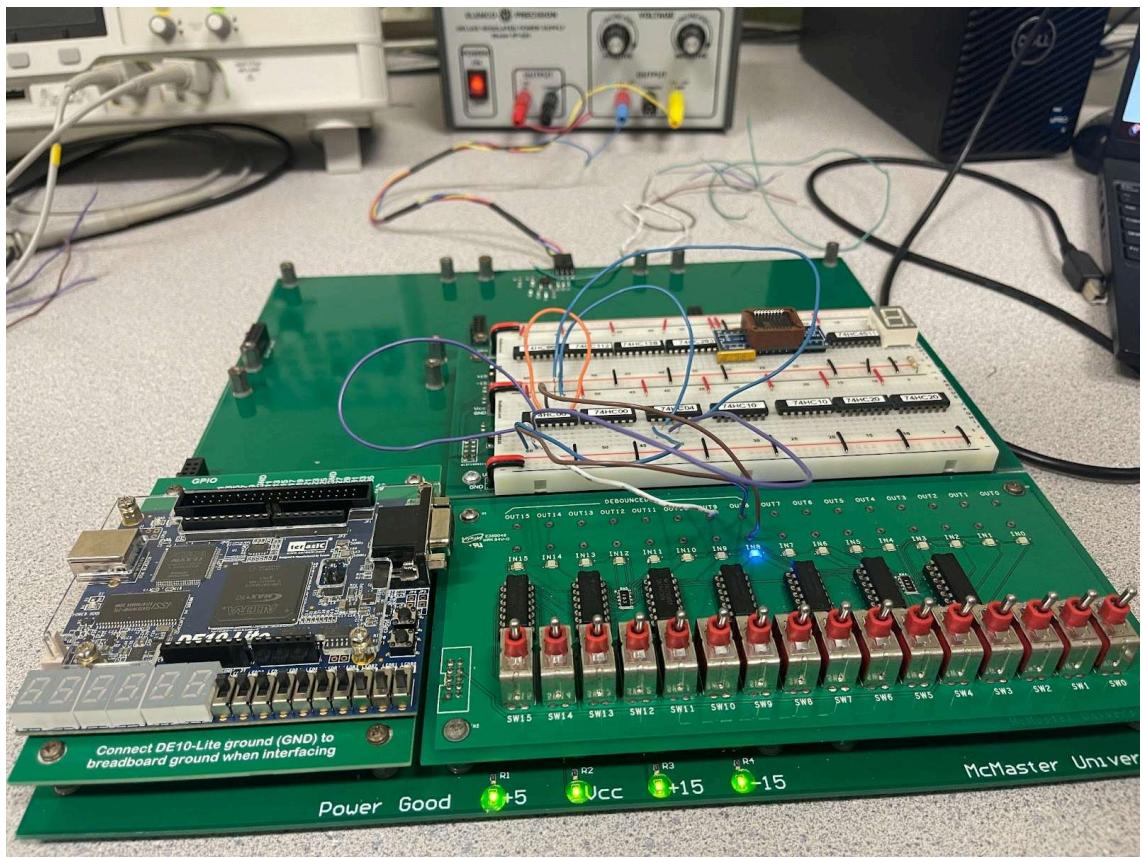


4.1



4.1

$$F(a, b, c, d) = \Sigma(0, 2, 5, 7, 8, 10, 13, 15)$$

$$\begin{aligned} f &= a'b'c'd' + a'b'cd' + ab'c'd + abc'd \\ &\quad + ab'c'd' + ab'cd' + abc'd + abcd \end{aligned}$$

$$m_0 + m_8 = b'c'd'$$

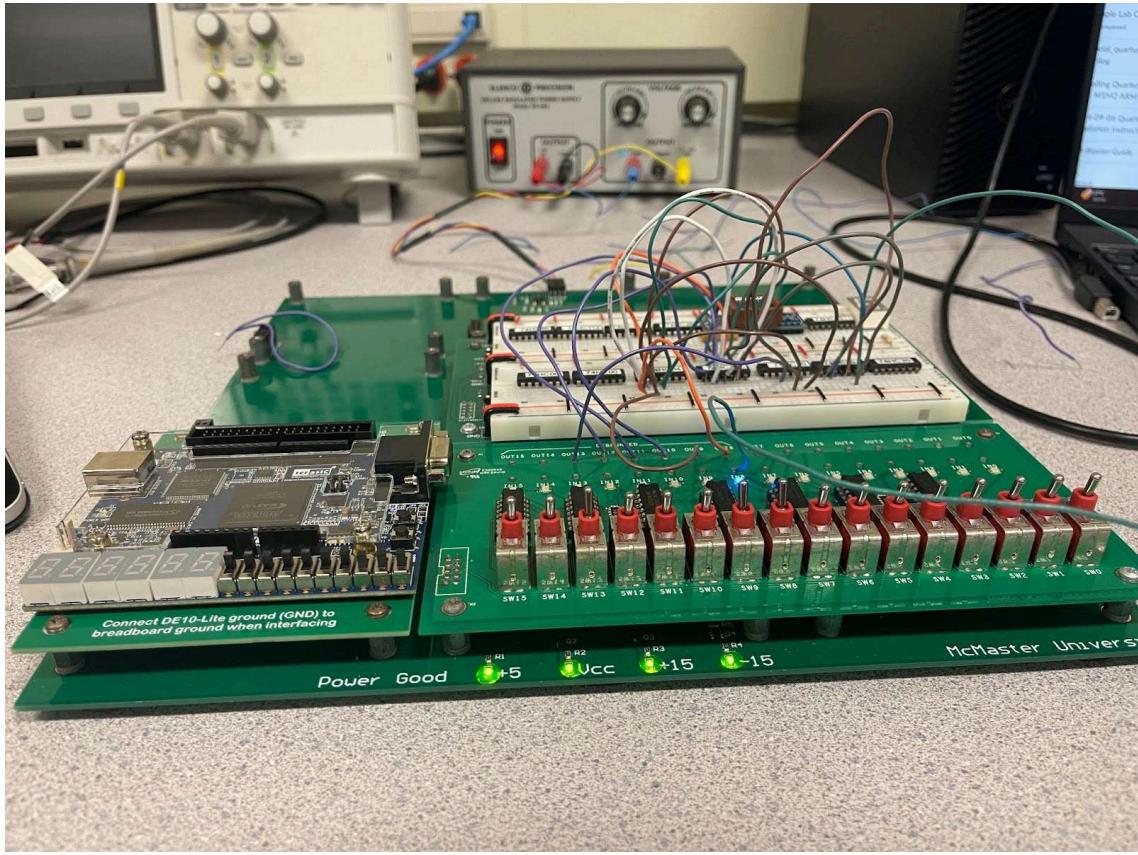
$$m_2 + m_{10} = b'cd' \Rightarrow F = bd' + bcd$$

$$m_5 + m_{13} = bc'd$$

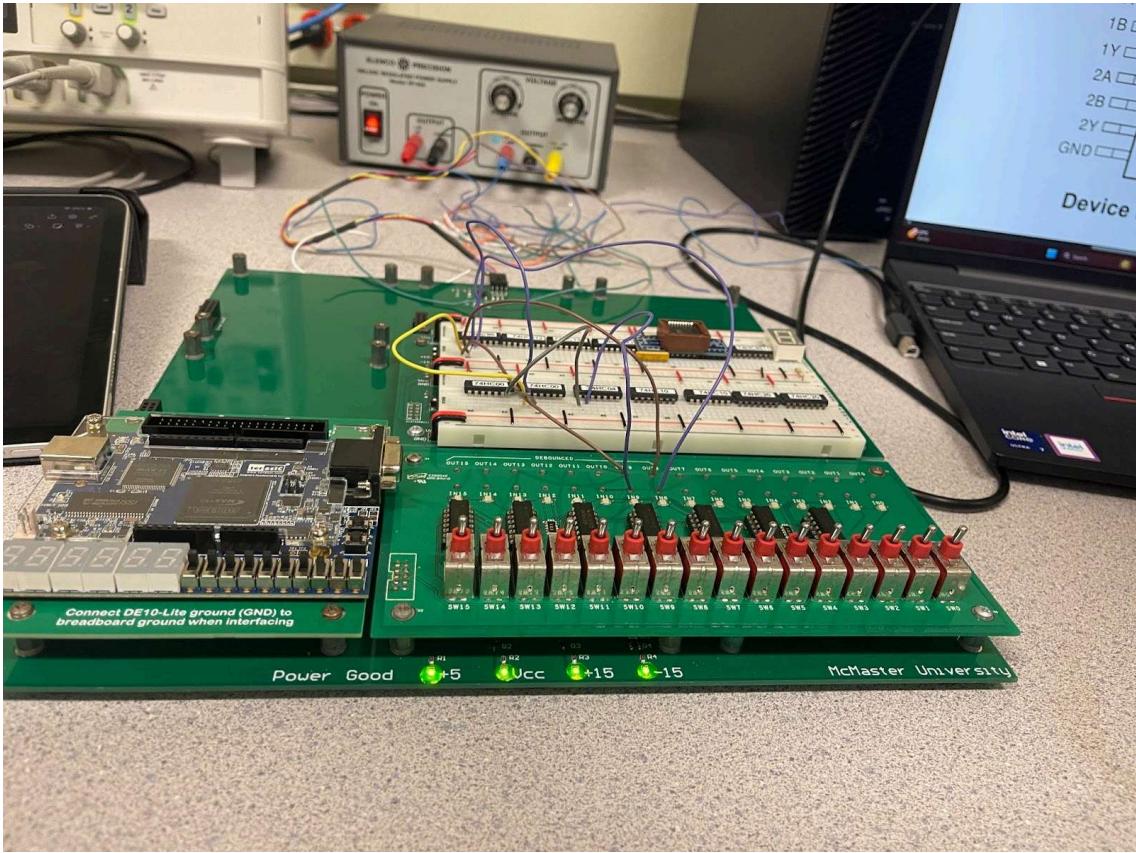
$$m_7 + m_{15} = bcd$$

$$= ((bd)' \cdot (bcd')')'$$

4.2



4.3



4.3

| <u>A</u> | <u>B</u> | <u>S</u> | <u>C_{out}</u> |
|----------|----------|----------|------------------------|
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |

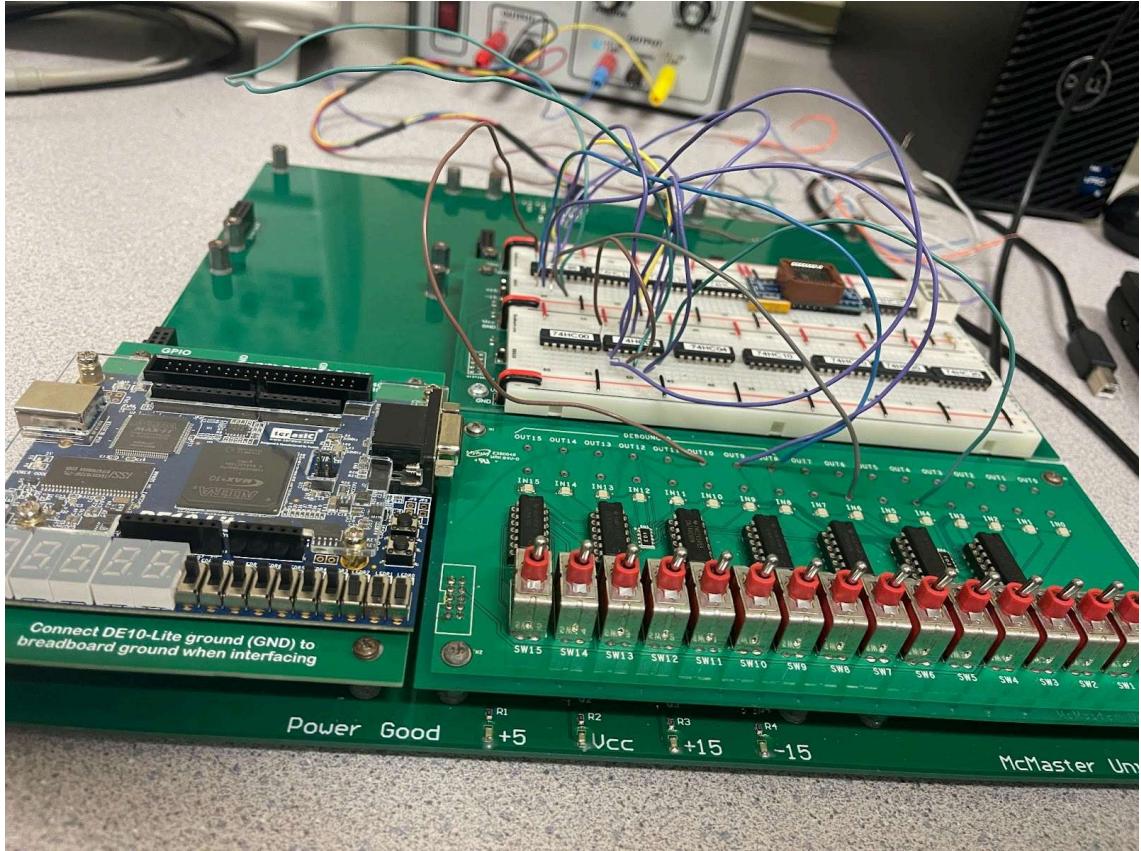
$$S = A \oplus B$$

$$C_{out} = A \cdot B$$

4.4

4.4

| A | B | C_{in} | S | C_{out} | |
|---|---|----------|---|-----------|------------------------------------|
| 0 | 0 | 0 | 0 | 0 | |
| 0 | 0 | 1 | 1 | 0 | $S = A \oplus B \oplus C_{in}$ |
| 0 | 1 | 0 | 1 | 0 | |
| 0 | 1 | 1 | 0 | 1 | $C_{out} = AB + BC_{in} + AC_{in}$ |
| 1 | 0 | 0 | 1 | 0 | |
| 1 | 0 | 1 | 0 | 1 | |
| 1 | 1 | 0 | 0 | 1 | |
| 1 | 1 | 1 | 1 | 1 | |



4.5

| C0 | A | B | Σ | Σ (unsigned) | Σ (2's comp) | C4 |
|----|------|------|----------|---------------------|---------------------|----|
| 0 | 0000 | 0000 | 0000 | 0 | 0 | 0 |
| 0 | 0000 | 0011 | 0011 | 3 | 3 | 0 |
| 0 | 0011 | 0000 | 0011 | 3 | 3 | 0 |
| 1 | 0011 | 0000 | 0100 | 4 | 4 | 0 |
| 0 | 0111 | 1000 | 1111 | 15 | -1 | 0 |
| 1 | 0111 | 1000 | 0000 | 0 | 0 | 1 |
| 0 | 1000 | 1000 | 0000 | 0 | 0 | 1 |
| 0 | 0011 | 1111 | 0010 | 2 | 2 | 1 |
| 0 | 0111 | 1111 | 0110 | 6 | 6 | 1 |
| 0 | 1001 | 1111 | 1000 | 8 | -8 | 1 |
| 0 | 1111 | 1111 | 1110 | 14 | -2 | 1 |
| 1 | 1111 | 1111 | 1111 | 15 | -1 | 1 |

4.5

Set $C_0 = 0$ Apply A/B

0000 / 0000

$\odot V_{\text{signed}} = C_3 \oplus C_4$

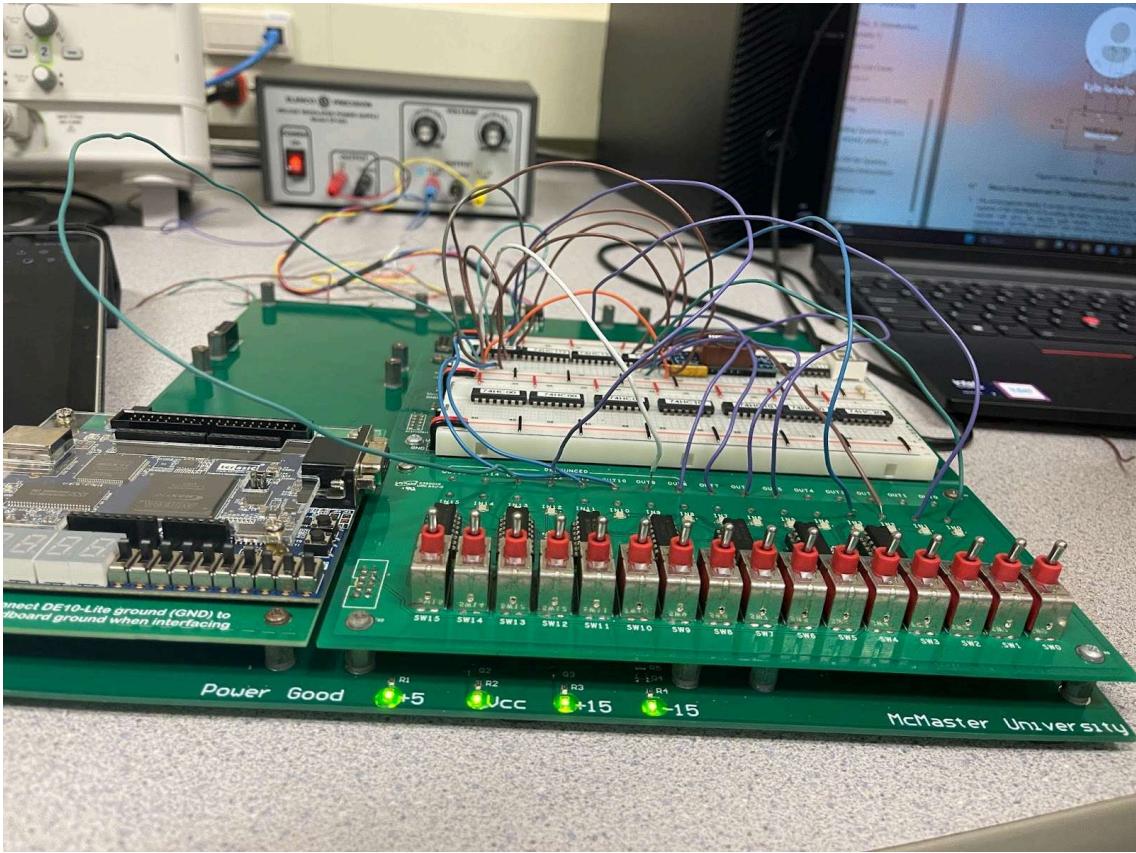
0001 / 0011

$S_3 = 1 \rightarrow \text{Negative}$

0 111 / 0001

1001 / 0110

4.6



4.6

$$S = 0 \quad A + B$$

$$S = 1 \quad A \cdot B$$

$$B_i' = B_i \oplus S \quad C_o = S$$

$$A + B_i \oplus S + C_o = A + B \text{ OR } A \cdot B$$

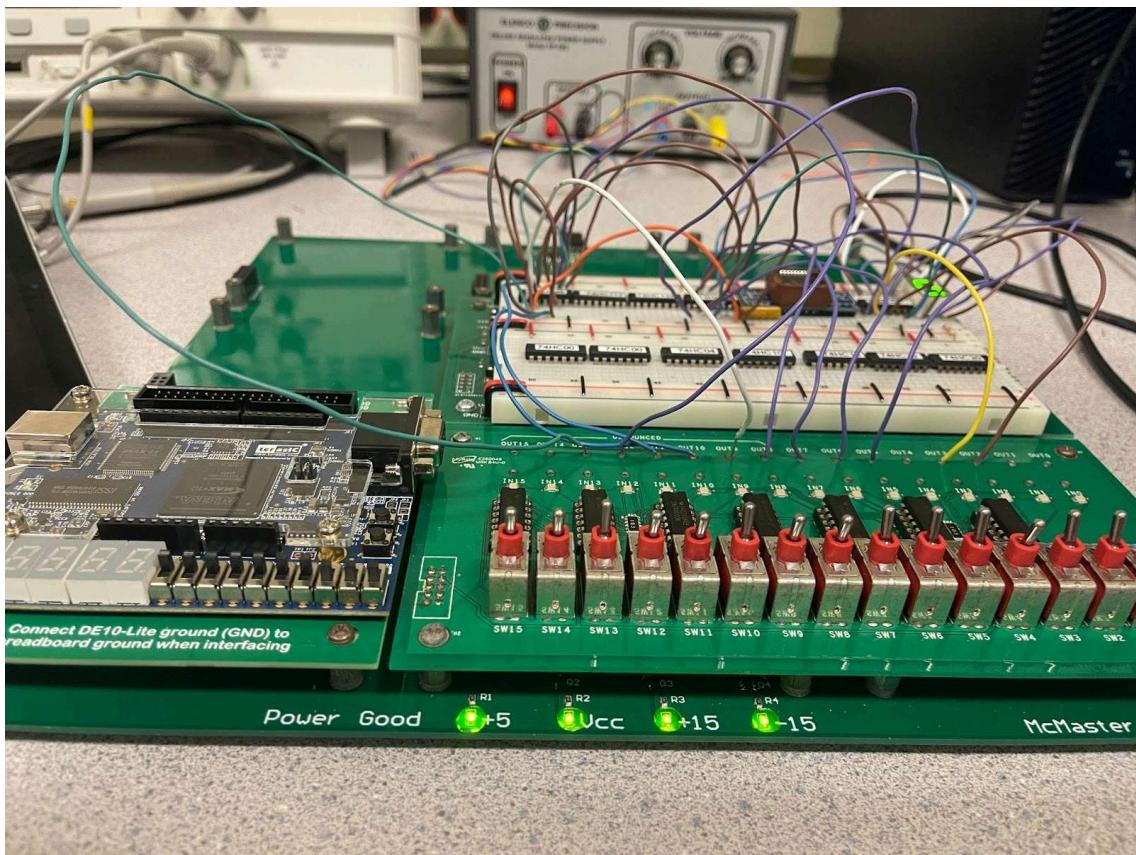
$$A + B' + C_o = A + B \text{ OR } A \cdot B$$

S can either add(+) or subtract (-)

So B_i is passed through XOR with $B_i' = B_i \oplus S$

and $C_o = S$

4.7



4.8

