

(P-5i)

$$\int x^2 \cdot (e^{\frac{x}{7}} + \sqrt[5]{x^2}) dx = \underbrace{\int x^2 \cdot e^{\frac{x}{7}} dx}_{\text{left}} + \underbrace{\int x^2 \cdot \sqrt[5]{x^2} dx}_{\text{right}} =$$

$$\int x^2 \cdot e^{\frac{x}{7}} dx = \left| \begin{array}{l} u = x^2 \quad u' = 2x \\ v' = e^{\frac{x}{7}} \quad v = 7 \cdot e^{\frac{x}{7}} \end{array} \right| =$$
$$= x^2 \cdot 7e^{\frac{x}{7}} + c - \int 2x \cdot 7e^{\frac{x}{7}} dx$$

$$\int 2x \cdot 7e^{\frac{x}{7}} dx = 14 \int x \cdot e^{\frac{x}{7}} dx = \left| \begin{array}{l} u = x \quad u' = 1 \\ v' = e^{\frac{x}{7}} \quad v = 7e^{\frac{x}{7}} \end{array} \right| =$$
$$= 14(x \cdot 7e^{\frac{x}{7}} + c - \int 1 \cdot 7e^{\frac{x}{7}} dx) = 14(7x \cdot e^{\frac{x}{7}} + c - 7 \int e^{\frac{x}{7}} dx)$$
$$= 14(7x e^{\frac{x}{7}} - 49e^{\frac{x}{7}} + c)$$

$$= x^2 \cdot 7e^{\frac{x}{7}} - 14(7x e^{\frac{x}{7}} - 49e^{\frac{x}{7}}) + \sqrt[5]{3} \frac{5x^{\frac{12}{5}}}{12} + c$$

$$\sqrt[5]{3} \int x^2 \cdot x^{\frac{2}{5}} dx =$$
$$= \sqrt[5]{3} \cdot \int x^{\frac{12}{5}} dx =$$
$$= \sqrt[5]{3} \cdot \frac{x^{\frac{12}{5}+1}}{\frac{12}{5}+1} + c = \sqrt[5]{3} \cdot \frac{5 \cdot \sqrt[5]{x^{17}}}{17} + c$$