Application 0 Kart – Corrigé

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C1-05

C2-09



Eléments de corrigé:

Question 1:

$$\begin{cases} X_o.\overrightarrow{X_2} + Y_0.\overrightarrow{Y_2} + Z_0.\overrightarrow{Z_2} \\ \overrightarrow{0} \end{cases} , \begin{cases} X_B.\overrightarrow{X_2} + Y_B.\overrightarrow{Y_2} \\ \overrightarrow{0} \end{cases}_B = \begin{cases} X_B.\overrightarrow{X_2} + Y_B.\overrightarrow{Y_2} \\ a(X_B.\overrightarrow{Y_2} - Y_B.\overrightarrow{X_2}) \end{cases}_0$$

Question 2

On isole 2: BAME: Torseurs de
$$0 \rightarrow 2$$
 et Cm: $\left\{ egin{align*} \vec{0} \\ C_m \cdot \vec{Z} \\ \end{array} \right\}_0$; poids: $\left\{ egin{align*} m_2 \cdot g \ \vec{Y} \\ \vec{0} \\ \end{array} \right\}_G = \left\{ egin{align*} m_2 \cdot g \ \vec{Y} \\ m_2 \cdot g \cdot l_2 \cdot \vec{X} \\ \end{bmatrix}_0$

Calcul du torseur cinétique:

$$\{C(2/R)\} = \begin{cases} m_2 \overrightarrow{VG \in 2/0} \\ \sigma(\overline{G_2,2/0)} \end{cases}_G; \overrightarrow{VG \in 2/0} = \overrightarrow{0}; \overrightarrow{\sigma(G_2;2/0)} = I(G_2,2) \overrightarrow{\Omega(2/0)} = -D.\dot{\theta}_2.\overrightarrow{Y_2} + C\dot{\theta}_2.\overrightarrow{Z}$$

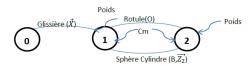
Calcul du torseur dynamique

$$\{D(2/R)\} = \left\{\begin{matrix} m_2 \Gamma \overline{G} \in \overline{2/0} \\ \delta(\overline{G_2}, 2/0) \end{matrix}\right\}_G; \overline{\Gamma G} \in \overline{2/0} = \overline{0}; \overline{\delta(G_2; 2/0)} = -D. \\ \dot{\overline{\theta}}_2. \overline{Y_2} + D\dot{\theta}_2^2. \overline{X_2} + C\ddot{\theta}_2. \\ \overline{Z} + D\dot{Z} +$$

PFS en O dans la base 2:

$$\begin{aligned} Sur\,\overrightarrow{Y_2}:X_0+X_B&=0\\ Sur\,\overrightarrow{Y_2}:Y_0+Y_B&=0\\ Sur\,\overrightarrow{Z}:Z_0&=0\\ Sur\,\overrightarrow{X_2}:-a.Y_B+m_2.g.l_2.\cos(\theta_2)&=D\dot{\theta}_2^2\\ Sur\,\overrightarrow{Y_2}:a.X_B-m_2.g.l_2.\sin(\theta_2)&=-D.\ddot{\theta}_2\\ Sur\,\overrightarrow{Z}:C_m&=C\ddot{\theta}_2 \end{aligned}$$

Question 3:



Question 4:

On isole {1+2} BAME:
$$\begin{cases} Y_{01}.\vec{Y} + Z_{01}.\vec{Z} \\ L_{01}.\vec{X} + M_{01}\vec{Y} + N_{01}.\vec{Z} \end{cases}_{D}$$

$$\begin{split} \{C(1+2/R)\} &= \{C(1/R)\} + \{C(2/R)\} \\ \{C(1/R)\} &= \begin{cases} m_1.\overrightarrow{V(G \in 1/0)} \\ \overrightarrow{0} \end{cases} \right\}_0 = \begin{cases} m_1.\overrightarrow{\lambda}.\overrightarrow{X} \\ \overrightarrow{0} \end{cases} \right\}_0 \\ \{C(2/R)\} &= \begin{cases} m_2 \overrightarrow{VG \in 2/0} \\ \sigma(\overrightarrow{G_2,2/0)} \end{cases}_G; \overrightarrow{VG \in 2/0} = \overrightarrow{\lambda}.\overrightarrow{X}; \\ \overrightarrow{\sigma(G_2;2/0)} &= I(0,2)\overrightarrow{\Omega(2/0)} = -D.\dot{\theta}_2.\overrightarrow{Y_2} + C\dot{\theta}_2.\overrightarrow{Z} \end{split}$$

Torseur dynamique:

$$\{D(1+2/R)\}=\{D(1/R)\}+\{D(2/R)\}$$

$$\begin{split} \{D(2/R)\} &= \begin{cases} m_2 \Gamma \overline{G \in 2/0} \\ \delta(\overline{G_2,2/0)} \end{cases}_G; \overline{\Gamma G \in 2/0} = \ddot{\lambda}.\vec{X}; \\ \overline{\delta(G_2;2/0)} &= -D.\ddot{\theta}_2.\overline{Y}_2^2 + D\dot{\theta}_2^2.\overline{X}_2^2 + C\ddot{\theta}_2.\vec{Z} \\ \overline{\delta(O;2/0)} &= \overline{\delta(G_2;2/0)} + \overline{OG}_2^2 \wedge m_2.\overline{\Gamma(G_2 \in 2/0)} \\ \overline{\delta(O;2/0)} &= -D.\ddot{\theta}_2.\overline{Y}_2^2 + D\dot{\theta}_2^2.\overline{X}_2^2 + C\ddot{\theta}_2.\vec{Z} + l_2.\vec{Z} \wedge m_2.\ddot{\lambda}.\vec{X} \\ \overline{\delta(O;2/0)} &= -D.\ddot{\theta}_2.\overline{Y}_2^2 + D\dot{\theta}_2^2.\overline{X}_2^2 + C\ddot{\theta}_2.\vec{Z} + l_2.m_2.\ddot{\lambda}.\vec{Y} \end{split}$$

PFS à {1+2}:

$$Sur \overrightarrow{X_0}: 0 = (m_1 + m_2).\ddot{\lambda}$$

$$Sur \overrightarrow{Y_0}: Y_{01} = m_1g + m_2g$$

$$Sur \overrightarrow{Z}: Z_0 = 0$$

$$Sur \overrightarrow{X_0}: L_{01} = D\dot{\theta}_2^2 \cos(\theta_2) + D.\ddot{\theta}_2 \sin(\theta_2)$$

$$Sur \overrightarrow{Y_0}: M_{01} = D\dot{\theta}_2^2 \sin(\theta_2) - D.\ddot{\theta}_2 \cos(\theta_2) + m_2.l_2.\ddot{\lambda}$$

$$Sur \overrightarrow{Z}: N_{01} = 0$$

Question 5:

Idem question 4 mais ajouter tous les termes complémentaires.

