### code

January 16, 2022

### 0.1 Exporting the results to PDF

Once you complete the assignments, export the entire notebook as PDF and attach it to your homework solutions. The best way of doing that is 1. Run all the cells of the notebook. 2. Export/download the notebook as PDF (File -> Download as -> PDF via LaTeX (.pdf)). 3. Concatenate your solutions for other tasks with the output of Step 2. On linux, you can use pdfunite, there are similar tools for other platforms, too. You can only upload a single PDF file to Moodle.

Make sure you are using nbconvert version 5.5 or later by running jupyter nbconvert --version. Older versions clip lines that exceed page width, which makes your code harder to grade.

### 1 Matrix Factorization

```
[]: import time
  import scipy.sparse as sp
  import numpy as np
  import warnings
  from scipy.sparse.linalg import svds
  from sklearn.linear_model import Ridge

import matplotlib.pyplot as plt
  %matplotlib inline
```

### 1.1 Restaurant recommendation

The goal of this task is to recommend restaurants to users based on the rating data in the Yelp dataset. For this, we try to predict the rating a user will give to a restaurant they have not yet rated based on a latent factor model.

Specifically, the objective function (loss) we wanted to optimize is:

$$\mathcal{L} = \min_{P,Q} \sum_{(u,i) \in S} (R_{ui} - \mathbf{q}_u \mathbf{p}_i^T)^2 + \lambda \sum_i \|\mathbf{p}_i\|^2 + \lambda \sum_u \|\mathbf{q}_u\|^2$$

where S is the set of (u, i) pairs for which the rating  $R_{ui}$  given by user u to restaurant i is known. Here we have also introduced two regularization terms to help us with overfitting where  $\lambda$  is hyperparameter that control the strength of the regularization. The task it to solve the matrix factorization via alternating least squares and stochastic gradient descent (non-batched, you may omit the bias).

**Hint 1**: Using the closed form solution for regression might lead to singular values. To avoid this issue perform the regression step with an existing package such as scikit-learn. It is advisable to use ridge regression to account for regularization.

**Hint 2**: If you are using the scikit-learn package remember to set fit\_intercept = False to only learn the coefficients of the linear regression.

### 1.1.1 Load and Preprocess the Data (nothing to do here)

```
[]: ratings = np.load("exercise 11 matrix factorization ratings.npy")
[]: # We have triplets of (user, restaurant, rating).
     ratings
[]: array([[101968,
                                   1],
                        1880,
            [101968,
                                   5],
                        284,
            [101968,
                        1378,
                                   2],
            [72452,
                        2100,
                                   4],
            [72452,
                       2050,
                                   5],
            [ 74861,
                                   5]])
                       3979,
```

Now we transform the data into a matrix of dimension [N, D], where N is the number of users and D is the number of restaurants in the dataset. We store the data as a sparse matrix to avoid out-of-memory issues.

```
[]: n_users = np.max(ratings[:,0] + 1)
n_restaurants = np.max(ratings[:,1] + 1)
R = sp.coo_matrix((ratings[:,2], (ratings[:,0], ratings[:,1])), shape=(n_users,u_n_restaurants)).tocsr()
R
```

```
[]: <337867x5899 sparse matrix of type '<class 'numpy.int64'>'
with 929606 stored elements in Compressed Sparse Row format>
```

To avoid the cold start problem, in the preprocessing step, we recursively remove all users and restaurants with 10 or less ratings.

Then, we randomly select 200 data points for the validation and test sets, respectively.

After this, we subtract the mean rating for each users to account for this global effect.

**Note:** Some entries might become zero in this process – but these entries are different than the 'unknown' zeros in the matrix. We store the indices for which we the rating data available in a separate variable.

```
[ ]: def cold_start_preprocessing(matrix, min_entries):
         Recursively removes rows and columns from the input matrix which have less \sqcup
      ⇒ than min_entries nonzero entries.
         Parameters
         matrix
                   : sp.spmatrix, shape [N, D]
                       The input matrix to be preprocessed.
         min_entries : int
                       Minimum number of nonzero elements per row and column.
         Returns
         _____
                   : sp.spmatrix, shape [N', D']
         matrix
                       The pre-processed matrix, where N' \le N and D' \le D
         print("Shape before: {}".format(matrix.shape))
         shape = (-1, -1)
         while matrix.shape != shape:
             shape = matrix.shape
             nnz = matrix > 0
             row_ixs = nnz.sum(1).A1 > min_entries
             matrix = matrix[row_ixs]
             nnz = matrix > 0
             col_ixs = nnz.sum(0).A1 > min_entries
             matrix = matrix[:, col_ixs]
         print("Shape after: {}".format(matrix.shape))
         nnz = matrix>0
         assert (nnz.sum(0).A1 > min_entries).all()
         assert (nnz.sum(1).A1 > min_entries).all()
         return matrix
```

## 1.1.2 Task 1: Implement a function that subtracts the mean user rating from the sparse rating matrix

```
[]: def shift_user_mean(matrix):
    """

    Subtract the mean rating per user from the non-zero elements in the input
    →matrix.

Parameters
    -----
    matrix: sp.spmatrix, shape [N, D]
    Input sparse matrix.
```

```
Returns
------
matrix: sp.spmatrix, shape [N, D]
The modified input matrix.

user_means: np.array, shape [N, 1]
The mean rating per user that can be used to recover the
absolute ratings from the mean-shifted ones.

"""

## BEGIN SOLUTION

user_means = np.mean(matrix, axis=1)
matrix = matrix.astype(np.float64) - user_means
## END SOLUTION

assert np.all(np.isclose(matrix.mean(1), 0))
return matrix, user_means
```

### 1.1.3 Split the data into a train, validation and test set (nothing to do here)

```
[]: def split_data(matrix, n_validation, n_test):
        Extract validation and test entries from the input matrix.
        Parameters
        matrix
                       : sp.spmatrix, shape [N, D]
                          The input data matrix.
        n validation
                        : int
                          The number of validation entries to extract.
         n\_test
                         : int
                           The number of test entries to extract.
        Returns
                        : sp.spmatrix, shape [N, D]
        matrix\_split
                          A copy of the input matrix in which the validation and \Box
      ⇒test entries have been set to zero.
        val_idx
                         : tuple, shape [2, n_validation]
                           The indices of the validation entries.
                        : tuple, shape [2, n_test]
         test\_idx
                           The indices of the test entries.
                        : np.array, shape [n_validation, ]
        val_values
                           The values of the input matrix at the validation indices.
```

```
test values
                        : np.array, shape [n_test, ]
                           The values of the input matrix at the test indices.
         11 11 11
         matrix_cp = matrix.copy()
         non_zero_idx = np.argwhere(matrix_cp)
         ixs = np.random.permutation(non_zero_idx)
         val_idx = tuple(ixs[:n_validation].T)
         test_idx = tuple(ixs[n_validation:n_validation + n_test].T)
         val_values = matrix_cp[val_idx].A1
         test_values = matrix_cp[test_idx].A1
         matrix_cp[val_idx] = matrix_cp[test_idx] = 0
         matrix_cp.eliminate_zeros()
         return matrix_cp, val_idx, test_idx, val_values, test_values
[]: R = cold_start_preprocessing(R, 20)
    Shape before: (337867, 5899)
    Shape after: (3529, 2072)
[]: n_validation = 200
    n_test = 200
     # Split data
```

```
R_train, val_idx, test_idx, val_values, test_values = split_data(R,__
→n_validation, n_test)
```

```
[]: # Remove user means.
     nonzero_indices = np.argwhere(R_train)
     R_shifted, user_means = shift_user_mean(R_train)
     # Apply the same shift to the validation and test data.
     val_values_shifted = val_values - user_means[np.array(val_idx).T[:,0]].A1
     test_values shifted = test_values - user_means[np.array(test_idx).T[:,0]].A1
```

### 1.1.4 Compute the loss function (nothing to do here)

```
[]: def loss(values, ixs, Q, P, reg_lambda):
         11 11 11
         Compute the loss of the latent factor model (at indices ixs).
         Parameters
         values : np.array, shape [n_ixs,]
             The array with the ground-truth values.
```

```
ixs: tuple, shape [2, n_ixs]
       The indices at which we want to evaluate the loss (usually the nonzero_
→ indices of the unshifted data matrix).
   Q: np.array, shape [N, k]
       The matrix Q of a latent factor model.
  P: np.array, shape [k, D]
       The matrix P of a latent factor model.
   reg\_lambda : float
       The regularization strength
  Returns
   _____
   loss : float
          The loss of the latent factor model.
  mean_sse_loss = np.sum((values - (Q.dot(P))[ixs])**2)
  regularization_loss = reg_lambda * (np.sum(np.linalg.norm(P, axis=0)**2) +__
→np.sum(np.linalg.norm(Q, axis=1) ** 2))
  return mean_sse_loss + regularization_loss
```

### 1.2 Alternating optimization

In the first step, we will approach the problem via alternating optimization, as learned in the lecture. That is, during each iteration you first update Q while having P fixed and then vice versa.

#### 1.2.1 Task 2: Implement a function that initializes the latent factors Q and P

```
Q: np.array, shape [N, k]
    The initialized matrix Q of a latent factor model.
P: np.array, shape [k, D]
    The initialized matrix P of a latent factor model.
np.random.seed(0)
## BEGIN SOLUTION
N = matrix.shape[0]
D = matrix.shape[1]
if (init=="random"):
    Q = np.random.rand(N, k)
    P = np.random.rand(k, D)
elif (init=="svd"):
    u, s, vt = svds(matrix, k)
    Q = u @ s
    P = vt
## END SOLUTION
assert Q.shape == (matrix.shape[0], k)
assert P.shape == (k, matrix.shape[1])
return Q, P
```

# 1.2.2 Task 3: Implement the alternating optimization approach and stochastic gradient approach

R : sp.spmatrix, shape [N, D]

The input matrix to be factorized.

non\_zero\_idx : np.array, shape [nnz, 2]

The indices of the non-zero entries of the un-shifted  $\Box$ 

 $\hookrightarrow$  matrix to be factorized.

nnz refers to the number of non-zero entries. Note that  $\sqcup$ 

 $\hookrightarrow this$  may be different

from the number of non-zero entries in the input matrix.

 $\hookrightarrow M$ , e.g. in the case

that all ratings by a user have the same value.

k: int

The latent factor dimension.

val\_idx : tuple, shape [2, n\_validation]

Tuple of the validation set indices.

 $n\_validation$  refers to the size of the validation set.

val\_values : np.array, shape [n\_validation, ]

The values in the validation set.

 $reg\_lambda$  : float

The regularization strength.

max\_steps : int, optional, default: 100

Maximum number of training steps. Note that we will ⊔

 $\hookrightarrow stop\ early\ if\ we\ observe$ 

no improvement on the validation error for a specified.

 $\hookrightarrow$  number of steps

(see "patience" for details).

init : str in ['random', 'svd'], default 'random'

The initialization strategy for P and Q. See function  $\Box$ 

 $\rightarrow$  initialize\_Q\_P for details.

log\_every : int, optional, default: 1

Log the training status every X iterations.

patience : int, optional, default: 5

Stop training after we observe no improvement of the  $\sqcup$ 

 $\rightarrow validation$  loss for X evaluation

iterations (see eval\_every for details). After we stop ⊔

 $\hookrightarrow$  training, we restore the best

observed values for Q and P (based on the validation  $\Box$ 

 $\hookrightarrow$  loss) and return them.

```
: int, optional, default: 1
   eval_every
                        Evaluate the training and validation loss every X steps.
\hookrightarrow If we observe no improvement
                        of the validation error, we decrease our patience by 1, _
\rightarrow else we reset it to *patience*.
                     : str, optional, default: sgd
   optimizer
                        If `sgd` stochastic gradient descent shall be used. u
→Otherwise, use alternating least squares.
   Returns
   _____
   best Q
                     : np.array, shape [N, k]
                        Best value for Q (based on validation loss) observed
\hookrightarrow during training
   best P
                     : np.array, shape [k, D]
                       Best value for P (based on validation loss) observed
\hookrightarrow during training
   validation_losses : list of floats
                         Validation loss for every evaluation iteration, can be ⊔
\hookrightarrowused for plotting the validation
                        loss over time.
   train_losses
                     : list of floats
                        Training loss for every evaluation iteration, can be ...
→used for plotting the training
                        loss over time.
   converged_after : int
                         it - patience*eval_every, where it is the iteration in_
\hookrightarrow which patience hits 0,
                        or -1 if we hit max_steps before converging.
   11 11 11
   ## BEGIN SOLUTION
   Q, P = initialize_Q_P(R, k, init)
   nnzs = tuple(non_zero_idx.T)
   values = R[nnzs].A1
   model = Ridge(alpha=reg_lambda, fit_intercept=False)
   curr_patience = patience
```

```
train_losses = []
   validation_losses = []
   prev_loss = None
   bestq = Q
   bestp = P
   for step in range(max_steps):
       if (optimizer == "sgd"):
           for idx in non_zero_idx:
               u, i = idx[0], idx[1]
               error = R[u,i] - Q[u,:]@P[:,i]
               Q[u,:] += 2*lr*(error*P[:,i] - reg_lambda*Q[u,:])
               P[:,i] += 2*lr*(error*Q[u,:] - reg_lambda*P[:,i])
       else:
           P = model.fit(Q, R).coef_.T
           Q = model.fit(P.T, R.T).coef_
       train_loss = loss(values, nnzs, Q, P, reg_lambda)
       train_losses.append(train_loss)
       if step % eval_every == 0:
           val_loss = loss(val_values, val_idx, Q, P, reg_lambda)
           validation_losses.append(val_loss)
           if (prev_loss == None):
               prev_loss = val_loss
               bestq = Q
               bestp = P
           elif (val_loss >= prev_loss):
               curr_patience -= 1
           else:
               curr_patience = patience
               prev_loss = val_loss
               bestq = Q
               bestp = P
       if step % log_every == 0:
           print(f"Iteration {step}, training loss {train_loss}, validation_
→loss: {val_loss}")
```

```
if curr_patience == 0:
    return bestq, bestp, validation_losses, train_losses, step -□
    →patience*eval_every

## END SOLUTION

return bestq, bestp, validation_losses, train_losses, -1
```

### 1.2.3 Train the latent factor (nothing to do here)

[]: warnings.filterwarnings("ignore")

```
Q_sgd, P_sgd, val_loss_sgd, train_loss_sgd, converged_sgd =_
 →latent_factor_alternating_optimization(
    R_shifted, nonzero_indices, k=100, val_idx=val_idx,__
 →val_values=val_values_shifted,
    reg_lambda=1e-4, init='random', max_steps=100, patience=10,__
 →optimizer='sgd', lr=1e-2
Iteration 0, training loss 1913079.2151871456, validation loss:
1926.4579207727056
Iteration 1, training loss 614026.4001069352, validation loss:
1049.7005575426556
Iteration 2, training loss 146449.63059935515, validation loss:
527.2866655889877
Iteration 3, training loss 61226.65438399374, validation loss: 458.5507202563196
Iteration 4, training loss 36834.42086907077, validation loss:
462.27078078076204
Iteration 5, training loss 27495.456497314935, validation loss:
467.8327806711508
Iteration 6, training loss 21207.66994654611, validation loss: 470.1966562465473
Iteration 7, training loss 16862.178702675774, validation loss:
473.2846946000175
Iteration 8, training loss 13880.212494956544, validation loss:
477.34503044557704
Iteration 9, training loss 11709.370453727981, validation loss:
481.5108125202826
Iteration 10, training loss 10043.317429016663, validation loss:
485.3808170460918
Iteration 11, training loss 8724.422148330637, validation loss:
488.8881773071899
Iteration 12, training loss 7661.006172825707, validation loss:
492.0178068031721
Iteration 13, training loss 6789.678948837059, validation loss: 494.73962891658
```

```
[]: warnings.filterwarnings("ignore")
     Q_als, P_als, val_loss_als, train_loss_als, converged_als =_
     →latent_factor_alternating_optimization(
         R_shifted, nonzero_indices, k=100, val_idx=val_idx,__
     →val_values=val_values_shifted,
         reg_lambda=1e-4, init='random', max_steps=100, patience=10, optimizer='als'
    Iteration 0, training loss 1560767.4818099355, validation loss:
    2604.1472874894207
    Iteration 1, training loss 1306142.5095206571, validation loss:
    2482.395308523441
    Iteration 2, training loss 1265965.9163291007, validation loss:
    2463.1023686092108
    Iteration 3, training loss 1254591.5464836305, validation loss:
    2459.3640057803314
    Iteration 4, training loss 1250151.0745797595, validation loss:
    2460.109722872749
    Iteration 5, training loss 1248086.083126195, validation loss: 2462.135578901375
    Iteration 6, training loss 1247022.1927940175, validation loss:
    2464.9837162351287
    Iteration 7, training loss 1246430.0720933112, validation loss:
    2468.5432983716278
    Iteration 8, training loss 1246077.5687334493, validation loss:
    2472.5469834416435
    Iteration 9, training loss 1245855.046172327, validation loss:
    2476.6872921667295
    Iteration 10, training loss 1245707.243764587, validation loss:
    2480.727499803756
    Iteration 11, training loss 1245604.4233051357, validation loss:
    2484.5220201200186
    Iteration 12, training loss 1245529.5686815053, validation loss:
    2487.997125606604
    Iteration 13, training loss 1245472.4297945707, validation loss:
    2491.1274942152954
```

## 1.2.4 Plot the validation and training losses over for each iteration (nothing to do here)

```
fig, ax = plt.subplots(1, 2, figsize=[10, 5])
fig.suptitle("Alternating optimization, k=100")

ax[0].plot(train_loss_sgd[1::], label='sgd')
ax[0].plot(train_loss_als[1::], label='als')
ax[0].set_title('Training loss')
ax[0].set_xlabel("Training iteration")
```

```
ax[0].set_ylabel("Loss")
ax[0].legend()

ax[1].plot(val_loss_sgd[1::], label='sgd')
ax[1].plot(val_loss_als[1::], label='als')
ax[1].set_title('Validation loss')
ax[1].set_xlabel("Training iteration")
ax[1].set_ylabel("Loss")
ax[1].legend()

plt.show()
```



### 2 Autoencoder and t-SNE

Hereinafter, we will implement an autoencoder and analyze its latent space via interpolations and t-SNE. For this, we will use the famous Fashion-MNIST dataset.

```
[]: from typing import List

from matplotlib.offsetbox import AnnotationBbox, OffsetImage
from matplotlib import pyplot as plt
from sklearn.decomposition import PCA
from sklearn.manifold import TSNE
import torchvision
```

```
from torchvision.datasets import FashionMNIST
import torch
from torch import nn
import torch.nn.functional as F
from torch.optim.lr_scheduler import ExponentialLR
from copy import deepcopy
```

Hint: If you run into memory issues simply reduce the batch\_size

```
[]: train_dataset = FashionMNIST(root='data', download=True, train=True, 
→ transform=torchvision.transforms.ToTensor())

test_dataset = FashionMNIST(root='data', download=True, train=False, 
→ transform=torchvision.transforms.ToTensor())

train_loader = torch.utils.data.DataLoader(train_dataset, batch_size=1024, 
→ shuffle=True,

num_workers=2, pin_memory=True)

test_loader = torch.utils.data.DataLoader(test_dataset, batch_size=1024, 
→ shuffle=False,

num_workers=2, pin_memory=True)
```

#### 2.0.1 Task 4: Define decoder network

Feel free to choose any architecture you like. Our model was this:

```
Autoencoder(
  (encode): Sequential(
    (0): Conv2d(1, 4, kernel_size=(3, 3), stride=(1, 1))
    (1): LeakyReLU(negative_slope=0.01)
    (2): Conv2d(4, 16, kernel_size=(3, 3), stride=(1, 1))
    (3): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mode=False)
    (4): LeakyReLU(negative_slope=0.01)
    (5): BatchNorm2d(16, eps=1e-05, momentum=0.1, affine=True, track_running_stats=True)
    (6): LeakyReLU(negative_slope=0.01)
    (7): Conv2d(16, 32, kernel_size=(3, 3), stride=(1, 1))
    (8): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mode=False)
    (9): LeakyReLU(negative_slope=0.01)
    (10): Conv2d(32, 32, kernel_size=(3, 3), stride=(1, 1))
    (11): LeakyReLU(negative_slope=0.01)
  )
  (decode): Sequential(
    (0): ConvTranspose2d(32, 32, kernel_size=(3, 3), stride=(1, 1))
    (1): LeakyReLU(negative_slope=0.01)
    (2): ConvTranspose2d(32, 16, kernel_size=(3, 3), stride=(2, 2), output_padding=(1, 1))
    (3): LeakyReLU(negative_slope=0.01)
    (4): BatchNorm2d(16, eps=1e-05, momentum=0.1, affine=True, track_running_stats=True)
    (5): ConvTranspose2d(16, 16, kernel_size=(3, 3), stride=(2, 2), output_padding=(1, 1))
    (6): LeakyReLU(negative_slope=0.01)
    (7): ConvTranspose2d(16, 16, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
```

```
(8): ConvTranspose2d(16, 4, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
        (9): ConvTranspose2d(4, 1, kernel_size=(3, 3), stride=(1, 1))
        (10): Sigmoid()
      )
    )
[]: class Autoencoder(nn.Module):
        ## BEGIN SOLUTION
        def init (self):
             super(Autoencoder, self).__init__()
             self.encoder = nn.Sequential(
                nn.Conv2d(1, 4, kernel\_size=(3, 3), stride=(1, 1)),
                 nn.LeakyReLU(negative_slope=0.01),
                 nn.Conv2d(4, 16, kernel\_size=(3, 3), stride=(1, 1)),
                 nn.MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1,__

→ceil_mode=False),
                nn.LeakyReLU(negative_slope=0.01),
                 nn.BatchNorm2d(16, eps=1e-05, momentum=0.1, affine=True,
      →track_running_stats=True),
                 nn.LeakyReLU(negative_slope=0.01),
                 nn.Conv2d(16, 32, kernel_size=(3, 3), stride=(1, 1)),
                nn.MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1,_
     nn.LeakyReLU(negative_slope=0.01),
                nn.Conv2d(32, 32, kernel_size=(3, 3), stride=(1, 1)),
                 nn.LeakyReLU(negative_slope=0.01)
             )
             self.decoder = nn.Sequential(
                 nn.ConvTranspose2d(32, 32, kernel_size=(3, 3), stride=(1, 1)),
                 nn.LeakyReLU(negative_slope=0.01),
                nn.ConvTranspose2d(32, 16, kernel_size=(
                     3, 3), stride=(2, 2), output_padding=(1, 1)),
                 nn.LeakyReLU(negative_slope=0.01),
                nn.BatchNorm2d(16, eps=1e-05, momentum=0.1,
                                affine=True, track_running_stats=True),
                nn.ConvTranspose2d(16, 16, kernel_size=(
                     3, 3), stride=(2, 2), output_padding=(1, 1)),
                nn.LeakyReLU(negative_slope=0.01),
                nn.ConvTranspose2d(16, 16, kernel_size=(
                     3, 3), stride=(1, 1), padding=(1, 1)),
                nn.ConvTranspose2d(16, 4, kernel_size=(
                     3, 3), stride=(1, 1), padding=(1, 1)),
                nn.ConvTranspose2d(4, 1, kernel_size=(3, 3), stride=(1, 1)),
                 nn.Sigmoid()
             )
```

```
self.decoder.apply(self.initialize_weight)
        self.encoder.apply(self.initialize_weight)
    def initialize_weight(self, module):
        if isinstance(module, (nn.ConvTranspose2d, nn.Conv2d)):
             nn.init.kaiming_normal_(module.weight, nonlinearity='relu')
        elif isinstance(module, nn.BatchNorm2d):
             nn.init.constant_(module.weight, 1)
             nn.init.constant_(module.bias, 0)
    def encode(self, x):
        return self.encoder.forward(x)
    def decode(self, x):
        return self.decoder.forward(x)
    ## END SOLUTION
    def forward(self, x):
        z = self.encode(x)
        x_{approx} = self.decode(z)
        assert x.shape == x_approx.shape
        return x_approx
print(Autoencoder())
Autoencoder(
  (encoder): Sequential(
    (0): Conv2d(1, 4, kernel_size=(3, 3), stride=(1, 1))
    (1): LeakyReLU(negative_slope=0.01)
    (2): Conv2d(4, 16, kernel_size=(3, 3), stride=(1, 1))
    (3): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1,
ceil_mode=False)
    (4): LeakyReLU(negative_slope=0.01)
    (5): BatchNorm2d(16, eps=1e-05, momentum=0.1, affine=True,
track_running_stats=True)
    (6): LeakyReLU(negative_slope=0.01)
    (7): Conv2d(16, 32, kernel_size=(3, 3), stride=(1, 1))
    (8): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1,
ceil_mode=False)
    (9): LeakyReLU(negative_slope=0.01)
    (10): Conv2d(32, 32, kernel_size=(3, 3), stride=(1, 1))
    (11): LeakyReLU(negative_slope=0.01)
  (decoder): Sequential(
    (0): ConvTranspose2d(32, 32, kernel_size=(3, 3), stride=(1, 1))
    (1): LeakyReLU(negative_slope=0.01)
```

```
(2): ConvTranspose2d(32, 16, kernel_size=(3, 3), stride=(2, 2),
output_padding=(1, 1))
    (3): LeakyReLU(negative_slope=0.01)
    (4): BatchNorm2d(16, eps=1e-05, momentum=0.1, affine=True,
track running stats=True)
    (5): ConvTranspose2d(16, 16, kernel_size=(3, 3), stride=(2, 2),
output padding=(1, 1))
    (6): LeakyReLU(negative_slope=0.01)
    (7): ConvTranspose2d(16, 16, kernel_size=(3, 3), stride=(1, 1), padding=(1,
1))
    (8): ConvTranspose2d(16, 4, kernel_size=(3, 3), stride=(1, 1), padding=(1,
1))
    (9): ConvTranspose2d(4, 1, kernel_size=(3, 3), stride=(1, 1))
    (10): Sigmoid()
 )
)
```

We see that our model transform the image from  $28 \cdot 28 = 784$  dimensional space down into a  $32 \cdot 3 \cdot 3 = 288$  dimensional space. However, note that the latent space also must contain some spatial information that the decoder needs for decoding.

```
[]: x = test_dataset[0][0][None, ...]
z = Autoencoder().encode(x)

print(x.shape)
print(z.shape)
print(Autoencoder().decode(z).shape)
```

```
torch.Size([1, 1, 28, 28])
torch.Size([1, 32, 3, 3])
torch.Size([1, 1, 28, 28])
```

#### 2.1 Task 5: Train the autoencoder

Of course, we must train the autoencoder if we want to analyze it later on.

```
[]: device = 0 if torch.cuda.is_available() else 'cpu'
model = Autoencoder().to(device)

optimizer = torch.optim.Adam(model.parameters(), lr=1e-3, weight_decay=1e-4)
scheduler = ExponentialLR(optimizer, gamma=0.999)

log_every_batch = 20

# defining patience to speed up training
patience = 10
curr_patience = 10
best_loss = None
best_weights = None
```

```
for epoch in range(50):
   model.train()
   train_loss_trace = []
   for batch, (x, _) in enumerate(train_loader):
        ## BEGIN SOLUTION
       x = x.to(device)
       x = model(x)
       loss = F.mse_loss(x_approx,x)
       loss.backward()
       optimizer.step()
        ## END SOLUTION
        train_loss_trace.append(loss.detach().item())
        if batch % log_every_batch == 0:
            print(f'Training: Epoch {epoch} batch {batch} - loss {loss}')
   model.eval()
   test_loss_trace = []
   for batch, (x, _) in enumerate(test_loader):
       x = x.to(device)
       x = model(x)
       loss = F.mse_loss(x_approx, x)
       test_loss_trace.append(loss.detach().item())
        if (best_loss == None or loss <= best_loss):</pre>
            best_weights = deepcopy(model.state_dict())
            best_loss = loss
            curr_patience = patience
        else:
            curr_patience -= 1
        if batch % log_every_batch == 0:
            print(f'Test: Epoch {epoch} batch {batch} loss {loss}')
   print(f'Epoch {epoch} finished - average train loss {np.
→mean(train_loss_trace)}, '
          f'average test loss {np.mean(test_loss_trace)}')
    if (curr_patience == 0):
      break
model.load_state_dict(best_weights)
```

Training: Epoch 0 batch 0 - loss 0.22105960547924042

Training: Epoch 0 batch 20 - loss 0.2440939098596573

Training: Epoch 0 batch 40 - loss 0.187652587890625

Test: Epoch 0 batch 0 loss 0.15293912589550018

Epoch 0 finished - average train loss 0.18025842005923642, average test loss 0.15142675042152404

Training: Epoch 1 batch 0 - loss 0.15250302851200104

Training: Epoch 1 batch 20 - loss 0.22972092032432556

Training: Epoch 1 batch 40 - loss 0.10326273739337921

Test: Epoch 1 batch 0 loss 0.1264612376689911

Epoch 1 finished - average train loss 0.14353578146231377, average test loss 0.12592412382364274

Training: Epoch 2 batch 0 - loss 0.14086087048053741

Training: Epoch 2 batch 20 - loss 0.12498904019594193

Training: Epoch 2 batch 40 - loss 0.12210098654031754

Test: Epoch 2 batch 0 loss 0.15943506360054016

Epoch 2 finished - average train loss 0.12632550867432255, average test loss 0.15964883267879487

Training: Epoch 3 batch 0 - loss 0.12337891012430191

Training: Epoch 3 batch 20 - loss 0.12574464082717896

Training: Epoch 3 batch 40 - loss 0.1139763593673706

Test: Epoch 3 batch 0 loss 0.10677484422922134

Epoch 3 finished - average train loss 0.11739583629167687, average test loss 0.10619214922189713

Training: Epoch 4 batch 0 - loss 0.11164586246013641

Training: Epoch 4 batch 20 - loss 0.13948604464530945

Training: Epoch 4 batch 40 - loss 0.141514852643013

Test: Epoch 4 batch 0 loss 0.16125158965587616

Epoch 4 finished - average train loss 0.14126976831989774, average test loss 0.15959856361150743

Training: Epoch 5 batch 0 - loss 0.18048477172851562

Training: Epoch 5 batch 20 - loss 0.16199259459972382

Training: Epoch 5 batch 40 - loss 0.15570378303527832

Test: Epoch 5 batch 0 loss 0.14271414279937744

Epoch 5 finished - average train loss 0.16010575981463415, average test loss 0.14148640483617783

Training: Epoch 6 batch 0 - loss 0.1500980257987976

Training: Epoch 6 batch 20 - loss 0.13786426186561584

Training: Epoch 6 batch 40 - loss 0.13549210131168365

Test: Epoch 6 batch 0 loss 0.1426888257265091

Epoch 6 finished - average train loss 0.1390710455381264, average test loss 0.1416544049978256

Training: Epoch 7 batch 0 - loss 0.13467301428318024

Training: Epoch 7 batch 20 - loss 0.13653507828712463

Training: Epoch 7 batch 40 - loss 0.13422717154026031

Test: Epoch 7 batch 0 loss 0.1363920420408249

Epoch 7 finished - average train loss 0.1344745836015475, average test loss 0.1353606879711151

Training: Epoch 8 batch 0 - loss 0.12869319319725037

Training: Epoch 8 batch 20 - loss 0.12171107530593872

Training: Epoch 8 batch 40 - loss 0.12050461024045944

Test: Epoch 8 batch 0 loss 0.1164807602763176

Epoch 8 finished - average train loss 0.12128467150663926, average test loss 0.11584777384996414

Training: Epoch 9 batch 0 - loss 0.11493651568889618

Training: Epoch 9 batch 20 - loss 0.11140702664852142

Training: Epoch 9 batch 40 - loss 0.11507546156644821

Test: Epoch 9 batch 0 loss 0.11392009258270264

Epoch 9 finished - average train loss 0.11368163788722734, average test loss 0.11338231489062309

Training: Epoch 10 batch 0 - loss 0.11618899554014206

Training: Epoch 10 batch 20 - loss 0.11657048016786575

Training: Epoch 10 batch 40 - loss 0.11569216102361679

Test: Epoch 10 batch 0 loss 0.11510530859231949

Epoch 10 finished - average train loss 0.11605353186191139, average test loss 0.11463154032826424

Training: Epoch 11 batch 0 - loss 0.11789952218532562

Training: Epoch 11 batch 20 - loss 0.11462733894586563

Training: Epoch 11 batch 40 - loss 0.11028798669576645

Test: Epoch 11 batch 0 loss 0.11055335402488708

Epoch 11 finished - average train loss 0.1132542059078055, average test loss 0.1106224425137043

Training: Epoch 12 batch 0 - loss 0.109492726624012

Training: Epoch 12 batch 20 - loss 0.10828885436058044

Training: Epoch 12 batch 40 - loss 0.10915444046258926

Test: Epoch 12 batch 0 loss 0.1097826436161995

Epoch 12 finished - average train loss 0.10942580765586789, average test loss 0.1098979465663433

Training: Epoch 13 batch 0 - loss 0.10987796634435654

Training: Epoch 13 batch 20 - loss 0.10837055742740631

Training: Epoch 13 batch 40 - loss 0.1076211929321289

Test: Epoch 13 batch 0 loss 0.10726995021104813

Epoch 13 finished - average train loss 0.10720554335137546, average test loss 0.10741868019104003

Training: Epoch 14 batch 0 - loss 0.1049274131655693

Training: Epoch 14 batch 20 - loss 0.1054273247718811

Training: Epoch 14 batch 40 - loss 0.10391013324260712

Test: Epoch 14 batch 0 loss 0.10466161370277405

Epoch 14 finished - average train loss 0.10471335141840628, average test loss 0.10472820028662681

Training: Epoch 15 batch 0 - loss 0.10422267019748688

Training: Epoch 15 batch 20 - loss 0.10467132925987244

Training: Epoch 15 batch 40 - loss 0.10411117225885391

Test: Epoch 15 batch 0 loss 0.1045895591378212

Epoch 15 finished - average train loss 0.10441087287361339, average test loss 0.10446633547544479

Training: Epoch 16 batch 0 - loss 0.10514512658119202

Training: Epoch 16 batch 20 - loss 0.10193284600973129

Training: Epoch 16 batch 40 - loss 0.10394955426454544

Test: Epoch 16 batch 0 loss 0.10486168414354324

Epoch 16 finished - average train loss 0.10381966639878386, average test loss 0.10514436438679695

Training: Epoch 17 batch 0 - loss 0.10477977991104126

Training: Epoch 17 batch 20 - loss 0.10611610114574432

Training: Epoch 17 batch 40 - loss 0.10511588305234909

Test: Epoch 17 batch 0 loss 0.1050676703453064

Epoch 17 finished - average train loss 0.1046742166755563, average test loss 0.1057390384376049

Training: Epoch 18 batch 0 - loss 0.10390881448984146

Training: Epoch 18 batch 20 - loss 0.10164777934551239

Training: Epoch 18 batch 40 - loss 0.10072976350784302

Test: Epoch 18 batch 0 loss 0.10410483181476593

Epoch 18 finished - average train loss 0.10276390081745083, average test loss 0.1038704313337803

Training: Epoch 19 batch 0 - loss 0.10397558659315109

Training: Epoch 19 batch 20 - loss 0.10580790042877197

Training: Epoch 19 batch 40 - loss 0.10557638108730316

Test: Epoch 19 batch 0 loss 0.10402453690767288

Epoch 19 finished - average train loss 0.10531063302088592, average test loss 0.1035535104572773

Training: Epoch 20 batch 0 - loss 0.10446595400571823

Training: Epoch 20 batch 20 - loss 0.10018998384475708

Training: Epoch 20 batch 40 - loss 0.10007140040397644

Test: Epoch 20 batch 0 loss 0.09790080785751343

Epoch 20 finished - average train loss 0.10002775401887247, average test loss 0.09840730354189872

Training: Epoch 21 batch 0 - loss 0.09668239206075668

Training: Epoch 21 batch 20 - loss 0.10204508155584335

Training: Epoch 21 batch 40 - loss 0.09947426617145538

Test: Epoch 21 batch 0 loss 0.09800439327955246

Epoch 21 finished - average train loss 0.09889460948564238, average test loss 0.09834456443786621

Training: Epoch 22 batch 0 - loss 0.09791015088558197

Training: Epoch 22 batch 20 - loss 0.09620548784732819

Training: Epoch 22 batch 40 - loss 0.09634800255298615

Test: Epoch 22 batch 0 loss 0.09812179207801819

Epoch 22 finished - average train loss 0.09687149208986152, average test loss 0.09782659560441971

Training: Epoch 23 batch 0 - loss 0.09793732315301895

Training: Epoch 23 batch 20 - loss 0.09892825037240982

Training: Epoch 23 batch 40 - loss 0.09935104846954346

Test: Epoch 23 batch 0 loss 0.09817545861005783

Epoch 23 finished - average train loss 0.09853253463062189, average test loss 0.09781977087259293

Training: Epoch 24 batch 0 - loss 0.09767583757638931

Training: Epoch 24 batch 20 - loss 0.09640657901763916

Training: Epoch 24 batch 40 - loss 0.09565369784832001

Test: Epoch 24 batch 0 loss 0.10063514113426208

Epoch 24 finished - average train loss 0.0973279729990636, average test loss 0.10029345899820327

Training: Epoch 25 batch 0 - loss 0.09735416620969772

Training: Epoch 25 batch 20 - loss 0.12745942175388336

Training: Epoch 25 batch 40 - loss 0.12764322757720947

Test: Epoch 25 batch 0 loss 0.09820715337991714

Epoch 25 finished - average train loss 0.12034376584372278, average test loss 0.09801411405205726

Training: Epoch 26 batch 0 - loss 0.09704458713531494

Training: Epoch 26 batch 20 - loss 0.09619958698749542

Training: Epoch 26 batch 40 - loss 0.09628253430128098

Test: Epoch 26 batch 0 loss 0.09825792163610458

Epoch 26 finished - average train loss 0.09629689371686871, average test loss 0.09797044917941093

Training: Epoch 27 batch 0 - loss 0.09648235142230988

Training: Epoch 27 batch 20 - loss 0.09925365447998047

Training: Epoch 27 batch 40 - loss 0.10211771726608276

Test: Epoch 27 batch 0 loss 0.10179444402456284

Epoch 27 finished - average train loss 0.10075451117956032, average test loss 0.1012374371290207

Training: Epoch 28 batch 0 - loss 0.10162962973117828

Training: Epoch 28 batch 20 - loss 0.10248631238937378

Training: Epoch 28 batch 40 - loss 0.10211378335952759

Test: Epoch 28 batch 0 loss 0.09956511855125427

Epoch 28 finished - average train loss 0.10062064268326355, average test loss 0.09935281574726104

Training: Epoch 29 batch 0 - loss 0.09721613675355911

Training: Epoch 29 batch 20 - loss 0.09993073344230652

Training: Epoch 29 batch 40 - loss 0.09966491907835007

Test: Epoch 29 batch 0 loss 0.09885279834270477

Epoch 29 finished - average train loss 0.09903087820542061, average test loss 0.09868963062763214

Training: Epoch 30 batch 0 - loss 0.09846356511116028

Training: Epoch 30 batch 20 - loss 0.09863436967134476

Training: Epoch 30 batch 40 - loss 0.09660438448190689

Test: Epoch 30 batch 0 loss 0.09694404900074005

Epoch 30 finished - average train loss 0.09756204927876844, average test loss 0.09684852734208108

Training: Epoch 31 batch 0 - loss 0.09696362167596817

Training: Epoch 31 batch 20 - loss 0.09686282277107239

Training: Epoch 31 batch 40 - loss 0.09796374291181564

Test: Epoch 31 batch 0 loss 0.09584121406078339

Epoch 31 finished - average train loss 0.09628970011816186, average test loss 0.09566466212272644

Training: Epoch 32 batch 0 - loss 0.09545659273862839

Training: Epoch 32 batch 20 - loss 0.09567335993051529

Training: Epoch 32 batch 40 - loss 0.0935555174946785

Test: Epoch 32 batch 0 loss 0.09500280767679214

Epoch 32 finished - average train loss 0.0953685723371425, average test loss 0.09488878920674323

Training: Epoch 33 batch 0 - loss 0.09536005556583405

Training: Epoch 33 batch 20 - loss 0.09432274848222733

Training: Epoch 33 batch 40 - loss 0.09282709658145905

Test: Epoch 33 batch 0 loss 0.09461606293916702

Epoch 33 finished - average train loss 0.0944494434246774, average test loss 0.09468849077820778

Training: Epoch 34 batch 0 - loss 0.0934622511267662

Training: Epoch 34 batch 20 - loss 0.09465780854225159

Training: Epoch 34 batch 40 - loss 0.09434635937213898

Test: Epoch 34 batch 0 loss 0.0954214334487915

Epoch 34 finished - average train loss 0.09458328998189862, average test loss 0.09560337886214257

Training: Epoch 35 batch 0 - loss 0.09390491992235184

Training: Epoch 35 batch 20 - loss 0.09593982249498367

Training: Epoch 35 batch 40 - loss 0.09475421160459518

Test: Epoch 35 batch 0 loss 0.09580021351575851

Epoch 35 finished - average train loss 0.09527153231329837, average test loss 0.09600725248456002

Training: Epoch 36 batch 0 - loss 0.0963989868760109

Training: Epoch 36 batch 20 - loss 0.09440147876739502

Training: Epoch 36 batch 40 - loss 0.09522144496440887

Test: Epoch 36 batch 0 loss 0.09579554200172424

Epoch 36 finished - average train loss 0.09533228838847856, average test loss 0.09606835320591926

Training: Epoch 37 batch 0 - loss 0.09472830593585968

Training: Epoch 37 batch 20 - loss 0.09508220851421356

Training: Epoch 37 batch 40 - loss 0.09575612843036652

Test: Epoch 37 batch 0 loss 0.09585006535053253

Epoch 37 finished - average train loss 0.0954828105740628, average test loss 0.09619750902056694

Training: Epoch 38 batch 0 - loss 0.09589995443820953

Training: Epoch 38 batch 20 - loss 0.09606580436229706

Training: Epoch 38 batch 40 - loss 0.09313579648733139

Test: Epoch 38 batch 0 loss 0.09501387178897858

Epoch 38 finished - average train loss 0.09510596298565299, average test loss 0.09535959139466285

Training: Epoch 39 batch 0 - loss 0.09505201876163483

Training: Epoch 39 batch 20 - loss 0.09335309267044067

Training: Epoch 39 batch 40 - loss 0.09613507241010666

Test: Epoch 39 batch 0 loss 0.09395071119070053

Epoch 39 finished - average train loss 0.09412857599682727, average test loss 0.09425866529345513

Training: Epoch 40 batch 0 - loss 0.09449775516986847

Training: Epoch 40 batch 20 - loss 0.09250371158123016

Training: Epoch 40 batch 40 - loss 0.09448319673538208

Test: Epoch 40 batch 0 loss 0.09388478100299835

Epoch 40 finished - average train loss 0.09371074604786049, average test loss 0.09418363198637962

Training: Epoch 41 batch 0 - loss 0.09663590788841248

Training: Epoch 41 batch 20 - loss 0.09768622368574142

Training: Epoch 41 batch 40 - loss 0.09485302120447159

Test: Epoch 41 batch 0 loss 0.09551290422677994

Epoch 41 finished - average train loss 0.09480705756252095, average test loss 0.09570447206497193

Training: Epoch 42 batch 0 - loss 0.09647510200738907

Training: Epoch 42 batch 20 - loss 0.09504137188196182

Training: Epoch 42 batch 40 - loss 0.09597695618867874

Test: Epoch 42 batch 0 loss 0.09808594733476639

Epoch 42 finished - average train loss 0.09687906200602903, average test loss 0.09819813743233681

Training: Epoch 43 batch 0 - loss 0.10084281861782074

Training: Epoch 43 batch 20 - loss 0.10199412703514099

Training: Epoch 43 batch 40 - loss 0.09803386777639389

Test: Epoch 43 batch 0 loss 0.098978191614151

Epoch 43 finished - average train loss 0.09898704290390015, average test loss 0.09900245815515518

Training: Epoch 44 batch 0 - loss 0.0995921716094017

Training: Epoch 44 batch 20 - loss 0.0993729829788208

Training: Epoch 44 batch 40 - loss 0.1004076674580574

Test: Epoch 44 batch 0 loss 0.09869487583637238

Epoch 44 finished - average train loss 0.09924743930667133, average test loss 0.09873597100377082

Training: Epoch 45 batch 0 - loss 0.09930220246315002

Training: Epoch 45 batch 20 - loss 0.09656540304422379

Training: Epoch 45 batch 40 - loss 0.09864326566457748

Test: Epoch 45 batch 0 loss 0.09620997309684753

Epoch 45 finished - average train loss 0.09714691707138289, average test loss 0.09639898985624314

Training: Epoch 46 batch 0 - loss 0.09557969868183136

Training: Epoch 46 batch 20 - loss 0.09750839322805405

Training: Epoch 46 batch 40 - loss 0.09351161122322083

Test: Epoch 46 batch 0 loss 0.09636478126049042

Epoch 46 finished - average train loss 0.09567569423530062, average test loss 0.09655911549925804

Training: Epoch 47 batch 0 - loss 0.09510691463947296

Training: Epoch 47 batch 20 - loss 0.09780419617891312

Training: Epoch 47 batch 40 - loss 0.10113314539194107

Test: Epoch 47 batch 0 loss 0.11261187493801117

Epoch 47 finished - average train loss 0.0995436770431066, average test loss 0.11313542276620865

```
Training: Epoch 48 batch 0 - loss 0.1116500124335289

Training: Epoch 48 batch 20 - loss 0.13702082633972168

Training: Epoch 48 batch 40 - loss 0.15179632604122162

Test: Epoch 48 batch 0 loss 0.15388794243335724

Epoch 48 finished - average train loss 0.13885430511781724, average test loss 0.15440610498189927

Training: Epoch 49 batch 0 - loss 0.15091174840927124

Training: Epoch 49 batch 20 - loss 0.15236112475395203

Training: Epoch 49 batch 40 - loss 0.11062931269407272

Test: Epoch 49 batch 0 loss 0.10247856378555298

Epoch 49 finished - average train loss 0.13321462172572895, average test loss 0.10279674902558326
```

### []: <All keys matched successfully>

```
[]: model.eval()
with torch.no_grad():
    latent = []
    for batch, (x, _) in enumerate(test_loader):
        latent.append(model.encode(x.to(device)).cpu())
    latent = torch.cat(latent)
```

### 2.2 PCA and t-SNE (nothing to do here)

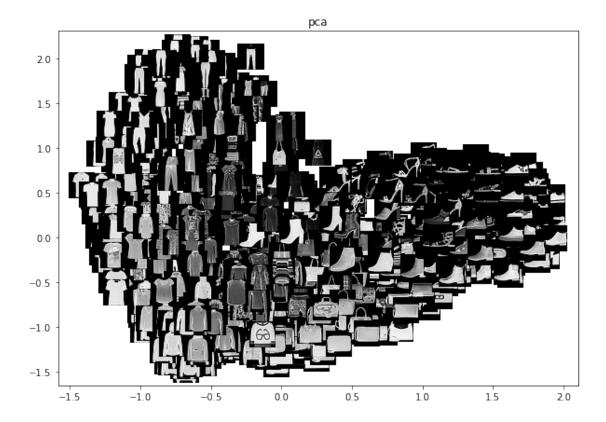
Next, we are going to look at some random images and their embeddings. Since 7x7 is still too large to visialize further dimensionality reduction techniques are required.

It is not uncommand that a neural network designer wants to understand whats going on in the latent space and therefore uses techniques such as t-SNE.

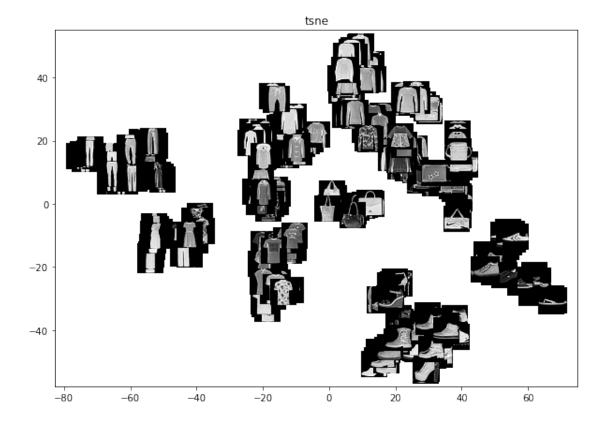
```
[]: def plot_latent(test_dataset: torch.utils.data.Dataset, z_test: torch.Tensor,_
      ⇔count: int,
                      technique: str, perplexity: float = 30):
         Fit t-SNE or PCA and plots the latent space. Moreover, we then display the \sqcup
      \hookrightarrow correspondig image.
         Parameters
         test\_dataset : torch.utils.data.DataSet
                         Dataset containing raw images to display.
                        : torch.Tensor
         z\_\mathit{test}
                          The transformed images.
         count
                        : int
                          Number of random images to sample
         technique
                        : str
                          Either "pca" or "tsne". Otherwise, a ValueError is thrown.
         perplexity : float, optional, default: 30.0
```

```
Perplexity is t-SNE is used.
  indices = np.random.choice(len(z_test), count, replace=False)
  inputs = z_test[indices]
  fig, ax = plt.subplots(figsize=(10, 7))
  ax.set_title(technique)
  if technique == 'pca':
       coords = PCA(n_components=2).fit_transform(inputs.reshape(count, -1))
  elif technique == 'tsne':
       coords = TSNE(n_components=2, perplexity=perplexity).
→fit_transform(inputs.reshape(count, -1))
  else:
      raise ValueError()
  for idx, (x, y) in zip(indices, coords):
       im = OffsetImage(test_dataset[idx][0].squeeze().numpy(), zoom=1,__
ab = AnnotationBbox(im, (x, y), xycoords='data', frameon=False)
       ax.add_artist(ab)
  ax.update_datalim(coords)
  ax.autoscale()
  plt.show()
```

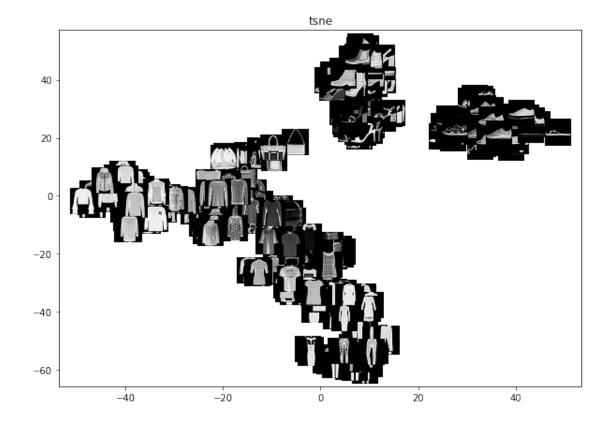
```
[]: plot_latent(test_dataset, latent, 1000, 'pca')
```



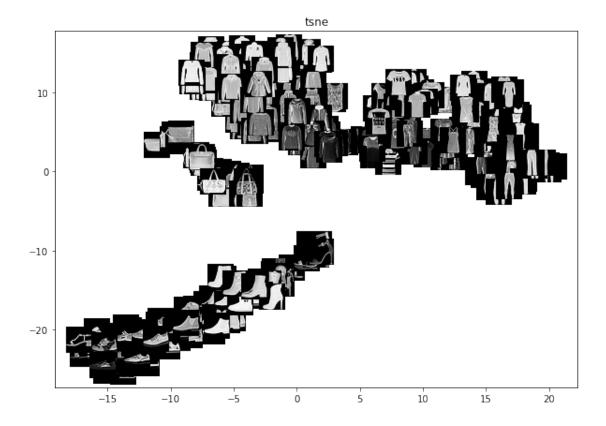
[]: plot\_latent(test\_dataset, latent, 300, 'tsne', perplexity=5)



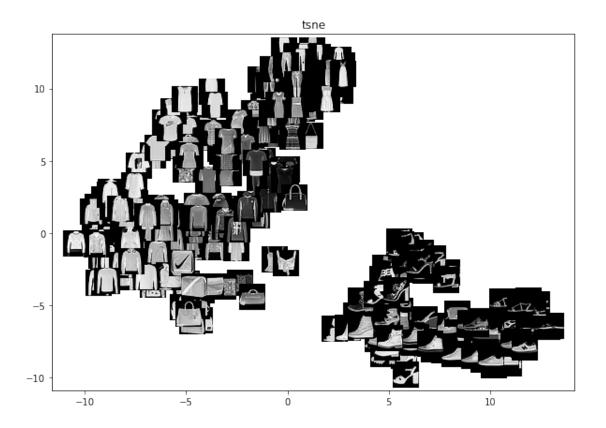
[]: plot\_latent(test\_dataset, latent, 300, 'tsne', perplexity=10)



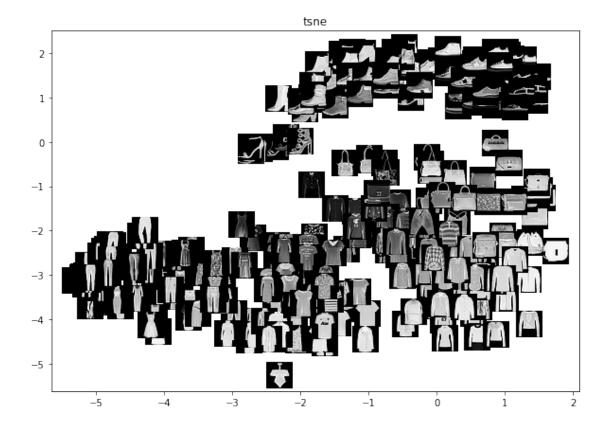
[]: plot\_latent(test\_dataset, latent, 300, 'tsne', perplexity=30)



[]: plot\_latent(test\_dataset, latent, 300, 'tsne', perplexity=50)



[]: plot\_latent(test\_dataset, latent, 300, 'tsne', perplexity=150)



### 2.3 Task 6: Linear Interpolation on the latent space

If the latent space has learned something meanigfull, we can leverage this for further analysis/downstream tasks. Anyways, we were wondering all along how the interpolation between a shoe and a pullover might look like.

For this we encode two images  $z_i = f_{enc}(x_i)$  and  $z_j = f_{enc}(x_j)$ . Then we linearly interpolate k equidistant locations on the line between  $z_i$  and  $z_j$ . Those locations are then be decoded by the decoder network  $f_{dec}(\ldots)$ .

```
[]: def interpolate_between(model: Autoencoder, test_dataset: torch.utils.data.

→Dataset, idx_i: int, idx_j: int, n = 12):

"""

Plot original images and the reconstruction of the linear interpolation in → the respective latent space embedding.

Parameters

-----

model : Autoencoder

The (trained) autoencoder.

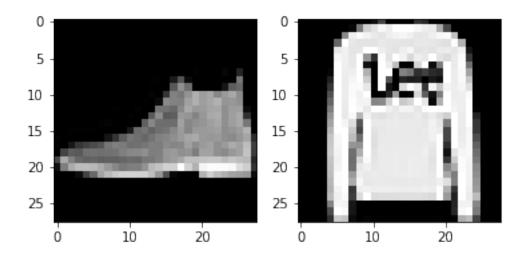
test_dataset : torch.utils.data.Dataset

Test images.
```

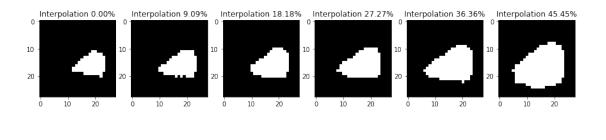
```
idx_i
                 : int
                   Id for first image.
   idx_j
                 : int
                   Id for second image.
                 : n, optional, default: 1
                   Number of intermediate interoplations (including original.
\rightarrow reconstructions).
  fig, ax = plt.subplots(1, 2, figsize=[6, 4])
  fig.suptitle("Original images")
  ax[0].imshow(test_dataset[idx_i][0][0].numpy(), cmap='gray')
  ax[1].imshow(test_dataset[idx_j][0][0].numpy(), cmap='gray')
   # Get embedding
  z_i = model.encode(test_dataset[idx_i][0].to(device)[None, ...])[0]
  z_j = model.encode(test_dataset[idx_j][0].to(device)[None, ...])[0]
  fig, ax = plt.subplots(2, n//2, figsize=[15, 8])
  ax = [sub for row in ax for sub in row]
  fig.suptitle("Reconstruction after interpolation in latent space")
  with torch.no_grad():
       ## BEGIN SOLUTION
       for i in range(0, n):
           interp = i/(n-1)
           flag = (z_i*(1-interp)+z_j*interp)
           fig_interpolation = model.decode(flag.to(device)[None, ...])
           ax[i].set_title(f"Interpolation {interp*100:.2f}%")
           ax[i].imshow(fig_interpolation[0][0].numpy(), cmap='gray')
       ## END SOLUTION
  plt.show()
```

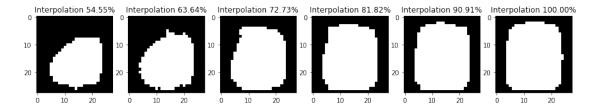
```
[]: interpolate_between(model, test_dataset, 0, 1)
```

## Original images



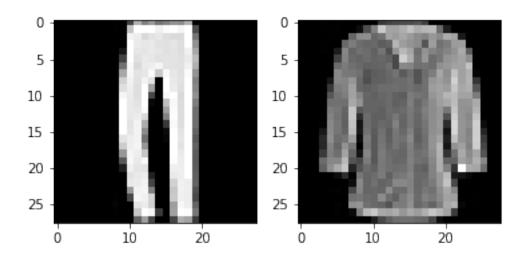
Reconstruction after interpolation in latent space



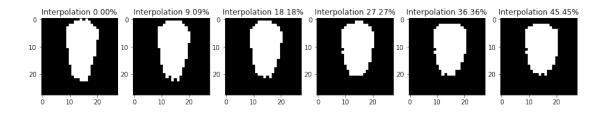


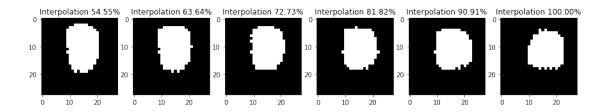
### []: interpolate\_between(model, test\_dataset, 2, 4)

### Original images



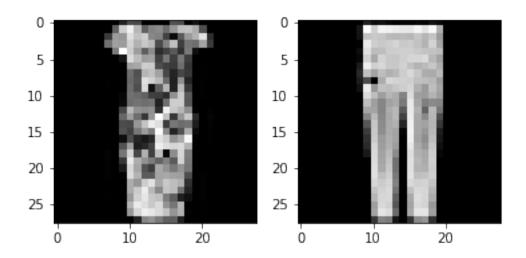
Reconstruction after interpolation in latent space





[]: interpolate\_between(model, test\_dataset, 100, 200)

### Original images



Reconstruction after interpolation in latent space

