Course: "Fundamentals of Cryptography".

Laboratory work No. 9. Hash functions

The task 1:

Calculate hash functions for 5 different combinations of **n** and **m** for each of the following tasks as

1.1.
$$h(n) = n \mod m$$

1.2.
$$h(n) = (h(n1) + h(n2) + h(n3) + h(n4) + h(n5) + h(n6)) \mod m$$

The values **n**, **n1-n6** and **m** are chosen from the tables of the initial IP permutation and the final IP permutation arbitrarily.

Combinations must be calculated for cases when:

A) even **n** and odd **m**;

C) odd n and even m.

Write a program that implements the implementation of points 1 and 2.

Record the results in the form of a table.

Task 2:

2.1. Suggest your own algorithm for fast transformation of a string of arbitrary length into a hash code.

Task 3:

3.1. Implement Schnopp's digital signature algorithm for arbitrary values of ${\bf p}$ and ${\bf q}$.

Schnorr's electronic signature algorithm.

At the first stage, the parameters of the algorithm are selected:

p is a simple number, for real problems its length should be 160 bits < p < 256 bits;

q is a prime number chosen so that it is a divisor of the number p-1);

 ${\bf g}$ is chosen according to a special procedure from ${\bf Z}_p$, where ${\bf Z}_p$ is the class of residues modulo ${\bf p}$;

H - hash function;

 \mathbf{x} is a random number from the interval [1, q-1]; \mathbf{x} – private key of the scheme;

y - public key of the scheme;

Y=g-x.

After the parameters are selected, the algorithm operations are performed:

1. Participant A chooses a random number k and calculates r=g*k(mod p).

(for this example the number \mathbf{g} is chosen arbitrarily)

2. Participant A creates a signature, for this purpose **e** and s are calculated according to the formulas

$$e = H(r,A);$$
 $s=k+xe.$

- 3. Signature (e,s) and text M are sent to participant B.
- 4. Participant B verifies the signature by calculating the values of r' and e',

$$r' = g*s*y*e mod p;$$

$$e' = h(r', m)$$
.

5. The values of e and e' are compared.

The task 4:

2.1. Write a program that implements items 1,2 and 4,5.