

**Report: Implement SUDOKU Solver****Explanation**

The problem is implemented based on the idea in this paper:

<https://www.lri.fr/~conchon/mpri/weber.pdf>

In brief, we represent each possible digit  $d$  in a cell  $i, j$  as variable  $x[i,j,d]$ . Following are propositional clauses:

- For each  $1 \leq i, j \leq 9$ , we have:
  - a clause  $x[i, j, 1] \vee \dots \vee x[i, j, 9]$  to ensure that cell  $[i, j]$  contains at least one of the nine digits.
  - And 36 clauses:  $x[i, j, d] \vee x[i, j, d']$  with  $(1 \leq d, d' \leq 9)$  to ensure that cell  $[i, j]$  does not contain two digits at the same time.
- For each row, column or block, stating that nine grid cells  $x[1], \dots, x[9]$  contain distinct values. Then for each  $1 \leq i < j \leq 9$ , we have,  $x[i] \neq d \vee x[j] \neq d$  for all  $1 \leq d \leq 9$

In addition, we also need clauses for cells contain number provided in the Sudoku puzzle.

**How the program works**

Here are the 4 steps performed during the execution of the program.

1. *Read input file*
2. *Generate CNF file*
3. *Run miniSAT against CNF file*
4. *Read miniSAT output file and display the result to user (and save to file as well)*

**Input file**

Use 0 for empty box. An example of sudoku input file content:

```
6 0 0 0 0 0 7 0 0
0 0 0 1 6 2 3 0 0
0 0 0 3 5 7 0 8 2
0 8 0 9 3 1 0 4 7
0 7 0 0 0 0 0 1 0
9 4 0 7 8 5 0 3 0
7 9 0 8 1 6 0 0 0
0 0 4 5 7 9 0 0 0
0 0 8 0 0 0 0 0 9
```

**MiniSAT path**

Please be noted that you have to update your miniSAT execution path to make sure the program will run properly.

**How to run the program**

```
ruby sudoku.rb <INPUT_FILE>
```

*\*Development enviroment*

+ *Mac OSX Yosemite*

+ *Ruby 2.2.0*