

$Q \in R^{L_Q \times d_{model}}$ $K \in R^{L_k \times d_{model}}$

$\frac{1}{\sqrt{d_k}} \times \text{sum}(\text{[red blocks]} \cdot [\text{red blocks}]^T)$

$\mathcal{A}(Q, K, V) = \frac{QK^T}{\sqrt{d_k}} V$ (a) Attention

Q $\bar{K} \in R^{L_{\bar{K}} \times d_{model}}$ $\bar{Q} \in R^{L_{\bar{Q}} \times d_{model}}$ \bar{Q} K

$\text{Top}(\text{[red blocks]} \cdot [\text{yellow blocks}]^T) \rightarrow \text{[blue blocks]} \rightarrow \frac{1}{\sqrt{d_k}} \times \text{sum}(\text{[blue blocks]} \cdot [\text{red blocks}]^T)$

$\mathcal{A}(Q, K, V) = \frac{\bar{Q} K^T}{\sqrt{d_k}} V$ (b) Probsparse attention

$Q_{period} \in R^{L_{period} \times d_{model}}$ $\bar{K} \ A_h \in R^{L_{\bar{K}} \times d_{model}}$

$\text{Top}(\text{[red blocks]} \cdot [\text{purple/green/grey blocks}] \odot [\text{olive blocks}]^T) \rightarrow \text{[blue blocks]} \rightarrow \text{Expand}(\frac{1}{\sqrt{d_k}} \times \text{sum}[\text{[blue blocks]} \cdot [\text{red blocks}]^T])$

(c) Periodic attention

- Matrix product
- ⊙ Hadamard product

$K_{period} \in R^{L_{period} \times d_{model}}$

\bar{Q} K

$\mathcal{A}(Q, K, V) = \frac{\bar{Q} K^T}{\sqrt{d_k}} V$

