
Geometric mean

For any $\mathbf{x} \in \mathbb{R}_{++}^n$, show the concavity of the geometric mean function defined as

$$f(\mathbf{x}) = (\prod_{i=1}^n x_i)^{1/n}.$$