

Generalized Evidence Passing for Effect Handlers

Efficient Compilation of Effect Handlers to C



Ningning Xie



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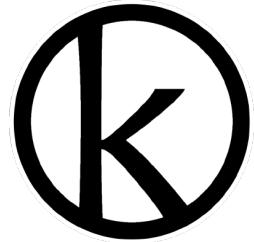


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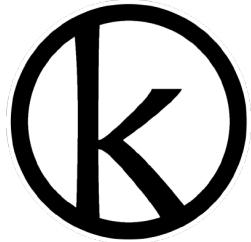


Research contributions



<https://koka-lang.github.io/>

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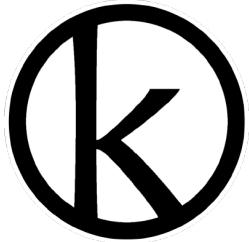


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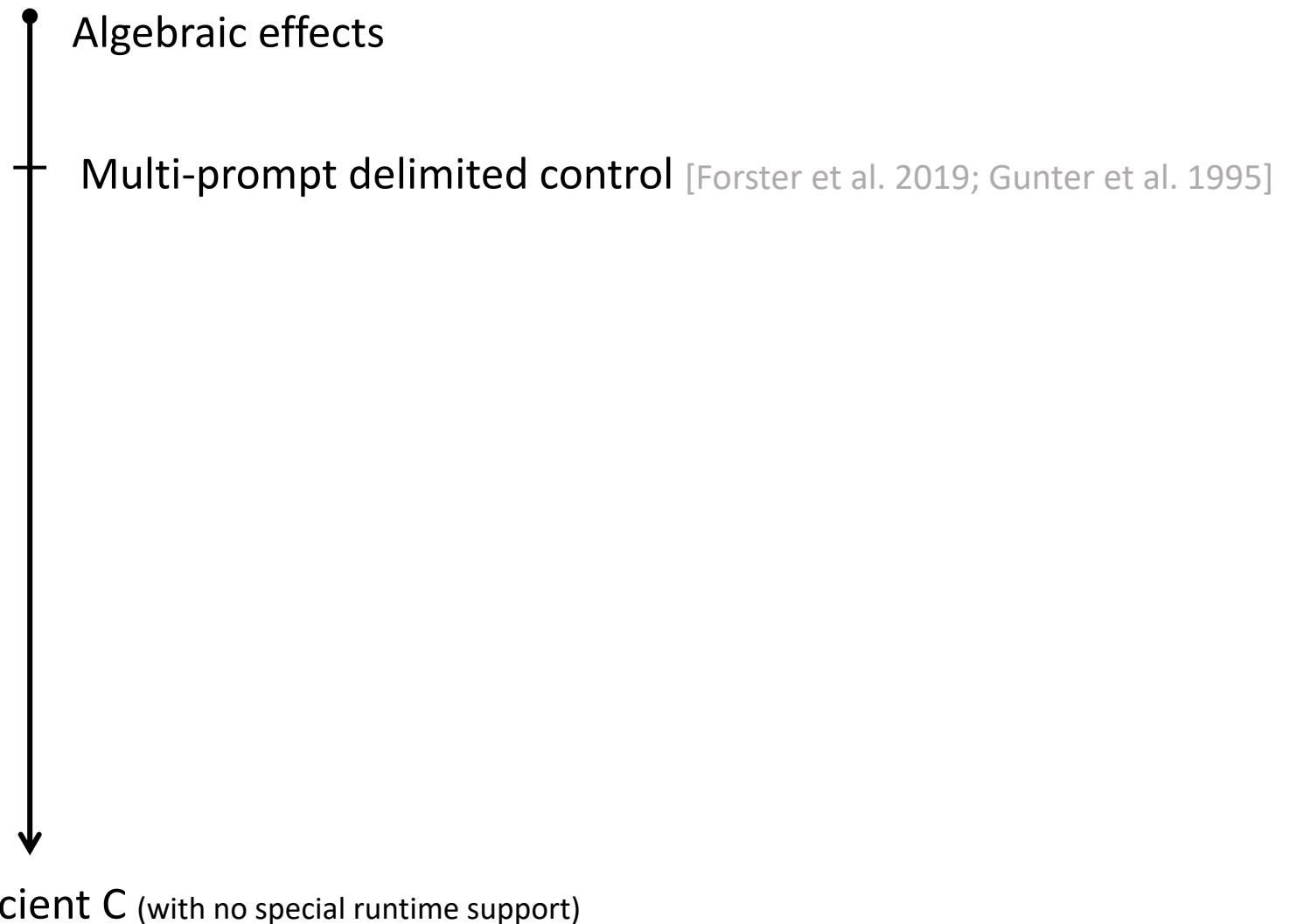
Algebraic effects

Efficient C (with no special runtime support)

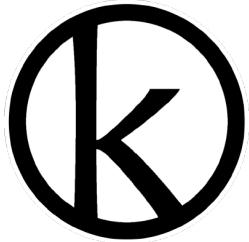
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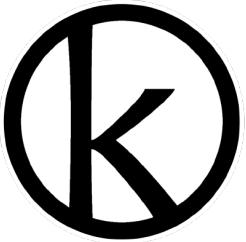
Research contributions



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 - Evidence-passing semantics
- ↓
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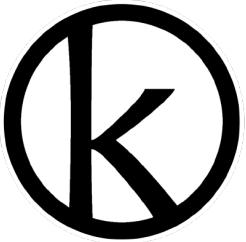
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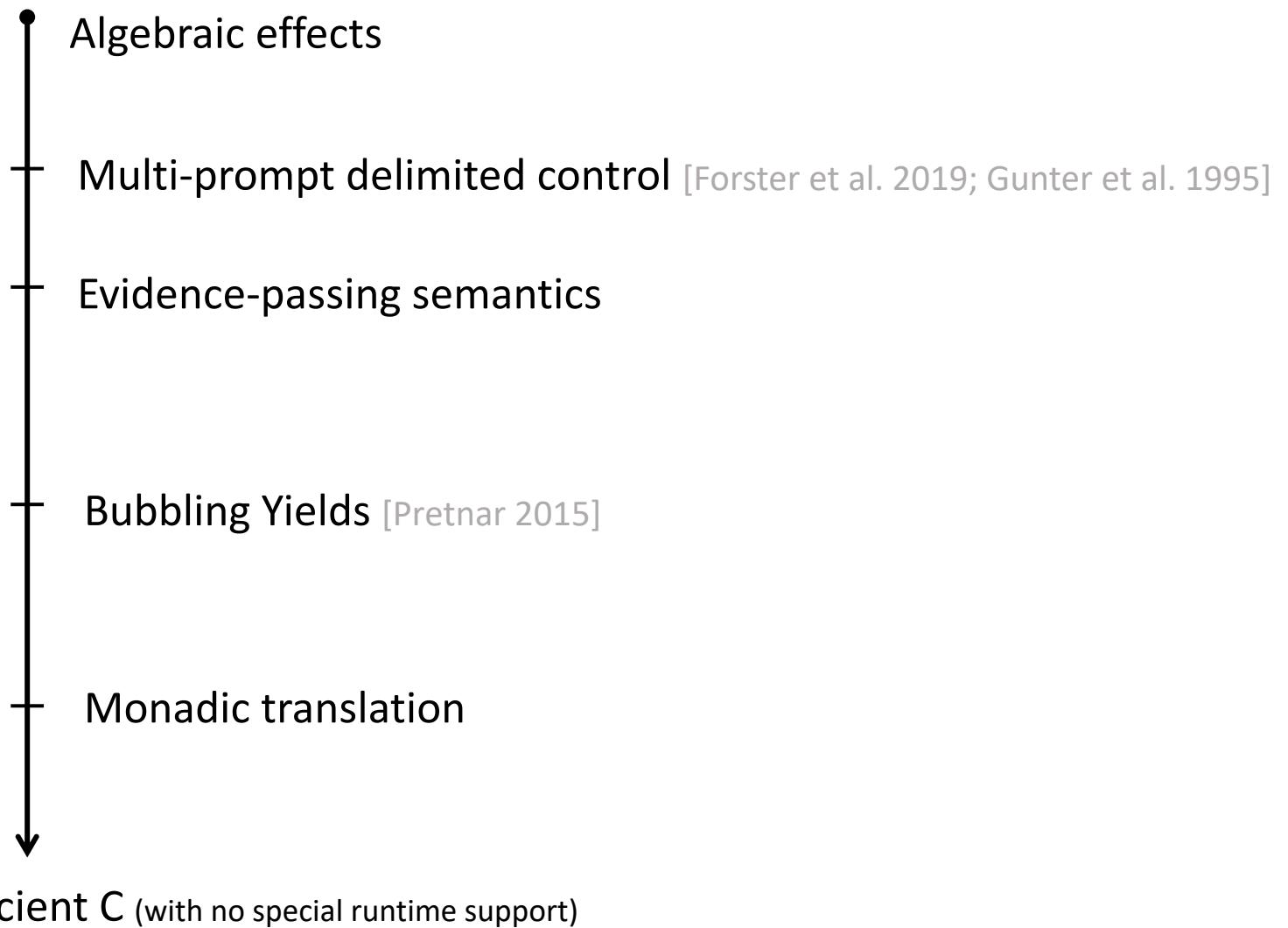
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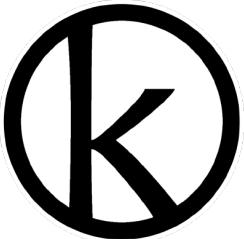
Research contributions



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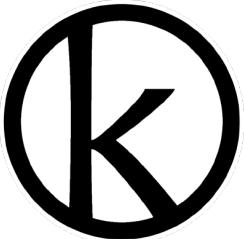


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- Multi-prompt delimited control [Forster et al. 2019; Gunter et al. 1995]
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 - optimization of tail-resumptive operations
 - insertion- versus canonical ordered evidence vector
- Bubbling Yields [Pretnar 2015]
 - short-cut resumption [Kiselyov and Ishii 2015]
- Monadic translation
 - bind-inlining and join-point sharing

Efficient C (with no special runtime support)

Research contributions



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PLDI 2021

Perceus: Garbage Free Reference Counting with Reuse

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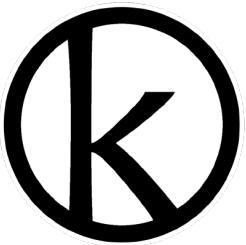
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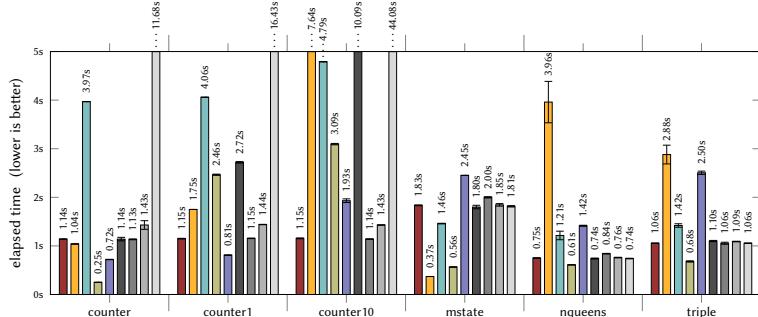
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Algebraic effects 101

```
effect read {
    ask : () -> int
}

handler {
    ask -> \x.\k. k 1
}
(\_.
    perform ask () + perform ask ()
)
```

Algebraic effects 101

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effect read {  
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Algebraic effects 101

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operation

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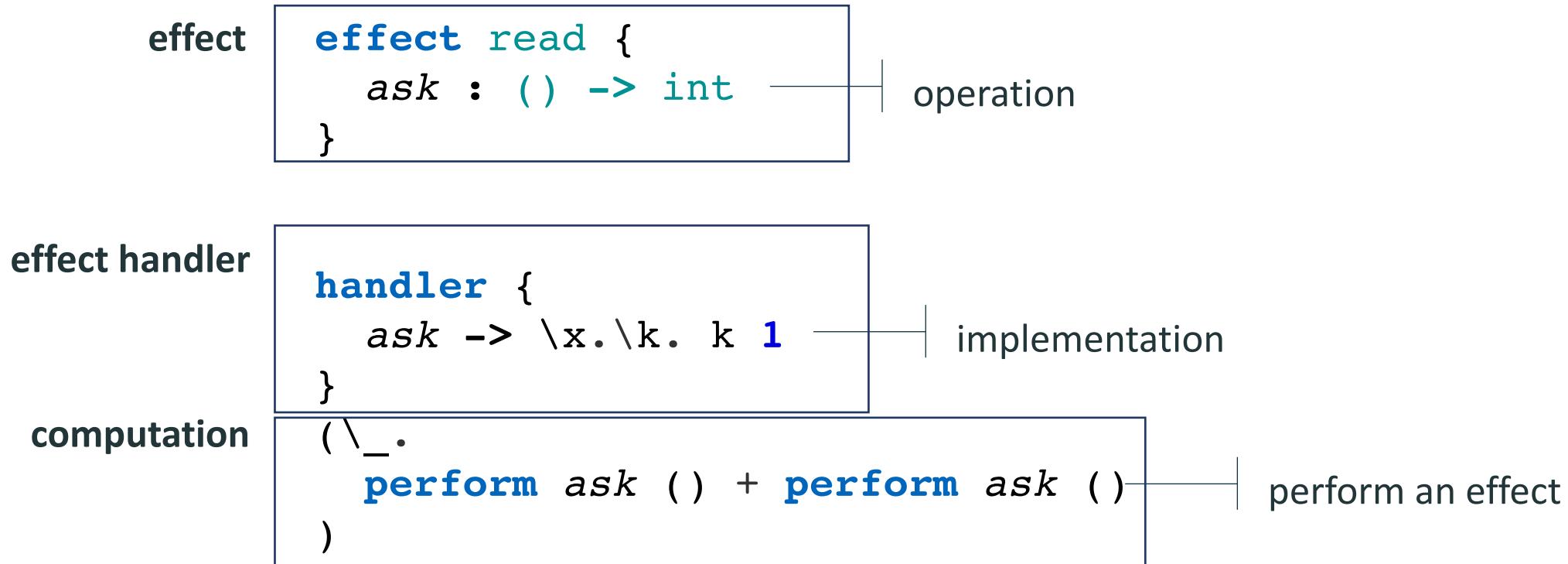
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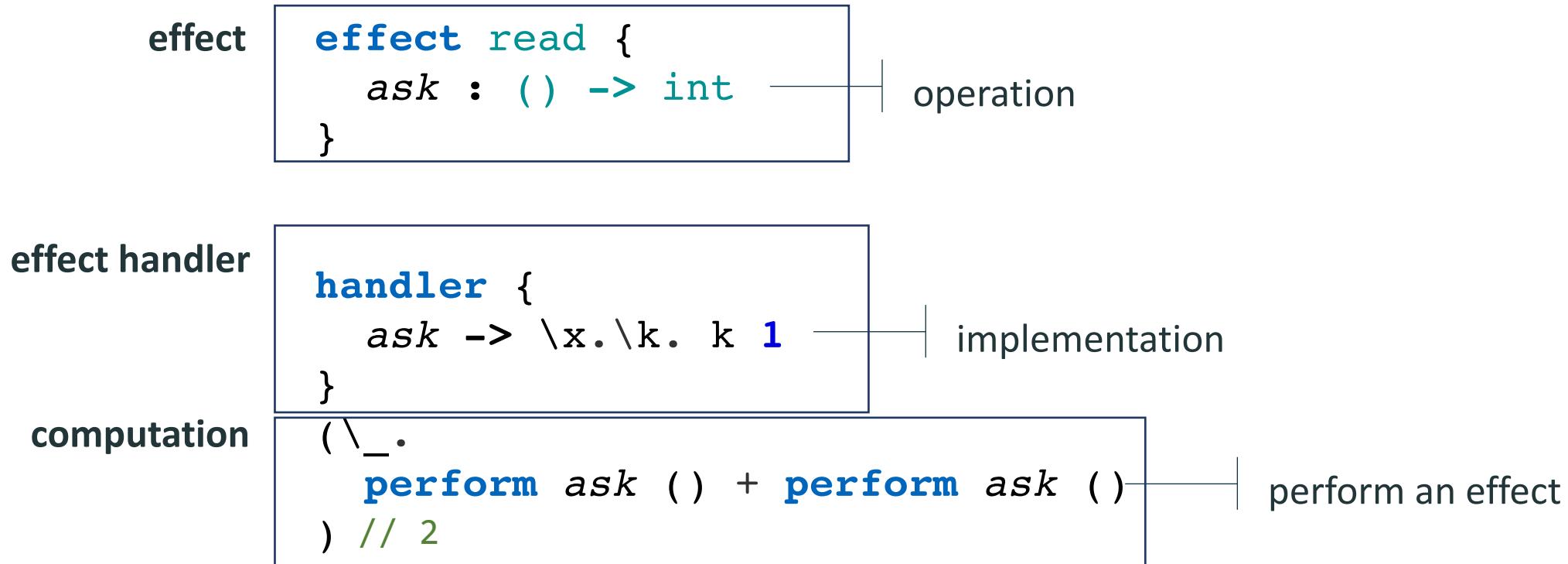
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```

Algebraic effects 101



Algebraic effects 101



Operational semantics of untyped algebraic effects

$$\textcircled{1} \quad (\textit{app}) \quad (\lambda x. e) \ v \quad \longrightarrow \quad e[x:=v]$$

$$\textcircled{2} \quad (\textit{handler}) \quad \text{handler } h \ f \quad \longrightarrow \quad \text{handle } h \ (f \ ())$$

$$\textcircled{3} \quad (\textit{return}) \quad \text{handle } h \ v \quad \longrightarrow \quad v$$

$$\textcircled{4} \quad (\textit{perform}) \quad \text{handle } h \ E[\text{perform } op \ v] \longrightarrow \begin{aligned} & f \ v \ (\lambda x. \text{handle } h \ E[x]) \\ & \text{iff } op \notin \text{bop}(E) \wedge (op \mapsto f) \in h \end{aligned}$$

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Operational semantics of untyped algebraic effects

① (app)

$(\lambda x. e) v$

$\longrightarrow e[x:=v]$

a unit-taking function as a computation

② (handler)

handler $h f$

$\longrightarrow \text{handle } h (f ())$

③ (return)

handle $h v$

$\longrightarrow v$

④ (perform)

handle $h E[\text{perform } op v]$

$\longrightarrow f v (\lambda x. \text{handle } h E[x])$
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evaluation context

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h is the
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get the operation
implementation f

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$\rightarrow v$

evaluation context

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handle $h E[\text{perform } op v]$

operation argument

$\rightarrow f v (\lambda x. \text{handle } h E[x])$

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operation argument

$f v$

resumption

$(\lambda x. \text{handle } h E[x])$

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The problem: compiling effect handlers efficiently

$$(perform) \quad \text{handle } h \text{ E[perform } op \nu] \longrightarrow f \nu (\lambda x. \text{handle } h \text{ E}[x]) \\ \text{iff } op \notin \text{bop}(E) \wedge (op \mapsto f) \in h$$

The problem: compiling effect handlers efficiently

$$\text{(perform)} \quad \text{handle } h \text{ E[perform } op \text{ } v] \longrightarrow f \text{ } v \text{ } (\lambda x. \text{ handle } h \text{ E}[x]) \\ \text{iff } op \notin \text{bop}(E) \wedge (op \mapsto f) \in h$$

Two potentially **expensive** runtime operations:

The problem: compiling effect handlers efficiently

evaluation context

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Two potentially **expensive** runtime operations:

1. **Searching**

a *linear* search through the current evaluation context to find the innermost handler for op

The problem: compiling effect handlers efficiently

evaluation context resumption

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evaluation context	resumption
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Two potentially **expensive** runtime operations:

1. **Searching**
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 2. **Capturing**
capture the evaluation context (i.e., stacks and registers) up to the found handler, and create a resumption function

The problem: compiling effect handlers efficiently

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This work:

Multi-prompt delimited control

Evidence-passing semantics

Monadic translation

Reader, formally

```
handler {  
    ask -> \x.\k. k 1  
}  
(\_.  
    perform ask () + perform ask ()  
)
```



Reader, formally

```
handler {  
    ask -> \x.\k. k 1  
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```

```
f = \x.\k. k 1  
h1 = ask -> f
```



Reader, formally

handler

h1

```
(\_.  
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)
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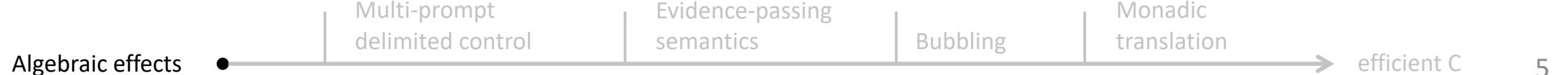
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Reader, formally

```
handler h1 (\_. perform ask () + perform ask ())
```

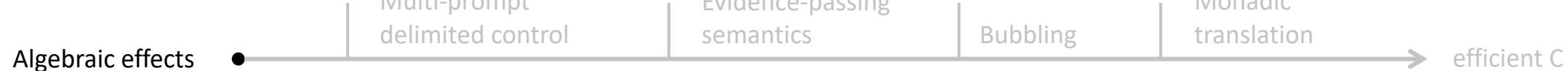
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```



Reader, formally

handler $h_1 (__. \text{perform } \text{ask} () + \text{perform } \text{ask} ())$
→ $(\text{handler}) \text{ handler } h f$ → $\text{handle } h (f ())$

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Reader, formally

handler $h1 (__. \text{perform} \ ask () + \text{perform} \ ask ())$
→ (*handler*) $\text{handler } h f$ → $\text{handle } h (f ())$
→ (*app*) $(\lambda x. e) v$ → $e[x:=v]$

```
f = \x.\k. k 1
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Reader, formally

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) handler h f → handle h (f ())
→ (app)      (λx. e) v → e[x:=v]
handle h1 (perform ask () + perform ask ())
```

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Reader, formally

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handle $h_1 (\text{perform } \text{ask} () + \text{perform } \text{ask} ())$

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→ (perform) handle h E[perform op v] → f v ( $\lambda x. \text{handle } h E[x]$ )
                                         iff  $op \notin \text{bop}(E) \wedge (op \mapsto f) \in h$ 

f () (\x. handle h1 (x + perform ask ()))

```

$f = \lambda x. \lambda k. k \ 1$
 $h1 = \text{ask} \rightarrow f$



Reader, formally

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→ (handler) handler h f → handle h (f ())
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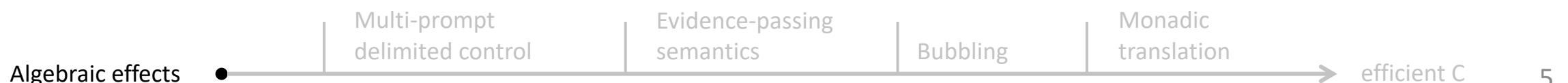
→ (app)*

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Reader, formally

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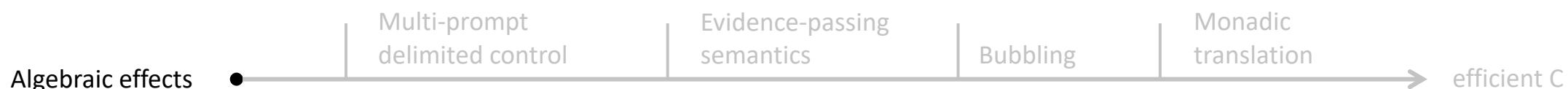
→ (app)*
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→ (app)*
    (\x. handle h1 (x + perform ask ()) 1

→ (app)

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→ (app)*
    (\x. handle h1 (x + perform ask ()) 1

→ (app)

handle h1 (1 + perform ask ())

```

$f = \lambda x. \lambda k. k \ 1$
 $h1 = \text{ask} \rightarrow f$



Reader, formally

```

handler h1 (\_. perform ask () + perform ask ())
→ (handler) handler h f → handle h (f ())
→ (app)      (λx. e) v → e[x:=v]

handle h1 (perform ask () + perform ask ())

→ (perform) handle h E[perform op v] → f v (λx. handle h E[x])
                                         iff op ∉ bop(E) ∧ (op ↦ f) ∈ h

f () (\x. handle h1 (x + perform ask ()))

→ (app)*
    (\x. handle h1 (x + perform ask ()) 1

→ (app)
    handle h1 (1 + perform ask ())

→* 2

```

Algebraic effects • Multi-prompt delimited control Evidence-passing semantics Bubbling Monadic translation → efficient C

```

f = \x.\k. k 1
h1 = ask -> f

```

Multi-prompt semantics

separating searching from capturing

Algebraic effects



Multi-prompt
delimited control

Evidence-passing
semantics

Bubbling

Monadic
translation

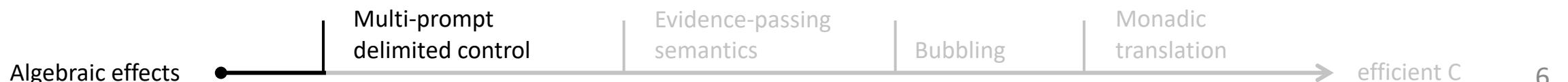
efficient C

Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  handle h1 (perform ask () + perform ask ())
→ (perform)
  f () (\x. handle h1 (x + perform ask ()))
→ (app)*
  (\x. handle h1 (x + perform ask ()) 1
→ (app)
  handle h1 (1 + perform ask ())
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```

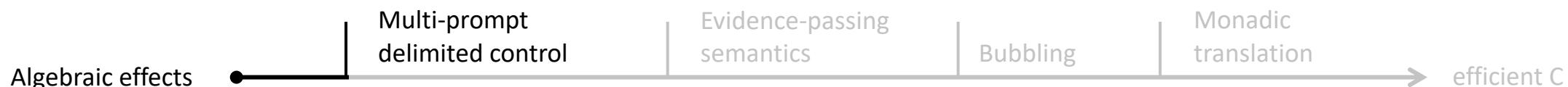


Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  handle h1 (perform ask () + perform ask ())
→ (perform)
  f () (\x. handle h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```



Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
    handle h1 (perform ask () + perform ask ())
→ (perform)
    f () (\x. handle h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```



Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform)
  f () (\x. prompt m1 h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```



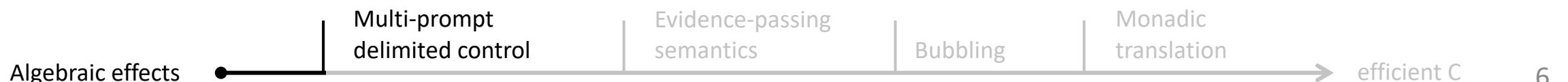
Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
prompt m1 h1 (perform ask () + perform ask ())
→ (perform)
f () (\x. prompt m1 h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```

m1: a unique marker
identifying handlers



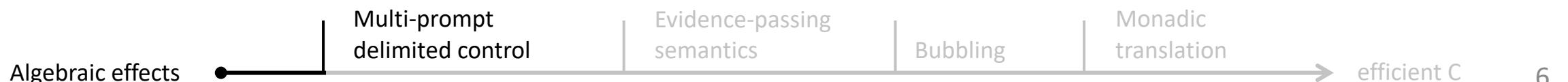
Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform)
  f () (\x. prompt m1 h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```

m1: a unique marker
identifying handlers



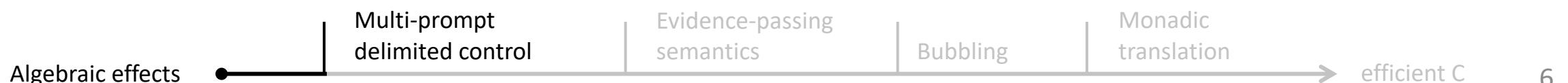
Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) iff op ∈ bop(E) ∧ (op ↦ f) ∈ h
  f () (\x. prompt m1 h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```

m1: a unique marker
identifying handlers



Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())  
→ (handler) (app)
```

```
prompt m1 h1 (perform ask () + perform ask ())  
→ (perform) iff op ∈ bop(E) ∧ (op ↦ f) ∈ h  
prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
```

```
f = \x.\k. k 1  
h1 = ask -> f
```

m1: a unique marker identifying handlers

```
f () (\x. prompt m1 h1 (x + perform ask ()))  
→* 2
```

Multi-prompt semantics

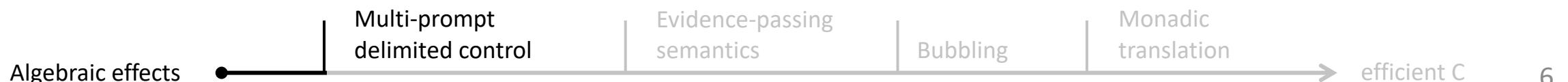
separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())  
→ (handler) (app)
```

```
prompt m1 h1 (perform ask () + perform ask ())  
→ (perform) iff op ∈ bop(E) ∧ (op ↦ f) ∈ h
```

```
prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())  
→ yielding to a handler identified by m1
```

```
f () (\x. prompt m1 h1 (x + perform ask ()))  
→* 2
```



```
f = \x.\k. k 1  
h1 = ask -> f
```

m1: a unique marker identifying handlers

yielding to a handler identified by m1

Multi-prompt semantics

separating searching from capturing

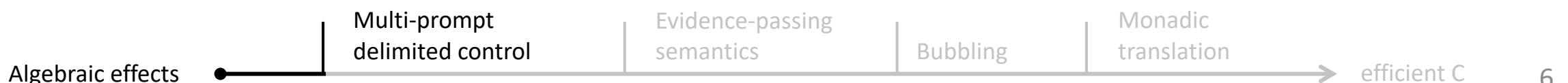
```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) iff op ∈ bop(E) ∧ (op ↦ f) ∈ h
  prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
  f () (\x. prompt m1 h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```

m1: a unique marker identifying handlers

yielding to a handler identified by m1

operation implementation partially applied to operation argument



Multi-prompt semantics

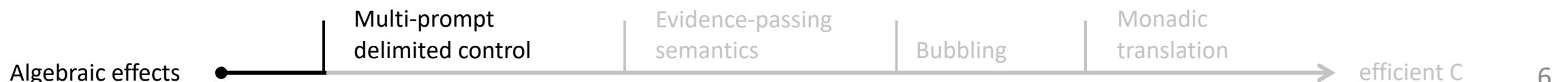
separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())  
→ (handler) (app)
```

```
prompt m1 h1 (perform ask () + perform ask ())  
→ (perform) iff op ∈ bop(E) ∧ (op ↦ f) ∈ h
```

```
prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())  
→ yielding to a handler identified by m1
```

```
f () (\x. prompt m1 h1 (x + perform ask ()))  
→* 2
```



```
f = \x.\k. k 1  
h1 = ask -> f
```

m1: a unique marker identifying handlers

yielding to a handler identified by m1

Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) iff op ∈ bop(E) ∧ (op ↦ f) ∈ h
  prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
→ (prompt)
  f () (\x. prompt m1 h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```

m1: a unique marker identifying handlers

yielding to a handler identified by m1

Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) iff op ∈ bop(E) ∧ (op ↦ f) ∈ h
  prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
→ (prompt)
  f () (\x. prompt m1 h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```

m1: a unique marker identifying handlers

yielding to a handler identified by m1

Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) iff op ∈ bop(E) ∧ (op ↦ f) ∈ h
  prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
→ (prompt)
  f () (\x. prompt m1 h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```

m1: a unique marker identifying handlers

yielding to a handler identified by m1

Multi-prompt semantics

separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) iff op ∈ bop(E) ∧ (op ↦ f) ∈ h   searching
  prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
→ (prompt)
  f () (\x. prompt m1 h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```

m1: a unique marker identifying handlers

yielding to a handler identified by m1



Multi-prompt semantics

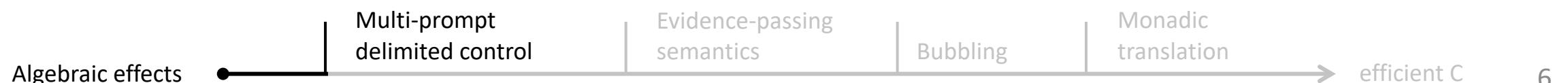
separating searching from capturing

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) iff op ∈ bop(E) ∧ (op ↦ f) ∈ h   searching
  prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
→ (prompt) capturing
  f () (\x. prompt m1 h1 (x + perform ask ()))
→* 2
```

```
f = \x.\k. k 1
h1 = ask -> f
```

m1: a unique marker identifying handlers

yielding to a handler identified by m1

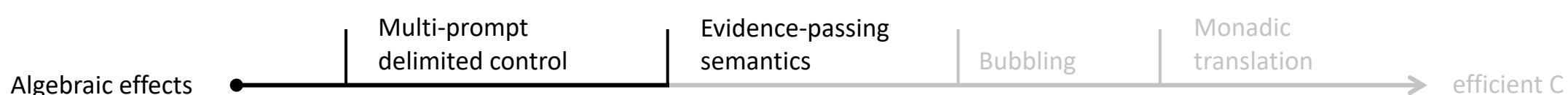


Evidence-passing semantics

make performs local: push down the current handlers as an evidence vector

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) iff op ∈ bop(E) ∧ (op ↦ f) ∈ h   searching
  prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
```

```
f = \x.\k. k 1
h1 = ask -> f
```



Evidence-passing semantics

make performs local: push down the current handlers as an evidence vector

```
f = \x.\k. k 1  
h1 = ask -> f
```

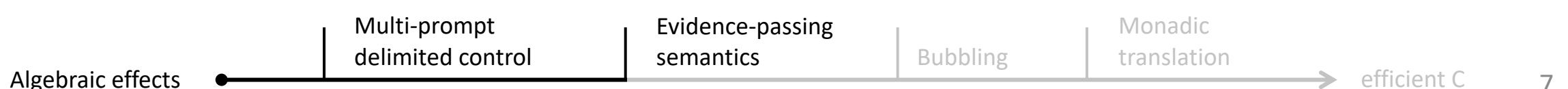
```
handler h1 (\_. perform ask () + perform ask ())
```

→ (handler) (app)

```
prompt m1 h1 (perform ask () + perform ask ())
```

→ (perform)

```
prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
```



Evidence-passing semantics

make performs local: push down the current handlers as an evidence vector

<<>>

```
handler h1 (\_. perform ask () + perform ask ())
```

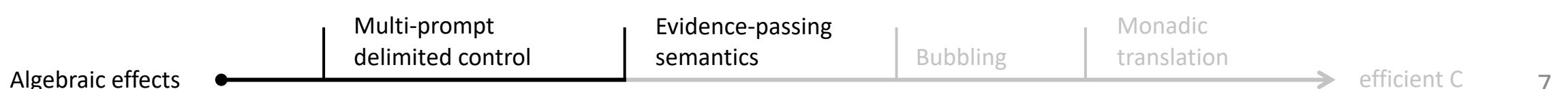
→ (handler) (app)

```
f = \x.\k. k 1  
h1 = ask -> f
```

```
prompt m1 h1 (perform ask () + perform ask ())
```

→ (perform)

```
prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
```



Evidence-passing semantics

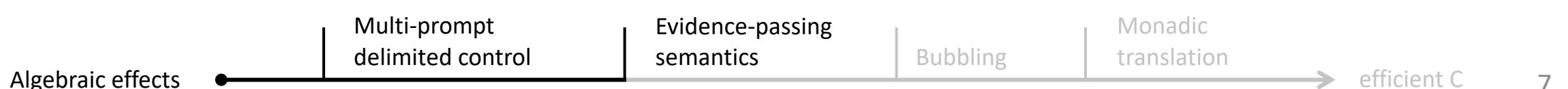
make performs local: push down the current handlers as an evidence vector

```
f = \x.\k. k 1  
h1 = ask -> f
```

handler h1 (_. **perform** ask () + **perform** ask ())
→ (handler) (app)

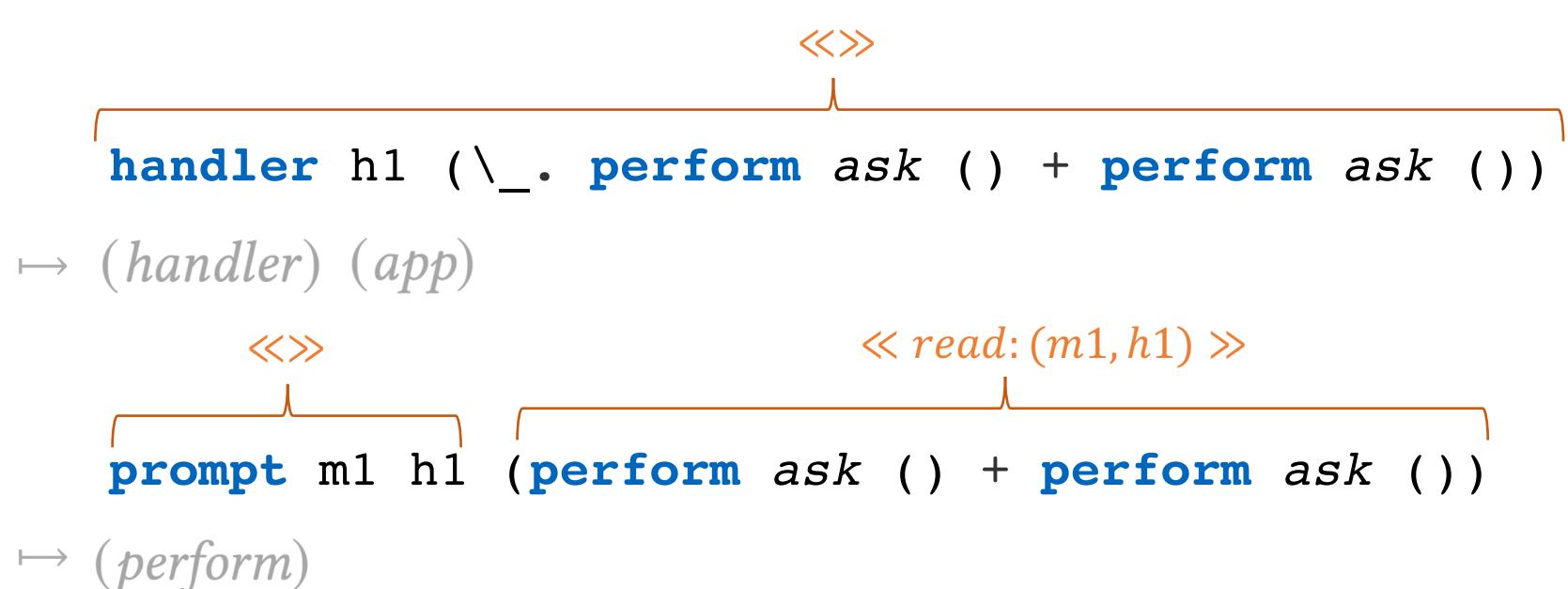
prompt m1 h1 (**perform** ask () + **perform** ask ())
→ (perform)

prompt m1 h1 (**yield** m1 (\k. f () k) + **perform** ask ())



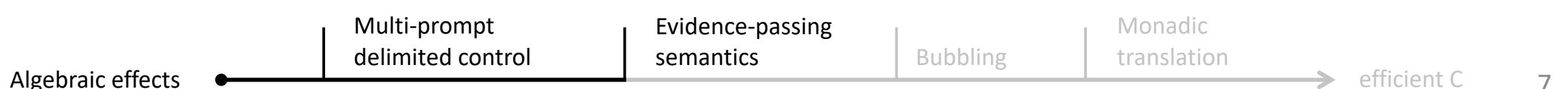
Evidence-passing semantics

make performs local: push down the current handlers as an evidence vector



```
f = \x.\k. k 1  
h1 = ask -> f
```

`prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())`



Evidence-passing semantics

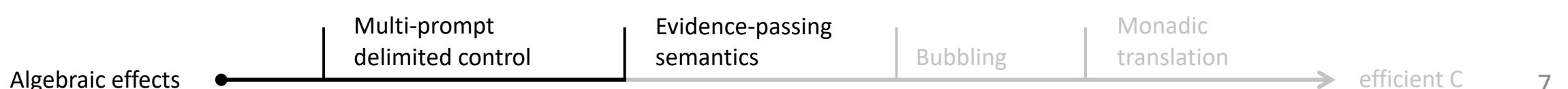
make performs local: push down the current handlers as an evidence vector

```
f = \x.\k. k 1  
h1 = ask -> f
```

`<<>>`

```
handler h1 (\_. perform ask () + perform ask ())  
→ (handler) (app)  
  
<<>> << read:(m1,h1) >>  
prompt m1 h1 (perform ask () + perform ask ())  
→ (perform) << read:(m1,h1) >>
```

```
prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
```



Evidence-passing semantics

make performs local: push down the current handlers as an evidence vector

```
f = \x.\k. k 1  
h1 = ask -> f
```

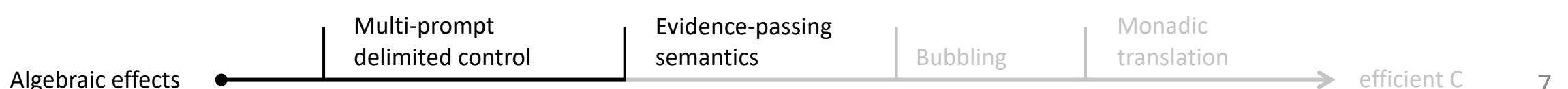
`handler h1 (_. perform ask () + perform ask ())`

→ `(handler) (app)`

`prompt m1 h1 (perform ask () + perform ask ())`

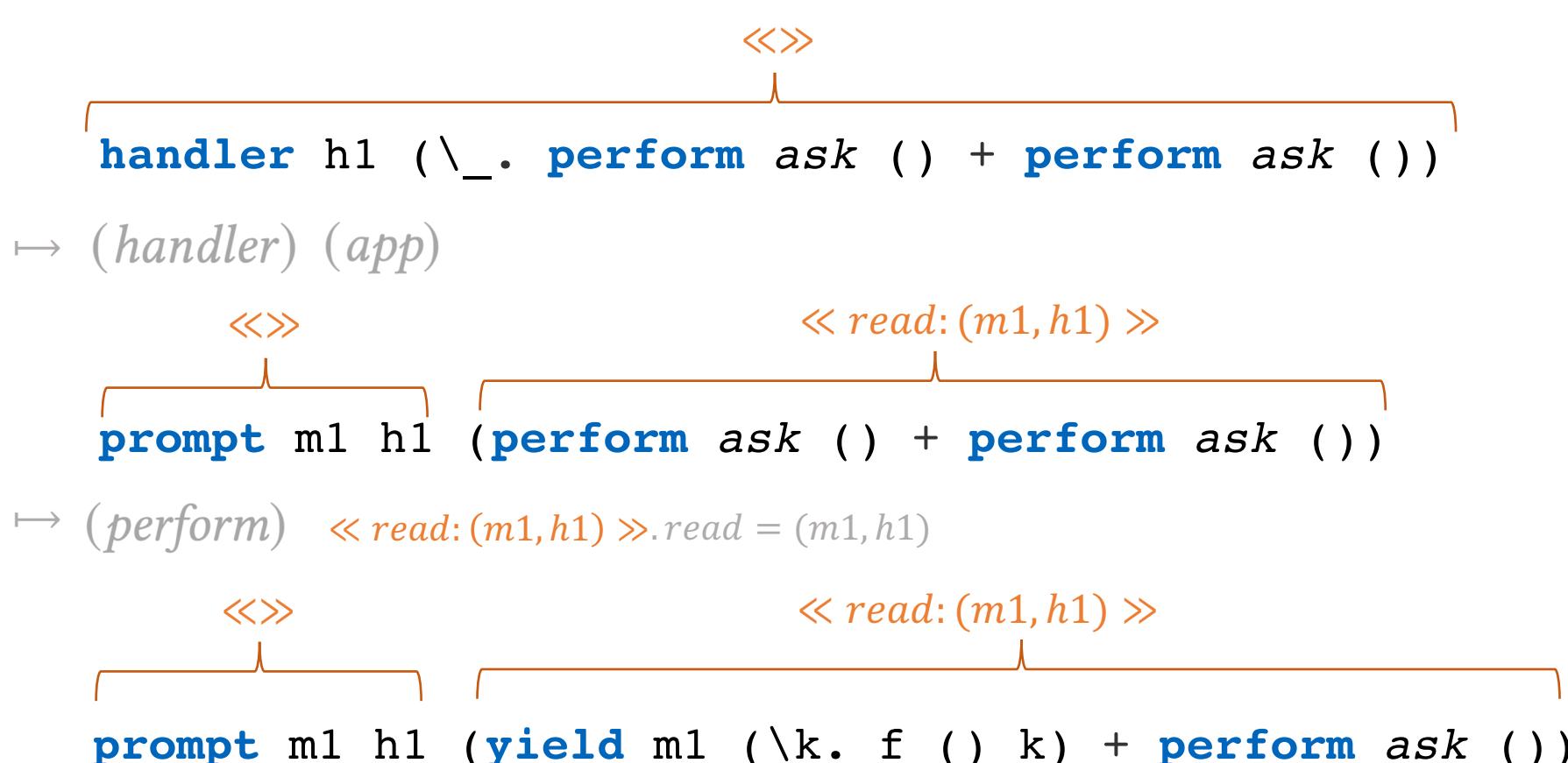
→ `(perform) << read: (m1, h1) >>.read = (m1, h1)`

`prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())`



Evidence-passing semantics

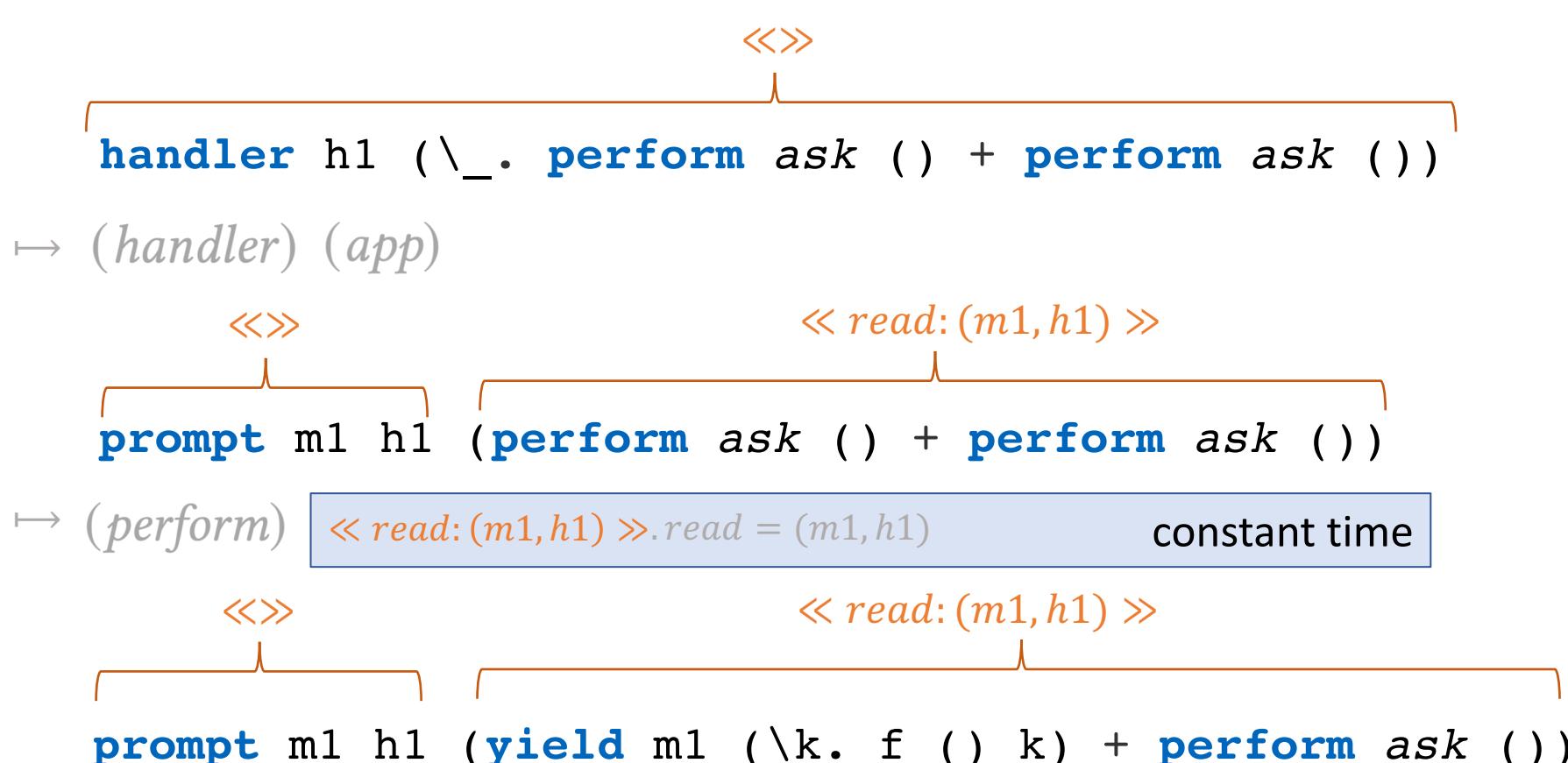
make performs local: push down the current handlers as an evidence vector



```
f = \x.\k. k 1  
h1 = ask -> f
```

Evidence-passing semantics

make performs local: push down the current handlers as an evidence vector



Optimization of tail-resumptive operations

avoid yields: evaluate tail-resumptive operations in-place

```
f = \x.\k. k 1  
h1 = ask -> f
```

```
handler h1 (\_. perform ask () + perform ask ())  
→ (handler) (app)  
    ↳ «»  
    ↳ prompt m1 h1 (perform ask () + perform ask ())  
        ↳ «read: (m1, h1) »  
        ↳ «»  
        ↳ prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())  
            ↳ «read: (m1, h1) »  
            ↳ «»
```

Optimization of tail-resumptive operations

avoid yields: evaluate tail-resumptive operations in-place

```
handler h1 (\_. perform ask () + perform ask ())  
→ (handler) (app)  
    ↳ << >>  
    ↳ prompt m1 h1 (perform ask () + perform ask ())  
→ (perform) << read: (m1, h1) >>.read = (m1, h1)  
    ↳ << >>  
    ↳ prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
```

```
f = \x.\k. k 1  
h1 = ask -> f
```

tail-resumptive operations
 $op \mapsto \lambda x. \lambda k. k e$
where $k \notin \text{fv}(e)$

Optimization of tail-resumptive operations

avoid yields: evaluate tail-resumptive operations in-place

```
handler h1 (\_. perform ask () + perform ask ())  
→ (handler) (app)  
    ↳ << >>  
    ↳ prompt m1 h1 (perform ask () + perform ask ())  
→ (perform) << read: (m1, h1) >>.read = (m1, h1)  
    ↳ << >>  
    ↳ prompt m1 h1 ( 1 + perform ask ())
```

```
f = \x.\k. k 1  
h1 = ask -> f
```

tail-resumptive operations
 $op \mapsto \lambda x. \lambda k. k e$
where $k \notin \text{fv}(e)$

Optimization of tail-resumptive operations

avoid yields: evaluate tail-resumptive operations in-place

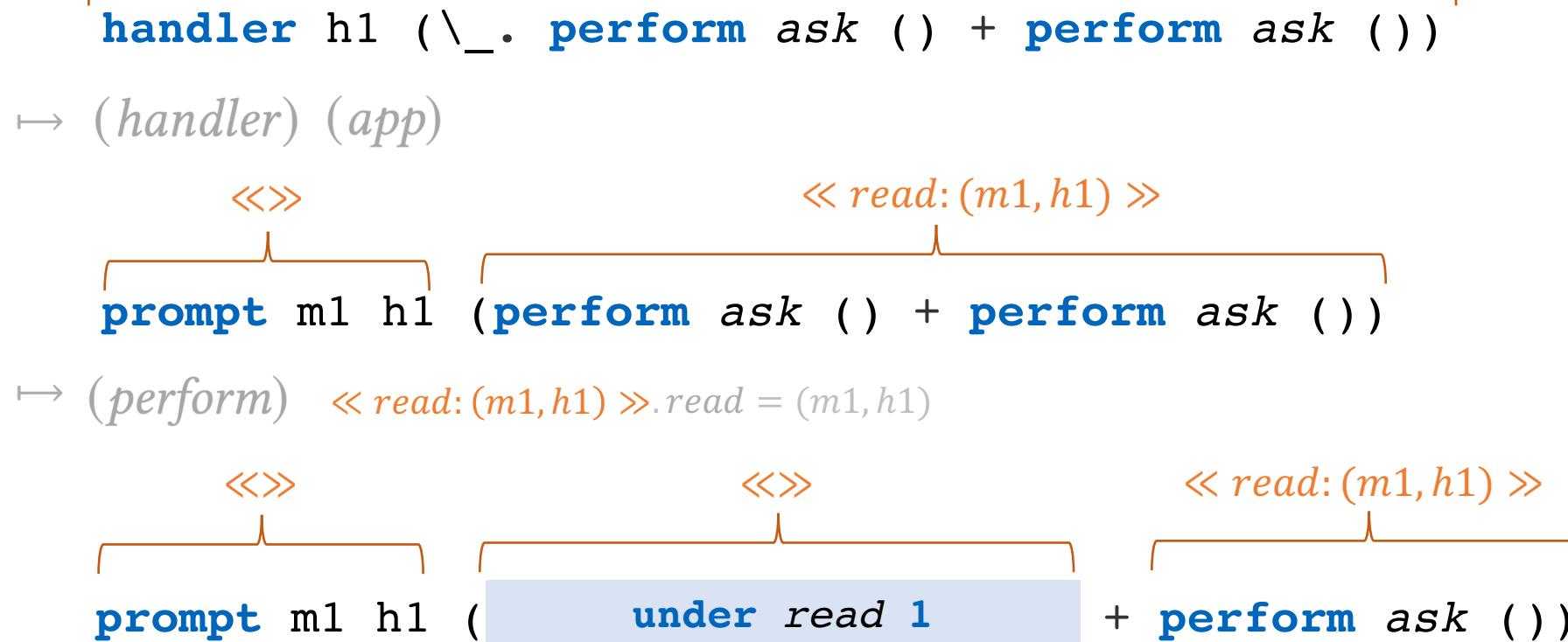
```
handler h1 (\_. perform ask () + perform ask ())  
→ (handler) (app)  
    ↳ << >>  
    ↳ prompt m1 h1 (perform ask () + perform ask ())  
→ (perform) << read: (m1, h1) >>.read = (m1, h1)  
    ↳ << >>  
    ↳ prompt m1 h1 (under read 1 + perform ask ())
```

```
f = \x.\k. k 1  
h1 = ask -> f
```

tail-resumptive operations
 $op \mapsto \lambda x. \lambda k. k e$
where $k \notin \text{fv}(e)$

Optimization of tail-resumptive operations

avoid yields: evaluate tail-resumptive operations in-place

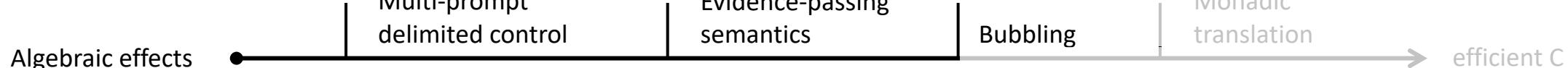


Bubbling yields

make yields local: bubbling it up until it meets its corresponding prompt frame

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) searching
  prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
→ (prompt) capturing
  f () (\x. prompt m1 h1 (x + perform ask ()))
```

```
f = \x.\k. k 1
h1 = ask -> f
```

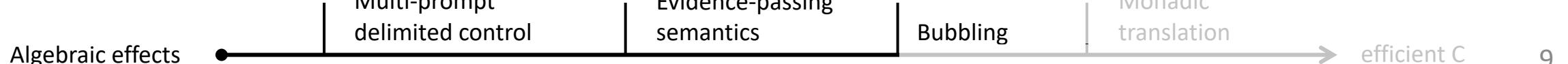


Bubbling yields

make yields local: bubbling it up until it meets its corresponding prompt frame

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) searching
  prompt m1 h1 (yield m1 (\k. f () k) + perform ask ())
→ (prompt) capturing
  f () (\x. prompt m1 h1 (x + perform ask ()))
```

```
f = \x.\k. 1 + k 1
h1 = ask -> f
```

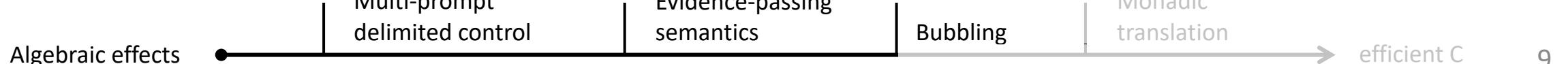


Bubbling yields

make yields local: bubbling it up until it meets its corresponding prompt frame

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (prompt) searching
  prompt m1 h1 • (+ perform ask ()) • yield m1 (\k. f () k)
→ (prompt) capturing
  f () (\x. prompt m1 h1 (x + perform ask ()))
```

```
f = \x.\k. 1 + k 1
h1 = ask -> f
```

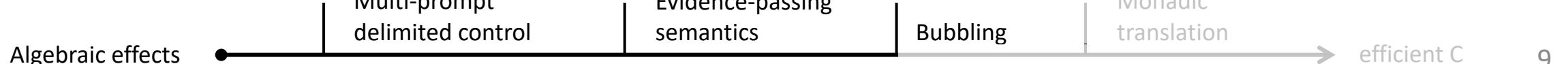


Bubbling yields

make yields local: bubbling it up until it meets its corresponding prompt frame

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) searching
  prompt m1 h1 • (+ perform ask ()) • yield m1 (\k. f () k)
→ (prompt) capturing
  f () (\x. prompt m1 h1 • (+ perform ask ()) • x)
```

```
f = \x.\k. 1 + k 1
h1 = ask -> f
```

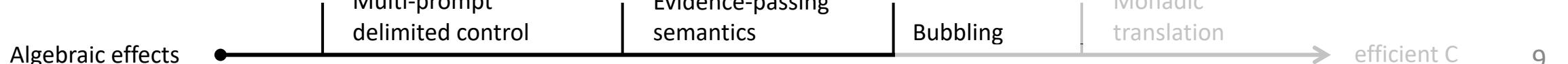


Bubbling yields

make yields local: bubbling it up until it meets its corresponding prompt frame

```
handler h1 (\_. perform ask () + perform ask ())
→ (handler) (app)
  prompt m1 h1 (perform ask () + perform ask ())
→ (perform) searching
  prompt m1 h1 • (+ perform ask ()) • yield m1 (\k. f () k)
→ (prompt) capturing
  f () (\x. prompt m1 h1 • (+ perform ask ()) • x)
```

```
f = \x.\k. 1 + k 1
h1 = ask -> f
```



Bubbling yields

make yields local: bubbling it up until it meets its corresponding prompt frame

```
handler h1 (\_. perform ask () + perform ask ())  
→ (handler) (app)
```

```
prompt m1 h1 (perform ask () + perform ask ())
```

```
→ (perform) searching
```

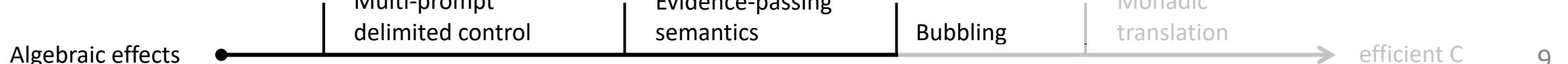
```
prompt m1 h1 • (+ perform ask ()) • yield m1 (\k. f () k) (\x. x)
```

```
→ (prompt) capturing
```

```
f () (\x. prompt m1 h1 • (+ perform ask ()) • x)
```

```
f = \x.\k. 1 + k 1  
h1 = ask -> f
```

partially built-up
resumption



Bubbling yields

make yields local: bubbling it up until it meets its corresponding prompt frame

```
handler h1 (\_. perform ask () + perform ask ())  
→ (handler) (app)
```

```
prompt m1 h1 (perform ask () + perform ask ())  
→ (perform) searching
```

```
f = \x.\k. 1 + k 1  
h1 = ask -> f
```

partially built-up resumption

```
prompt m1 h1 • (+ perform ask ()) • yield m1 (\k. f () k) (\x. x)
```

```
→ (prompt) capturing
```

```
f () (\x. prompt m1 h1 • (+ perform ask ()) • x)
```

Bubbling yields

make yields local: bubbling it up until it meets its corresponding prompt frame

```
handler h1 (\_. perform ask () + perform ask ())  
→ (handler) (app)
```

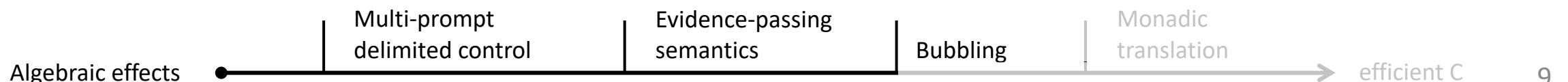
```
prompt m1 h1 (perform ask () + perform ask ())  
→ (perform) searching
```

```
prompt m1 h1 • (+ perform ask ()) • yield m1 (\k. f () k) (\x. x)  
→ (app1) bubbling
```

```
→ (prompt) capturing  
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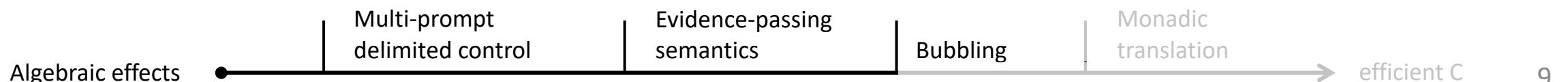
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prompt m1 h1 (perform ask () + perform ask ())  
→ (perform) searching
```

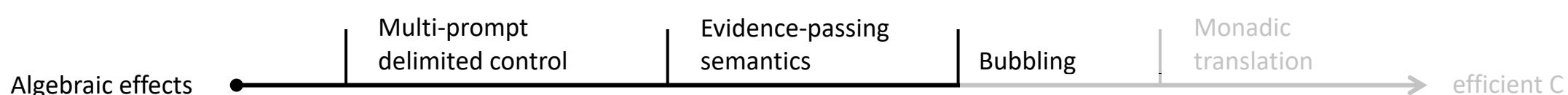
```
prompt m1 h1 • (+ perform ask ()) • yield m1 (\k. f () k) (\x. x)  
→ (app1) bubbling
```

```
prompt m1 h1 • yield m1 (\k. f () k) (\x. (+ perform ask ()) • x)  
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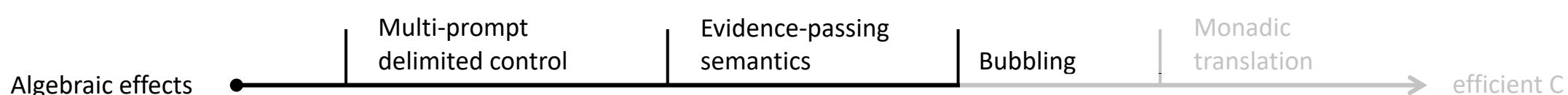
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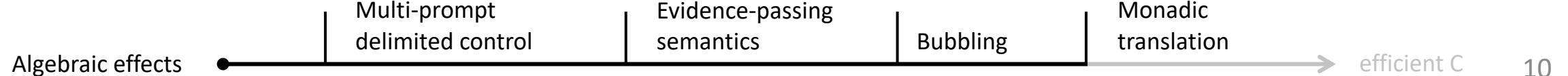
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h1 = ask -> f
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partially built-up
resumption



Monadic translation

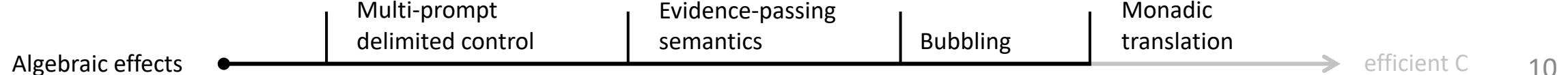
all transitions are local: translate algebraic effects into a pure lambda calculus with a multi-prompt delimited control monad



Monadic translation

all transitions are local: translate algebraic effects into a pure lambda calculus with a multi-prompt delimited control monad

```
handler h1 (\_. perform ask () + perform ask ())
```

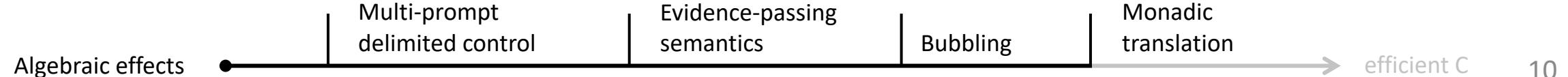


Monadic translation

all transitions are local: translate algebraic effects into a pure lambda calculus with a multi-prompt delimited control monad

```
handler h1 (\_. perform ask () + perform ask ())
```

↝



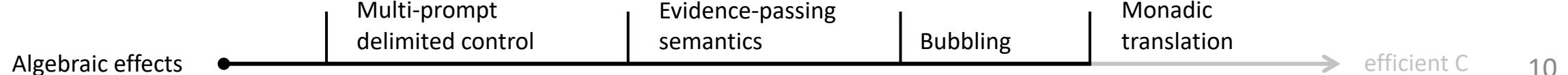
Monadic translation

all transitions are local: translate algebraic effects into a pure lambda calculus with a multi-prompt delimited control monad

```
handler h1 (\_. perform ask () + perform ask ())
```

~~~

```
handler h1 (\_. perform ask () ▷ (\x. perform ask () ▷ (\y. Pure (x + y))))
```



# Monadic translation

all transitions are local: translate algebraic effects into a pure lambda calculus with a multi-prompt delimited control monad

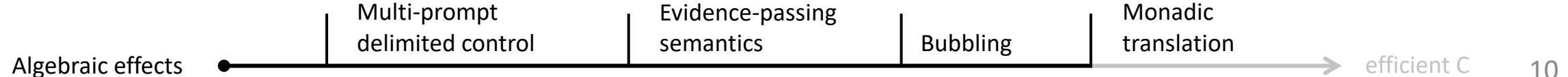
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A evidence-passing multi-prompt delimited control monad

```
type Mon μ α = Evv μ → Ctl μ α
```



Monadic translation

all transitions are local: translate algebraic effects into a pure lambda calculus with a multi-prompt delimited control monad

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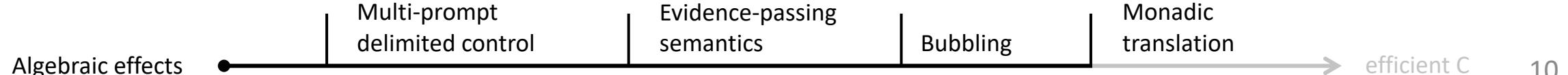
~~~

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A evidence-passing multi-prompt delimited control monad

evidence passing

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```



# Monadic translation

all transitions are local: translate algebraic effects into a pure lambda calculus with a multi-prompt delimited control monad

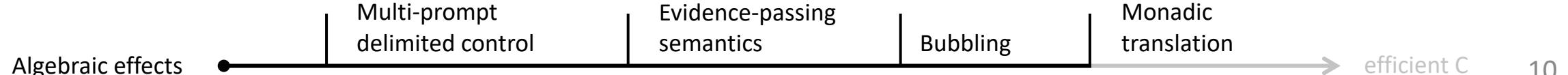
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handler h1 (\_. perform ask () ▷ (\x. perform ask () ▷ (\y. Pure (x + y))))
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A evidence-passing multi-prompt delimited control monad

evidence passing
type $\text{Mon } \mu \alpha = \boxed{\text{Ev} \nu \mu \rightarrow \text{Ctl } \mu \alpha}$
control monad



Monadic translation

all transitions are local: translate algebraic effects into a pure lambda calculus with a multi-prompt delimited control monad

```
handler h1 (\_. perform ask () + perform ask ())
```

~w~

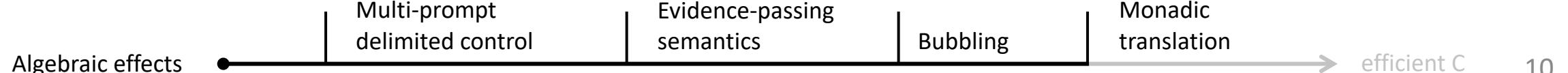
```
handler h1 (\_. perform ask () ▷ (\x. perform ask () ▷ (\y. Pure (x + y))))
```

A evidence-passing multi-prompt delimited control monad

$$\text{evidence passing}$$
$$\text{type Mon } \mu \alpha = \boxed{\text{Ev} \nu \mu \rightarrow \text{Ctl } \mu \alpha}$$

control monad

$$\begin{aligned} e \triangleright g &= \lambda w. \text{case } e w \text{ of Pure } x \rightarrow g x w \\ &\quad \text{Yield } m f k \rightarrow \text{Yield } m f (\lambda x. k x \triangleright g) \end{aligned}$$



Monadic translation

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handler h1 (\_. perform ask () + perform ask ())
```

~w~

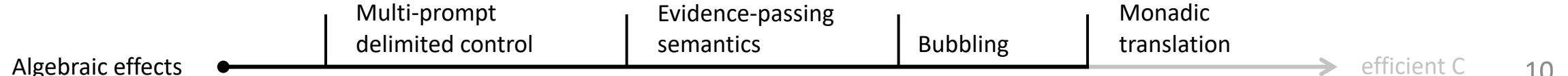
```
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A evidence-passing multi-prompt delimited control monad

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control monad

$$e \triangleright g = \lambda w. \text{case } e w \text{ of Pure } x \rightarrow g x w \longrightarrow \boxed{\text{pass the result and the current evidence}}$$
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Monadic translation

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~~~

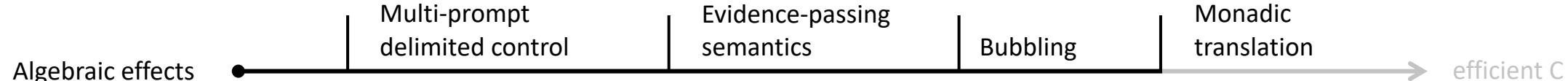
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A evidence-passing multi-prompt delimited control monad

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# Compiling to C

```
handler h1 (\_. perform ask () + perform ask ())
```

~~~

```
handler h1 (\_. perform ask () ▷ (\x. perform ask () ▷ (\y. Pure (x + y))))
```

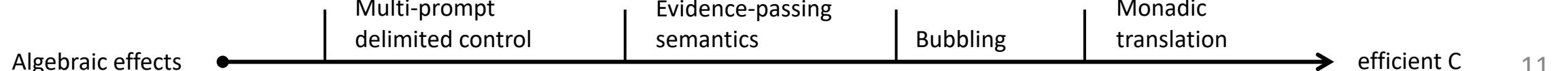
Compiling to C

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~~~

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handler h1 (\_. perform ask () > (\x. perform ask () > (\y. Pure (x + y))))
```

```
int expr( unit_t u, context_t* ctx) {
    int x = perform_ask( ctx->w[0], unit, ctx );
    if (ctx->is_yielding) { yield_extend(&join2,ctx); return 0; }
    int y = perform_ask( ctx->w[0], unit, ctx );
    if (ctx->is_yielding) { yield_extend(alloc_closure_join1(x,ctx),ctx); return 0; }
    return (x+y); }
```



# Compiling to C

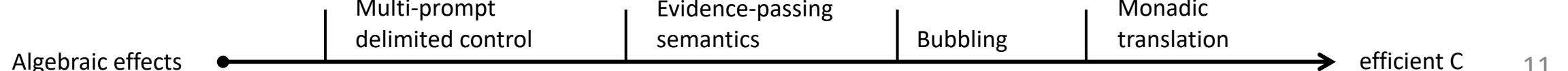
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evidence passing

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Compiling to C

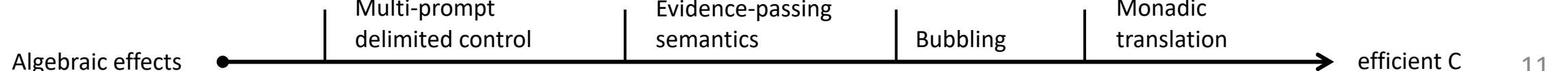
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int expr( unit_t u, context_t* ctx) { constant-time look-up
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# Compiling to C

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~>

```
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Compiling to C

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~~~

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```

control  
monad

Algebraic effects

Multi-prompt  
delimited control

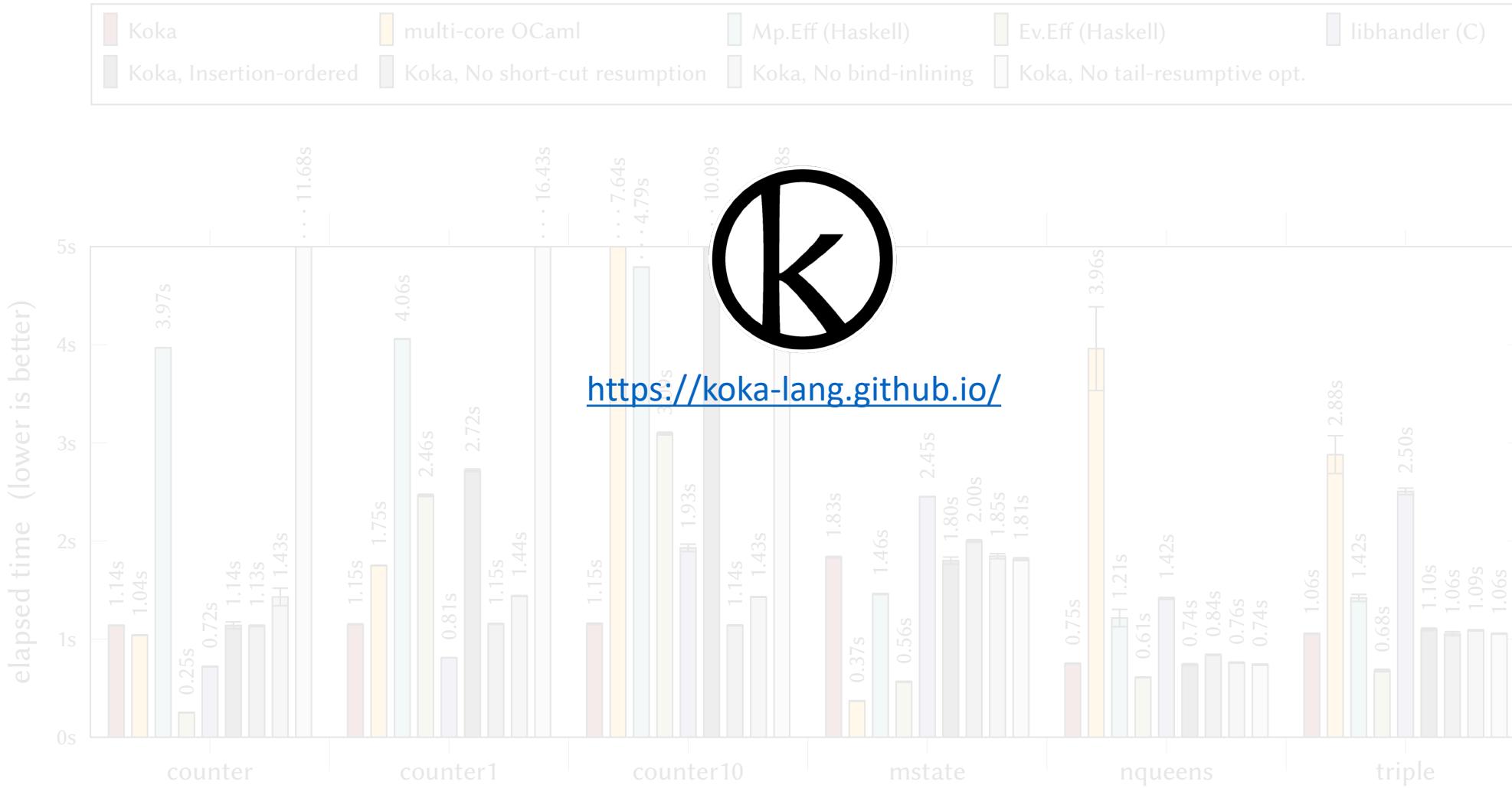
Evidence-passing  
semantics

Bubbling

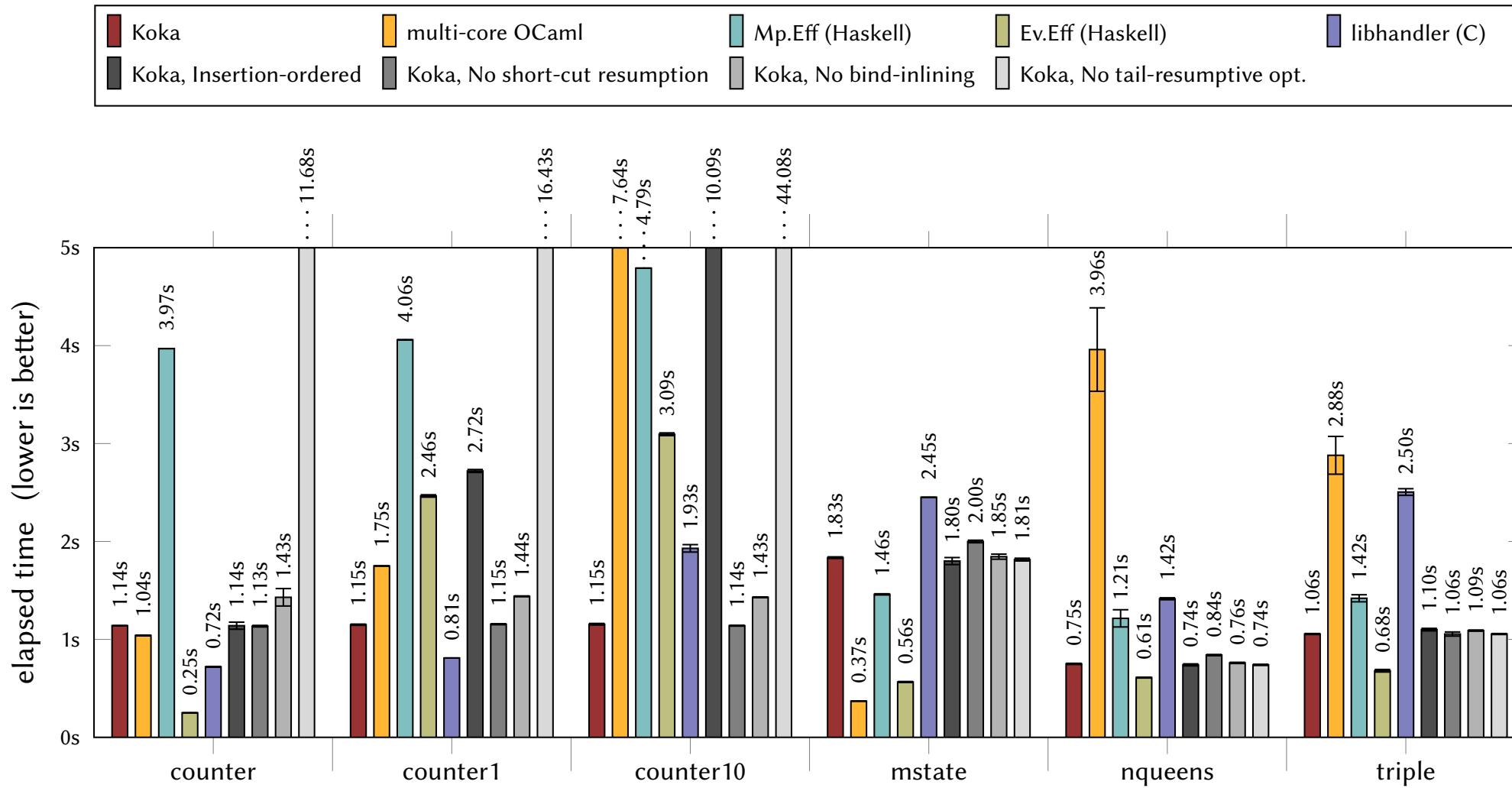
Monadic  
translation

efficient C

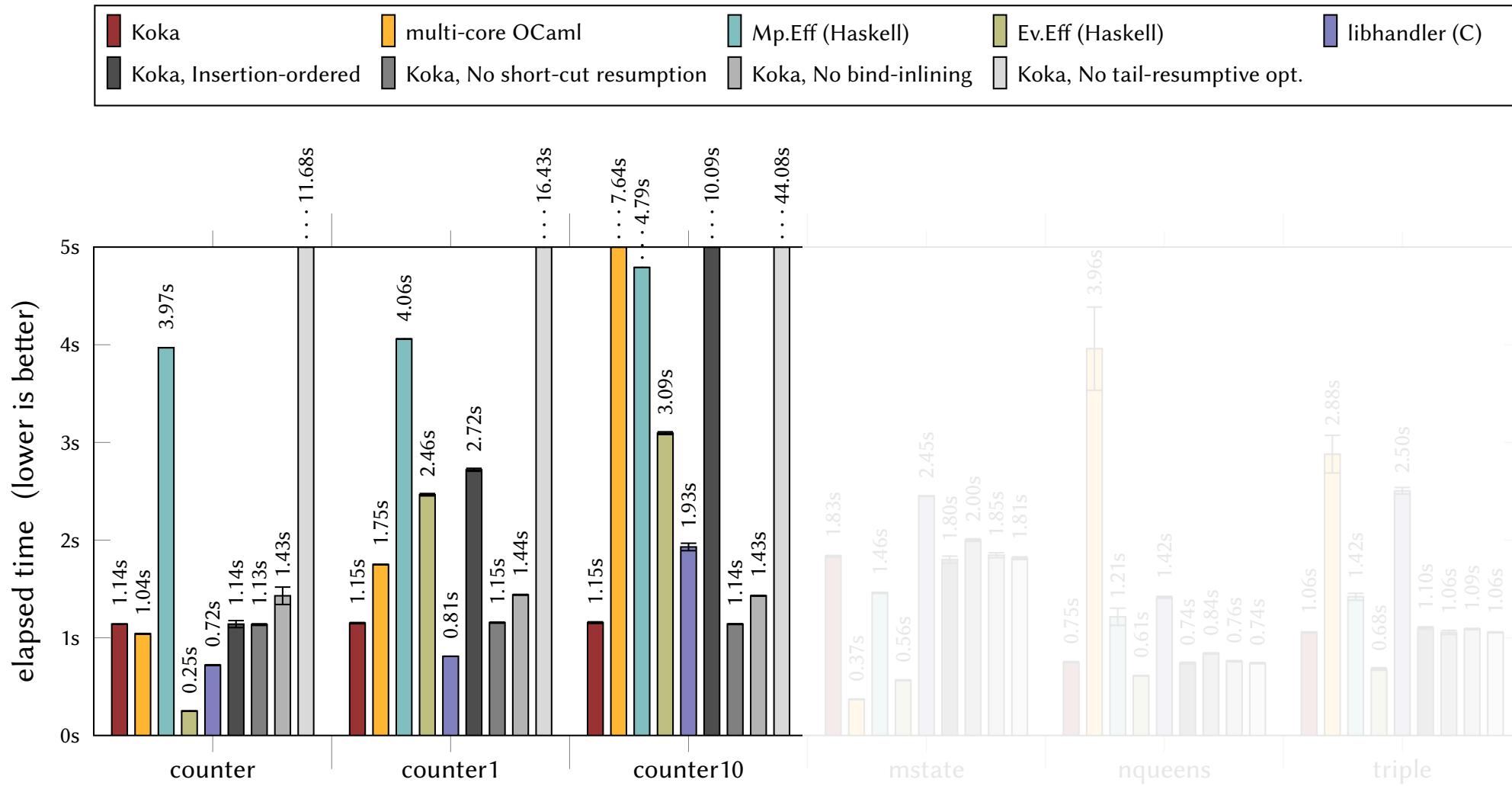
# Benchmarks



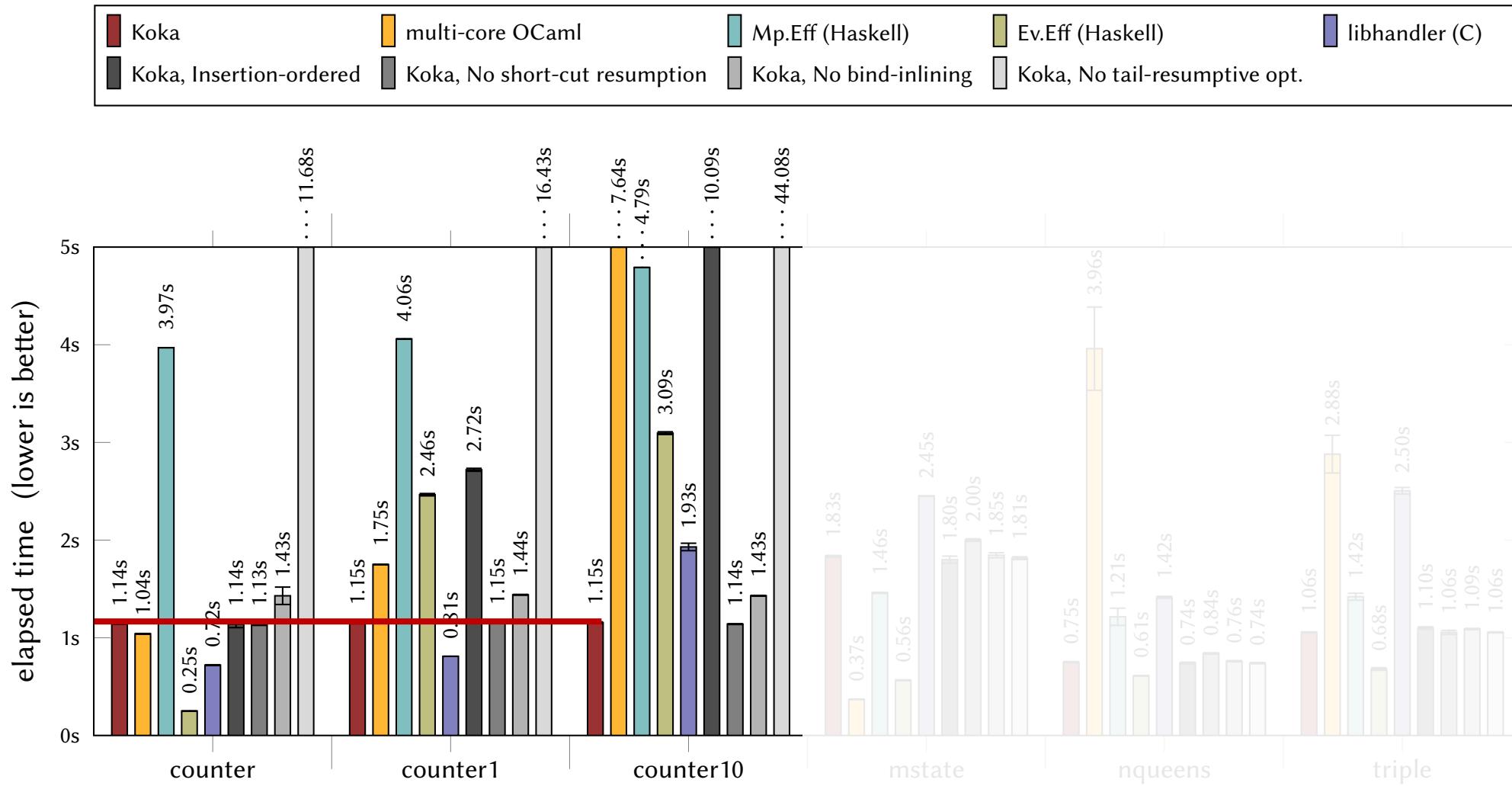
# Benchmarks



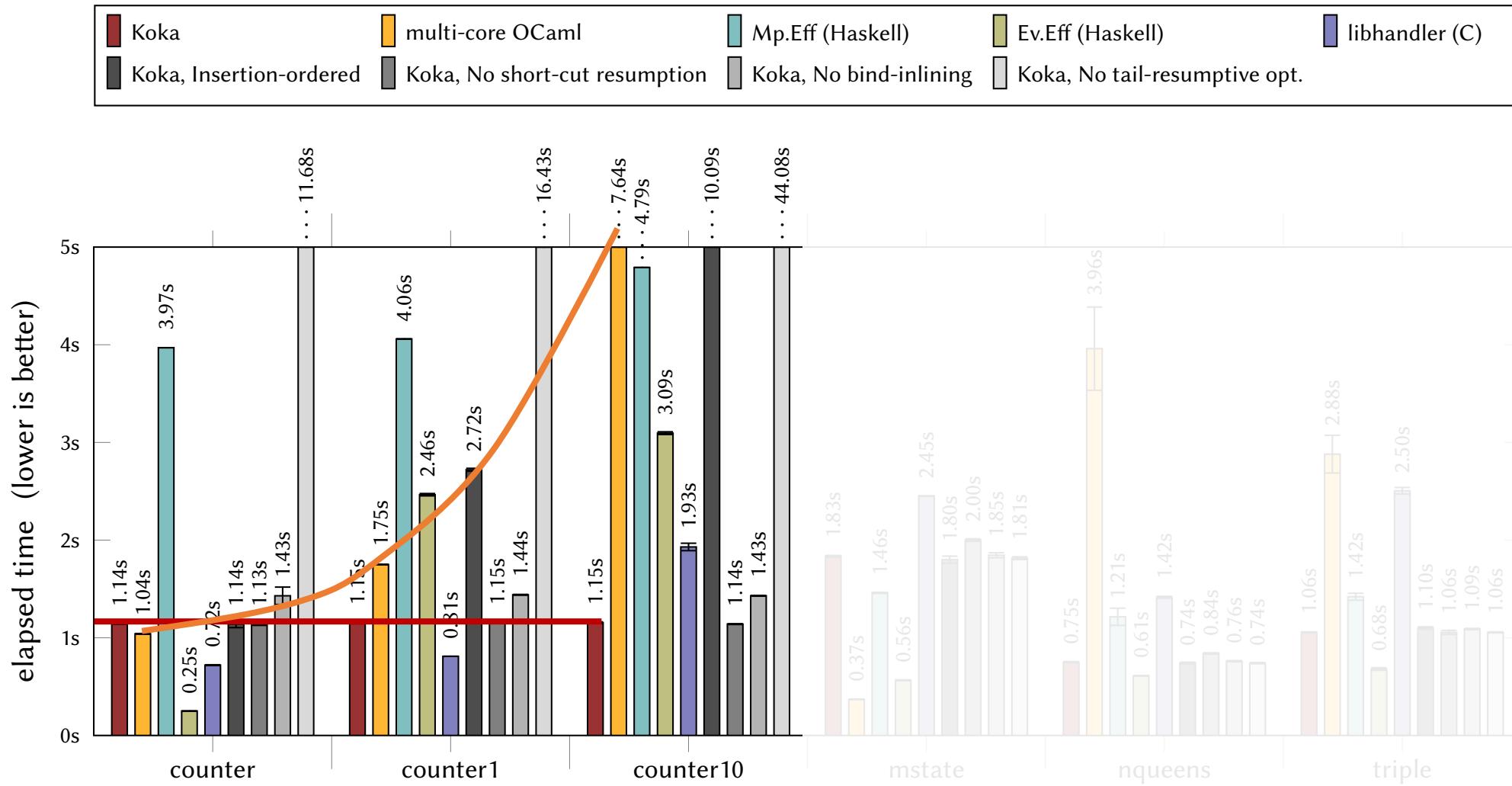
# Benchmarks



# Benchmarks

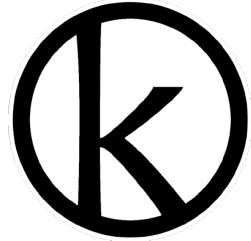


# Benchmarks



# Excited to know more?

## Programming with Effect Handlers and FBIP in Koka



<https://koka-lang.github.io/>

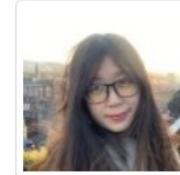
**Who** *Daan Leijen, Ningning Xie*

**Track** ICFP 2021 Tutorials

**When** (EST) Thu 26 Aug 2021 12:30 - 14:00 at [Tutorials](#) - Programming with Effect Handlers and FBIP in Koka 1



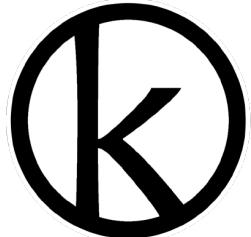
**Daan Leijen**  
[Microsoft Research](#)  
[United States](#)



**Ningning Xie**  
[University of Hong Kong](#)  
China

# Excited to know more?

## Programming with Effect Handlers and FBIP in Koka



<https://koka-lang.github.io/>

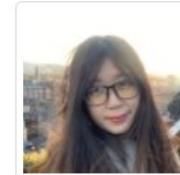
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**Daan Leijen**  
[Microsoft Research](#)  
[United States](#)



**Ningning Xie**  
[University of Hong Kong](#)  
China



**Hackage :: [Package]**

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### mpeff: Efficient effect handlers based on evidence-passing semantics

[ control, effect, library, mit ] [ Propose Tags ]

See the [Control.Mp.Eff](#) module or README.md for further information

[[Skip to Readme](#)]

Versions

[RSS] [faq]

0.1.0.0

[Change log](#)

<https://hackage.haskell.org/package/mpeff>

# Generalized Evidence Passing for Effect Handlers

Efficient Compilation of Effect Handlers to C

---



Ningning Xie



香 港 大 學  
THE UNIVERSITY OF HONG KONG

Daan Leijen



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