

Solving Sudoku using Hill Climbing

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1 Problem Description

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Given an incomplete Sudoku puzzle where some of the cells are filled with digits and others are left empty, the task is to fill in the empty cells while ensuring that the completed puzzle satisfies the Sudoku constraints.

2 Hill Climbing Algorithm

Hill climbing is a local search algorithm that iteratively improves a candidate solution by making incremental changes. In the context of solving Sudoku, the hill climbing algorithm works as follows:

- 1. Initialization: Start with a randomly filled Sudoku board.
- 2. Neighbor Generation: Generate a neighboring solution by making a small change to the current solution.
- 3. Evaluation: Calculate the score of the neighbor solution based on the duplicate digits in rows, columns, and subgrids.
- 4. Move Selection: If the neighbor solution has a lower score, move to that solution. Otherwise, continue with the current solution.
- 5. Termination: Repeat steps 2-4 until a solution score of 0 is found or restart the algorithm if a certain number of iterations are done.

3 Common Problems

While hill climbing is a straightforward algorithm, there are some common challenges when applying

reachable from the current state

it to Sudoku: • Local Optima: Hill climbing can get stuck in local optima where no better solution is

4 Used Algorithms

Three versions of neighbor generators have been implemented:

- RandPosFill Randomly select a position from the cells that need to be filled with a number and then generate a random number to fill it.
- **BestPosFill** Randomly select a position from the cells that need to be filled with a number. Then, fill it with a number that minimizes the number of conflicts in the current row and column.

SwapTwoRandom Randomly select two positions from the cells that need to be filled with a number and then swap them.

5 Results

The SwapTwoRandom strategy proved less effective than RandPosFill and BestPosFill. This is due to its reliance on purely random starting states, ignoring collision counts. Consequently, random cell swaps do little to solve the puzzle, failing even on easier ones with fewer than 10 missing values.s

Therefore, I conducted tests using only the Rand-PosFill and BestPosFill strategies on 9x9 and 16x16 Sudoku grids with different numbers of empty cells. Please refer to the table below for the summarized outcomes.

- 15/25 Missing Values: Quite challenging, requires logical reasoning and careful deduc-
- 30/35 Missing Values: Very challenging, needs advanced techniques like X-wing and swordfish.