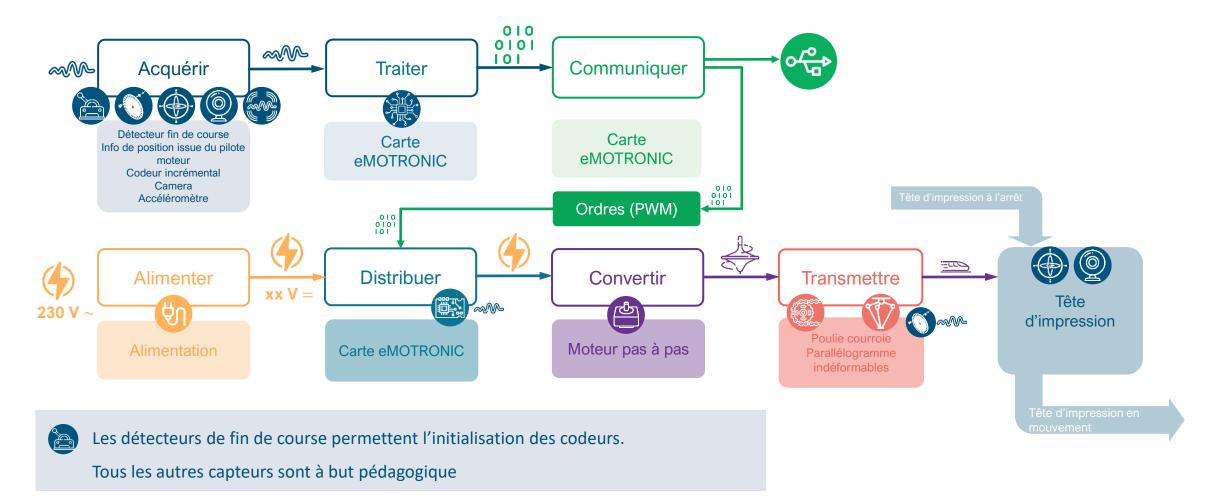


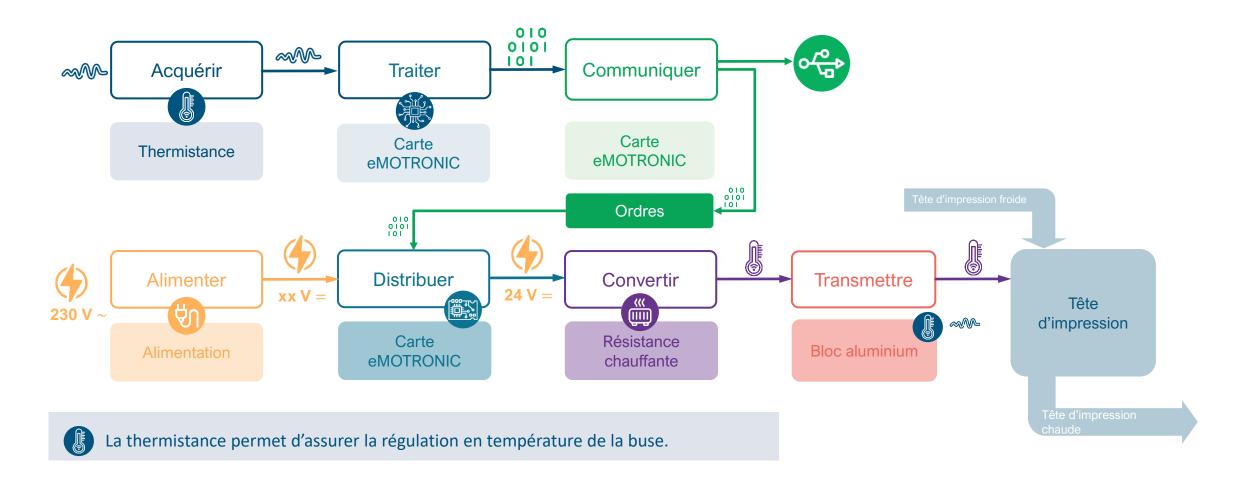
Lkj
Lkj
Qcsdv
Cs:;m;
Mù;m;
Üm;ùm

02 Chaîne fonctionnelle

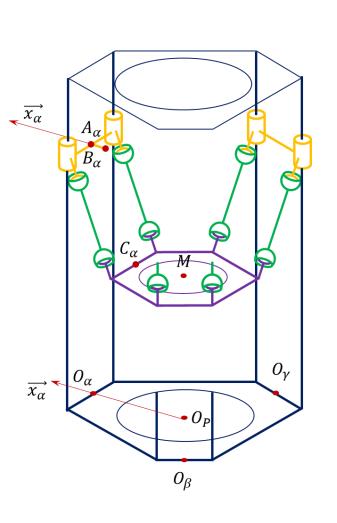
Chaine fonctionnelle de l'axe Z_{γ}

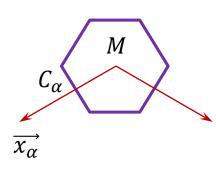


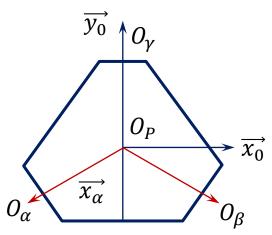
Chaine fonctionnelle de la tête chauffante



04 – Résolution cinématique







$$\square \overrightarrow{O_P O_\alpha} = L \overrightarrow{x_\alpha}$$

$$\Box \overrightarrow{O_{\alpha} A_{\alpha}} = z_{\alpha} \overrightarrow{z_0}$$

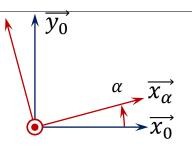
$$\Box \overrightarrow{A_{\alpha}B_{\alpha}} = -e\overrightarrow{x_{\alpha}}$$

$$\square \overrightarrow{B_{\alpha}C_{\alpha}} = L_b \overrightarrow{u_{\alpha}}$$

$$\Box \overrightarrow{C_{\alpha}M} = -d\overrightarrow{x_{\alpha}}$$

$$\Box \overrightarrow{O_P M} = x_M \overrightarrow{x_0} + y_M \overrightarrow{y_0} + z_M \overrightarrow{z_0}$$

 $\overrightarrow{x_0}$ \square On pose $\ell = L - e - d$



☐ La fermeture géométrique permet d'écrire que

$$\square \iff \overrightarrow{O_P O_\alpha} + \overrightarrow{O_\alpha A_\alpha} + \overrightarrow{A_\alpha B_\alpha} + \overrightarrow{B_\alpha C_\alpha} + \overrightarrow{C_\alpha M} = x_M \overrightarrow{x_0} + y_M \overrightarrow{y_0} + z_M \overrightarrow{z_0}$$

$$\square \iff L\overrightarrow{x_{\alpha}} + z_{\alpha}\overrightarrow{z_{0}} - e\overrightarrow{x_{\alpha}} + L_{b}\overrightarrow{u_{\alpha}} - d\overrightarrow{x_{\alpha}} = x_{M}\overrightarrow{x_{0}} + y_{M}\overrightarrow{y_{0}} + z_{M}\overrightarrow{z_{0}}$$

$$\Box \Leftrightarrow L_b \overrightarrow{u_\alpha} = x_M \overrightarrow{x_0} + y_M \overrightarrow{y_0} + z_M \overrightarrow{z_0} - L \overrightarrow{x_\alpha} - z_\alpha \overrightarrow{z_0} + e \overrightarrow{x_\alpha} + d \overrightarrow{x_\alpha}$$

$$\square \Leftrightarrow L_b \overrightarrow{u_\alpha} = x_M \overrightarrow{x_0} + y_M \overrightarrow{y_0} + z_M \overrightarrow{z_0} + (-L + e + d) \overrightarrow{x_\alpha} - z_\alpha \overrightarrow{z_0}$$

$$\Box \Leftrightarrow L_b \overrightarrow{u_\alpha} = x_M \overrightarrow{x_0} + y_M \overrightarrow{y_0} + (z_M - z_\alpha) \overrightarrow{z_0} - \ell \overrightarrow{x_\alpha}$$

$$\square \Leftrightarrow L_b \overrightarrow{u_\alpha} = x_M \overrightarrow{x_0} + y_M \overrightarrow{y_0} + (z_M - z_\alpha) \overrightarrow{z_0} - \ell(\cos \alpha \overrightarrow{x_0} + \sin \alpha \overrightarrow{y_0})$$

$$\square \iff L_b \overrightarrow{u_\alpha} = (x_M - \ell \cos \alpha) \overrightarrow{x_0} + (y_M - \ell \sin \alpha) \overrightarrow{y_0} + (z_M - z_\alpha) \overrightarrow{z_0}$$

$$\Box \Rightarrow L_b^2 = (x_M - \ell \cos \alpha)^2 + (y_M - \ell \sin \alpha)^2 + (z_M - z_\alpha)^2$$

$$\Box \Rightarrow L_b^2 - (x_M - \ell \cos \alpha)^2 - (y_M - \ell \sin \alpha)^2 = (z_M - z_\alpha)^2$$

$$\square \overrightarrow{O_P O_\alpha} = L \overrightarrow{x_\alpha}$$

$$\square \overrightarrow{O_{\alpha} A_{\alpha}} = z_{\alpha} \overrightarrow{z_0}$$

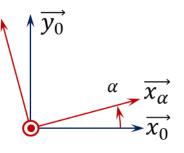
$$\Box \overrightarrow{A_{\alpha}B_{\alpha}} = -e\overrightarrow{x_{\alpha}}$$

$$\square \overrightarrow{B_{\alpha}C_{\alpha}} = L_{b}\overrightarrow{u_{\alpha}}$$

$$\Box \overrightarrow{C_{\alpha}M} = -d\overrightarrow{x_{\alpha}}$$

$$\square \overrightarrow{O_P M} = x_M \overrightarrow{x_0} + y_M \overrightarrow{y_0} + z_M \overrightarrow{z_0}$$

 \square On pose $\ell = L - e - d$



☐ On a vu que:

$$z_{\alpha} = z_{M} - \sqrt{L_{b}^{2} - (x_{M} - \ell \cos \alpha)^{2} - (y_{M} - \ell \sin \alpha)^{2}} \text{ avec } \alpha = -150^{\circ}$$

$$z_{\beta} = z_{M} - \sqrt{L_{b}^{2} - (x_{M} - \ell \cos \beta)^{2} - (y_{M} - \ell \sin \beta)^{2}} \text{ avec } \beta = -30^{\circ}$$

$$z_{\gamma} = z_{M} - \sqrt{L_{b}^{2} - (x_{M} - \ell \cos \gamma)^{2} - (y_{M} - \ell \sin \gamma)^{2}} \text{ avec } \gamma = 90^{\circ}$$

$$z_{\beta} = z_{M} - \sqrt{L_{b}^{2} - (x_{M} - \ell \cos \beta)^{2} - (y_{M} - \ell \sin \beta)^{2}}$$
 avec $\beta = -30$

$$z_{\gamma} = z_{M} - \sqrt{L_{b}^{2} - (x_{M} - \ell \cos \gamma)^{2} - (y_{M} - \ell \sin \gamma)^{2}}$$
 avec $\gamma = 90^{\circ}$