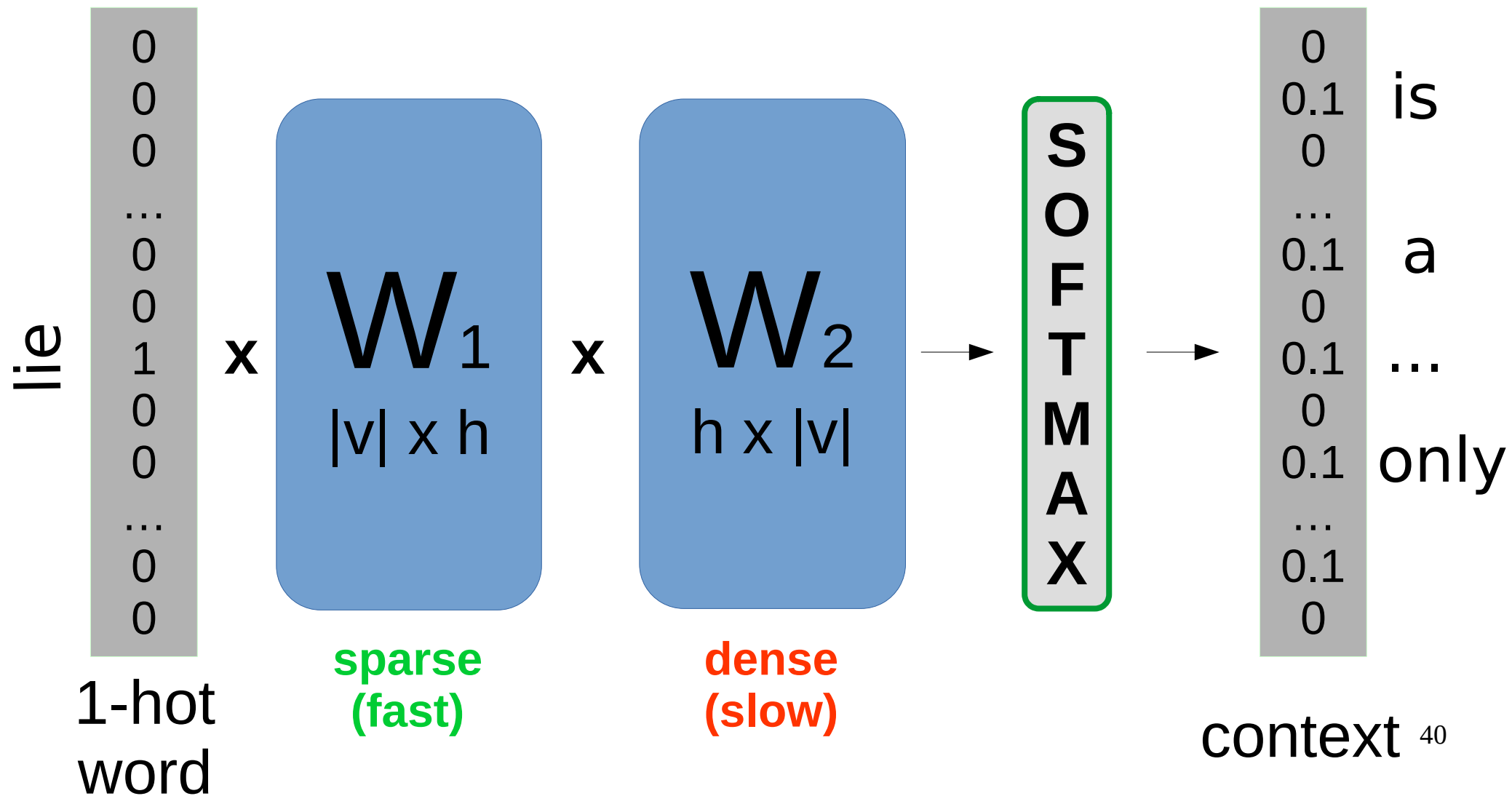


Embedding

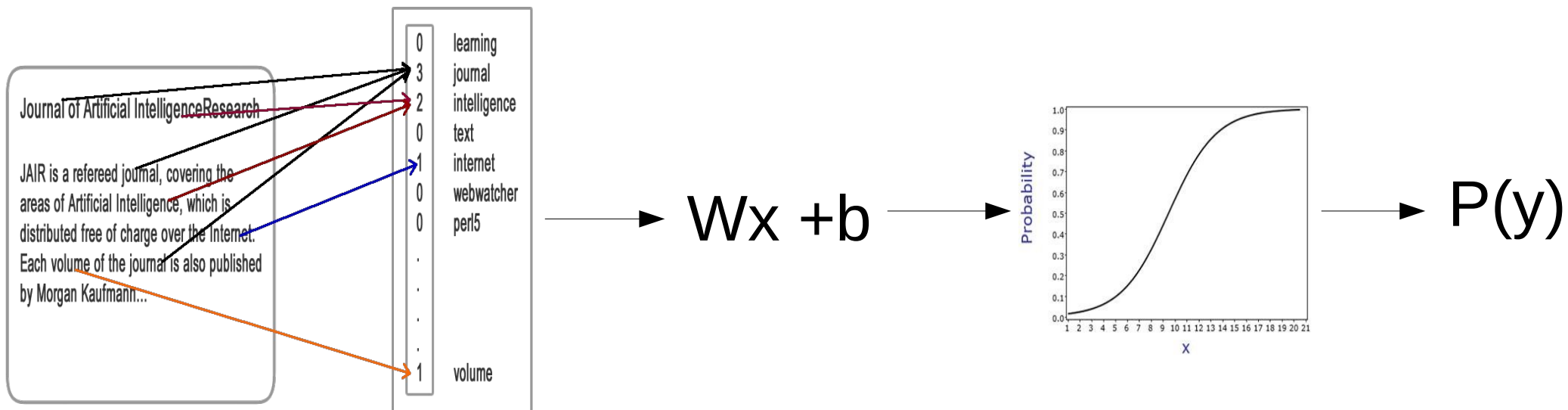


Embedding: word2vec

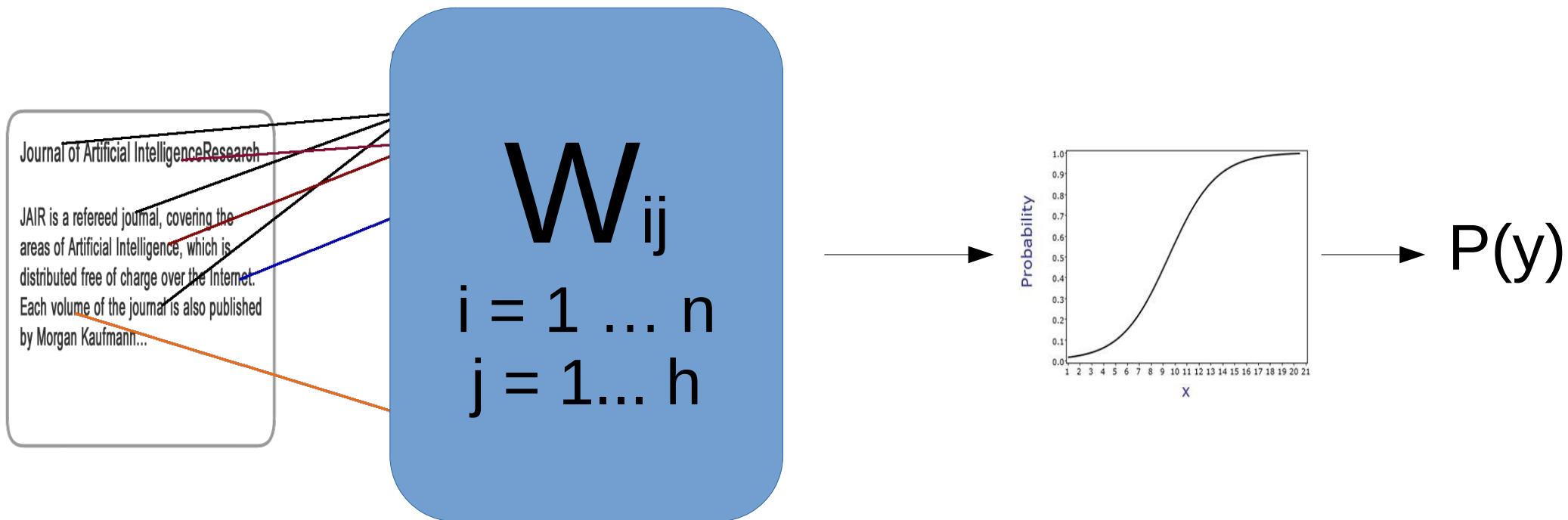
“Peace is a lie , there is only passion .”



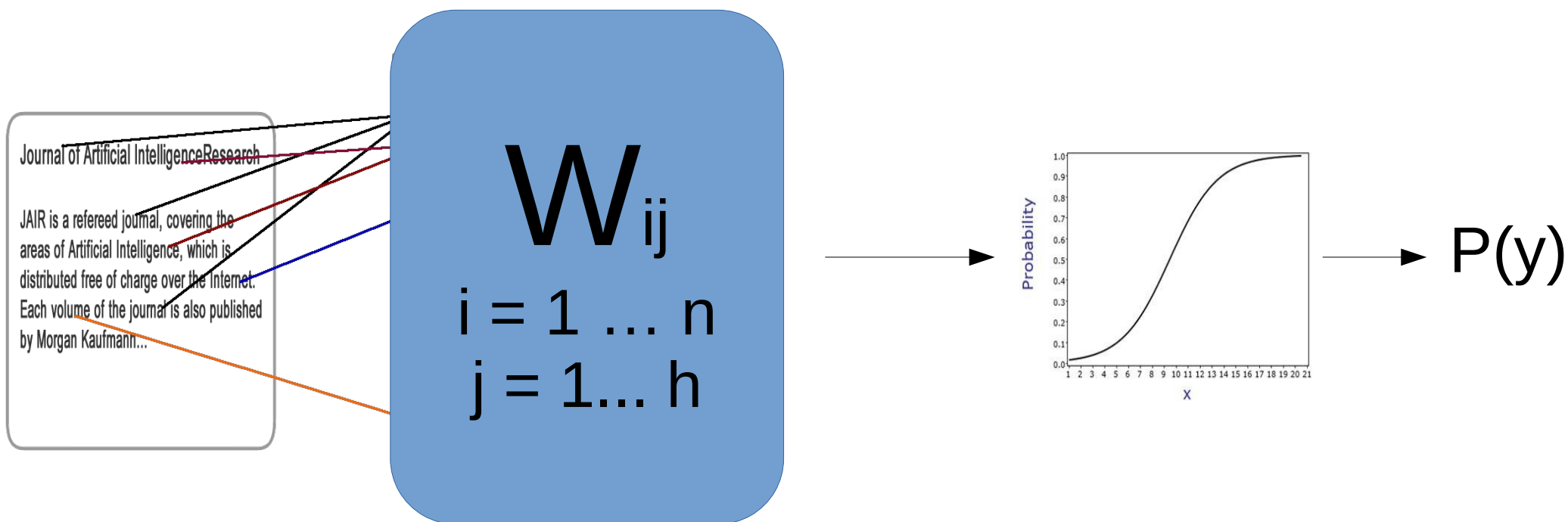
Text Classification (again)



Text Classification (again)

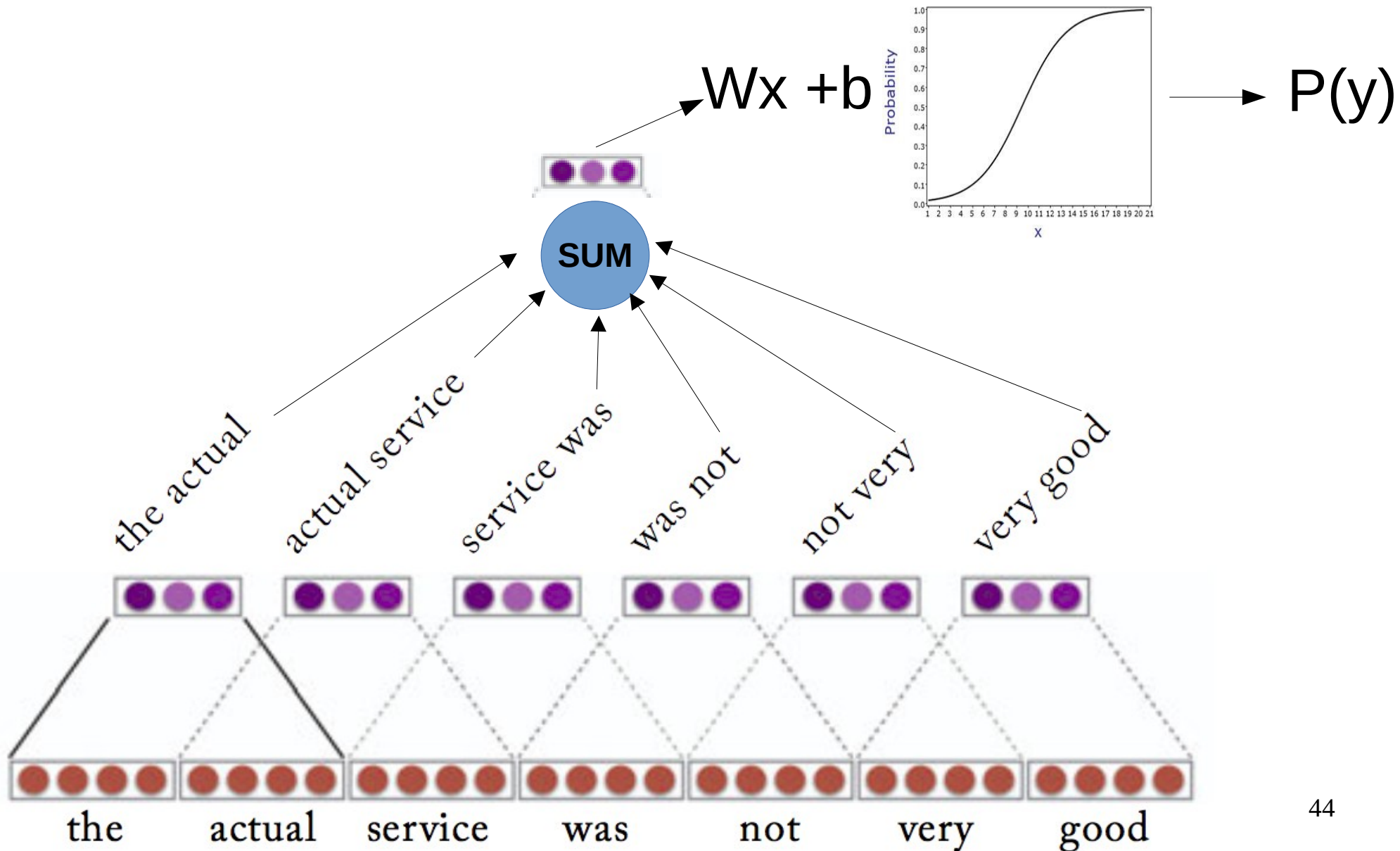


Text Classification (again)



Model does not know about word order. How to fix that?

Text Convolution



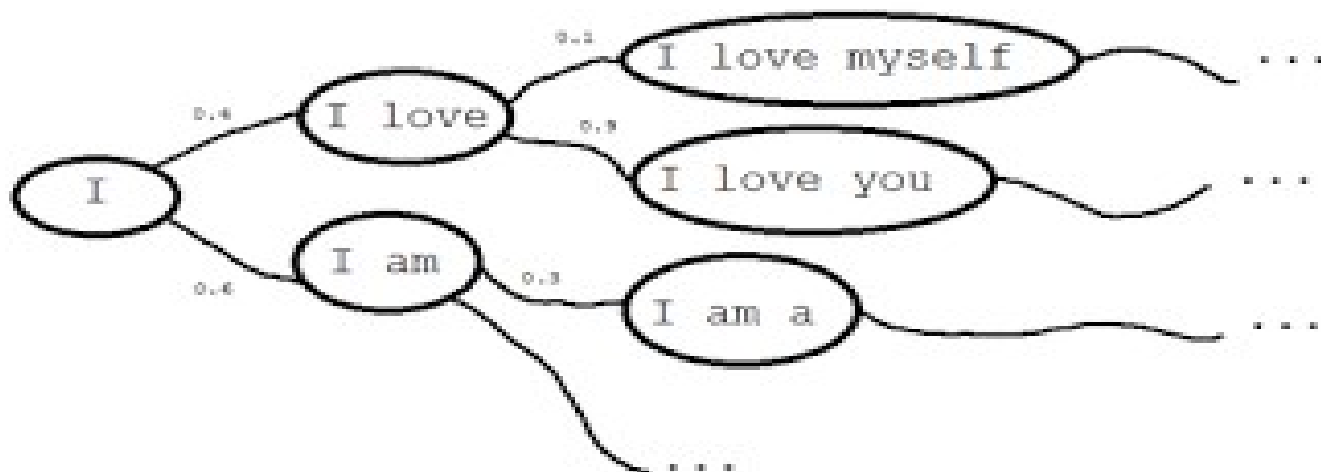
[Insert 5 minute break here]

Language model

Objective:

- Learn $P(\text{text})$

$$P(\text{text}) = P(w_0, w_1, \dots, w_n) = P(w_0) \cdot P(w_1 | w_0) \cdot P(w_2 | w_1 w_0) \cdot \dots \cdot P(w_n | \dots)$$



Language model

Why learning it?

- Detect languages as $P(\text{text}|\text{language})$
- Sentiment analysis $P(\text{text}|\text{happy})$
- Any text analysis you can imagine
- Generate texts!
 - Cool article <http://bit.ly/1K610Ie>
 - Generating clickbait: <http://bit.ly/21cZM70>

Language model

- Actual distribution

$$P(\text{text}) = P(w_0, w_1, \dots, w_n) = P(w_0) \cdot P(w_1 | w_0) \cdot P(w_2 | w_1 w_0) \cdot \dots \cdot P(w_n | \dots)$$

- Bag of words assumption (independent words)

$$P(\text{text}) = P(w_0, w_1, \dots, w_n) = P(w_0) \cdot P(w_1) \cdot P(w_2) \cdot \dots \cdot P(w_n)$$

- **Anything better?**

Language model

- Actual distribution

$$P(\text{text}) = P(w_0, w_1, \dots, w_n) = P(w_0) \cdot P(w_1 | w_0) \cdot P(w_2 | w_1 w_0) \cdot \dots \cdot P(w_n | \dots)$$

- Bag of words assumption (independent words)

$$P(\text{text}) = P(w_0, w_1, \dots, w_n) = P(w_0) \cdot P(w_1) \cdot P(w_2) \cdot \dots \cdot P(w_n)$$

- Markov assumption

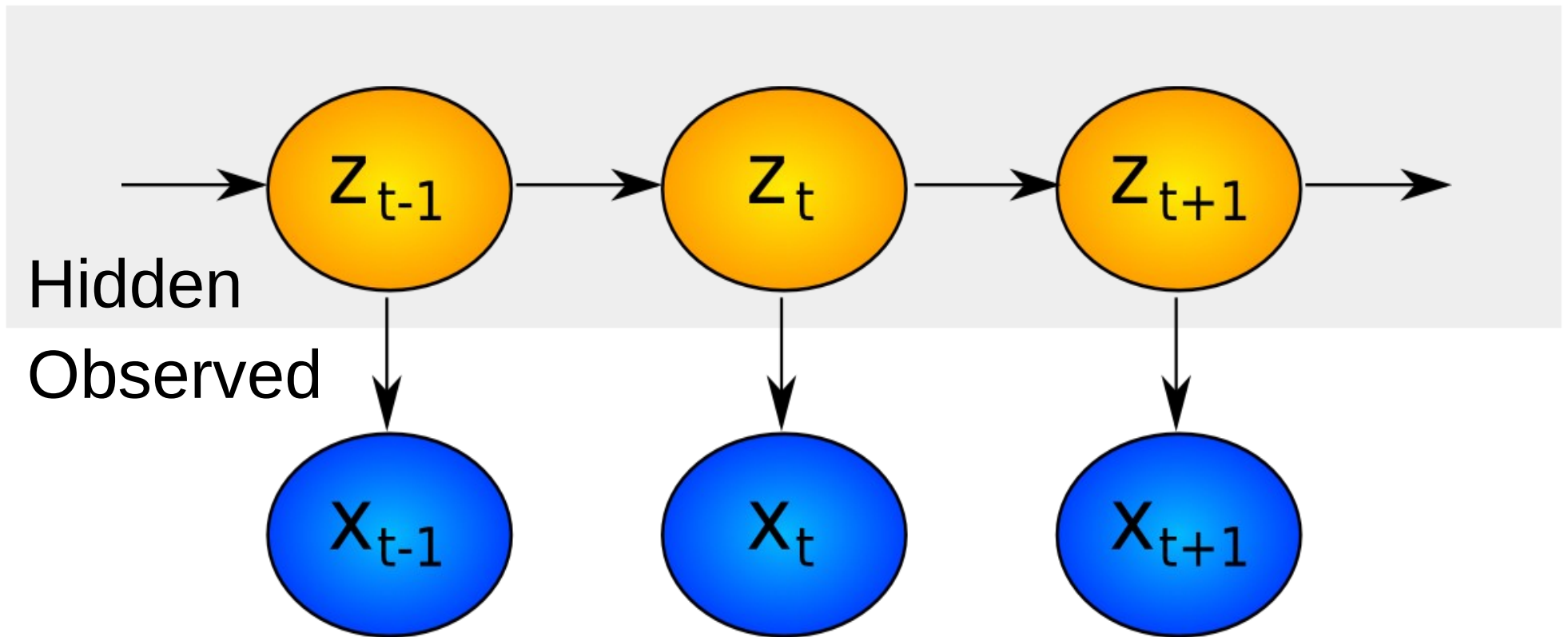
$$P(\text{text}) = P(w_0, w_1, \dots, w_n) = P(w_0) \cdot P(w_1 | w_0) \cdot P(w_2 | w_1) \cdot \dots \cdot P(w_n | w_{n-1})$$

- also 3-gram, 5-gram, 100-gram

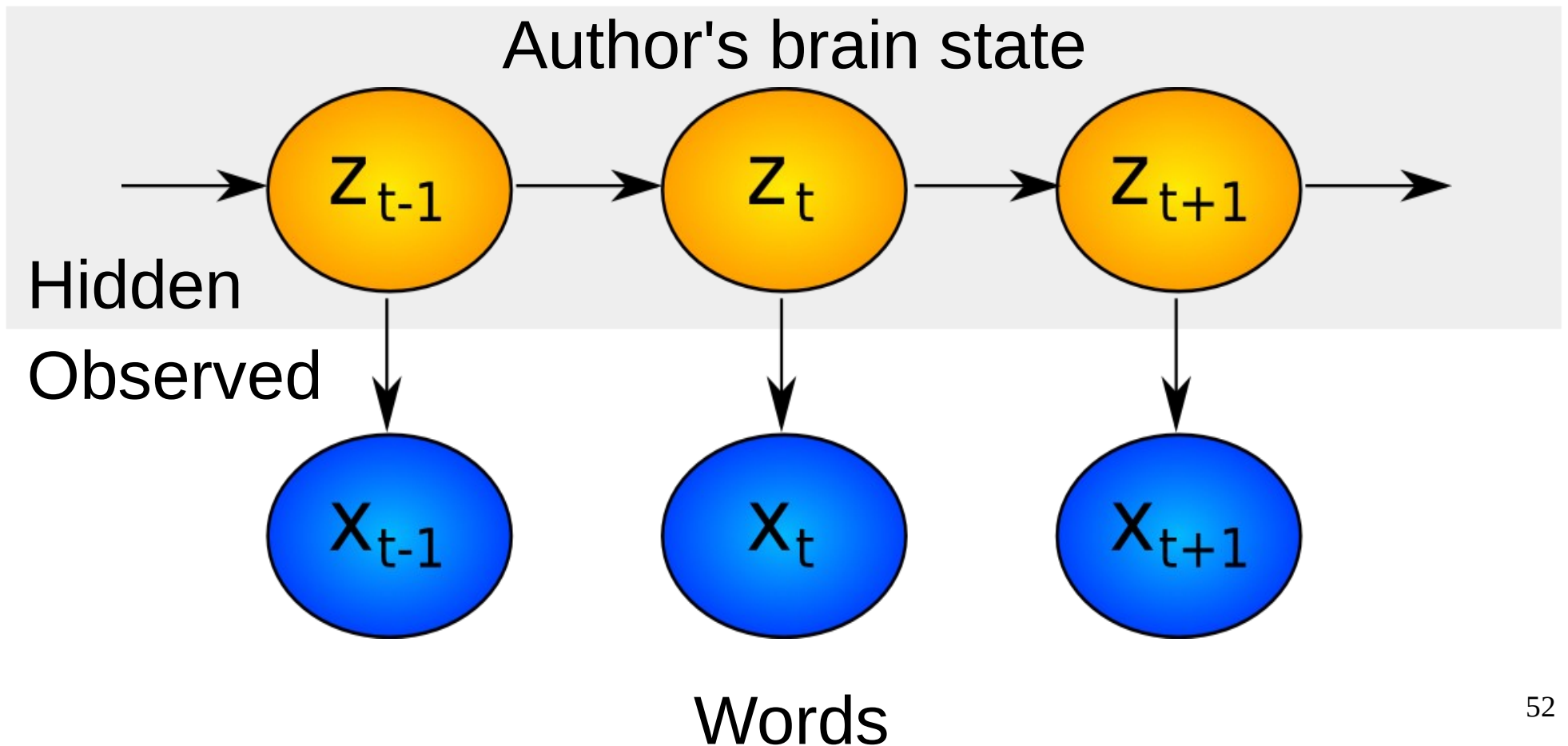
Can we learn* arbitrarily long dependencies?

* without infinitely many parameters

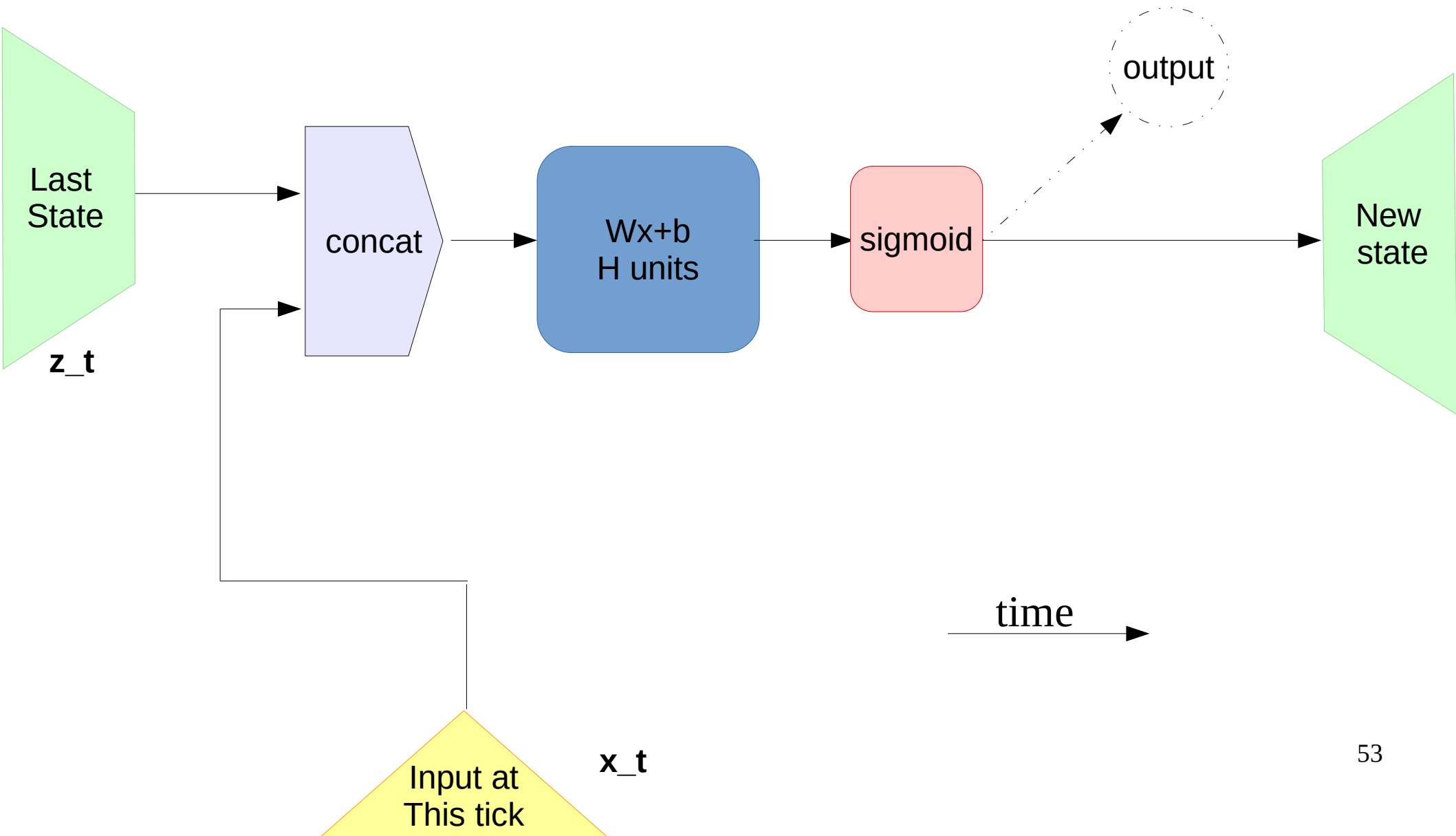
Hidden Markov Models: what's hidden



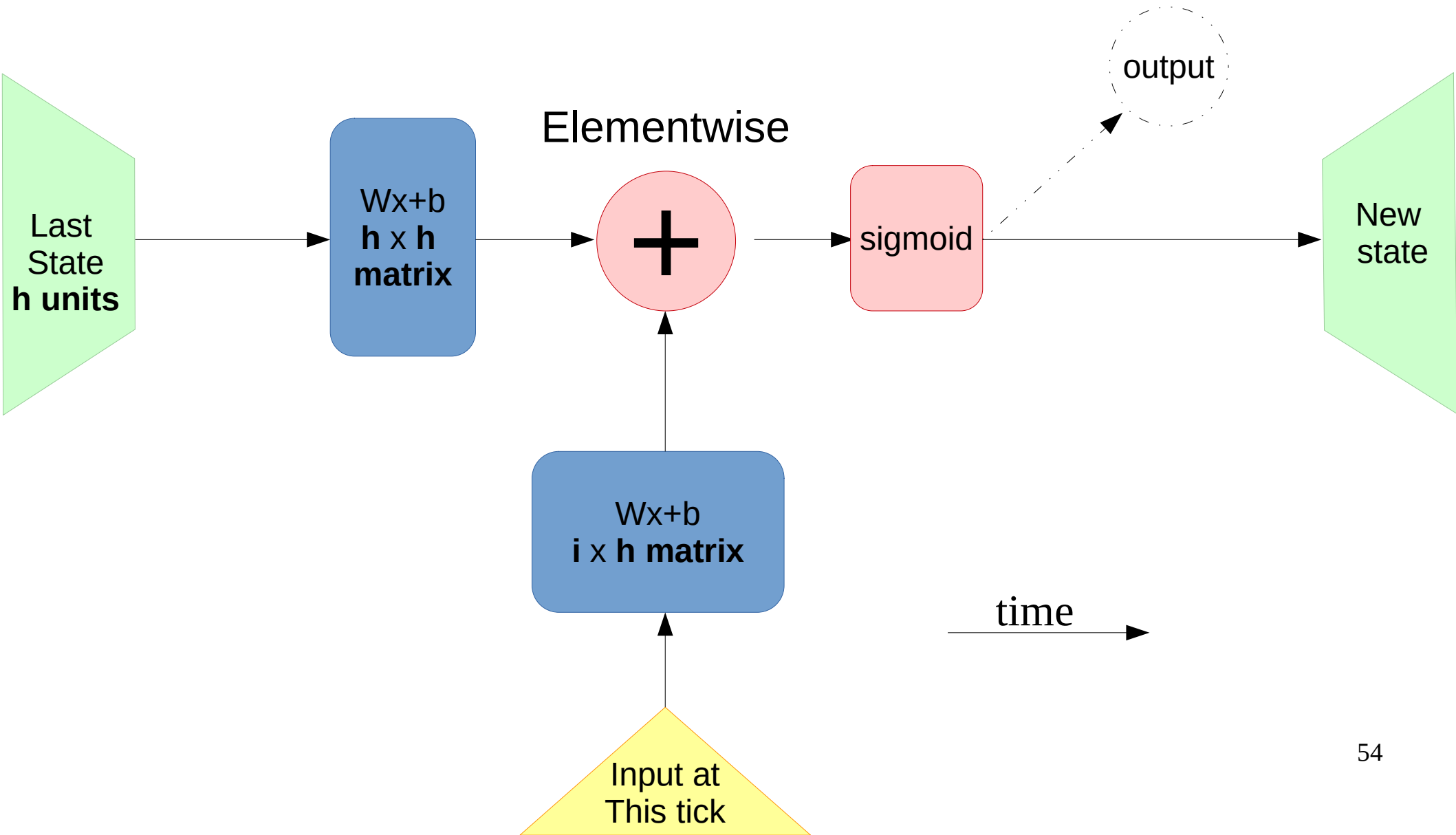
Hidden Markov Models: what is hidden



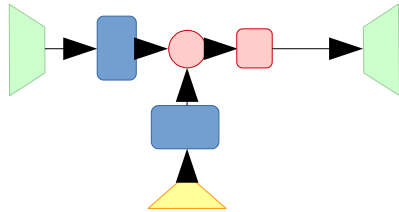
Recurrent neural network: one step



Recurrent neural network: one step

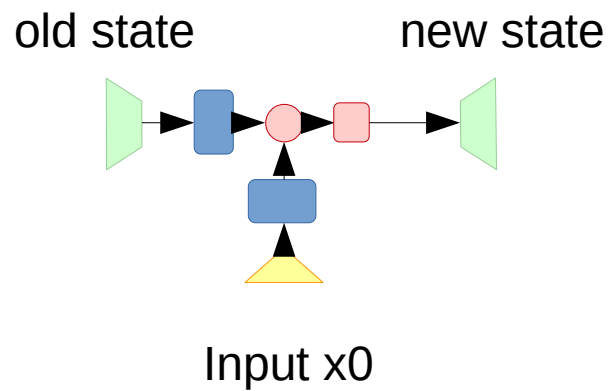


Recurrent neural network

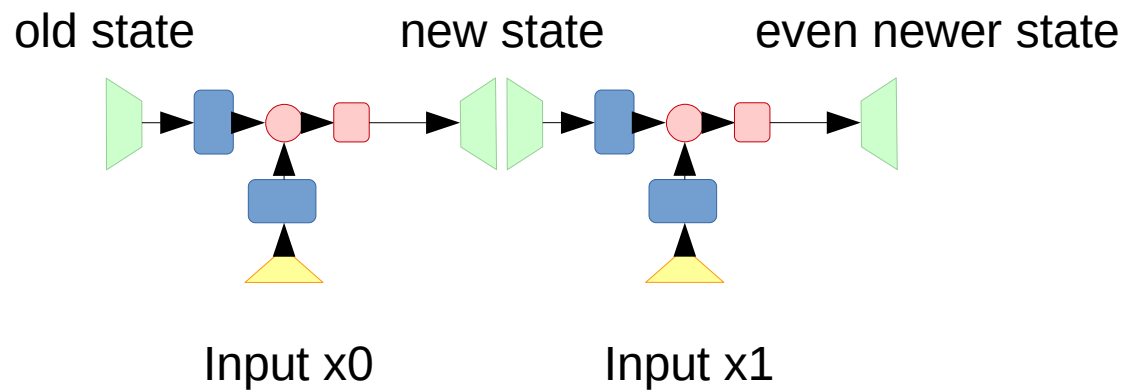


Zoom-out
of previous slide

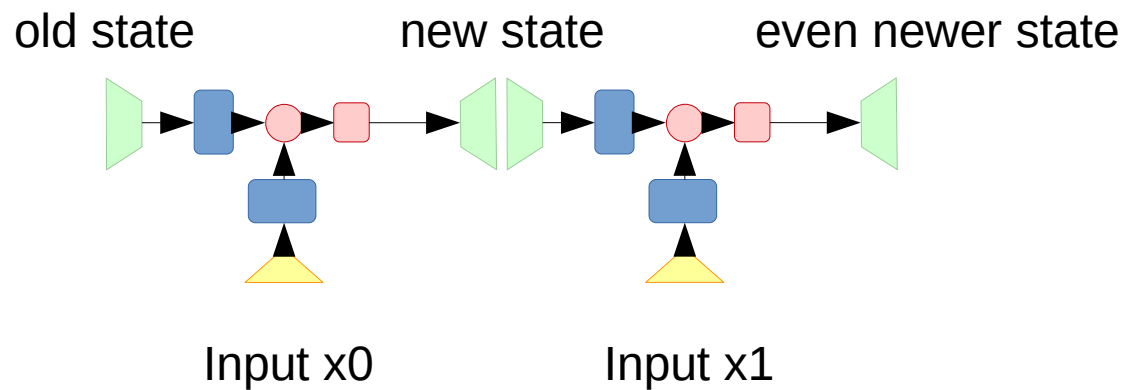
Recurrent neural network



Recurrent neural network

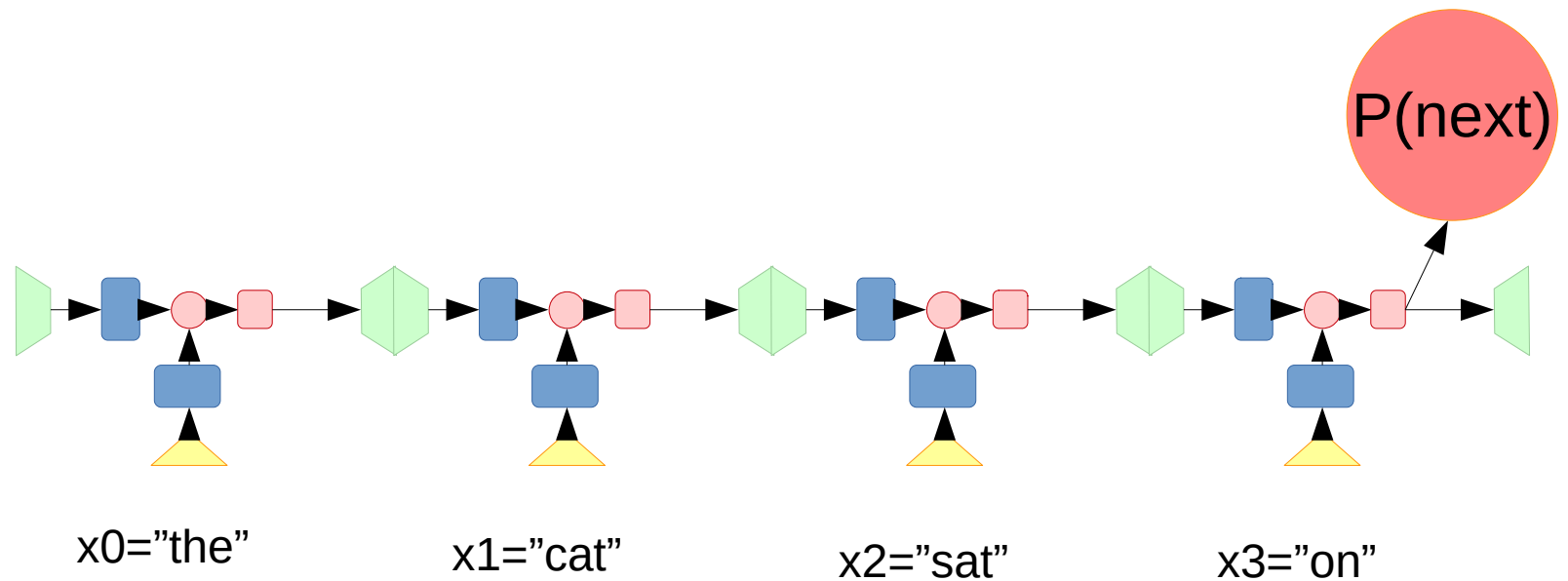


Recurrent neural network

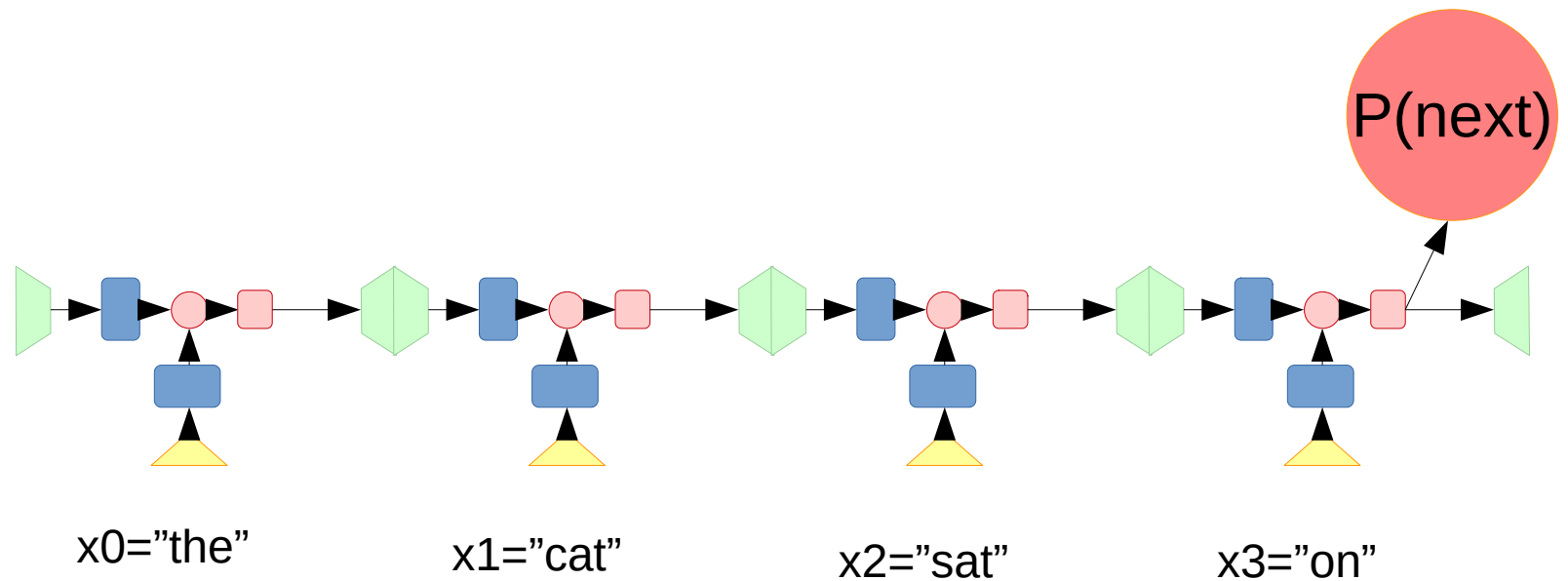


We use **same weight matrices** for all steps

Recurrent neural network

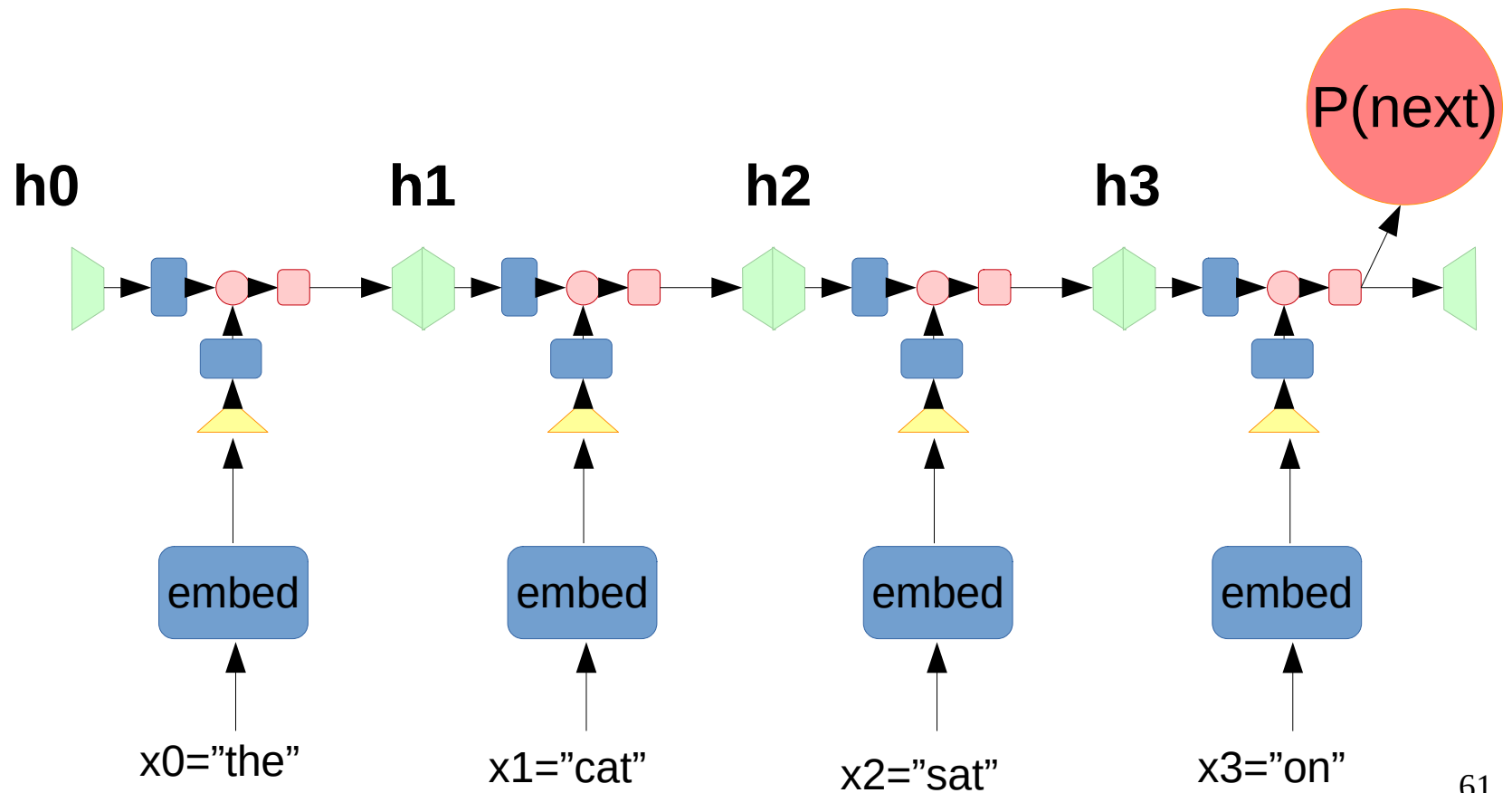


Recurrent neural network



How can we represent words?

Recurrent neural network

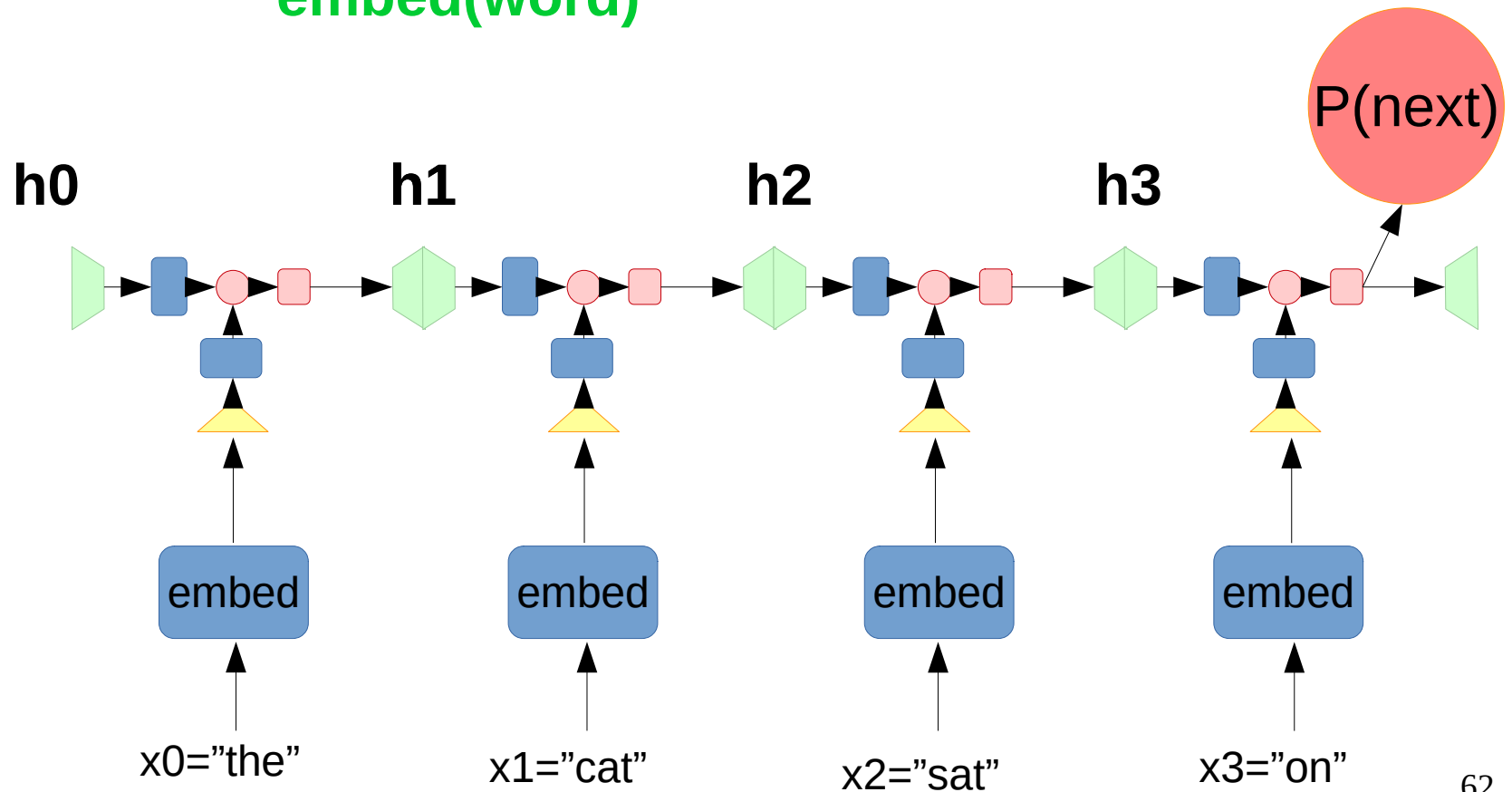


Recurrent neural network

$$h_0 = \bar{0}$$

$$h_1 = \sigma(W_{hid} \cdot h_0 + W_{inp} \cdot x_0 + b)$$

 **embed(word)**

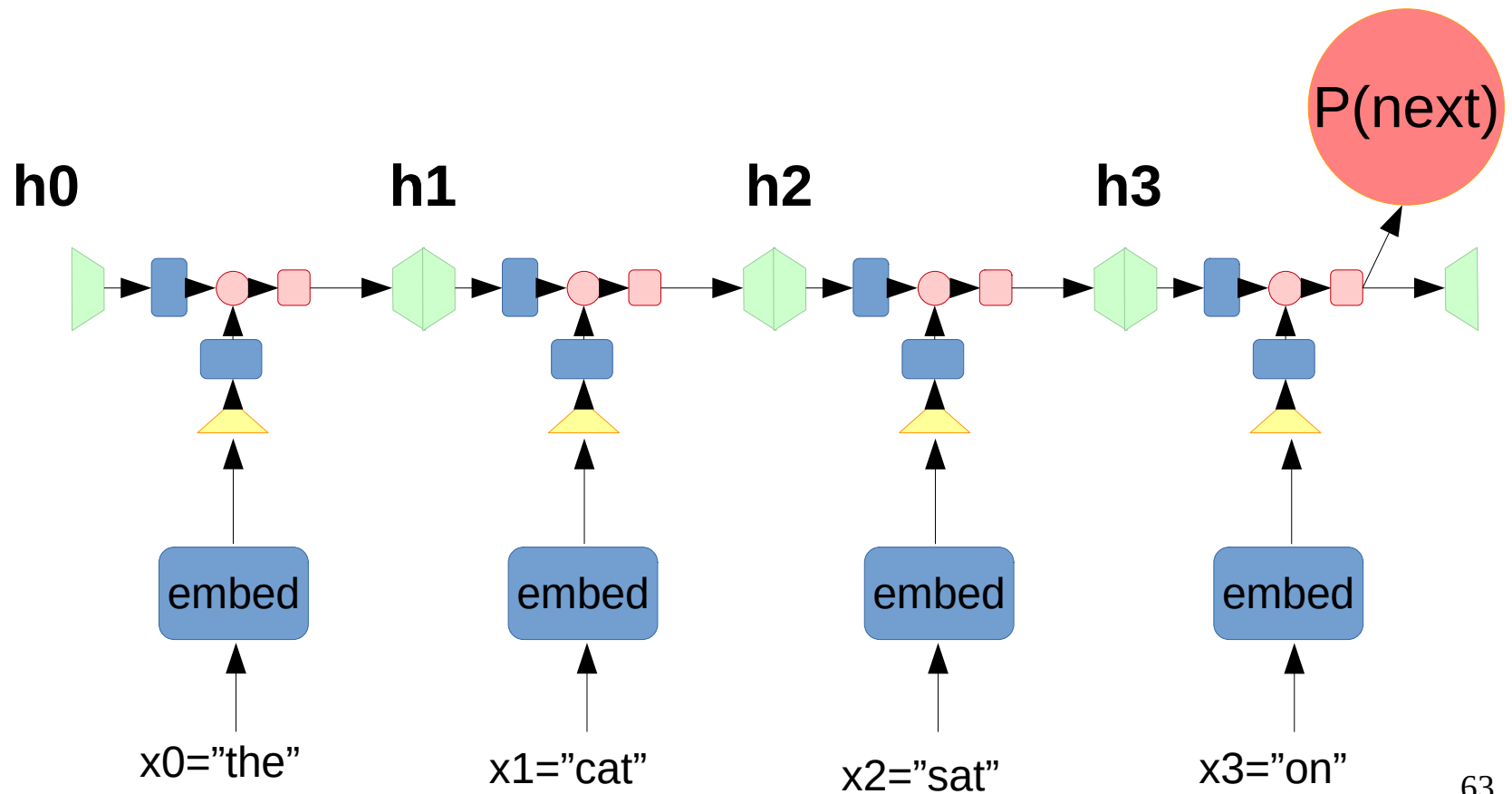


Recurrent neural network

$$h_0 = \bar{0}$$

$$h_1 = \sigma(W_{hid} \cdot h_0 + W_{inp} \cdot x_0 + b)$$

$$h_2 = ?$$



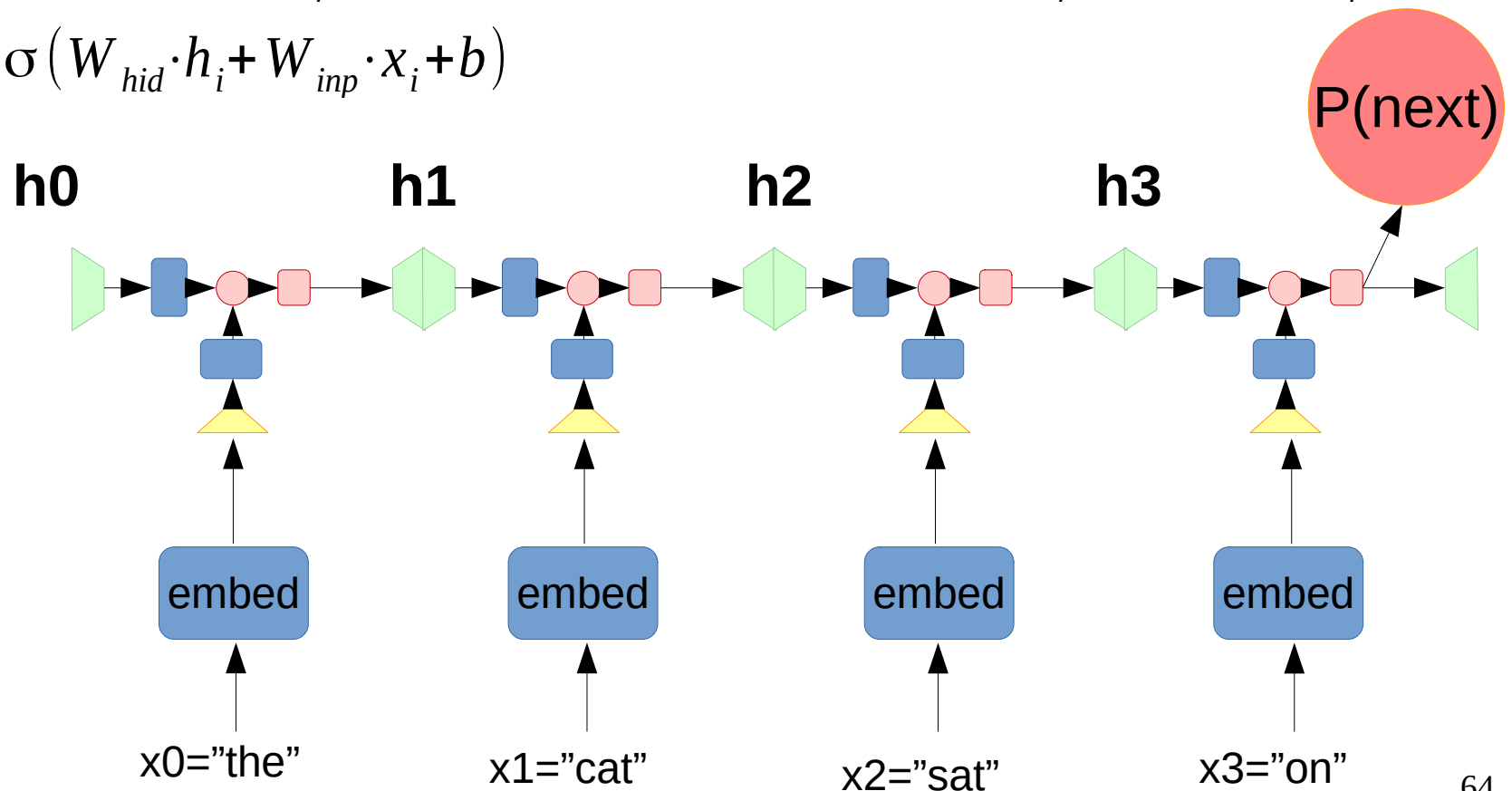
Recurrent neural network

$$h_0 = \bar{0}$$

$$h_1 = \sigma(W_{hid} \cdot h_0 + W_{inp} \cdot x_0 + b)$$

$$h_2 = \sigma(W_{hid} \cdot h_1 + W_{inp} \cdot x_1 + b) = \sigma(W_{hid} \cdot \sigma(W_{hid} \cdot h_0 + W_{inp} \cdot x_0 + b) + W_{inp} \cdot x_1 + b)$$

$$h_{i+1} = \sigma(W_{hid} \cdot h_i + W_{inp} \cdot x_i + b)$$



Recurrent neural network

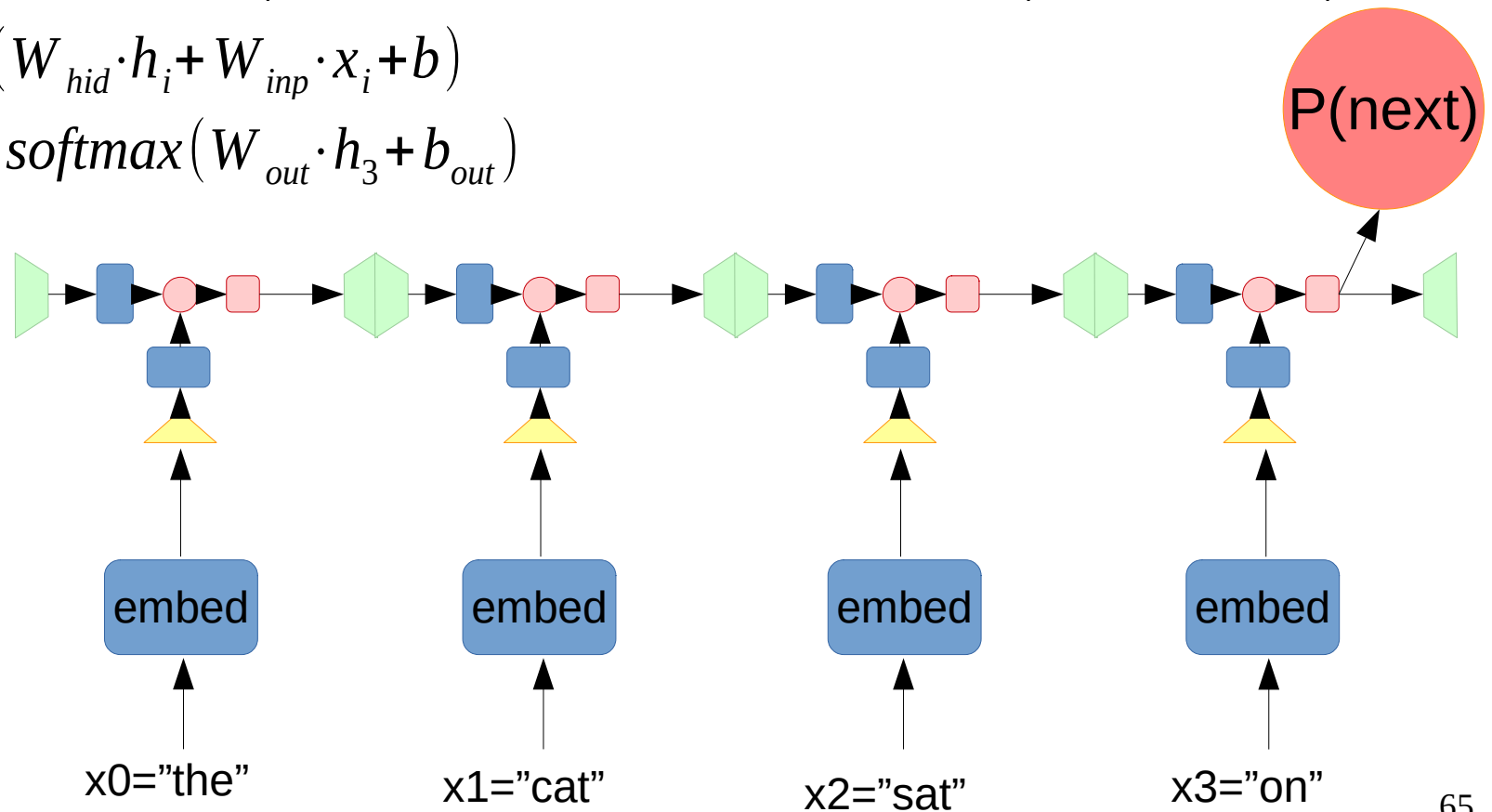
$$h_0 = \bar{0}$$

$$h_1 = \sigma(W_{hid} \cdot h_0 + W_{inp} \cdot x_0 + b)$$

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$$h_{i+1} = \sigma(W_{hid} \cdot h_i + W_{inp} \cdot x_i + b)$$

$$P(x_4) = \text{softmax}(W_{out} \cdot h_3 + b_{out})$$

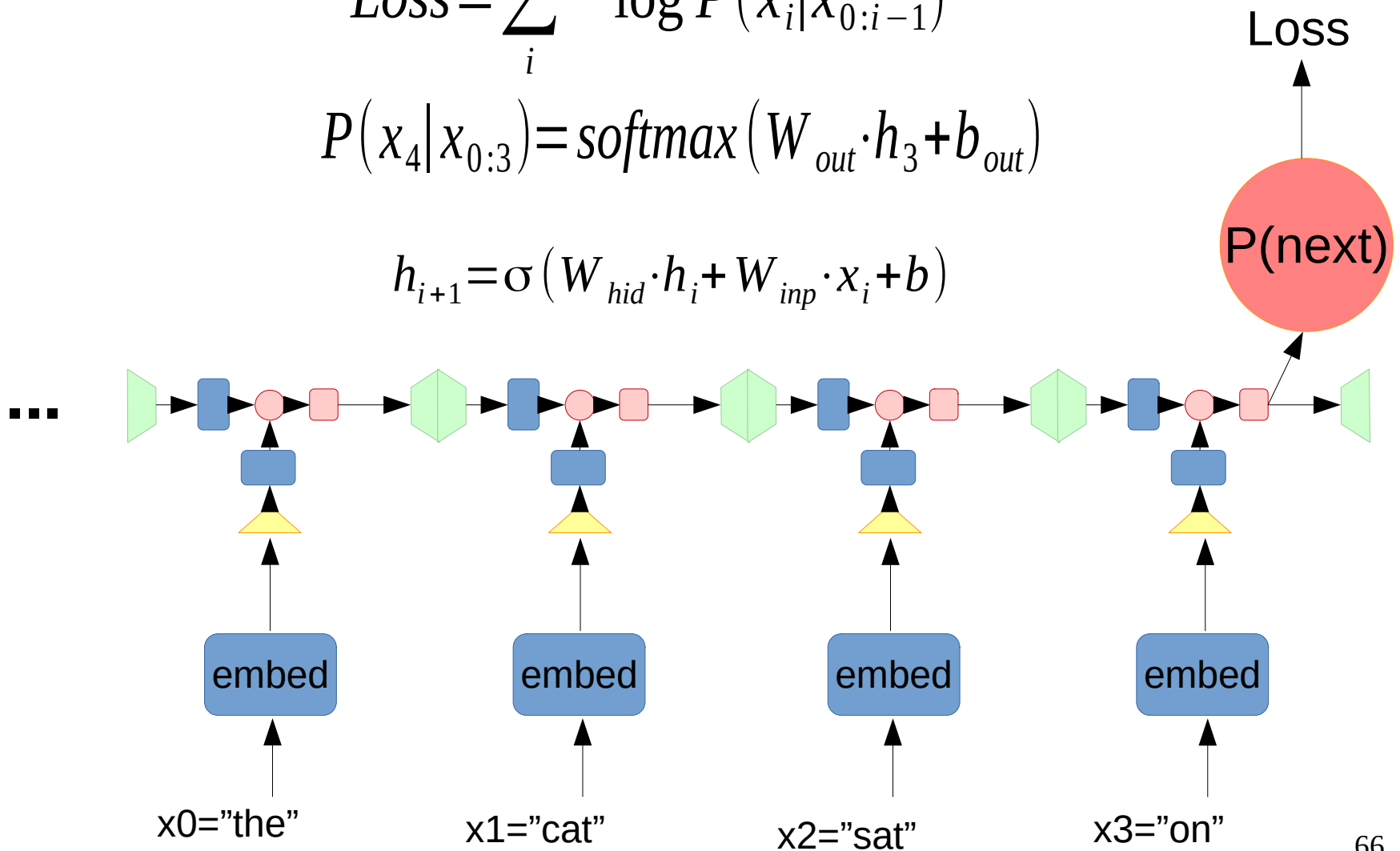


Recurrent neural network

$$Loss = \sum_i -\log P(x_i | x_{0:i-1})$$

$$P(x_4 | x_{0:3}) = \text{softmax}(W_{out} \cdot h_3 + b_{out})$$

$$h_{i+1} = \sigma(W_{hid} \cdot h_i + W_{inp} \cdot x_i + b)$$



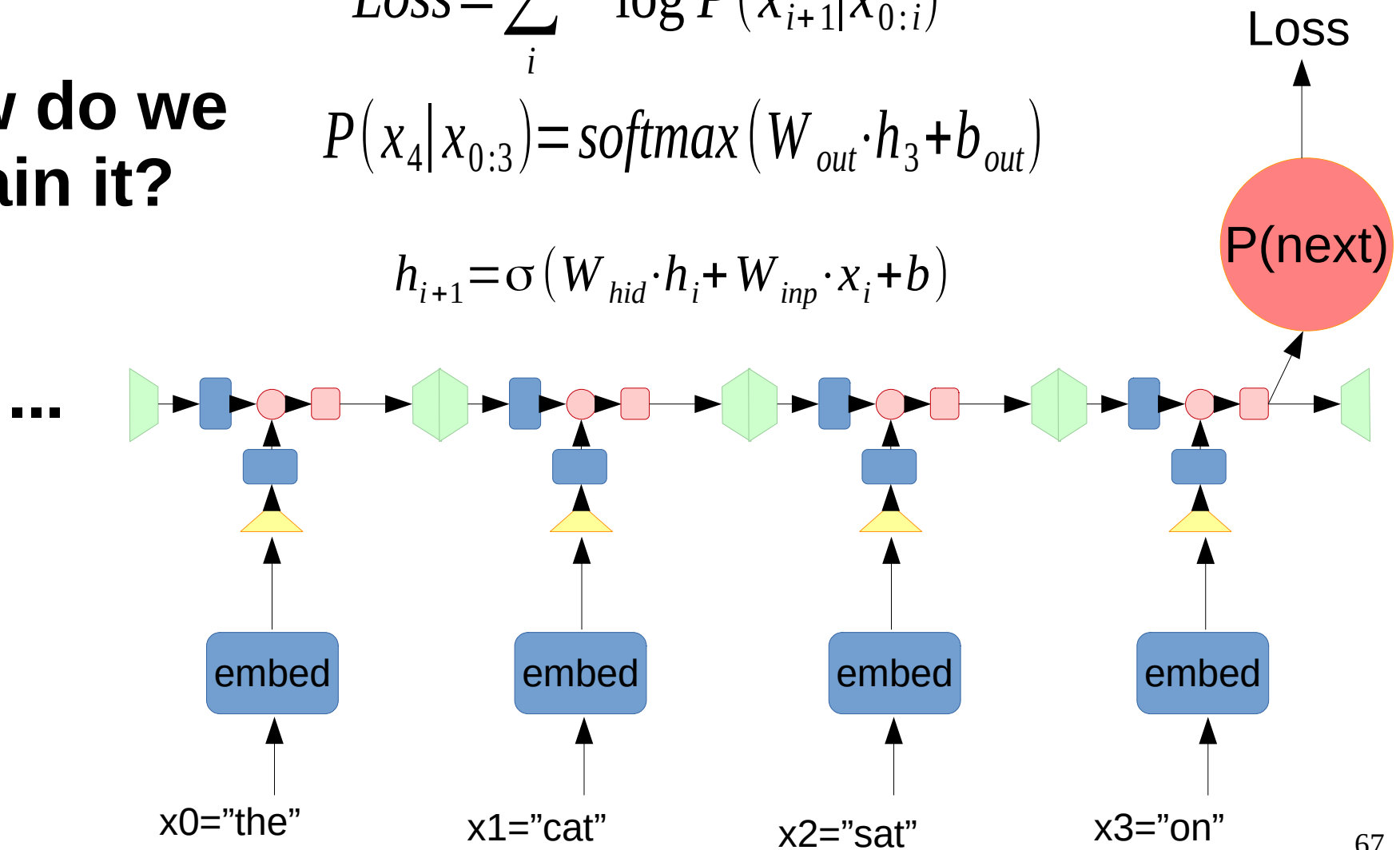
Recurrent neural network

**How do we
train it?**

$$Loss = \sum_i -\log P(x_{i+1} | x_{0:i})$$

$$P(x_4 | x_{0:3}) = \text{softmax}(W_{out} \cdot h_3 + b_{out})$$

$$h_{i+1} = \sigma(W_{hid} \cdot h_i + W_{inp} \cdot x_i + b)$$

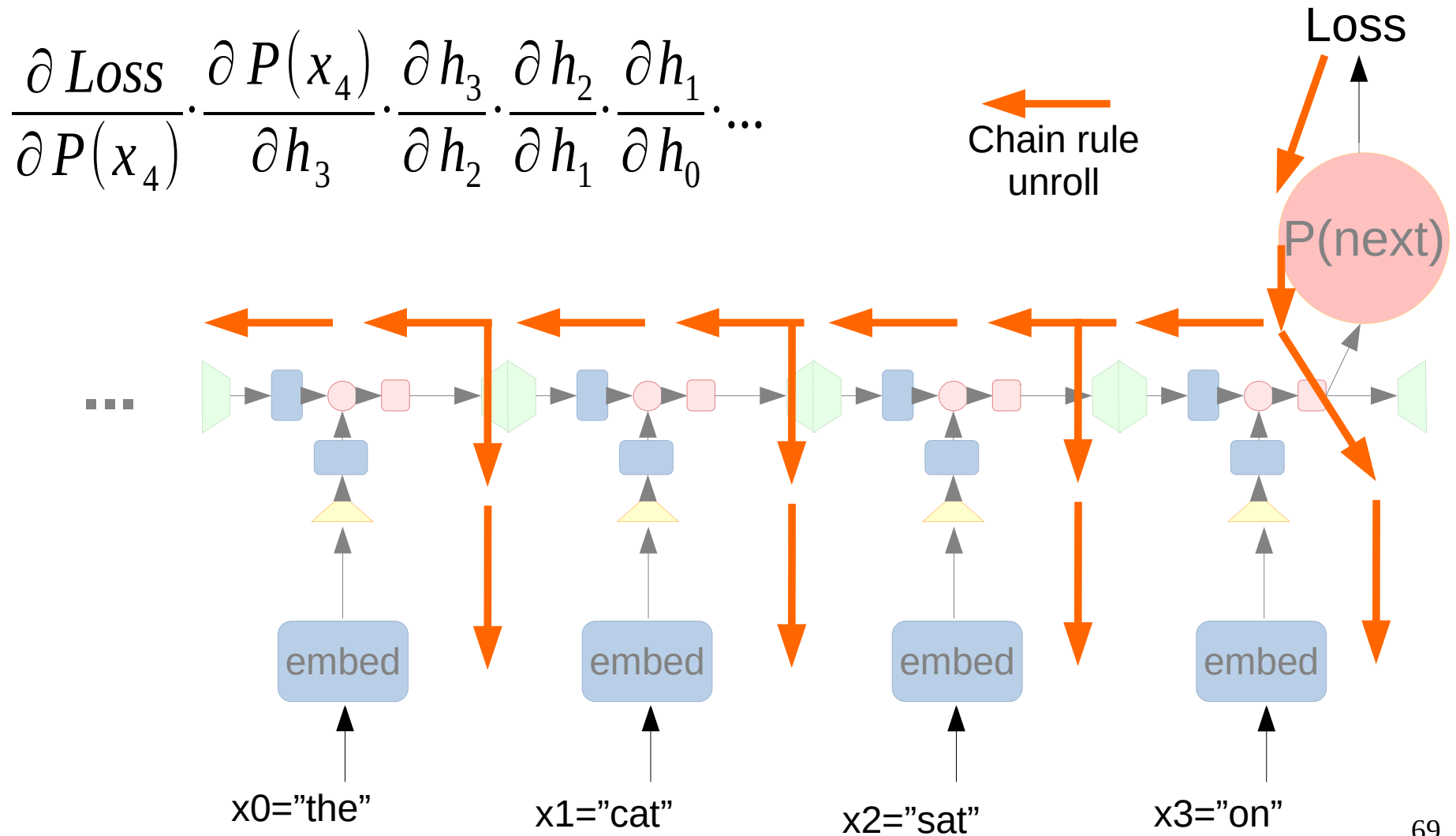


**WHAT ARE WE DOING TODAY,
BRAIN?**

**THE SAME THING WE DO EVERY DAY, PINKY.
BACKPROPAGATE**

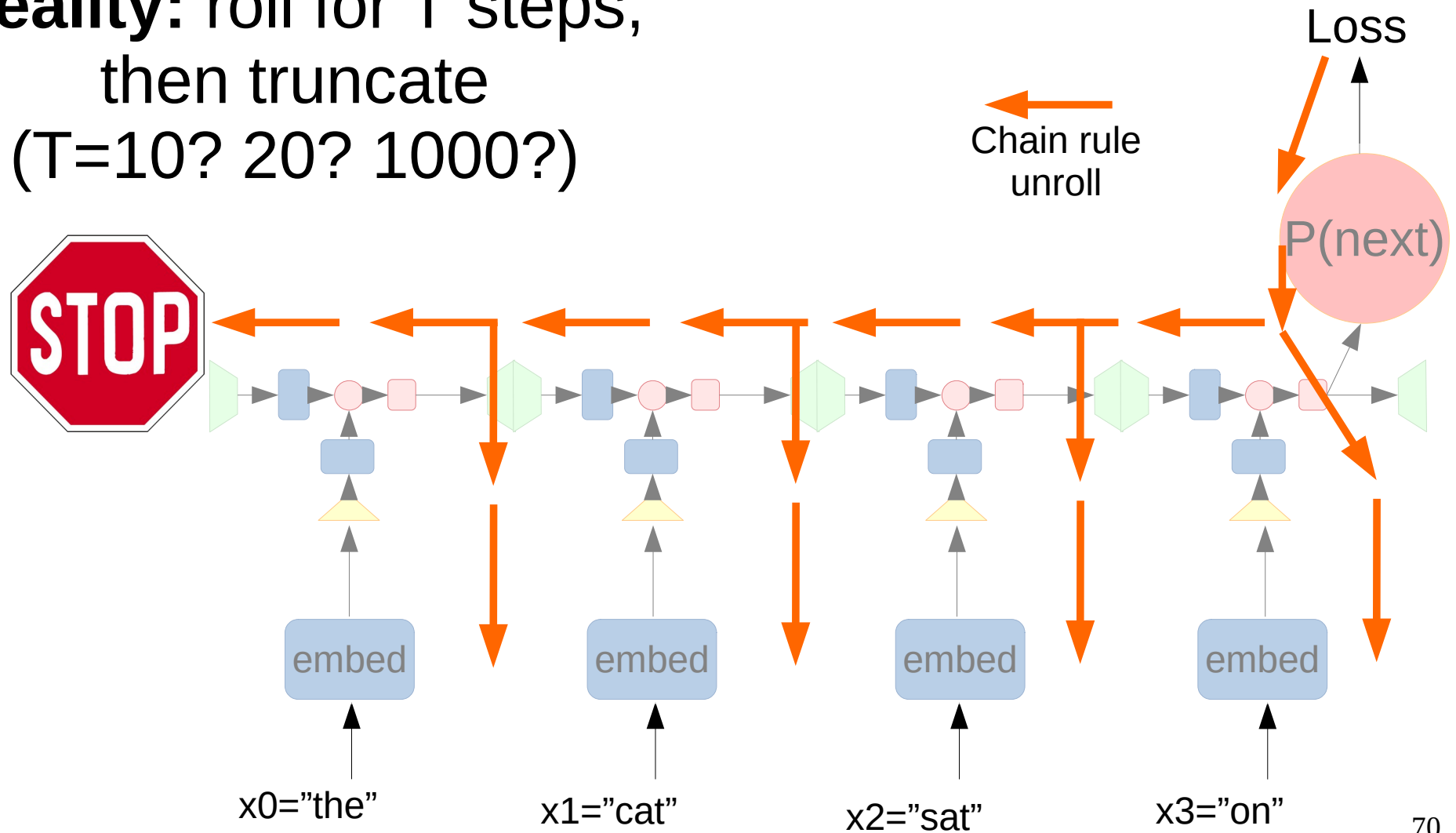
memegenerator.net

Backpropagation through time



Truncated BPTT

Reality: roll for T steps,
then truncate
(T=10? 20? 1000?)



End of part 1

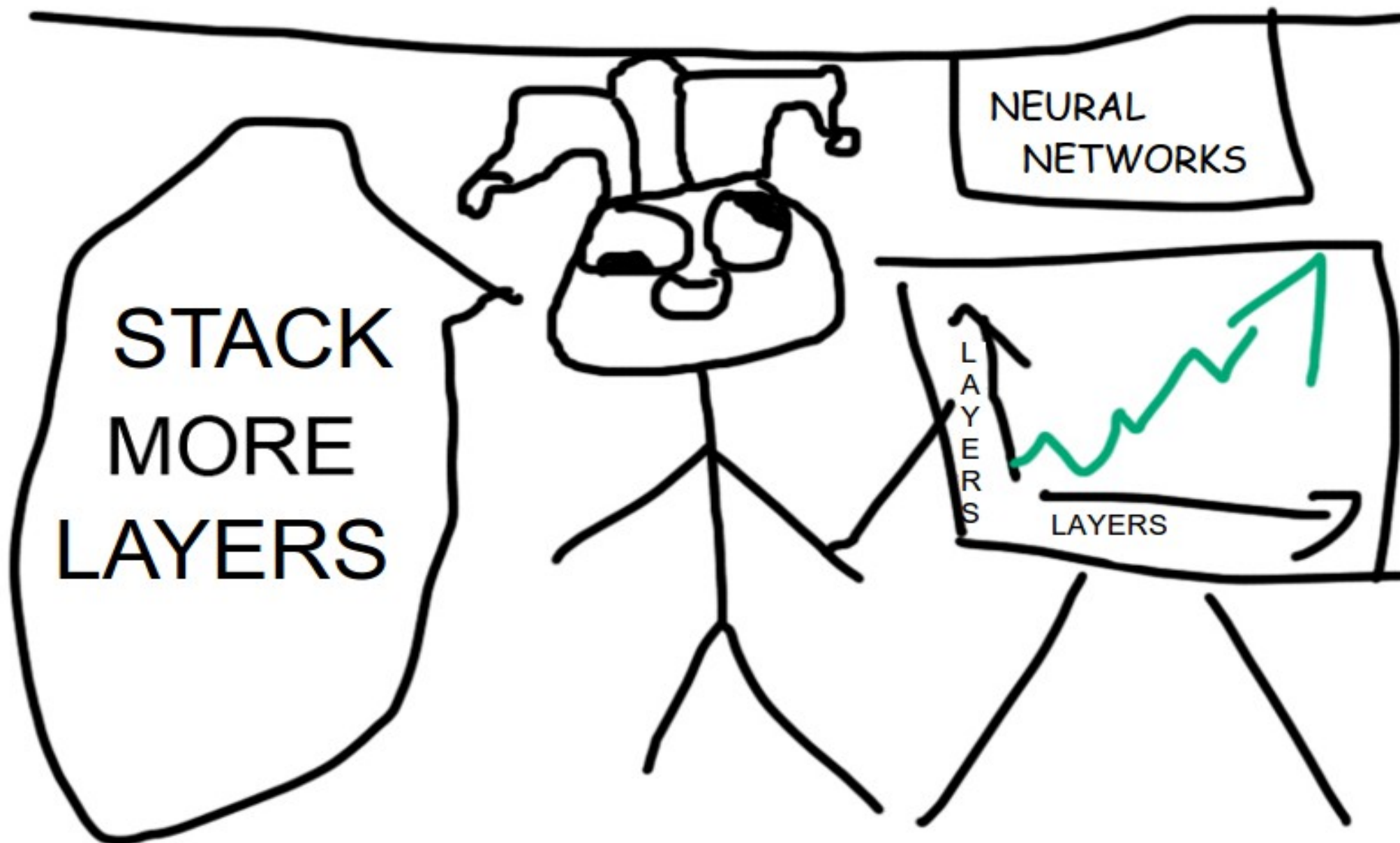
Questions for coffee break:

A) how would you apply
RNN
to generate random
handwriting?

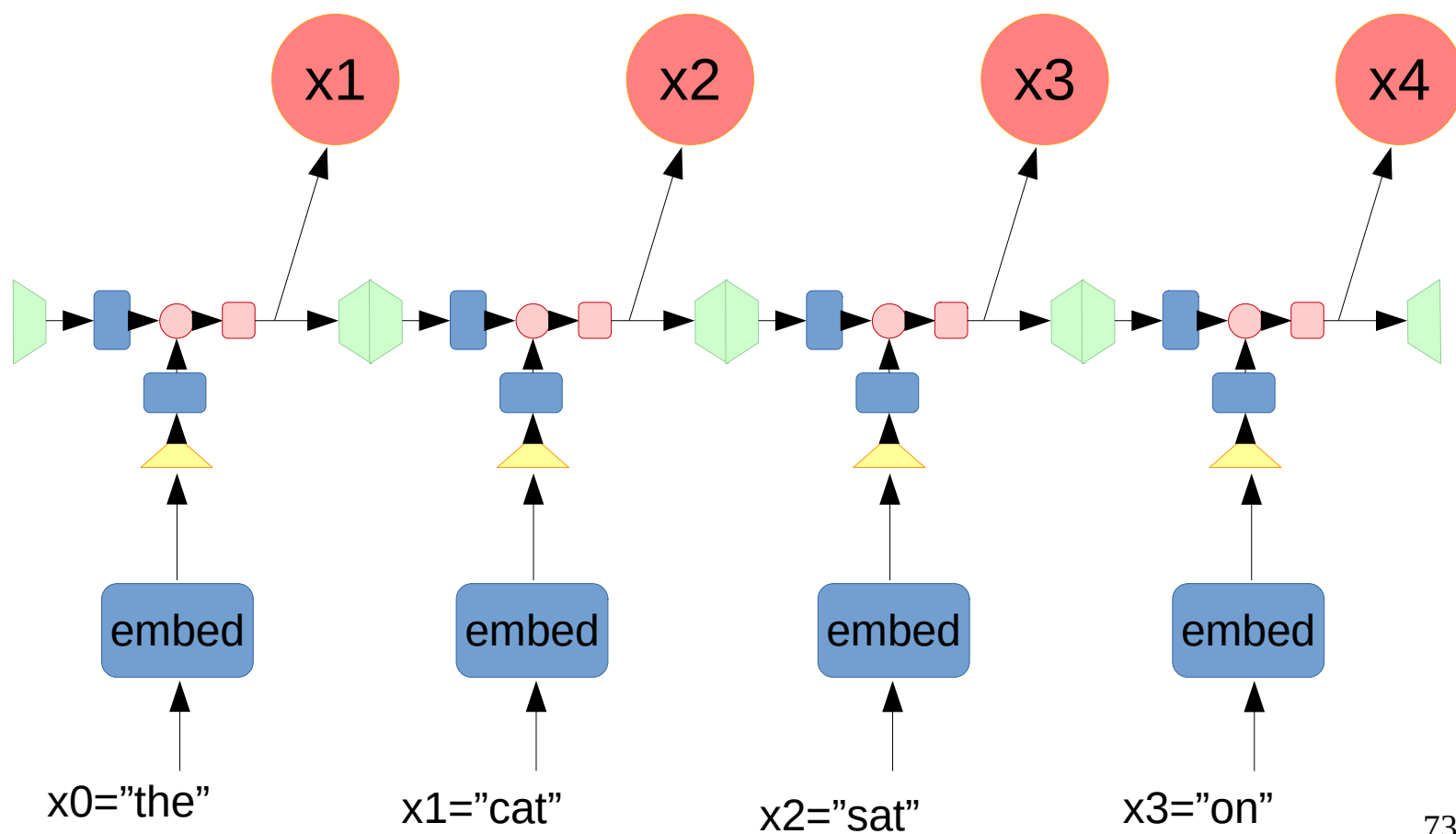
Machine learning Mastery
Machine Learning Mastery
Machine Learning Mastery

B) how would you
apply RNN
for sentiment
classification?



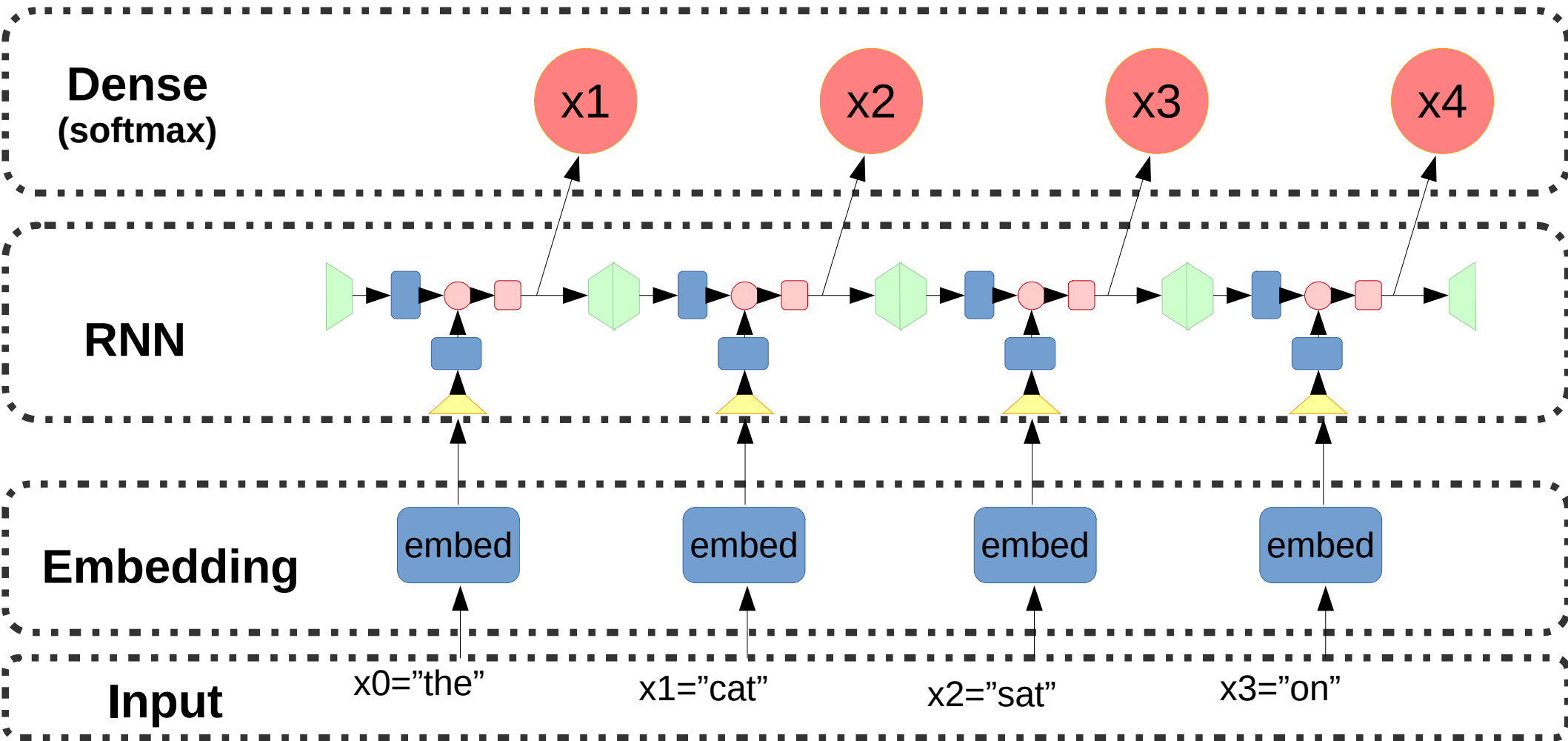


What is layer, again?

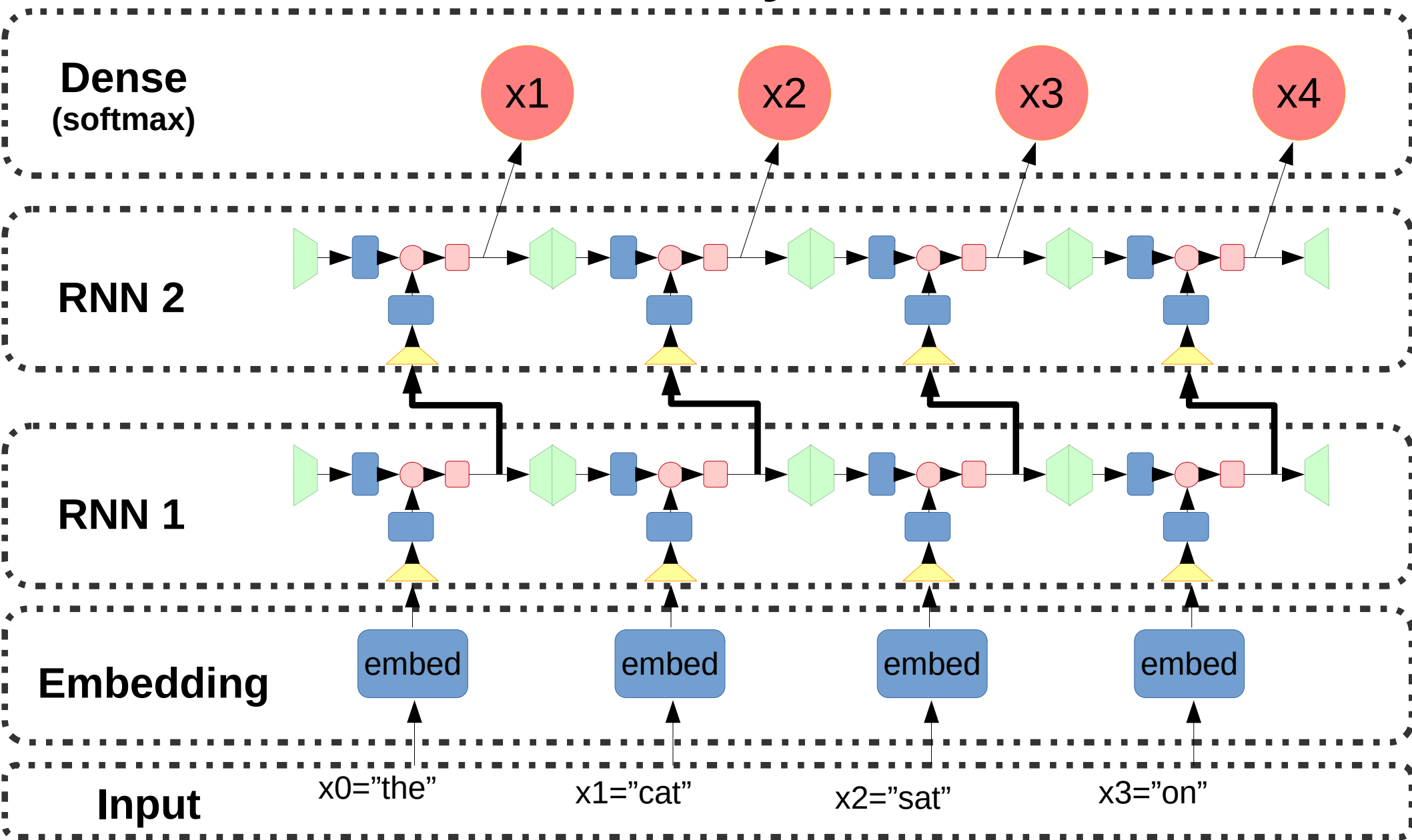


Layers

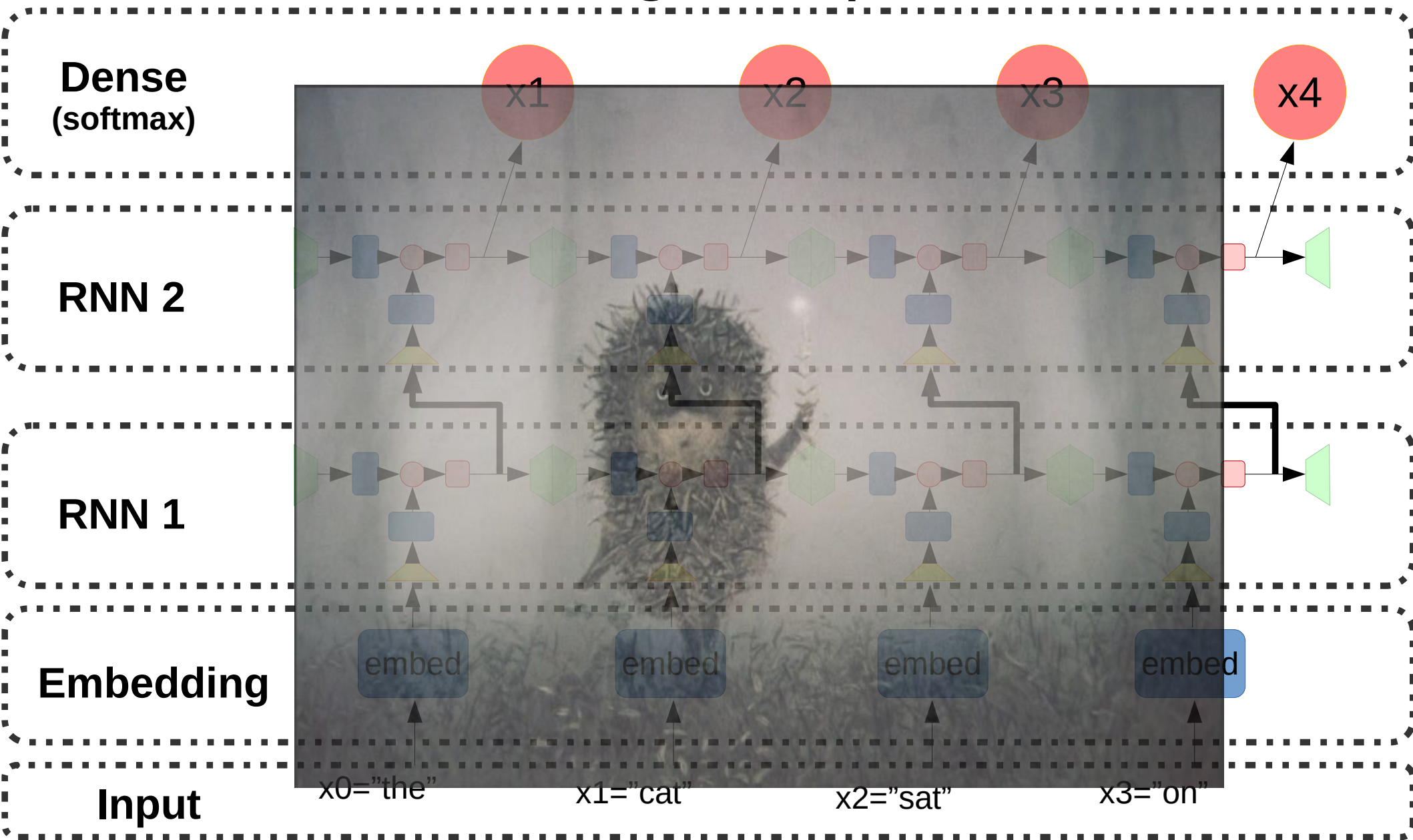
Where to stick more layers?



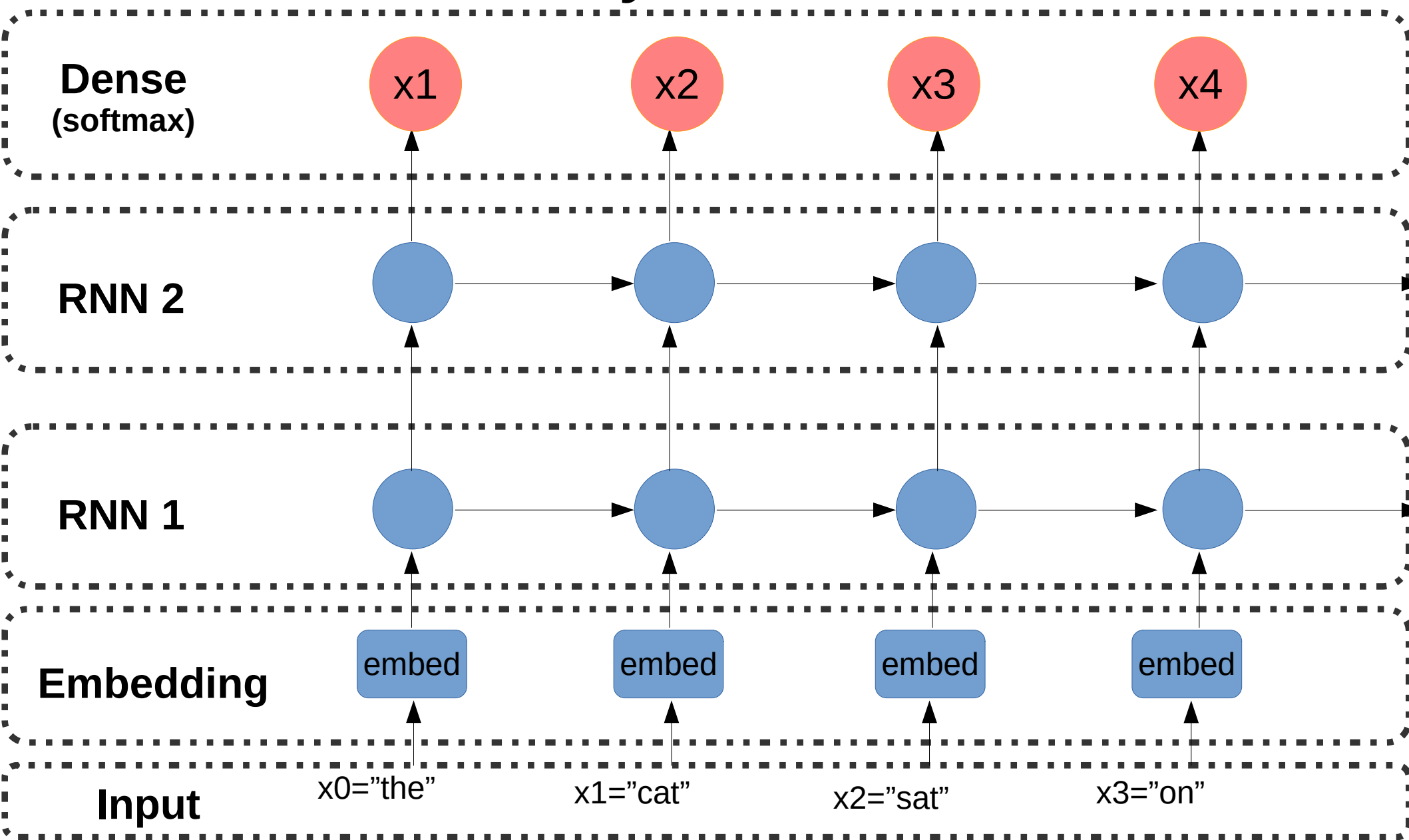
More layers



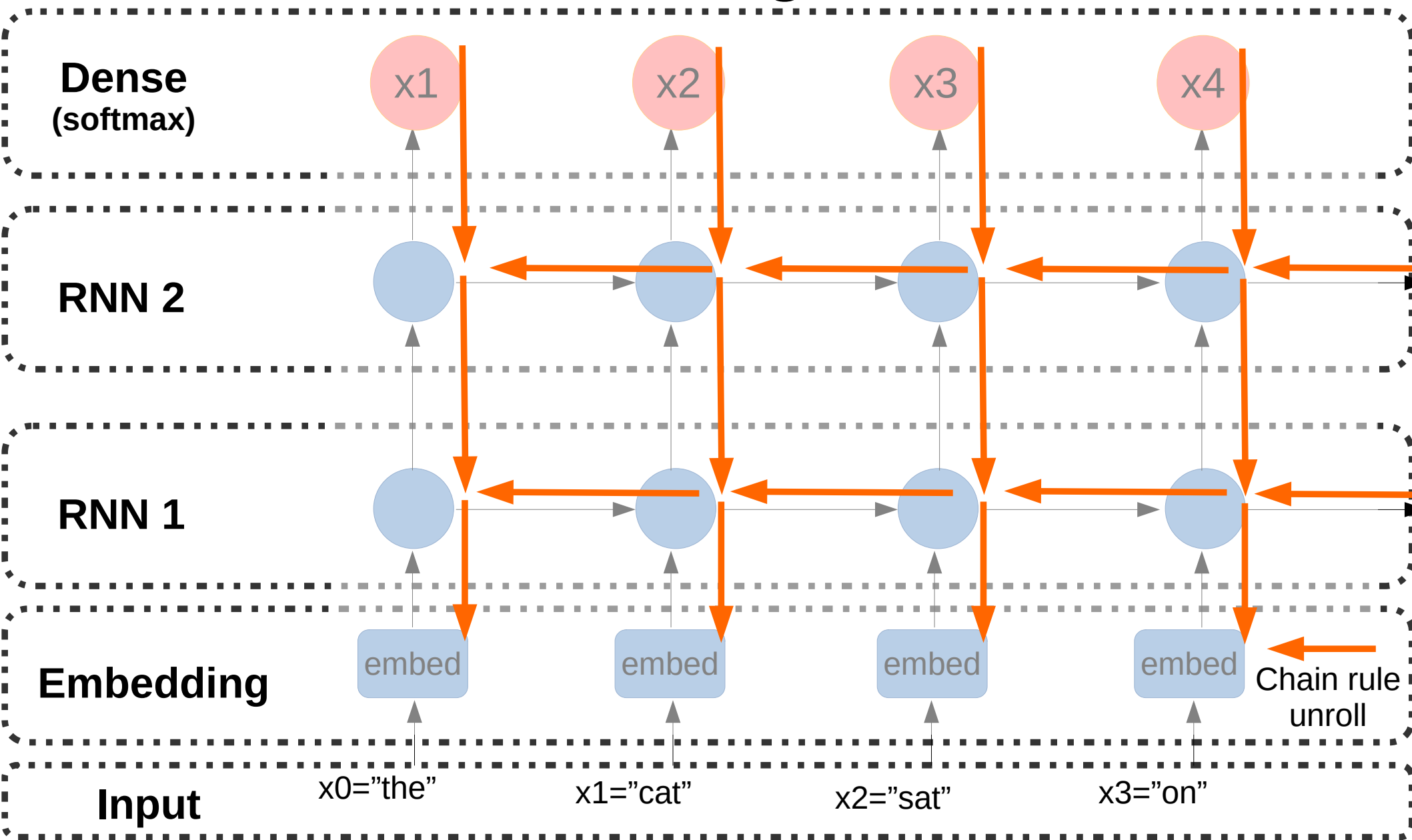
Too f**king complicated



2-layer RNN



BPTT again

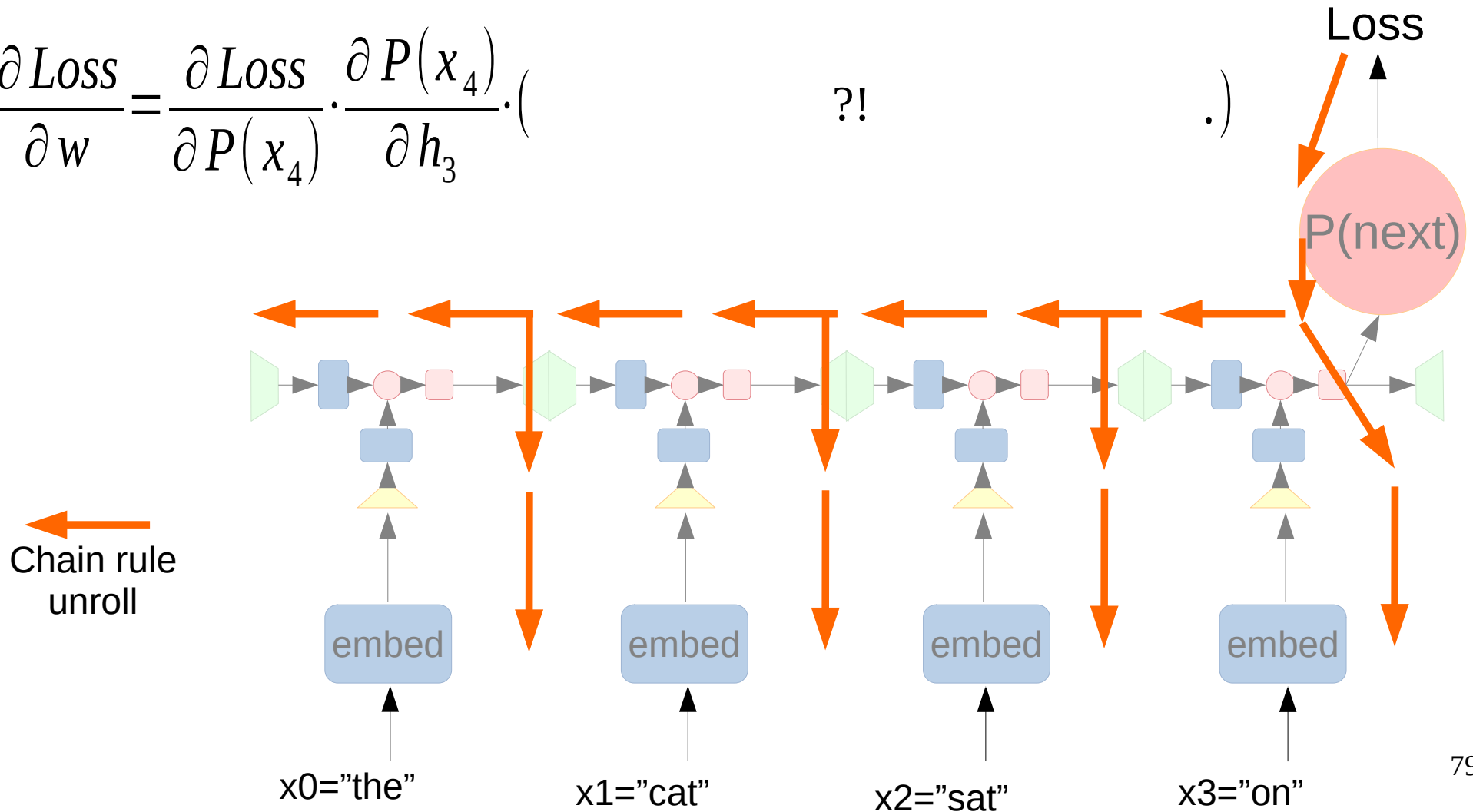


BPTT Again

$$h_{i+1} = \sigma(W_{hid} \cdot h_i + W_{inp} \cdot x_i + b)$$

$$\frac{\partial Loss}{\partial w} = \frac{\partial Loss}{\partial P(x_4)} \cdot \frac{\partial P(x_4)}{\partial h_3} \cdot ($$

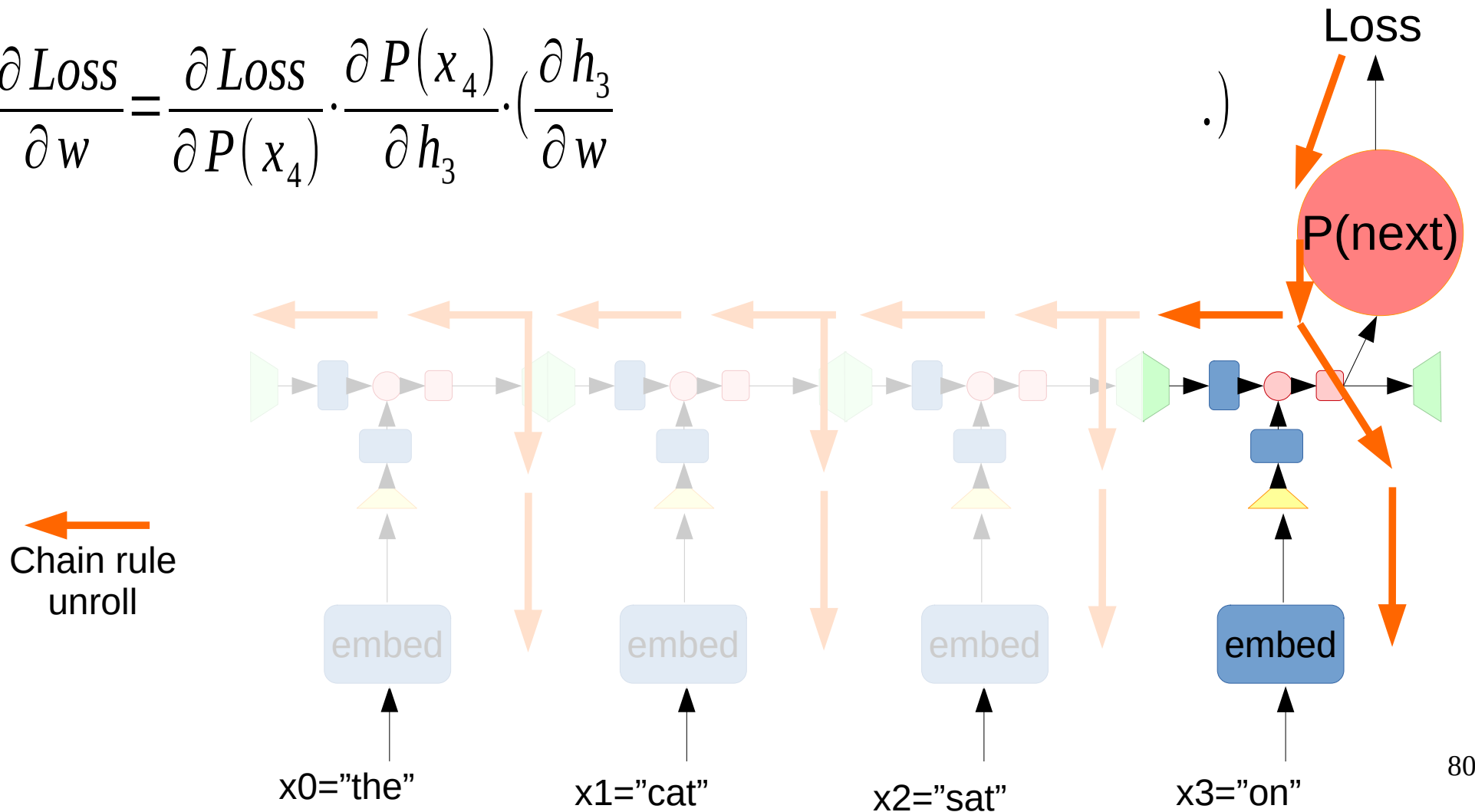
?!)



BPTT Again

$$h_{i+1} = \sigma(W_{hid} \cdot h_i + W_{inp} \cdot x_i + b)$$

$$\frac{\partial Loss}{\partial w} = \frac{\partial Loss}{\partial P(x_4)} \cdot \frac{\partial P(x_4)}{\partial h_3} \cdot \left(\frac{\partial h_3}{\partial w} \right)$$

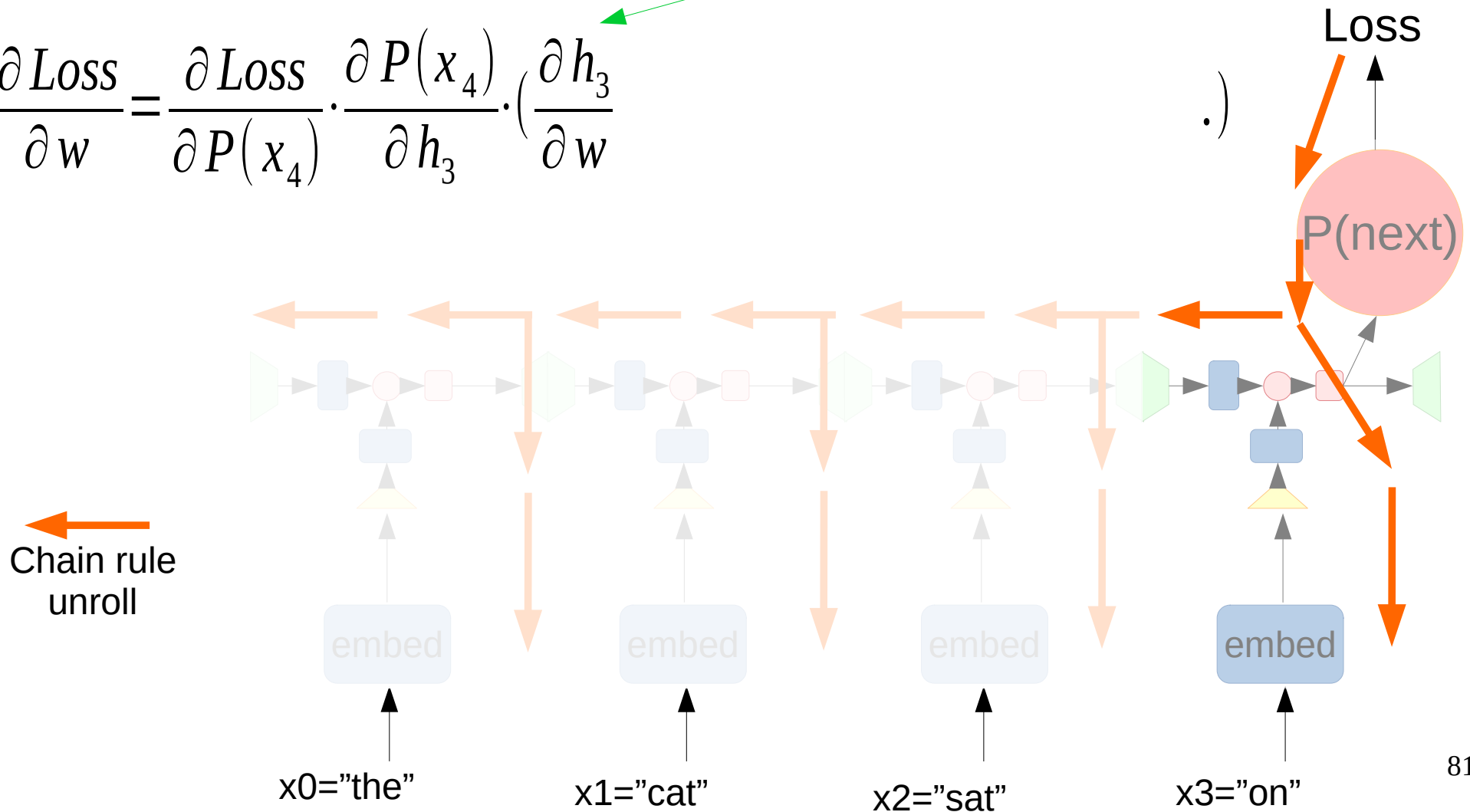


BPTT Again

$$h_{i+1} = \sigma(W_{hid} \cdot h_i + W_{inp} \cdot x_i + b)$$

consider h_2 constant

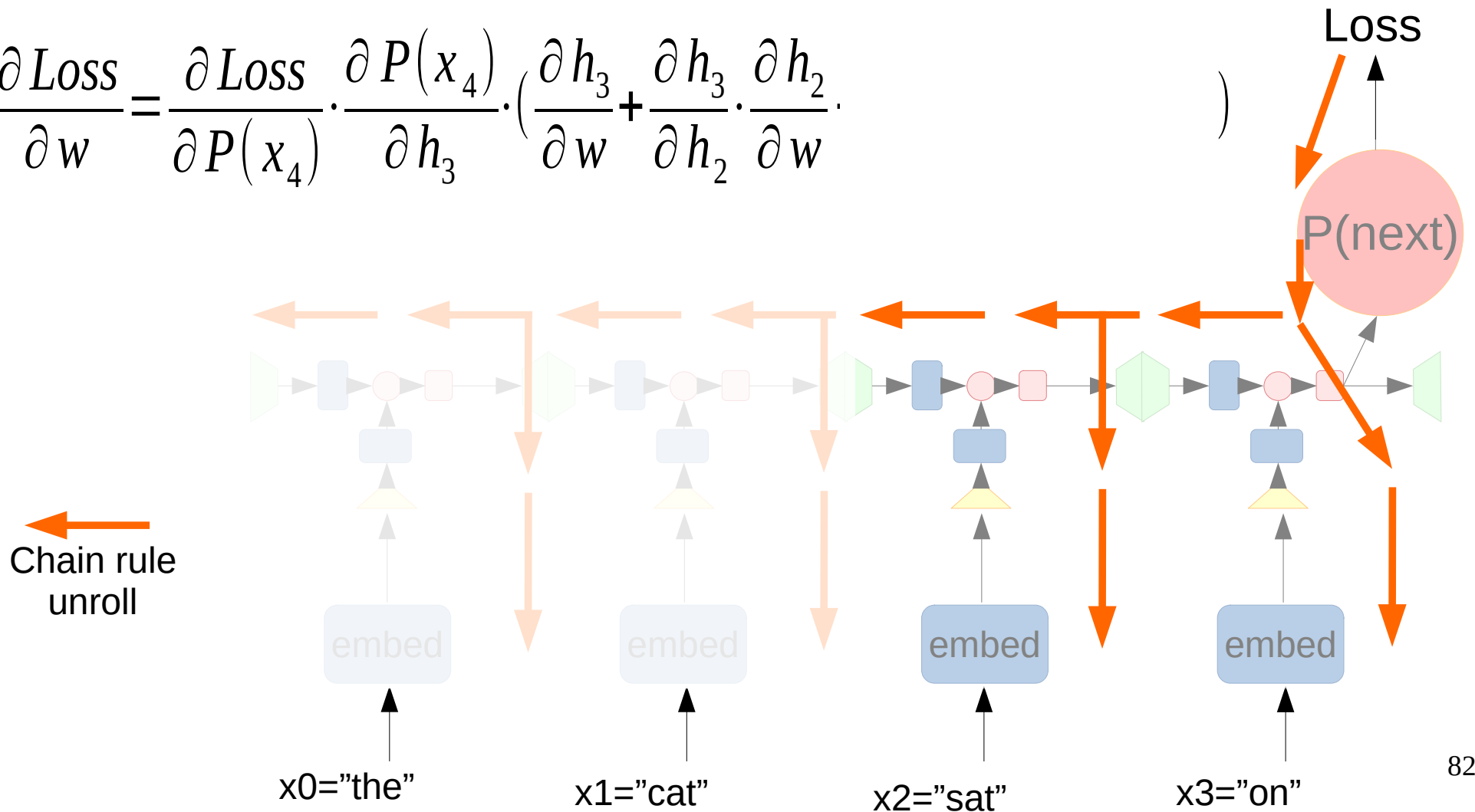
$$\frac{\partial Loss}{\partial w} = \frac{\partial Loss}{\partial P(x_4)} \cdot \frac{\partial P(x_4)}{\partial h_3} \cdot \left(\frac{\partial h_3}{\partial w} \right)$$



BPTT Again

$$h_{i+1} = \sigma(W_{hid} \cdot h_i + W_{inp} \cdot x_i + b)$$

$$\frac{\partial Loss}{\partial w} = \frac{\partial Loss}{\partial P(x_4)} \cdot \frac{\partial P(x_4)}{\partial h_3} \cdot \left(\frac{\partial h_3}{\partial w} + \frac{\partial h_3}{\partial h_2} \cdot \frac{\partial h_2}{\partial w} \right)$$

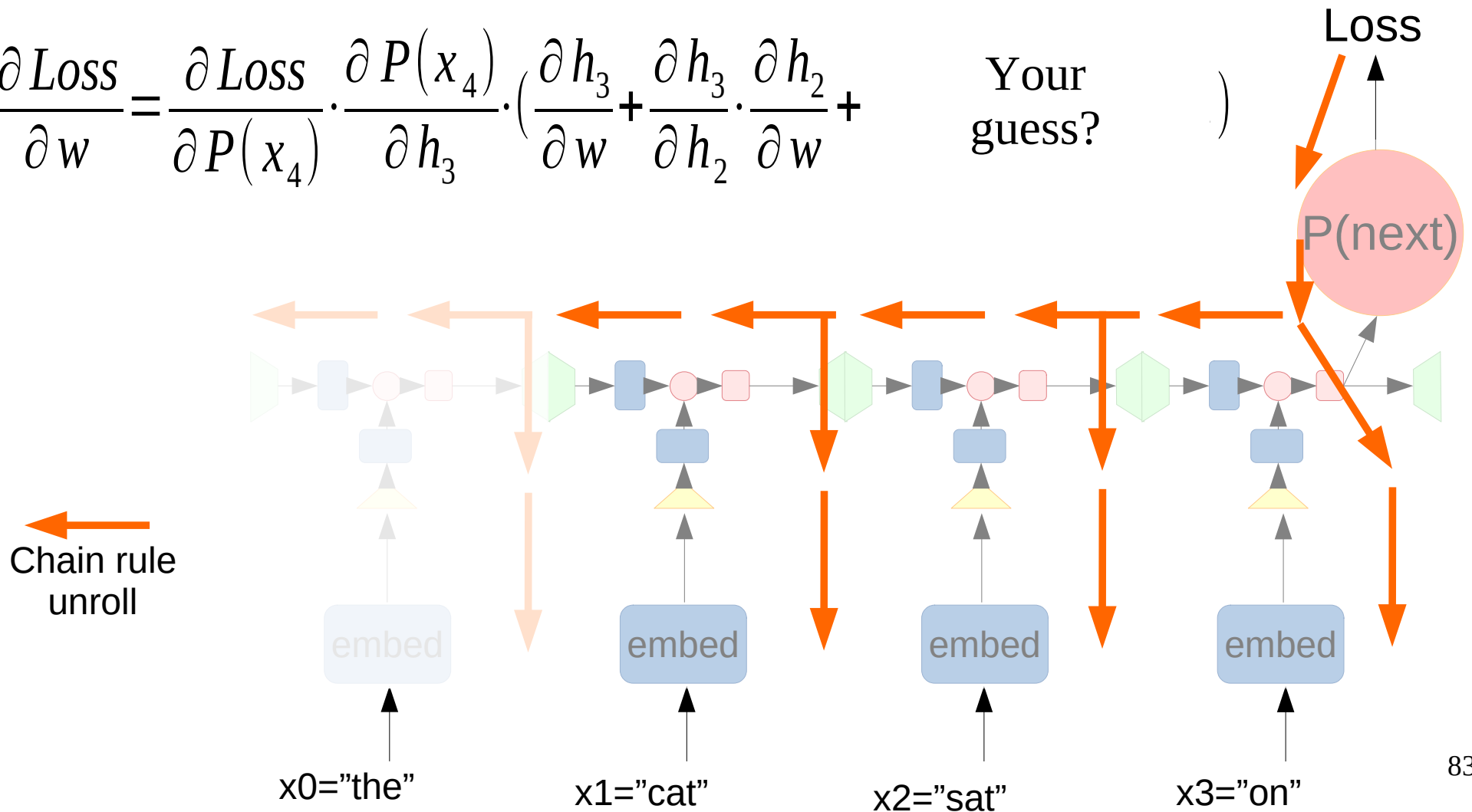


BPTT Again

$$h_{i+1} = \sigma(W_{hid} \cdot h_i + W_{inp} \cdot x_i + b)$$

$$\frac{\partial Loss}{\partial w} = \frac{\partial Loss}{\partial P(x_4)} \cdot \frac{\partial P(x_4)}{\partial h_3} \cdot \left(\frac{\partial h_3}{\partial w} + \frac{\partial h_3}{\partial h_2} \cdot \frac{\partial h_2}{\partial w} + \dots \right)$$

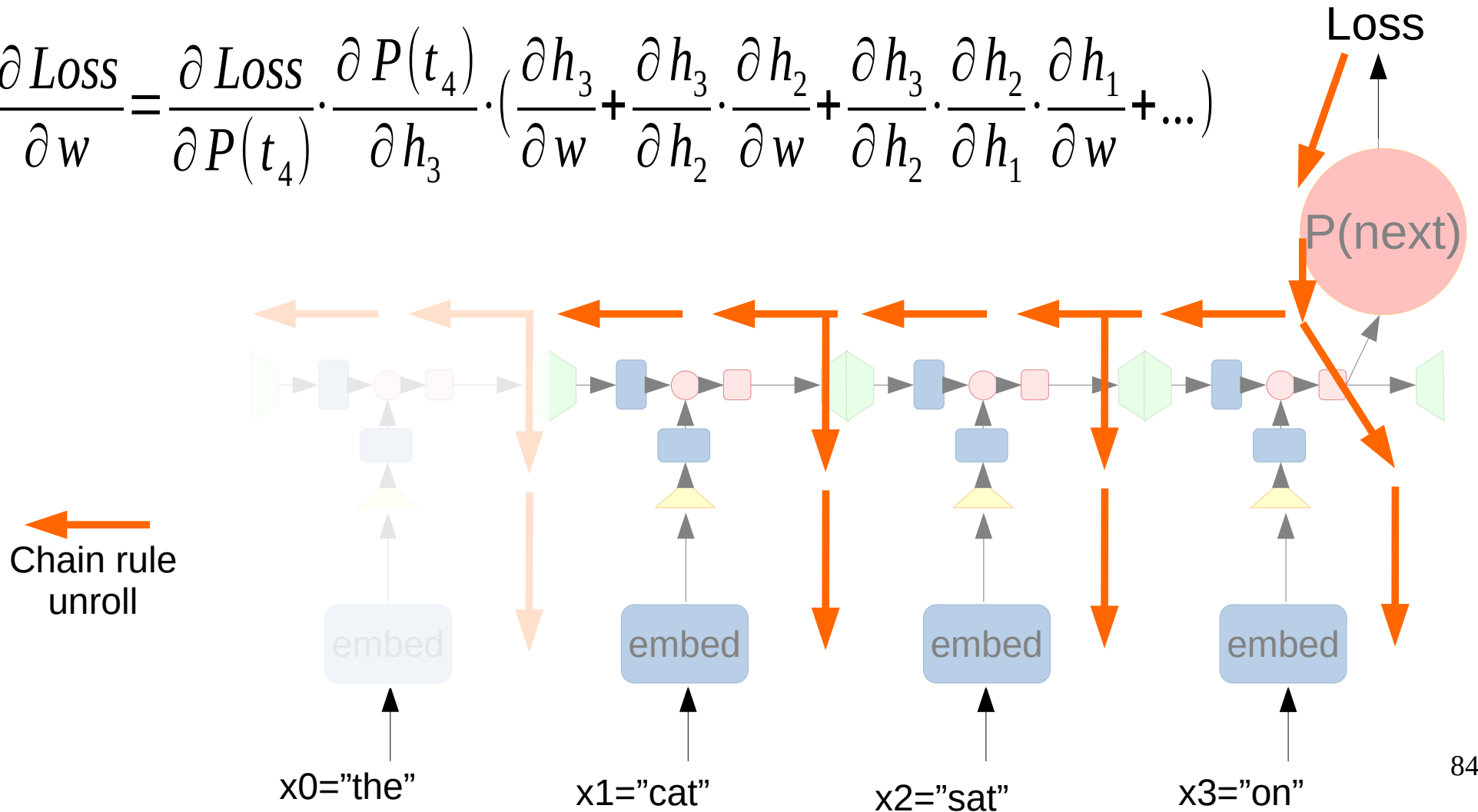
Your guess?



BPTT Again

$$h_{i+1} = \sigma(W_{hid} \cdot h_i + W_{inp} \cdot x_i + b)$$

$$\frac{\partial Loss}{\partial w} = \frac{\partial Loss}{\partial P(t_4)} \cdot \frac{\partial P(t_4)}{\partial h_3} \cdot \left(\frac{\partial h_3}{\partial w} + \frac{\partial h_3}{\partial h_2} \cdot \frac{\partial h_2}{\partial w} + \frac{\partial h_3}{\partial h_2} \cdot \frac{\partial h_2}{\partial h_1} \cdot \frac{\partial h_1}{\partial w} + \dots \right)$$

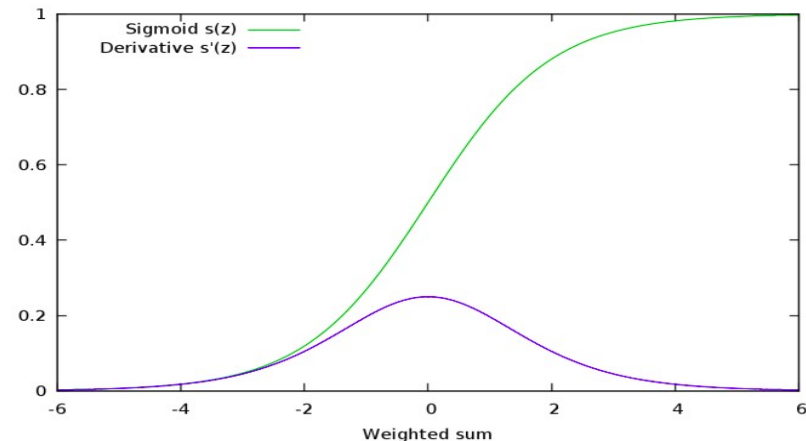


Gradient explosion and vanishing

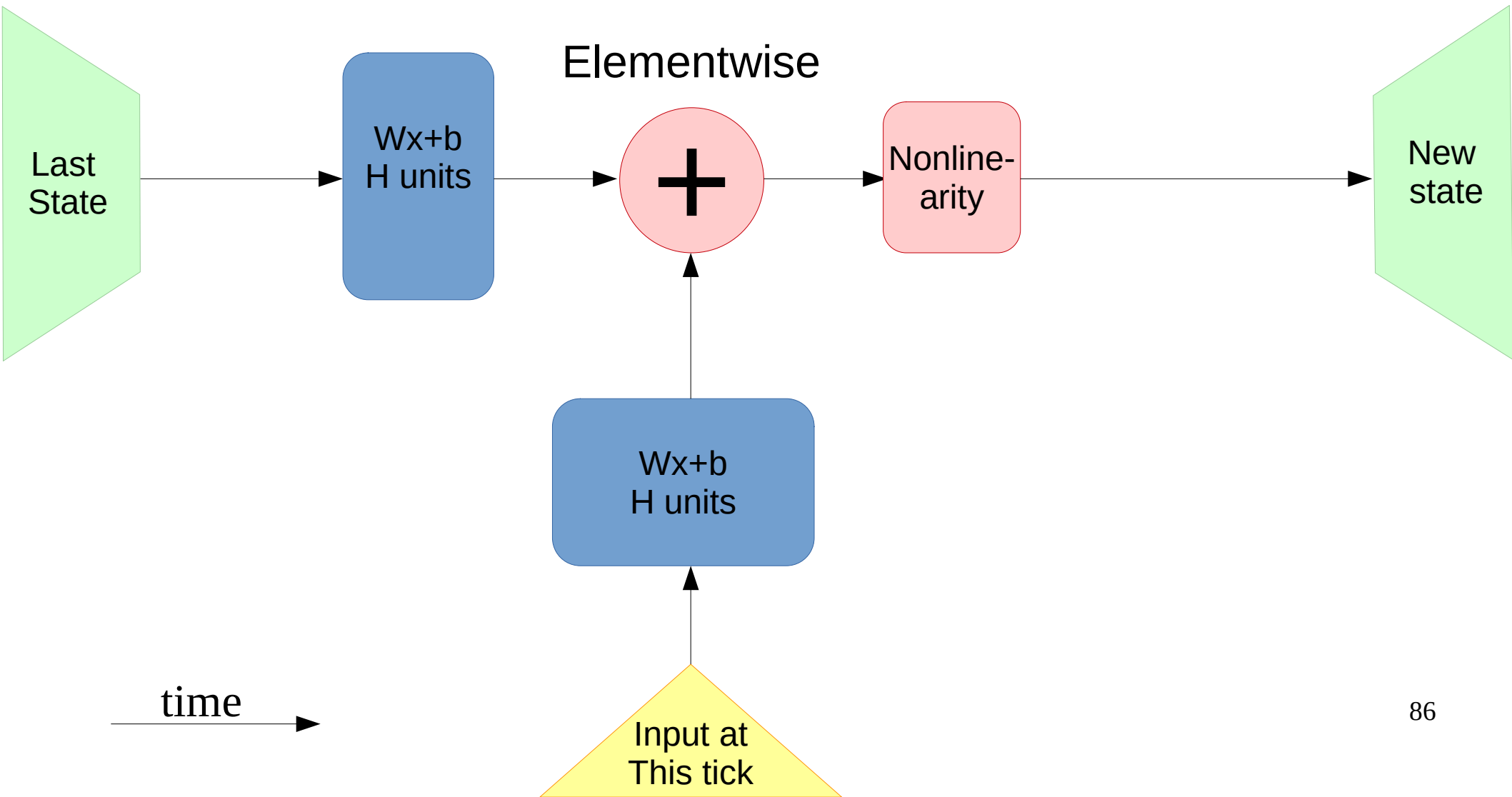
$$h_{i+1} = \sigma(W_{hid} \cdot h_i + W_{inp} \cdot x_i + b)$$

$$\frac{\partial Loss}{\partial w} = \frac{\partial Loss}{\partial P(x_4)} \cdot \frac{\partial P(x_4)}{\partial h_3} \cdot \left(\frac{\partial h_3}{\partial w} + \frac{\partial h_3}{\partial h_2} \cdot \frac{\partial h_2}{\partial w} + \frac{\partial h_3}{\partial h_2} \cdot \frac{\partial h_2}{\partial h_1} \cdot \frac{\partial h_1}{\partial w} + \dots \right)$$

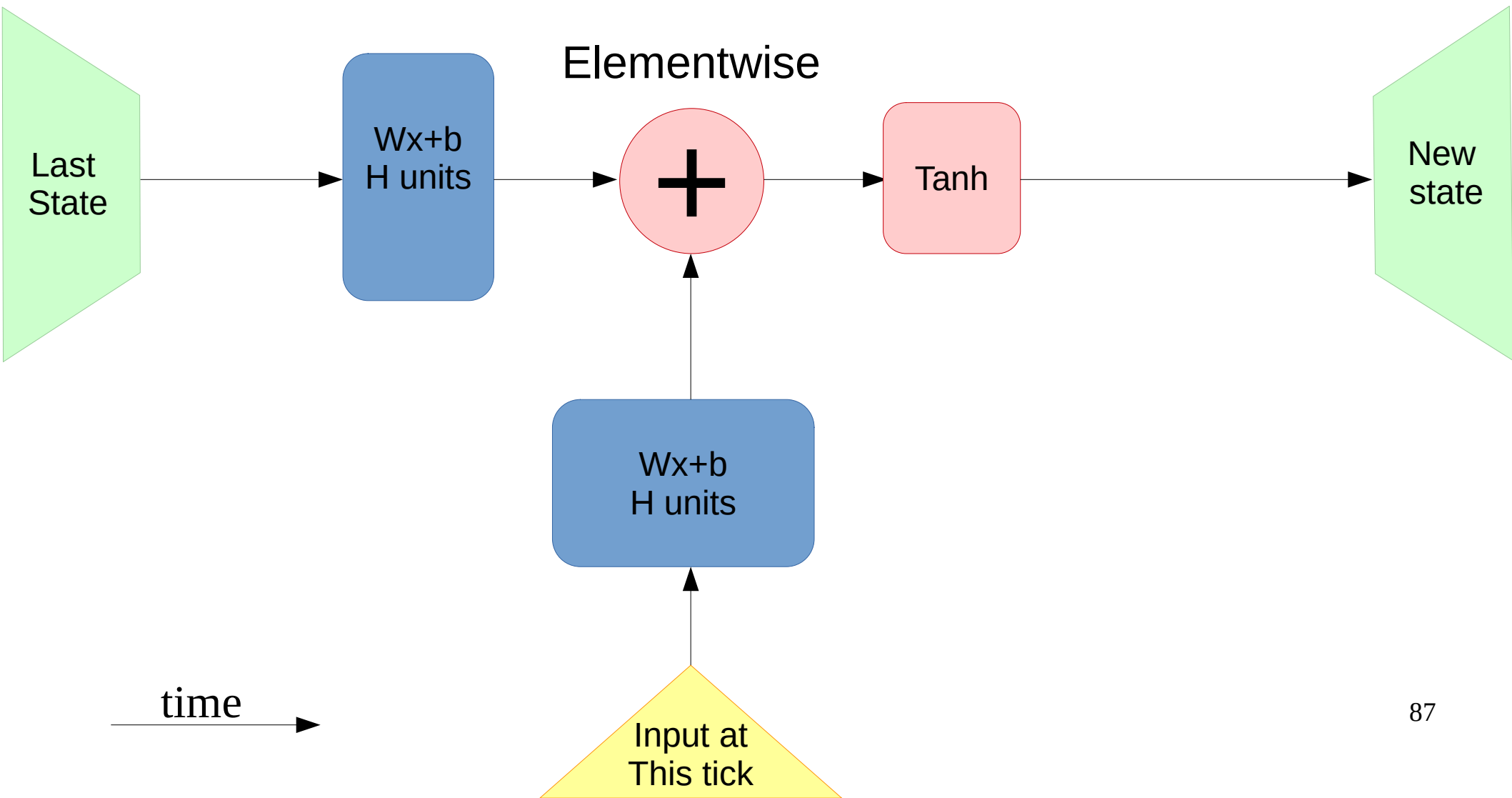
- Many sigmoids near 0 or 1
 - Gradients $\rightarrow 0$
 - Not training for long-term dependencies
- Many nonzero values
 - Derivative stacks to >1
 - Gradients $\rightarrow \text{inf}$
 - Weights $\rightarrow \text{shit}$



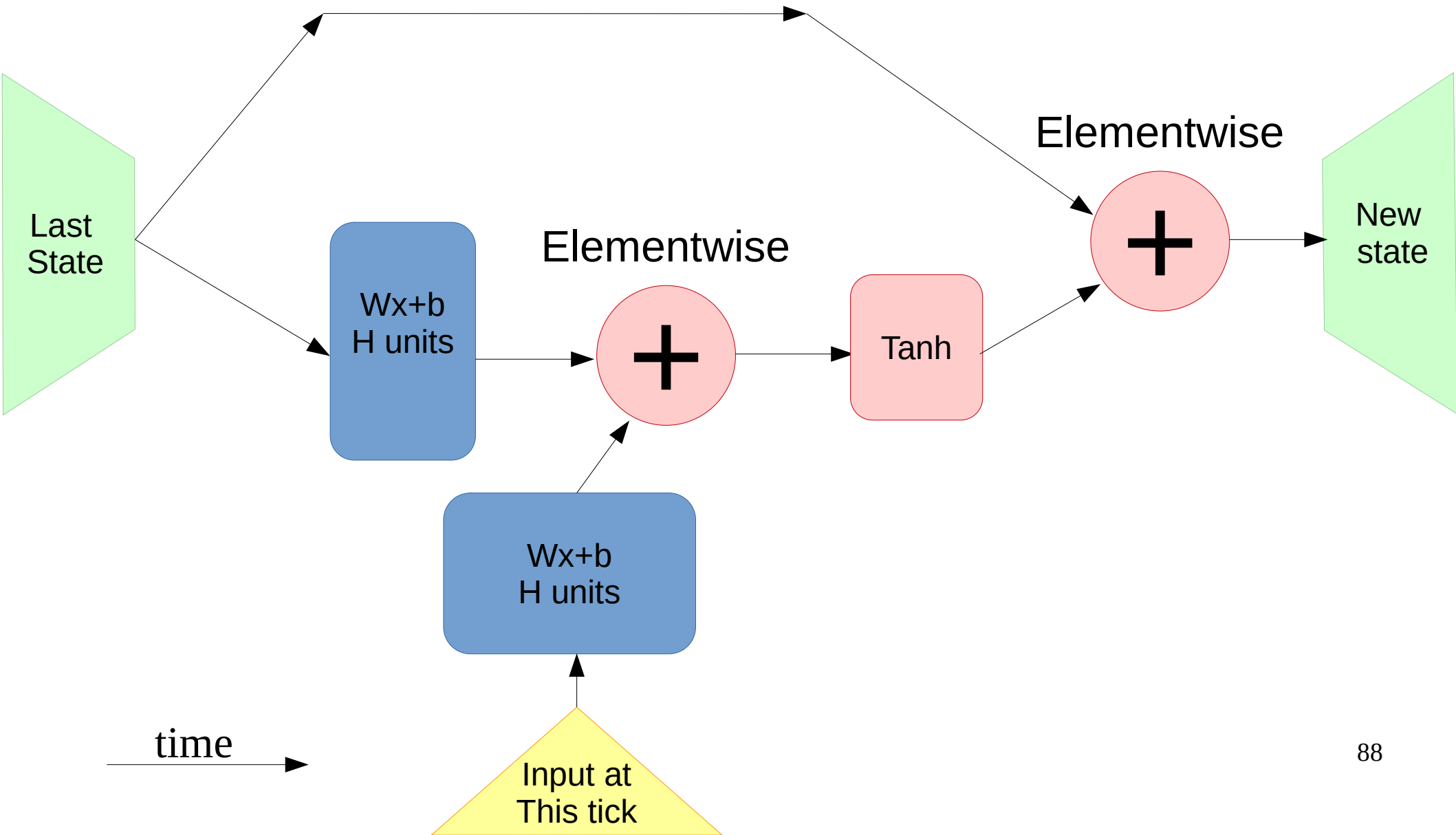
RNN step



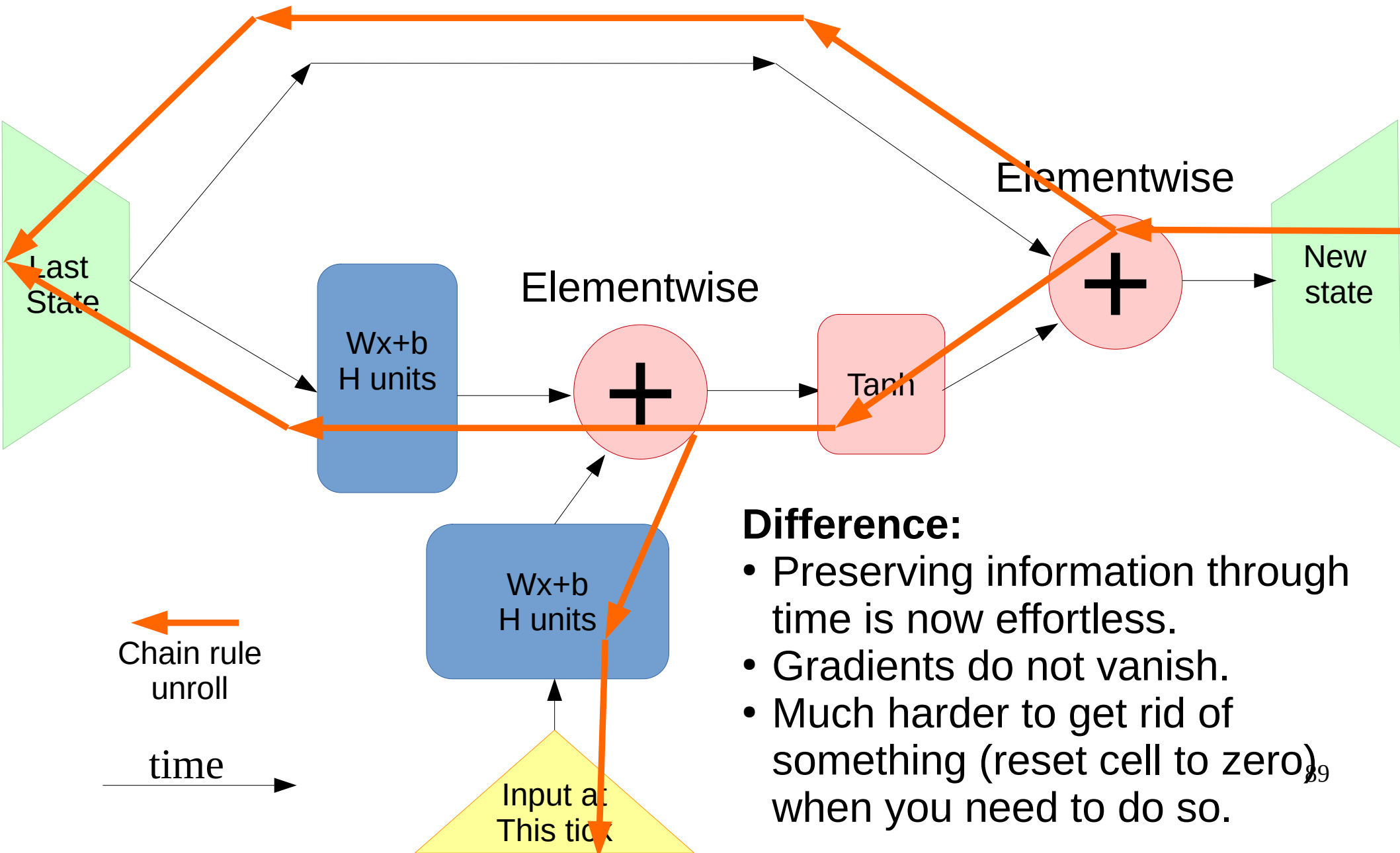
RNN step



Residual RNN step



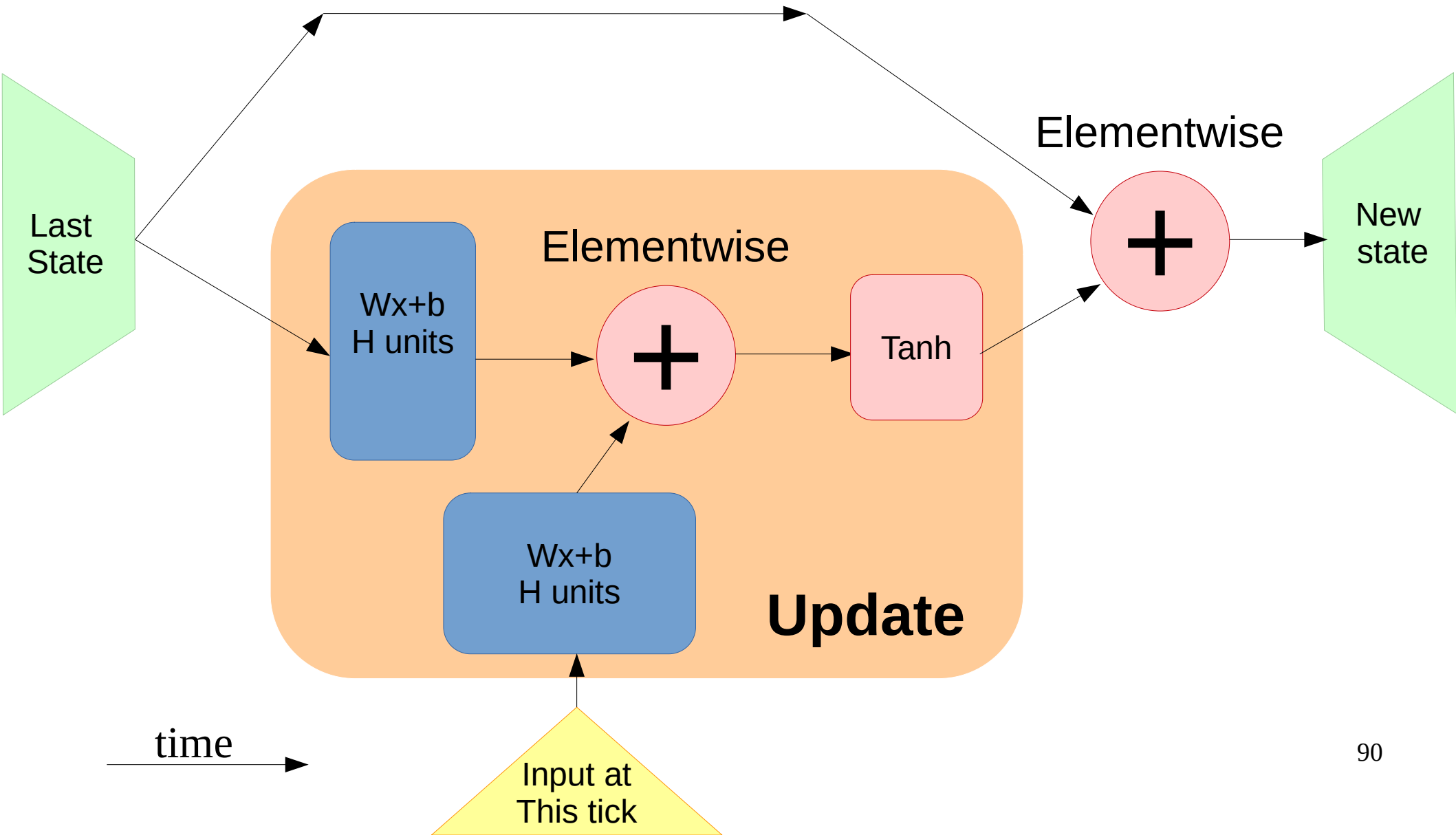
Residual RNN step



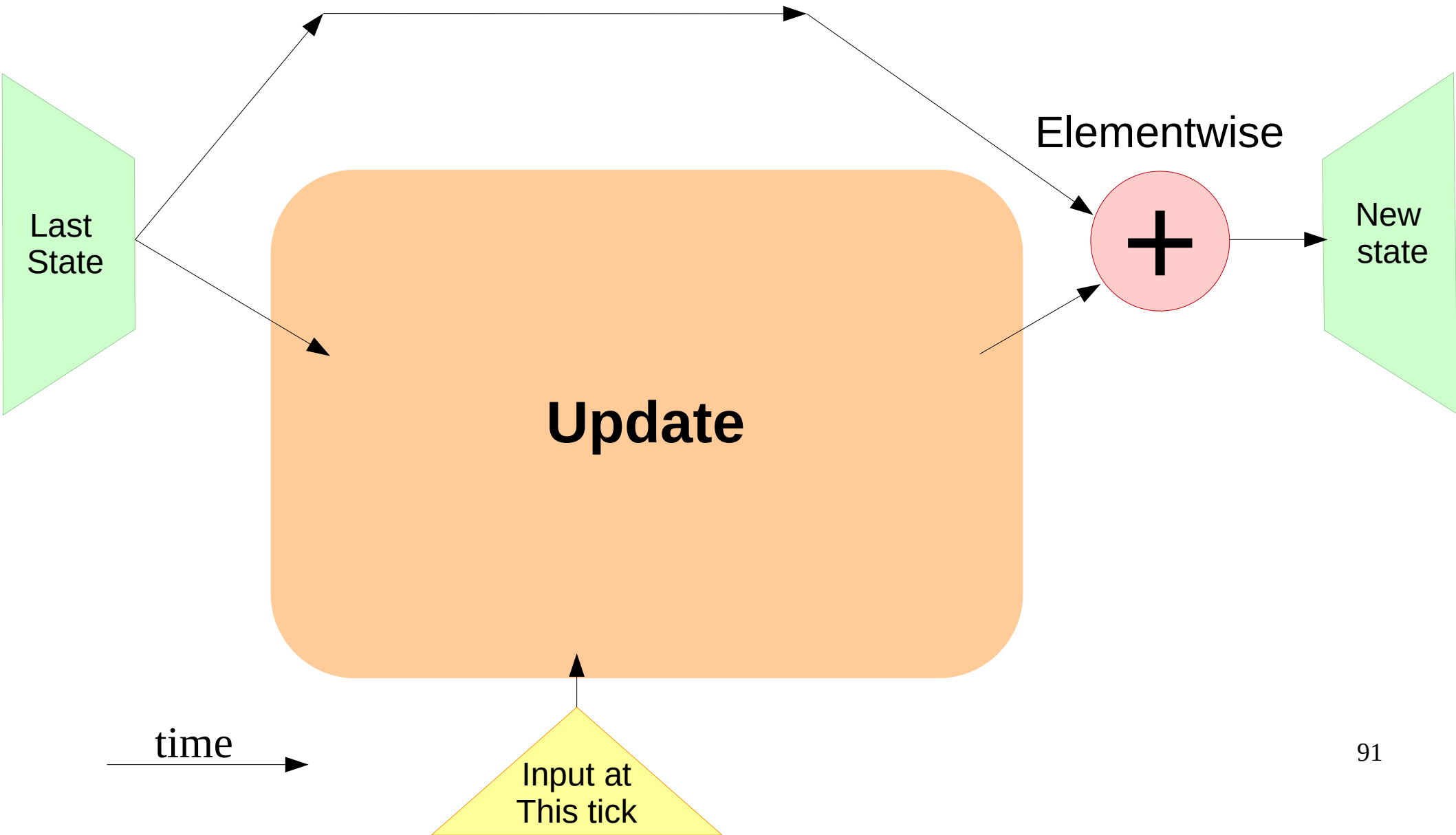
Difference:

- Preserving information through time is now effortless.
- Gradients do not vanish.
- Much harder to get rid of something (reset cell to zero) when you need to do so.

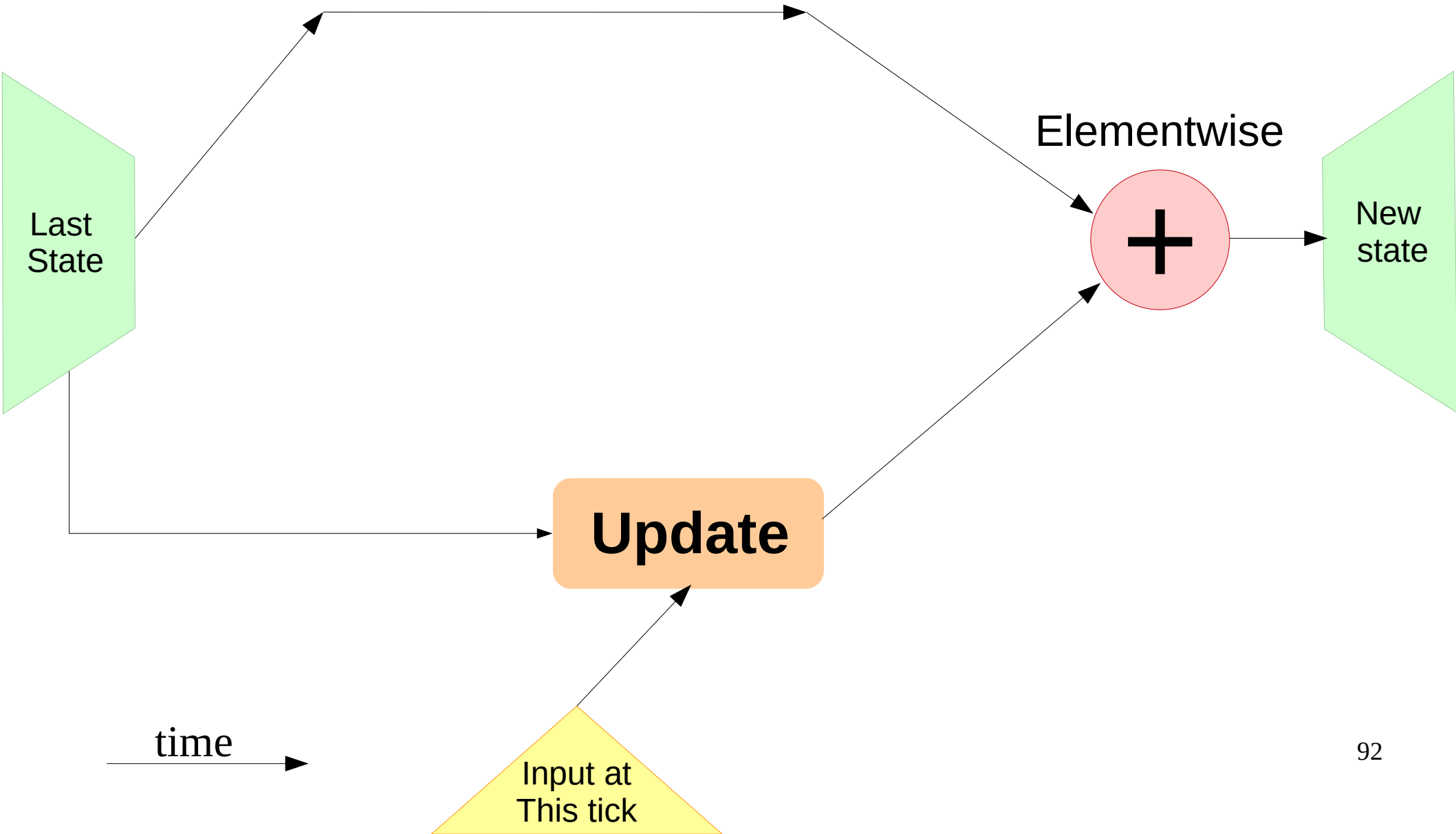
Residual RNN step



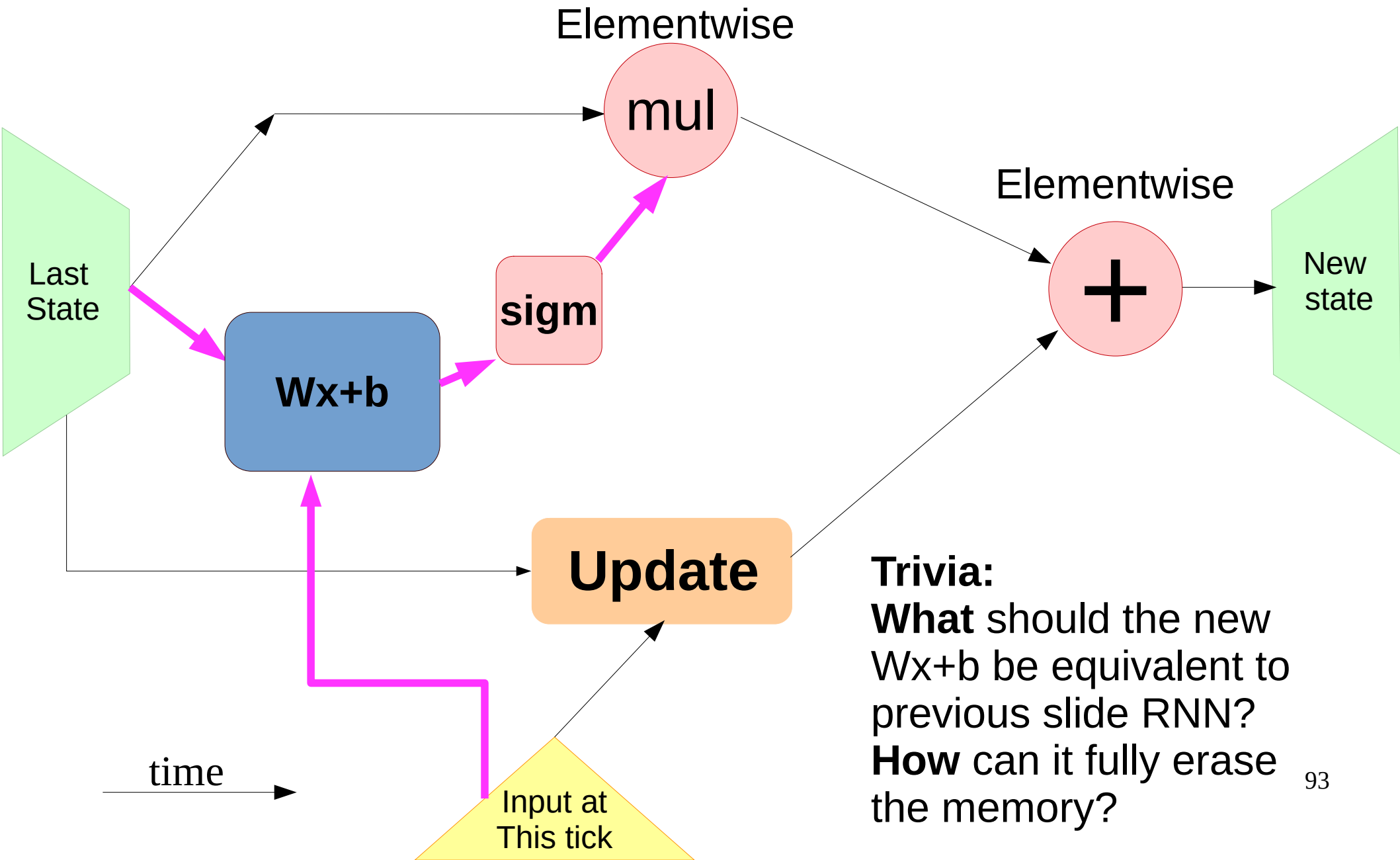
Residual RNN step



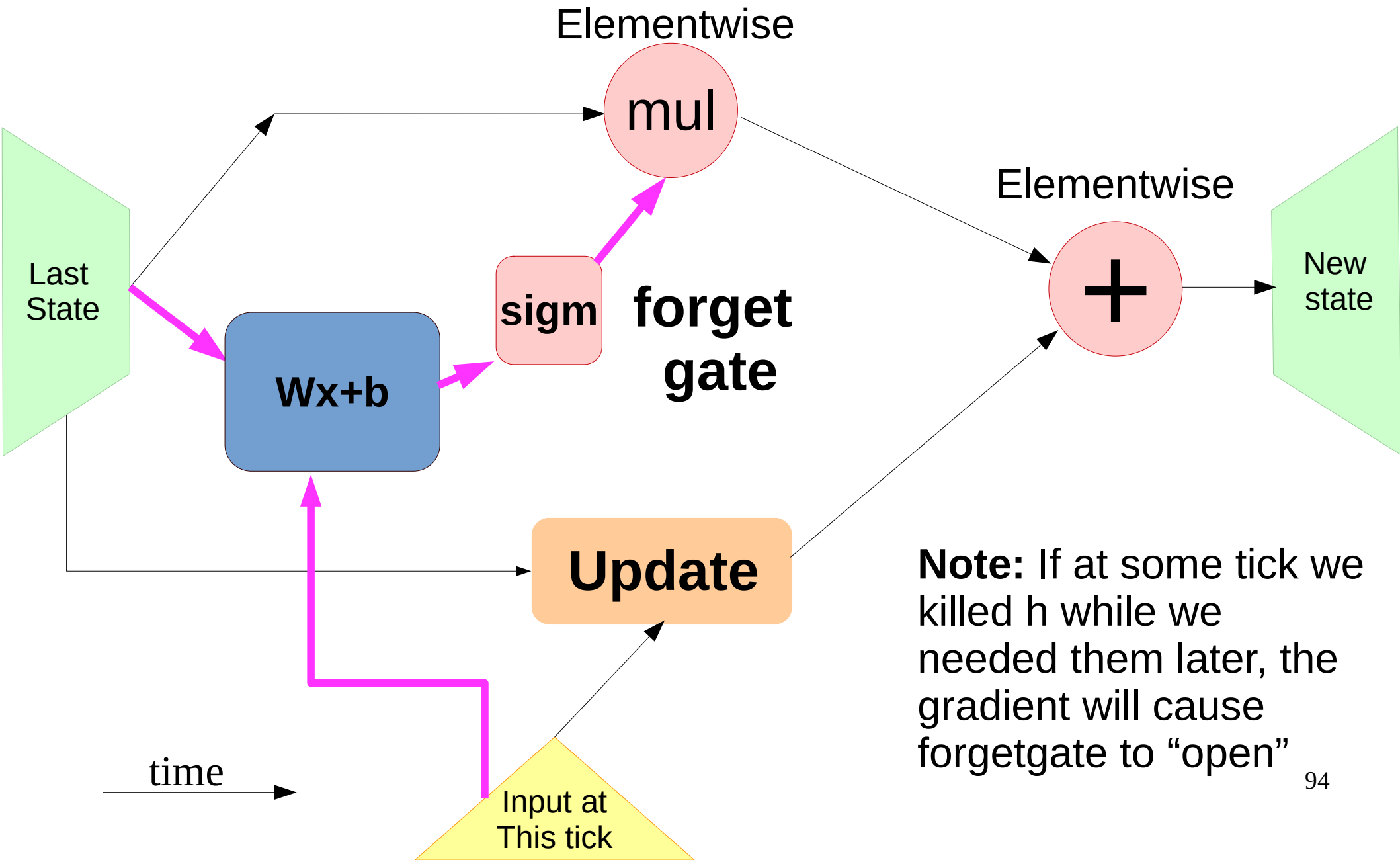
Residual RNN step



Residual RNN step

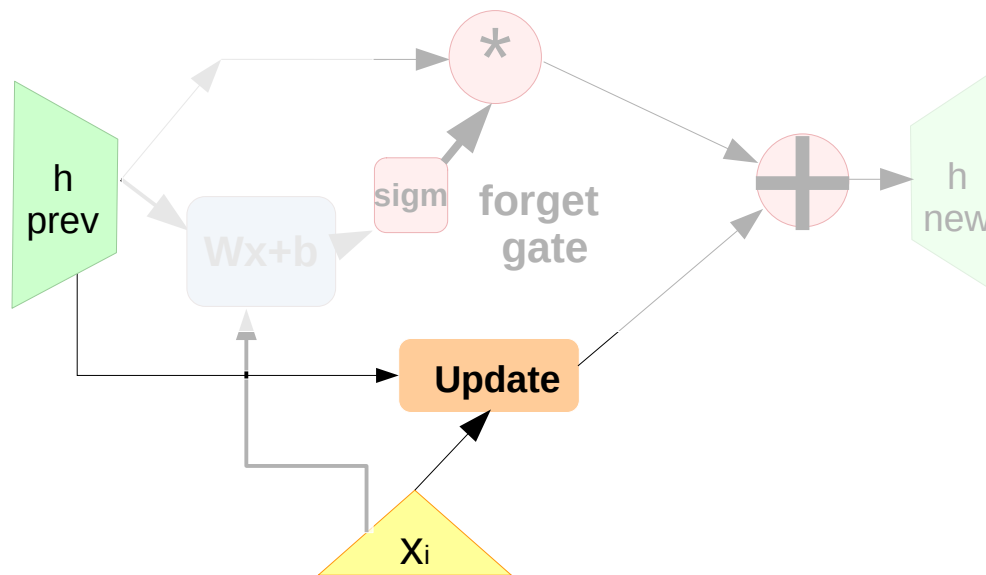


Residual RNN step



What we drew

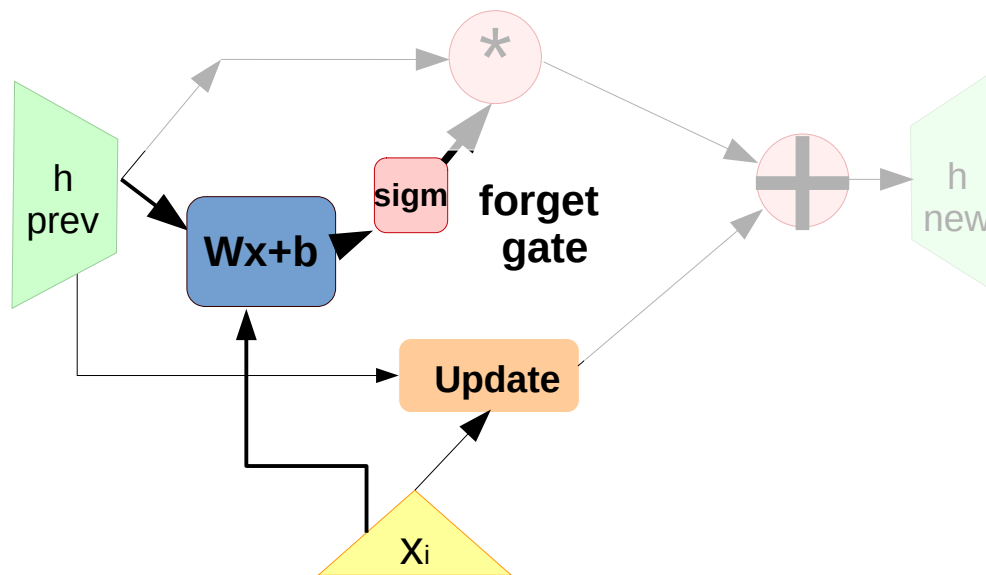
$$\text{update}(x_i, h_{i-1}) = \tanh(W_{hid}^{update} \cdot h_{i-1} + W_{inp}^{update} \cdot x_i + b^{update})$$



What we drew

$$\text{update}(x_i, h_{i-1}) = \tanh(W_{hid}^{update} \cdot h_{i-1} + W_{inp}^{update} \cdot x_i + b^{update})$$

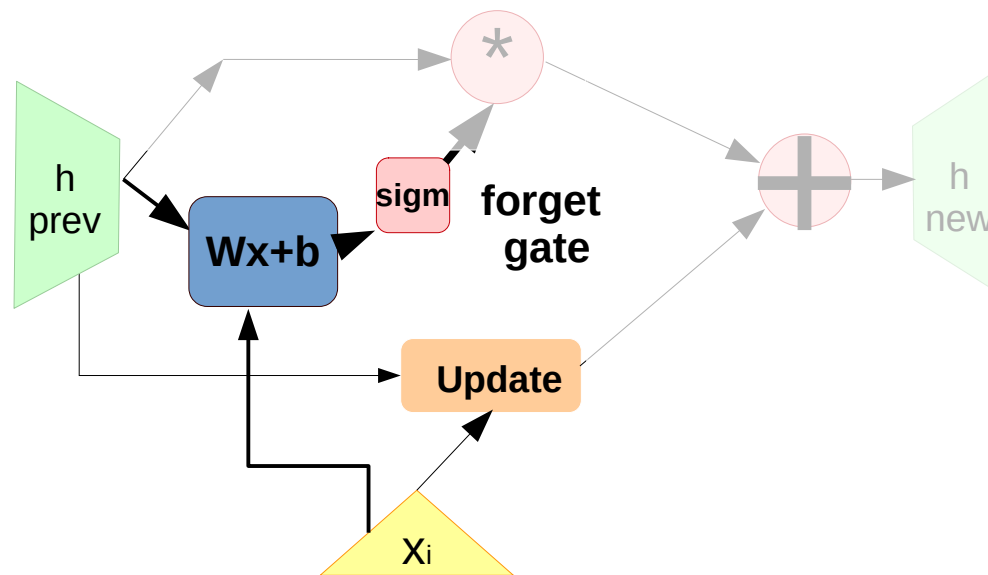
$$\text{forget}(x_i, h_{i-1}) = \sigma(W_{hid}^{forget} \cdot h_{i-1} + W_{inp}^{forget} \cdot x_i + b^{forget})$$



What we drew

$$\text{update}(x_i, h_{i-1}) = \tanh(W_{hid}^{update} \cdot h_{i-1} + W_{inp}^{update} \cdot x_i + b^{update})$$

$$\text{forget}(x_i, h_{i-1}) = \sigma(W_{hid}^{forget} \cdot h_{i-1} + W_{inp}^{forget} \cdot x_i + b^{forget})$$



**How to compute
h_new?**

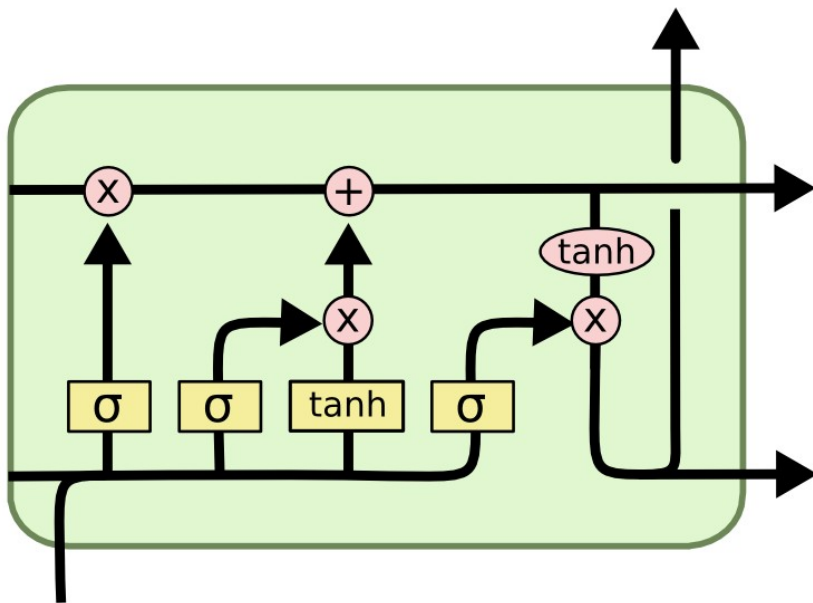
What we drew

$$\text{update}(x_i, h_{i-1}) = \tanh(W_{hid}^{update} \cdot h_{i-1} + W_{inp}^{update} \cdot x_i + b^{update})$$

$$\text{forget}(x_i, h_{i-1}) = \sigma(W_{hid}^{forget} \cdot h_{i-1} + W_{inp}^{forget} \cdot x_i + b^{forget})$$

$$h_i(x_i, h_{i-1}) = \text{forget}(x_i, h_{i-1}) \cdot h_{i-1} + \text{update}(x_i, h_{i-1})$$

LSTM



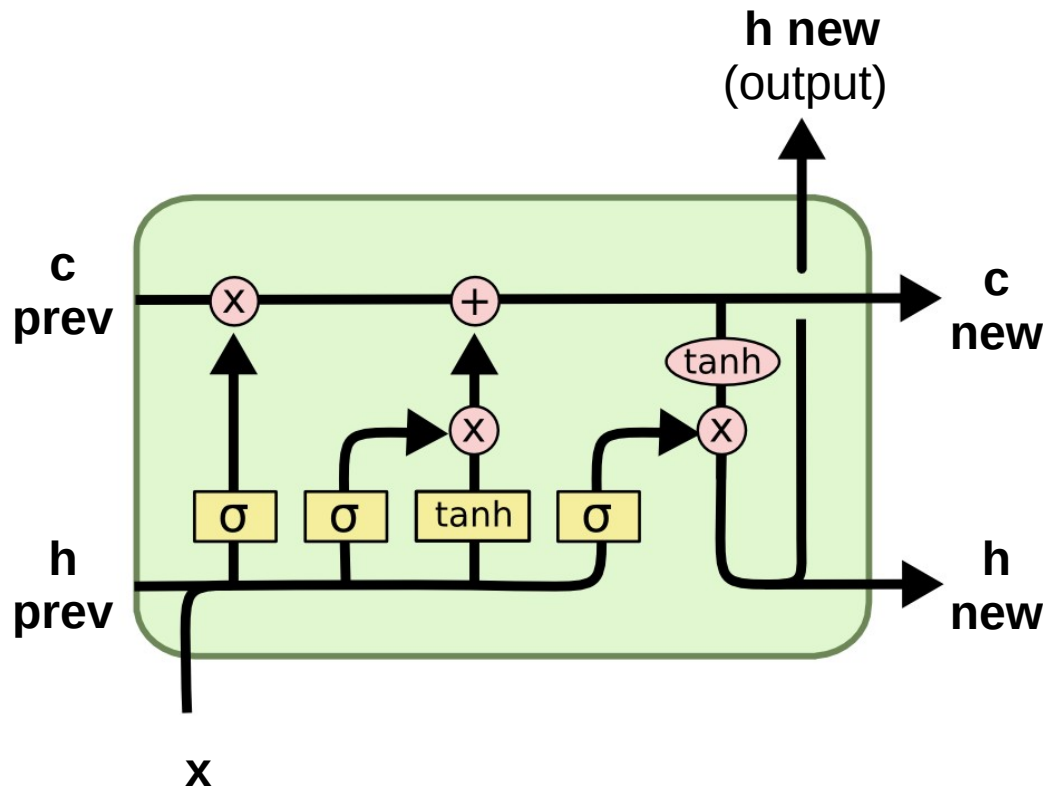
2 hidden states:

- Cell (“private” state)
- Output (“public” state)

4 blocks:

- Update
- Forget gate
- Input gate
- Output gate

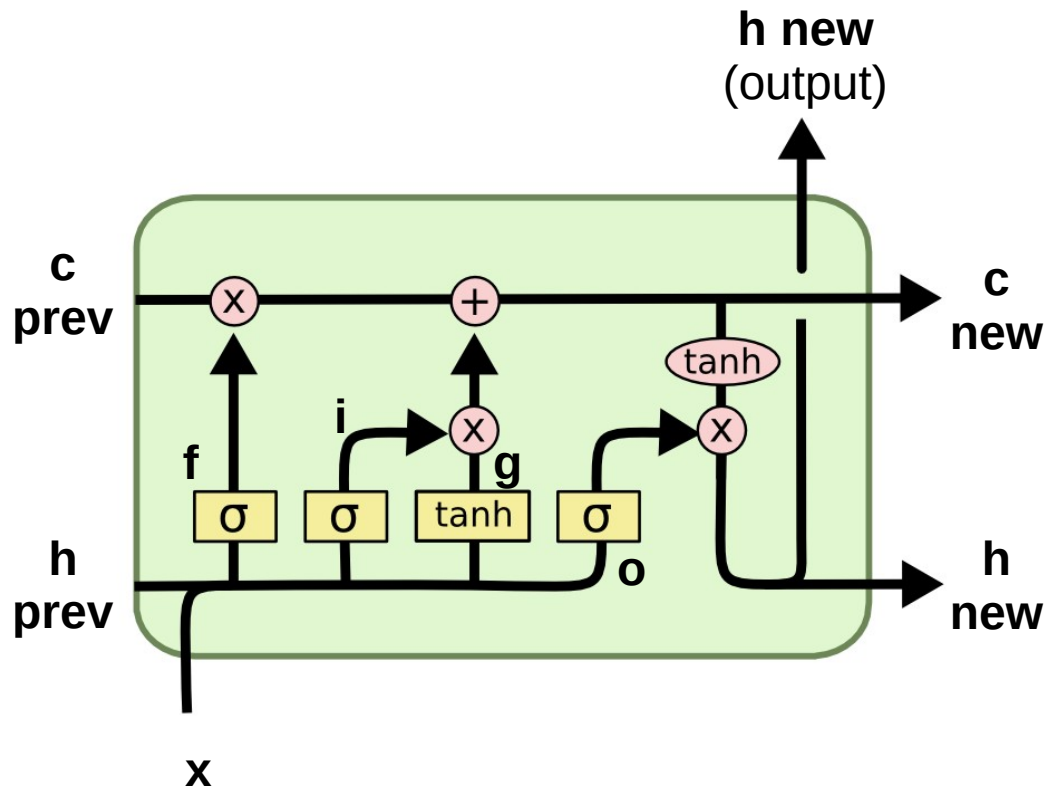
LSTM



$$\begin{aligned}
 i_t &= \text{Sigm}(\theta_{xi}x_t + \theta_{hi}h_{t-1} + b_i) \\
 f_t &= \text{Sigm}(\theta_{xf}x_t + \theta_{hf}h_{t-1} + b_f) \\
 o_t &= \text{Sigm}(\theta_{xo}x_t + \theta_{ho}h_{t-1} + b_o) \\
 g_t &= \text{Tanh}(\theta_{xg}x_t + \theta_{hg}h_{t-1} + b_g) \\
 c_t &= f_t \otimes c_{t-1} + i_t \otimes g_t \\
 h_t &= o_t \otimes \text{Tanh}(c_t)
 \end{aligned}$$

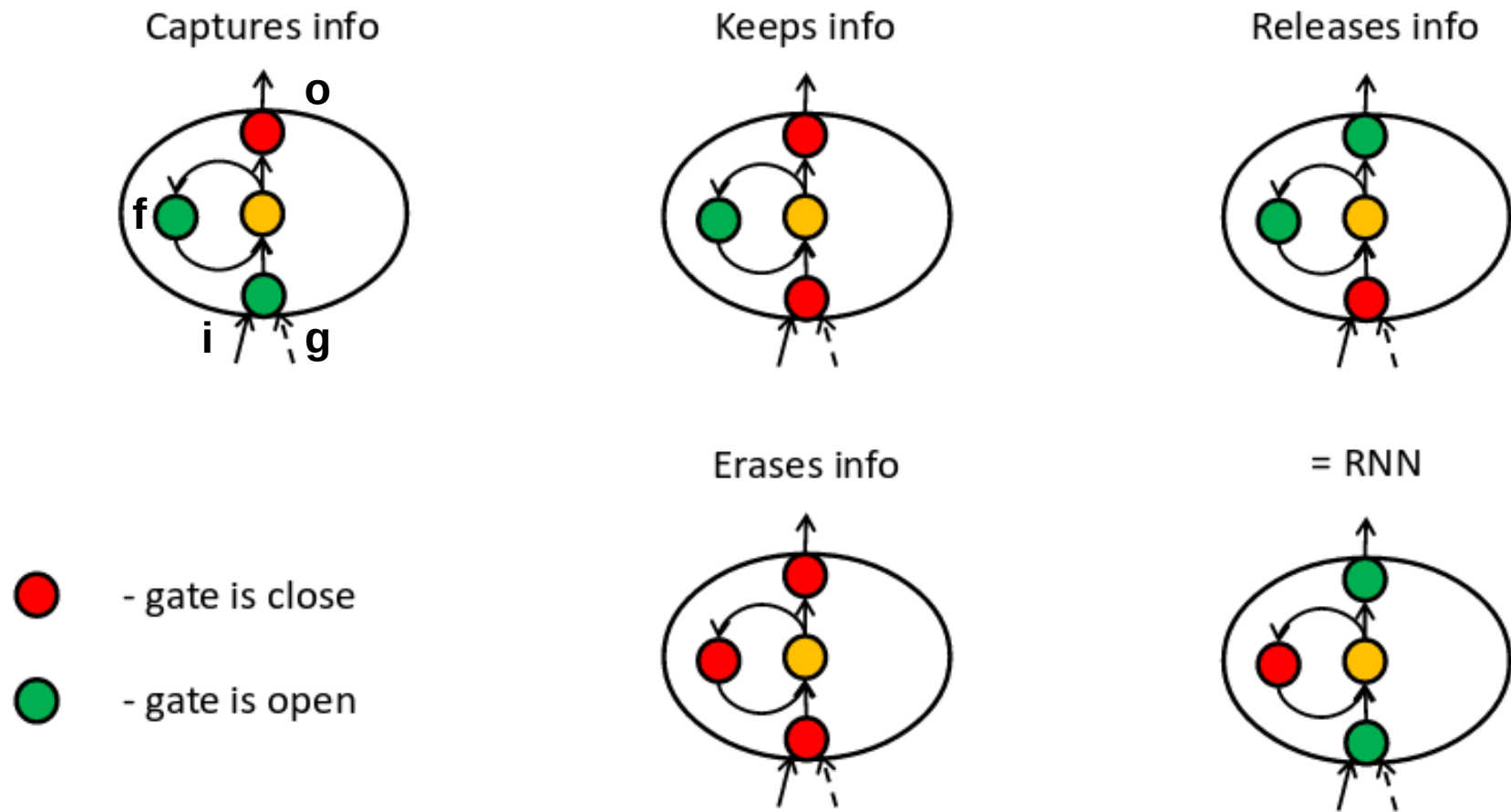
Where are the gates?

LSTM

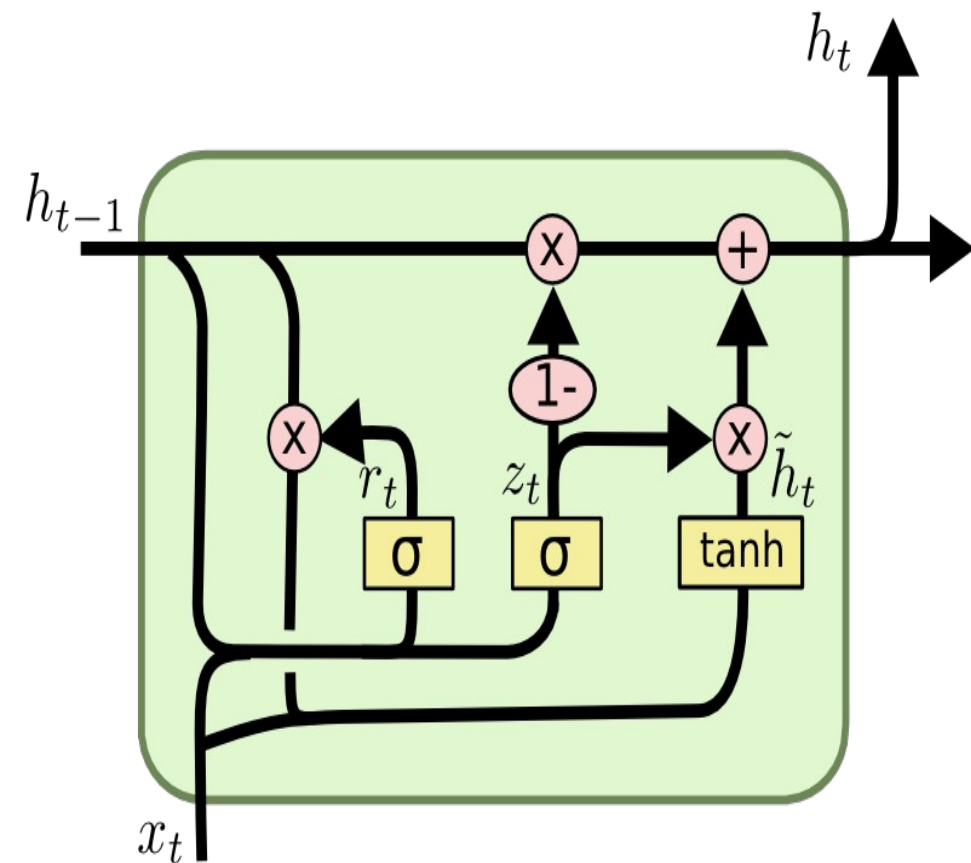


$$\begin{aligned}
 i_t &= \text{Sigm}(\theta_{xi}x_t + \theta_{hi}h_{t-1} + b_i) \\
 f_t &= \text{Sigm}(\theta_{xf}x_t + \theta_{hf}h_{t-1} + b_f) \\
 o_t &= \text{Sigm}(\theta_{xo}x_t + \theta_{ho}h_{t-1} + b_o) \\
 g_t &= \text{Tanh}(\theta_{xg}x_t + \theta_{hg}h_{t-1} + b_g) \\
 c_t &= f_t \otimes c_{t-1} + i_t \otimes g_t \\
 h_t &= o_t \otimes \text{Tanh}(c_t)
 \end{aligned}$$

LSTM: not a monster



GRU



$$z_t = \sigma(W_z \cdot [h_{t-1}, x_t])$$

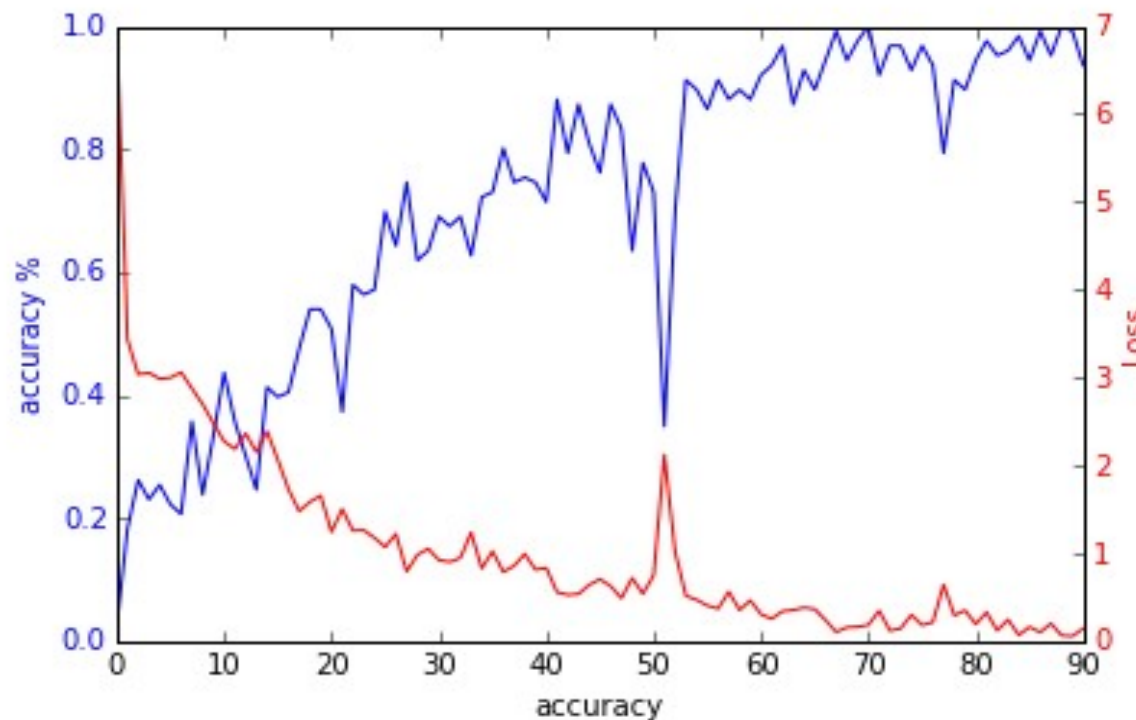
$$r_t = \sigma(W_r \cdot [h_{t-1}, x_t])$$

$$\tilde{h}_t = \tanh(W \cdot [r_t * h_{t-1}, x_t])$$

$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$

Okay, the gradients no longer vanish
except they still do, if only slower

But how do we deal with exploding grads?



Ideas?

Gradient clipping

At each time tick,

- check if grad abs value is more than ... 5?
- If so, clip it
 - large positive is now 5,
 - large negative is now -5
- How large is too large?
 - Reduce clipping threshold until explosions disappear

Gradient clipping

Where do I clip?

- Clip each element of $\delta L / \delta w$
- Clip each element of $\delta h_{i+1} / \delta h_i$
- Clip whole $\delta L / \delta w$ by norm
 - If $\left\| \frac{\delta L}{\delta w} \right\| > 5$, scale $\frac{\delta L}{\delta w} / \left\| \frac{\delta L}{\delta w} \right\| \cdot 5$

Generating stuff

Easy:

- Names, small phrases
- Arxiv article titles
- Orthographically correct delirium

Medium:

- Music (notes)
- Organic molecules (SMILES)

Hard:

- C/C++ source code
- Articles (LaTeX full text)
- Your course projects >.<
- Seq2Seq

Nuff

Coding time!

