

- pymdp: A Python library for active inference in discrete
- state spaces
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Software

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Statement of Need

Active inference is an account of cognition and behavior in complex systems which brings together action, perception, and learning under the theoretical mantle of Bayesian inference (Friston et al., 2009, 2012, 2015, 2017). Active inference has seen growing applications in academic research, especially in fields that seek to model human or animal behavior (Adams et al., 2021; Holmes et al., 2021; Parr et al., 2020). The majority of applications have focused on cognitive neuroscience, with a particular focus on modelling decision-making under uncertainty (Schwartenbeck et al., 2015; Smith et al., 2020; Smith, Kirlic, et al., 2021). Nonetheless, the framework has broad applicability and has recently been applied to diverse disciplines, ranging from computational models of psychopathology (Montague et al., 2012; Smith, Kirlic, et al., 2021), control theory (Baioumy et al., 2021; Baltieri & Buckley, 2019; Millidge et al., 2020) and reinforcement learning (Fountas et al., 2020; Millidge, 2020; Sajid et al., 2021; Tschantz, Baltieri, et al., 2020; Tschantz, Millidge, et al., 2020), through to social cognition (Adams et al., 2021; Tison & Poirier, 2021; Wirkuttis & Tani, 2021) and even real-world engineering problems (Fox, 2021; Martínez et al., 2021; Moreno, 2021). While in recent years, some of the code arising from the active inference literature has been written in open source languages like Python and Julia (Çatal et al., 2020; T. W. van de Laar & Vries, 2019; Millidge, 2020; Tschantz, Seth, et al., 2020; Ueltzhöffer, 2018), to-date, the most popular software for simulating active inference agents is the DEM toolbox of SPM (Friston et al., 2008; Smith, Friston, et al., 2021), a MATLAB library originally developed for the statistical analysis and modelling of neuroimaging data (Penny et al., 2007). DEM contains a reliable, reproducible set of functions for studying active inference, but the use of the toolbox can be restrictive for researchers in settings where purchasing a MATLAB license is financially costly. And although active inference researchers have relied heavily on DEM for simulating and fitting models of behavior, most of its functionality is restricted to single MATLAB scripts or functions, particularly one called spm_MDP_VB_X.m, that lack modularity and often must be customized for applications on a domain-specific basis. Increasing interest in active inference, manifested both in terms of sheer number of cited research papers as well as diversifying applications across disciplines, has thus created a need for generic, widely-available, and userfriendly code for simulating active inference in open-source scientific computing languages like

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Python. The software we present here, pymdp, represents a significant step in this direction:
namely, we provide the first open-source package for simulating active inference with discrete
state-space generative models. The name pymdp derives from the fact that the package is
written in the Python programming language and concerns discrete, Markovian generative
models of decision-making, which take the form of Markov Decision Processes or MDPs.

pymdp is a Python package that is directly inspired by the active inference routines contained in DEM. However, pymdp is has a modular, flexible structure that allows researchers to build and simulate active inference agents quickly and with a high degree of customization. We developed pymdp in the hopes that it will increase the accessibility and exposure of the active inference framework to researchers, engineers, and developers with diverse disciplinary backgrounds. In the spirit of open-source software, we also hope that it spurs new innovation, development, and collaboration in the growing active inference and wider Bayesian modelling communities.

₅₇ Introduction

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Simulations of active inference are commonly performed in discrete time and space (Da Costa et al., 2020; Friston et al., 2015). This is partially motivated by the mathematical tractability of performing inference with discrete probability distributions, but also by the intuition of modelling choice behavior as a sequence of discrete, mutually-exclusive choices, in e.g. psychophysics or decision-making experiments. The most popular generative models – used to realize active inference in this context – are partially-observable Markov Decision Processes or *POMDPs* (Kaelbling et al., 1998). POMDPs are state-space models that model the environment in terms of hidden states that stochastically change over time, as a function of both the current state of the environment as well as the behavioral output of an agent (control states or actions). Crucially, the environment is *partially-observable*, i.e. the hidden states are not directly observed by the agent, but can only be inferred through observations that relate to hidden states in a probabilistic manner, such that observations are modelled as being generated stochastically from the current hidden state. This necessitates both "perceptual" inference of hidden states as well as control.

As such, in most POMDP problems, an agent is tasked with inferring the hidden state of its environment and then choosing a sequence of control states or actions to change hidden states in a way that leads to desired outcomes (maximizing reward, or occupancy within some preferred set of states).

Usage

pymdp offers a suite of robust, tested, and modular routines for simulating active inference agents equipped with partially-observable Markov Decision Process (POMDP) generative models. Mathematically, a POMDP comprises a joint distribution over observations o, hidden states s, control states u and hyperparameters ϕ : $P(o, s, u, \phi)$. This joint distribution further factorizes into a set of categorical and Dirichlet distributions: the likelihoods and priors of the generative model. With pymdp, one can build a generative model using a set of prior and likelihood distributions, initialize an agent, and then link it to an external environment to run active inference processes - all in a few lines of code. The Agent and Env (environment) APIs of pymdp are built according to the standardized framework of OpenAIGym commonly used in reinforcement learning, where an agent and environment object recursively exchange observations and actions over time (Brockman et al., 2016).



Customizability

- In order to enhance the user-friendliness of pymdp without sacrificing flexibility, we have built the library to be highly modular and customizable, such that agents in pymdp can be specified at a variety of levels of abstraction with desired parameterisations. The methods of the Agent class can thus be called in any particular order, depending on the application, and furthermore they can be specified with various keyword arguments that entail choices of implementation details at lower levels.
- By retaining a modular structure throughout the package's dependency hierarchy, pymdp also affords the ability to flexibly compose different low level functions. This allows users to customize and integrate their active inference loops with desired inference algorithms and policy selection routines. For instance, one could sub-class the Agent class and write a customized step() function, that combines whichever components of active inference one is interested in.

Related software packages

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The DEM toolbox within SPM in MATLAB is the current gold-standard in active inference modelling. In particular, simulating an active inference process in DEM consists of defining the generative model in terms of a fixed set of matrices and vectors, and then calling the spm_MDP_VB_X.m function to simulate a sequence of trials. pymdp, by contrast, provides a user-friendly and modular development experience, with core functionality split up into different libraries that separately perform the computations of active inference in a standalone fashion. Moreover, pymdp provides the user the ability to write an active inference process at different levels of abstraction depending on the user's level of expertise or skill with the package - ranging from the high level Agent functionality, which allows the user to define and simulate an active inference agent in just a few lines of code, all the way to specifying a particular variational inference algorithm (e.g. marginal-message passing (Parr et al., 2019)) for the agent to use during state estimation. In the DEM toolbox of SPM, this would require setting undocumented flags or else manually editing the routines in spm_MDP_VB_X.m to enable or disable bespoke functionality. There has been one recent attempt at creating a comprehensive user-guide for building active inference agents in DEM (Smith, Friston, et al., 2021), though to our knowledge there has not been a package devoted to the open source development of these powerful software tools.

A recent related, but largely non-overlapping project is ForneyLab, which provides a set of Julia libraries for performing approximate Bayesian inference via message passing on Forney Factor Graphs (T. van de Laar et al., 2018). Notably, this package has also seen several applications in simulating active inference processes, using ForneyLab as the backend for the inference algorithms employed by an active inference agent (Ergul et al., 2020; T. van de Laar et al., 2021; T. W. van de Laar & Vries, 2019; Vanderbroeck et al., 2019). While ForneyLab focuses on including a rigorous set of message passing routines that can be used to simulate active inference agents, pymdp is specifically designed to help users quickly build agents (regardless of their underlying inference routines) and plug them into arbitrary environments to run active inference in a few easy steps.

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