# Wall sheared thermal convection: heat transfer enhancement and turbulence relaminarization

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We studied the flow organization and heat transfer properties in two-dimensional and three-dimensional Rayleigh-Bénard cells that are imposed with different types of wall shear. The external wall shear is added with the motivation of manipulating flow mode to control heat transfer efficiency. We imposed three types of wall shear that may facilitate the single-roll, the horizontally stacked double-roll, and the vertically stacked double-roll flow modes, respectively. Direct numerical simulations are performed for fixed Rayleigh number (Ra) of  $Ra = 10^8$  and fixed Prandtl number (Pr) of Pr = 5.3, while the wall shear Reynolds number  $(Re_w)$  is in the range of  $60 \leqslant Re_w \leqslant 6000$ . Generally, we found enhanced heat transfer efficiency and global flow strength with the increase of  $Re_w$ . However, even with the same magnitude of global flow strength, the heat transfer efficiency varies significantly when the cells are under different types of wall shear. An interesting finding is that by increasing the wall shear strength, the thermal turbulence is relaminarized, and more surprisingly, the heat transfer efficiency in the laminar state is higher than that in the turbulent state. We found the enhanced heat transfer efficiency at the laminar regime is due to the formation of more stable and stronger convection channels. We propose the origin of thermal turbulence laminarization is the reduced amount of thermal plumes. Because plumes are mainly responsible for turbulent kinetic energy production, when the detached plumes are swept away by the wall shear, the reduced number of plumes leads to weaker turbulent kinetic energy production. We also quantify the efficiency of facilitating heat transport via external shearing, and found that for larger  $Re_w$ , the enhanced heat transfer efficiency comes at a price of a larger expenditure of mechanical energy.

Key words: Bénard convection, plumes/thermals, turbulent convection

#### 1. Introduction

Thermal convection occurs ubiquitously in nature and has wide applications in industry. A paradigm for the study of thermal convection is the Rayleigh-Bénard (RB) convection, which is a fluid layer heated from the bottom and cooled from the top (Ahlers et al. 2009; Lohse & Xia 2010; Chillà & Schumacher 2012; Xia 2013). The control parameters of the canonical RB system include the Rayleigh number (Ra, defined later

in the paper) that describes the strength of the buoyancy force relative to the thermal and viscous dissipative effects, and the Prandtl number (Pr) that represents the thermophysical fluid properties. One of the response parameters of the RB system is the Nusselt number (Nu) which characterizes the global heat transfer efficiency. Various approaches have been designed to enhance the heat transfer efficiency of the convection cells, such as adding roughness to the walls (Ciliberto & Laroche 1999; Wagner & Shishkina 2015; Jiang et al. 2018; Rusaouën et al. 2018; Zhu et al. 2019), introducing vibration forcing (Wang et al. 2020; Yang et al. 2020a), adding dispersed phase of particles or bubbles (Lakkaraju et al. 2013; Guzman et al. 2016; Gvozdić et al. 2018; Wang et al. 2019; Yang et al. 2022), confinement (Huang et al. 2013; Chong et al. 2017; Zhang et al. 2022), rotation (Zhong et al. 2009; Stevens et al. 2009, 2013; Yang et al. 2020b), the addition of passive barriers (Liu & Huisman 2020), and so on.

Roche et al. (2002) and Chillà et al. (2004) conjectured that the internal flow structure is correlated with global heat transfer. Sun et al. (2005) compared the Nu in a leveled cell and a tilted cell, correspondingly, the large-scale circulation (LSC) plane sweeps azimuthally or is locked in a particular orientation. They showed that the Nu is larger in the leveled cell, indicating that different flow structures can results in different values of Nu. Xi & Xia (2008) observed both the single-roll and the double-roll flow structures in the LSC. They examined the average Nu corresponding to a particular flow structure and found that the single-roll flow structure is more efficient for heat transfer. Weiss & Ahlers (2011) further confirmed the occurrence of a double-roll structure in the LSC, and the higher heat transfer efficiency of the single-roll state. van der Poel et al. (2011, 2012) numerically showed the coexistence of different turbulent structures also exists in simple two-dimensional RB cells with various cell aspect ratios. They also studied the effect of various velocity boundary conditions (i.e., no-slip, stress-free, and periodic boundary conditions) on the heat transfer and flow topoplogy (van der Poel et al. 2014), and they showed either the roll-like or the zonal flow can appear under different velocity boundary conditions. Adopting Fourier mode decompositions, Xi et al. (2016) presented direct evidence that the first Fourier mode is more efficient for heat transfer in a cylindrical cell. Xu et al. (2020) analyzed the coherent flow structure in two-dimensional square convection cells. Results from both Fourier mode decomposition and proper orthogonal decomposition indicate that the single-roll flow mode and the horizontally stacked doubleroll mode are efficient for heat transfer on average; in contrast, the vertically stacked double-roll mode is inefficient for heat transfer on average. A natural question arises on how to manipulate flow mode to control heat transfer efficiency.

In this work, we impose various types of wall shear to control the internal flow mode, which further leads to modification of heat transfer. Previously, Blass  $et\ al.\ (2020,\ 2021)$  added a Couette type shear (i.e., the top and bottom walls move in opposite directions with constant speed  $u_w$ ) to the RB system as an attempt to trigger the transition to the ultimate convection regime (Kraichnan 1962). With the increasing wall shear strength, they observed the variation of flow states from a buoyancy-dominated regime to a shear-dominated regime. In the buoyancy dominated regime, the flow structure is similar to that in the canonical RB convection; in the transitional regime, the rolls are increasingly elongated with increasing shear; in the shear dominated regime, there are large-scale meandering rolls. Jin  $et\ al.\ (2022)$  further added the Couette type shear to convection cells that have rough walls, and the moving rough plates introduce an external shear to strengthen the LSC. As a result, the interaction between the LSC and secondary flows within cavities are increased, and more thermal plumes are triggered. In this work, our motivation of imposing wall shear is to facilitate various flow modes (i.e., the single-roll, the horizontally stacked double-roll, and the vertically stacked double-roll modes) in the

convection cell to further control heat transfer efficiency. Specifically, we will add the (m,n) type of wall shear to the RB system, and such types of wall shear are expected to facilitate m rolls in the horizontal direction and n rolls in the vertical direction. The use of shear modulated boundary conditions essentially leads to mixed convection, which has received considerable attention due to its importance in many engineering applications such as cooling of electronic devices, coating, and float glass production (Hunt 1991; Shankar & Deshpande 2000). The rest of this paper is organized as follows. In section 2, we present numerical details for the simulations. In section 3, general flow and heat transfer features are presented, and heat transfer enhancement under various types of wall shear is reported. An interesting finding is thermal turbulence relaminarization under the imposed wall shear, and we then discuss the possible mechanism behind it. In addition, we quantify the efficiency of facilitating heat transport via external shearing. In section 4, the main findings of the present work are summarized.

#### 2. Numerical method

#### 2.1. Direct numerical simulation of incompressible thermal convection

We consider incompressible thermal convection under the Boussinesq approximation. The temperature is treated as an active scalar, and its influence on the velocity field is realized through the buoyancy term; all the transport coefficients are assumed to be constants. The governing equations can be written as

$$\nabla \cdot \mathbf{u} = 0 \tag{2.1}$$

$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} = -\frac{1}{\rho_0} \nabla P + \nu \nabla^2 \mathbf{u} + g\beta (T - T_0) \hat{\mathbf{y}}$$
(2.2)

$$\frac{\partial T}{\partial t} + \mathbf{u} \cdot \nabla T = \alpha \nabla^2 T \tag{2.3}$$

where **u** is the fluid velocity, P and T are pressure and temperature of the fluid, respectively.  $\beta$ ,  $\nu$ , and  $\alpha$  are the thermal expansion coefficient, kinematic viscosity, and thermal diffusivity, respectively. The zero subscripts (0) refer to the reference values. g is the gravity acceleration value, and  $\hat{\mathbf{y}}$  is the unit vector parallel to the gravity. With the following non-dimensional group

$$\mathbf{x}^* = \mathbf{x}/H, \quad t^* = t/\sqrt{H/(g\beta\Delta_T)}, \quad \mathbf{u}^* = \mathbf{u}/\sqrt{g\beta\Delta_T H},$$

$$P^* = P/(\rho_0 g\beta\Delta_T H), \quad T^* = (T - T_0)/\Delta_T$$
(2.4)

Then, Eqs. (2.1-2.3) can be rewritten in dimensionless form as

$$\nabla \cdot \mathbf{u}^* = 0 \tag{2.5}$$

$$\frac{\partial \mathbf{u}^*}{\partial t^*} + \mathbf{u}^* \cdot \nabla \mathbf{u}^* = -\nabla P^* + \sqrt{\frac{Pr}{Ra}} \nabla^2 \mathbf{u}^* + T^* \hat{\mathbf{y}}$$
 (2.6)

$$\frac{\partial T^*}{\partial t^*} + \mathbf{u}^* \cdot \nabla T^* = \sqrt{\frac{1}{PrRa}} \nabla^2 T^*$$
 (2.7)

Here, H is the cell height and  $\Delta_T$  is the temperature difference between heating and cooling walls. In the following, for convenience, we will drop the superscript star (\*) to denote a dimensionless variable. The dimensionless parameters of the Rayleigh number (Ra), the Prandtl number (Pr) and the cell aspect ratio  $(\Gamma_{\parallel})$  in the plane parallel to the

LSC's circulation plane and  $\Gamma_{\perp}$  in the plane perpendicular to the LSC) are defined as

$$Ra = \frac{g\beta\Delta_T H^3}{\nu\alpha}, \quad Pr = \frac{\nu}{\alpha}, \quad \Gamma_{\parallel} = \frac{L}{H}, \quad \Gamma_{\perp} = \frac{W}{H}$$
 (2.8)

where L is cell length and W is the cell width.

We adopt the spectral element method (Patera 1984) implemented in the opensource Nek5000 solver (version v19.0) as the numerical tool for the direct numerical simulation. In the Nek5000 solver, the effective grid number equals the product of spectral element number and polynomial order. We set the spectral elements for the velocity with polynomial order N and the spectral elements for the pressure with polynomial order N-2 (to avoid spurious pressure modes). Similar to previous turbulent flow simulations (Kooij et al. 2018), we fix the polynomial order as N=8. The viscous term is treated implicitly with the second-order backward difference scheme, while the convection term and other terms are treated with an explicit second-order extrapolation scheme. The discretized system is solved with preconditioned conjugate gradient (PCG) iteration, and Jacobi preconditioning is adopted for the linear velocity system. A pressure correction step follows the solution of the discretized system, which is also solved with PCG iteration; and the linear pressure system is solved by the multilevel overlapping Schwarz method. As for the energy equation (i.e., temperature governed by convectiondiffusion type equation), the transient term is treated implicitly with the second-order backward difference scheme, and the convection term is treated with an explicit secondorder extrapolation scheme. For the Navier-Stokes and convection-diffusion equations, the temporal derivative applies a Courant-Friedrichs-Lewy constraint of  $\max(|\mathbf{u}|\Delta t/\Delta x) \approx$ 0.5. More numerical details of the spectral element method and validation of the Nek5000 solver can be found in (Fischer 1997; Fischer et al. 2002; Deville et al. 2002; Kooij et al. 2018). To verify the results obtained from the Nek5000 solver, we also performed a set of simulations at wall shear Reynolds number ( $Re_w$ , defined later in the paper) of 100 using an in-house solver based on the lattice Boltzmann (LB) method (Xu et al. 2017, 2019; Xu & Li 2023). The results from the open-source Nek5000 solver and the in-house LB solver are shown to be consistent.

#### 2.2. Simulation settings

As illustrated in figure 1, the dimensions H, L and W correspond to the y, x and zin the Cartesian coordinates. The top and the bottom of the horizontal walls are kept at constant low and high temperatures of  $T_{cold}$  and  $T_{hot}$ , respectively, while the vertical sidewalls are adiabatic. For the velocity at the walls, we designed the (m,n) type wall shear to facilitate the flow structure with m rolls in the x-direction and n rolls in the y-direction. Specifically, we consider three types of wall shear boundary conditions: the (1, 1) type wall shear that may facilitate the single-roll flow mode (see figures 1a and 1d), the (2, 1) type wall shear that may facilitate the horizontally stacked double-roll mode (see figures 1b and 1e), and the (1, 2) type wall shear that may facilitate the vertically stacked double-roll mode (see figures 1c and 1f). Under the (1, 1) type wall shear, the velocity boundary conditions are (i) at  $0 \le x \le L$  and y = 0, we have  $\mathbf{u} = (-u_w, 0, 0)$ ; (ii) at  $0 \leqslant x \leqslant L$  and y = H, we have  $\mathbf{u} = (u_w, 0, 0)$ ; (iii) at x = 0 and  $0 \leqslant y \leqslant H$ , we have  $\mathbf{u} = (0, u_w, 0)$ ; (iv) at x = L and  $0 \le y \le H$ , we have  $\mathbf{u} = (0, -u_w, 0)$ . Similar mathematical formulations for the velocity boundary conditions under the (2, 1) type and the (1, 2) type wall shear can be easily written (not present here for clarity). When an external wall shear is introduced, an additional control parameter of wall shear Reynolds number  $(Re_w = Hu_w/\nu)$  is needed. Here,  $u_w$  is the wall shear velocity. Simulation results are provided for fixed Rayleigh number of  $Ra = 10^8$ , fixed Prandtl number of Pr = 5.3

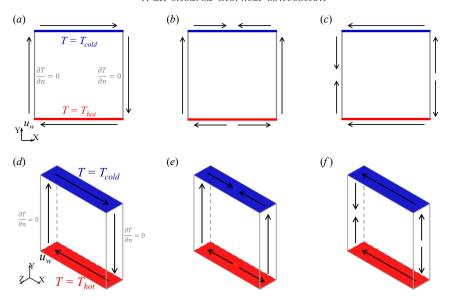


FIGURE 1. Schematic illustration of the shear convection cells in (a-c) two-dimension (2-D) and (d-f) three-dimension (3-D), for (a, d) the (1, 1) type wall shear, (b, e) the (2, 1) type wall shear, and (c, f) the (1, 2) type wall shear boundary conditions.

[corresponds to the working fluids of water at 31°C (Zhang et al. 2017)] and fixed aspect ratio of  $\Gamma_{\parallel} = 1$ . In the 3-D cases, we consider aspect ratios of  $\Gamma_{\perp} = 1/8$  and 1/4 such that the LSC is confined in the x-y plane, enabling easy manipulation of the flow mode via wall shear. The wall shear Reynolds number is in the range of  $60 \le Re_w \le 6000$  for 2-D cases, and  $Re_w = 100$  and 3000 for 3-D cases. In the simulation, after the initial transient stage, we run at least 5000  $t_f$  for 2-D cases and 800  $t_f$  for 3-D cases to obtain the statistics. Here,  $t_f$  denotes free-fall time units:  $t_f = \sqrt{H/(g\beta\Delta_T)}$ . We check whether the grid spacing  $\Delta_q$  and time interval  $\Delta_t$  are properly resolved by comparing them with the Kolmogorov and Batchelor scales. The Kolmogorov length scale can be estimated as  $\eta_K = (\nu^3/\langle \varepsilon_u \rangle)^{1/4}$ , the Batchelor length scale can be estimated as  $\eta_B = \eta_K P r^{-1/2}$ (Batchelor 1959; Silano et al. 2010), and the Kolmogorov time scale can be estimated as  $\tau_{\eta} = \sqrt{\nu/\langle \varepsilon \rangle}$ . In the canonical RB convection, we adopted spectral elements of  $64 \times 64$ for 2-D cases,  $32 \times 32 \times 5$  for 3-D cases with  $\Gamma_{\perp} = 1/8$ , and  $32 \times 32 \times 9$  for 3-D cases with  $\Gamma_{\perp} = 1/4$ ; the corresponding effective grid number is listed in table 1. In the wall-sheared thermal convection, we adopted a finer distributed spectral element of  $96 \times 96$  for 2-D cases,  $44 \times 44 \times 7$  for 3-D cases with  $\Gamma_{\perp} = 1/8$ , and  $44 \times 44 \times 13$  for 3-D cases with  $\Gamma_{\perp} = 1/4$ . We estimate the global kinetic energy dissipation rate as  $\langle \varepsilon_u \rangle = RaPr^{-2}(Nu-1)\nu^3/H^4$  in the canonical RB convection (Shraiman & Siggia 1990), and  $\langle \varepsilon_u \rangle = \sqrt{Pr/Ra\langle (\partial_i u_i') \rangle_{V,t}}$ in the wall-sheared convection (Pope 2000). Here, the subscripts i and j are dummy indices, and  $\langle \cdots \rangle_{V,t}$  denotes the spatial and temporal average. As shown in table 1, the maximum grid spacing  $(\Delta_g)_{\text{max}}$  is less than (or comparable) to the Kolmogorov and Batchelor length scales for 2-D cases (or 3-D cases); the maximum time interval  $(\Delta_t)_{\text{max}}$  is far less than the Kolmogorov time scale for all the cases. Thus, adequate spatial and temporal resolution is guaranteed. Each simulation was conducted with 48 Message Passing Interface (MPI) processes on an in-house cluster that required around 12,000 core hours for 2-D cases and 50,000 core hours for 3-D cases.

Wall shear type	$Re_w$	$\Gamma_{\perp}$	Effective grid number	$(\Delta_g)_{\mathrm{max}}/\eta_K$	$(\Delta_g)_{\mathrm{max}}/\eta_B$	$(\Delta_t)_{\mathrm{max}}/ au_\eta$
_	0	_	$512 \times 512$	0.26	0.60	0.0019
	0	1/8	$256 \times 256 \times 40$	0.51	1.17	0.0068
	0	1/4	$256 \times 256 \times 72$	0.52	1.17	0.0054
	Ü	-/ -	200 X 200 X 12	0.02	1111	0.0001
(1, 1) type	60	_	$768 \times 768$	0.13	0.30	0.0009
( / / 01	100	-	$768 \times 768$	0.13	0.30	0.0008
	200	-	$768 \times 768$	0.13	0.30	0.0008
	500	-	$768 \times 768$	0.12	0.28	0.0007
	800	-	$768 \times 768$	0.11	0.24	0.0005
	100	1/8	$352 \times 352 \times 56$	0.34	0.77	0.0046
	100	1/4	$352 \times 352 \times 104$	0.35	0.80	0.0032
(2, 1) type	60	-	$768 \times 768$	0.15	0.35	0.0012
	100	-	$768 \times 768$	0.14	0.33	0.0010
	200	-	$768 \times 768$	0.14	0.32	0.0009
	500	-	$768 \times 768$	0.13	0.31	0.0006
	100	1/8	$352 \times 352 \times 56$	0.32	0.74	0.0041
	100	1/4	$352 \times 352 \times 104$	0.34	0.78	0.0032
	3000	1/4	$352 \times 352 \times 104$	0.55	1.26	0.0017
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(1, 2) type	60	-	$768 \times 768$	0.17	0.39	0.0012
	100	-	$768 \times 768$	0.14	0.33	0.0009
	200	-	$768 \times 768$	0.13	0.30	0.0007
	500	-	$768 \times 768$	0.12	0.27	0.0007
	800	-	$768 \times 768$	0.11	0.25	0.0004
	1000	- 1./0	$768 \times 768$	0.10	0.23	0.0003
	100	1/8	$352 \times 352 \times 56$	0.34	0.79	0.0038
	100	1/4	$352 \times 352 \times 104$	0.38	0.87	0.0039
	3000	1/4	$352 \times 352 \times 104$	0.53	1.22	0.0016

Table 1. A posteriori check of spatial and temporal resolutions of the simulations. The columns from left to right indicate the following: imposed wall shear type ('-' denotes convection without wall shear), the wall shear Reynolds number  $Re_w$ , cell aspect ratio  $\Gamma_{\perp}$  in the plane perpendicular to the LSC ('-' denotes 2-D cases), effective grid number (i.e., the product of spectral element number and polynomial order), the ratio of maximum grid spacing over the Kolmogorov length scale, the ratio of maximum grid spacing over the Batchelor length scale, the ratio of maximum time interval over the Kolmogorov time scale. Note that not all the simulations in this work are listed in the table.

#### 3. Results and discussion

### 3.1. Global flow and heat transfer features

Typical snapshots of temperature field and flow field under the three types of wall shear are shown in figures 2, and the corresponding video can be viewed in the supplementary movie 1. Here, the Ra is fixed as  $Ra = 10^8$  and the Pr is fixed as Pr = 5.3. At small wall shear strength of  $Re_w = 100$ , the convection is still buoyancy-dominated, plumes detach from thermal boundary layers and further self-organize into the LSC; meanwhile, the flow structure in the convection cell is influenced by the imposed wall shear. For the convenience of comparison, we also provide the flow and heat transfer patterns in the canonical RB convection without wall shear (see Appendix A). The single-roll flow structure appears under the (1, 1) type wall shear (see figures 2a and 2g), whilst the corner rolls are suppressed compared to that without wall shear; the horizontally stacked double-roll flow structure appears under the (2, 1) type wall shear (see figures 2b and 2h);

the vertically stacked double-roll flow structure appears under the (1, 2) type wall shear (see figures 2c and 2i). At large wall shear strength of  $Re_w = 4000$  in 2-D and  $Re_w = 3000$ in 3-D, the convection is shear-dominated, and the flow structures inside the convection cell are completely influenced by the external wall shear. For example, under the (1, 1) type wall shear (see figures 2d and 2j), the hot (or cold) fluids near the bottom (or top) wall are swept away by the LSC in the clockwise direction, and rise (or fall) along the left (or right) vertical wall, while the fluids in the bulk region are well-mixed. Similar observation can be found for the flow structure under the (2, 1) type wall shear (see figures 2e and 2k), while the cold fluids also fall along the vertical mid-plane of the cell. As for the flow structure under the (1, 2) type wall shear, in the 2-D case (see figure 2f), the top and bottom subregions are completed separated without heat transfer between each other, acting as a "thermal barrier" exists at the half height of the cell; however, in the 3-D case (see figure 21), we did not observe a complete separation of hot and cold fluids. We infer the differences in flow structure between 2-D and 3-D configurations are due to the flow state: in the steady laminar flow (as in the 2-D case), the rising hot fluids and falling cold fluids can remain stable boundaries; while in the turbulent flow (as in the 3-D case), the hot and cold fluids are more mixed. We also checked the flow field within the  $\Gamma_{\perp} = 1/8$  cell, where the flow is in a laminar state, and we indeed found a separation of hot and cold fluids.

With simulations of three different types of wall shear in the range of  $60 \le Re_w \le 6000$ , we can obtain the phase diagram of whether the flow is in the turbulent state or laminar state, as shown in figure 3(a) for 2-D cases. Here, we placed numerical probers in the cell and analyzed the time recordings of local velocity and temperature series to determine the flow states (Heslot et al. 1987; Silano et al. 2010). We determined the flow is in the laminar state if the time recordings do not vary with time (i.e., steady laminar state) or the power spectral density (PSD) of the time recordings exhibits characteristic peaks (i.e., unsteady laminar state); otherwise, if the PSD of the time recording exhibit continuous spectra, the flow is in the turbulent state. In Appendix B, we give examples of temperature series and the corresponding PSD at the location of (0.25, 0.5) in the 2-D convection cell under (1, 1) type wall shear. The phase diagram of the flow states can be understood in terms of competition between buoyancy and shear effects, which can be quantified by the Richardson number as  $Ri = Ra/(Re_w^2 Pr)$ . In figure 3(b), we redraw the phase diagram of the flow states at different Ri. For lower  $Re_w$  (i.e., higher Ri at fixed Ra and Pr), the flow is buoyancy dominated and possesses the key features of turbulent convection; for higher  $Re_w$  (i.e., lower Ri), the flow is shear dominated and enters a laminar state. Turbulent laminarisation is counterintuitive and it is recently found in pipe flow by amplifying wall shear (Kühnen et al. 2018; Scarselli et al. 2019). It should also be noted that when the  $Re_w$  further increases, the wall shear would introduce flow instability and the flow would transit to a turbulent state again. However, our numerical tests show that the flow can remain laminar for a wide range of  $Re_{w}$  in 2-D cases, a further transition to shear turbulence may occur at a much higher  $Re_w$ . We also found that the shear instability is prominent in 3-D cases, particularly when  $\Gamma_{\perp}$  is larger, thus the flow remains laminar in a smaller range of wall shear Reynolds number. For example, at  $Re_w = 3000$ , the flow is laminar in convection cells with  $\Gamma_{\perp} = 1/8$  under all three types of wall shear; while the flow is laminar only under the (1, 1) type wall shear in the  $\Gamma_{\perp} = 1/4$  cell.

We then examine the global response parameters of Nusselt number (Nu) and Reynolds number (Re) on the control parameter  $Re_w$ . Here, the heat transfer efficiency is calculated as  $Nu = \sqrt{Ra \cdot Pr} \langle vT \rangle_{V,t} + 1$ , the global flow strength is calculated as  $Re = \sqrt{\|\mathbf{u}\|^2} \rangle_{V,t} H/\nu$ . The measured Nu and Re as a function of  $Re_w$  for various types of

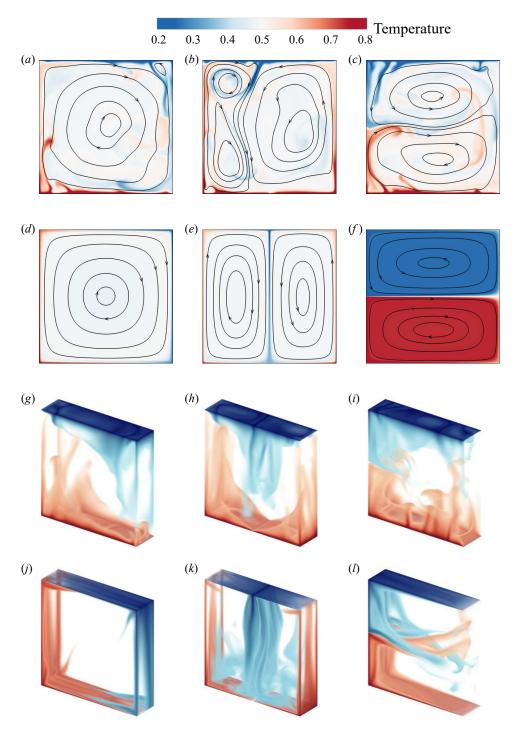


FIGURE 2. Typical instantaneous temperature field (contours in 2-D and volume rendering in 3-D) and flow field (streamlines in 2-D) at (a-c)  $Re_w=100$ , (d-f)  $Re_w=4000$ , (g-i)  $Re_w=100$  and  $\Gamma_{\perp}=1/4$ , (j-l)  $Re_w=3000$  and  $\Gamma_{\perp}=1/4$ , under (left-column) the (1,1) type wall shear, (middle-column) the (2,1) type wall shear, (right-column) the (1,2) type wall shear.

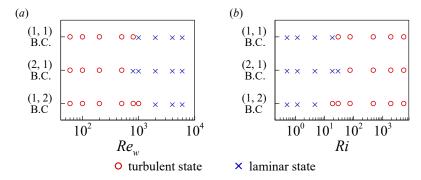


FIGURE 3. Phase diagram of the flow states (a) at different  $Re_w$  and (b) at different Ri in 2-D cases.

wall shear in 2-D cells are shown in figures 4(a) and 4(b), respectively. Generally, with the increase of  $Re_w$ , we can observe enhanced heat transfer efficiency and global flow strength for all three types of wall shear. However, at  $Re_w \leq 200$  for the (1, 2) type wall shear, the flow structure gradually changes from an LSC that spans the whole cell to the vertically stacked double-roll mode, leading to a decreased Nu value (Xu et al. 2020). To clearly visualize the relative changes of Nu and Re after imposing the wall shear, we further plot  $(Nu - Nu_0)/Nu_0$  and  $(Re - Re_0)/Re_0$  as a function of  $Re_w$  in figures 4(c) and 4(d), respectively. Here,  $Nu_0$  and  $Re_0$  are the Nusselt and Reynolds numbers in the absence of wall shear, respectively. Among the three types of wall shear, at the same  $Re_w$ , the (2,1) type wall shear results in the largest magnitude of heat transfer efficiency up to 568%; and the (1, 2) type wall shear results in the smallest one around 179%. The trend is consistent with our expectation that facilitating the horizontally stacked double-roll flow modes is efficient for heat transfer, yet facilitating the vertically stacked double-roll is inefficient for heat transfer (Xu et al. 2020). On the other hand, as  $Re_w$ increases, all three types of wall shear exhibit a similar trend of increasing global flow strength. The results indicate that in even with the same magnitude of flow strength, the heat transfer efficiency of the convection cell still varies significantly under different types of wall shear. In addition, we provide tabulated value of Nusselt and Reynolds numbers for 3-D cases in table 2. We can conclude heat transfer enhancement can also be found in 3-D configurations.

Figure 5 shows the scaling of the global quantities in 2-D cells, such as Nu and Re, on one of the control parameters Ra (for  $10^6 \leqslant Ra \leqslant 10^9$ ), whilst the control parameters  $Re_w$  is fixed as  $Re_w = 100$  and Pr is fixed as Pr = 5.3. We also provide Nu and Rein the canonical RB convection without shear. Previously, Zhang et al. (2017) provided tabulated values of the Nu and Re versus the Ra at Pr = 5.3. Our simulation results on the canonical RB convection are in good agreement with that reported by Zhang et al. (2017). The data shown in figure 5 indicates that in the buoyancy dominated regime (i.e., when Ra is larger at fixed  $Re_w$ ), the increase of Nu and Re gradually approaches the power-law relations of  $Nu \propto Ra^{0.30}$  and  $Re \propto Ra^{0.59}$ , consistent with previous results reported in the canonical RB convection (Ciliberto et al. 1996; van der Poel et al. 2012; Huang & Xia 2016; Zhang et al. 2017; Xu et al. 2021). Overall, the global heat transfer and momentum quantities reveal that the simulated system possesses the key features of turbulent convection in the buoyancy dominated regime. In the shear dominated regime (i.e., when Ra is smaller at fixed  $Re_w$ ), the scaling behavior of Nu and Re with Radeviate significantly from that of the canonical RB convection, suggesting heat transfer and momentum exchange are not solely governed by the boundary layer.

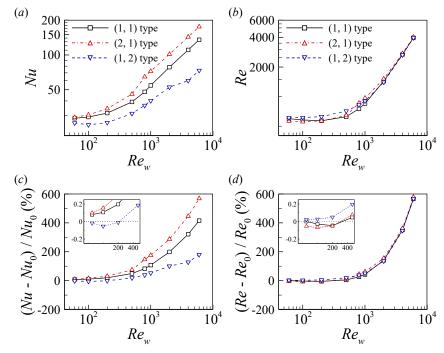


FIGURE 4. (a) Nusselt number, (b) Reynolds number; (c) values of  $Nu/Nu_0 - 1$ , and (d) values of  $Re/Re_0 - 1$  as a function of  $Re_w$  for various types of wall shear in the 2-D cases. Here,  $Nu_0$  and  $Re_0$  are the Nusselt and Reynolds numbers in the absence of wall shear, respectively. The insets magnify  $Re_w$  in the range  $100 \le Re_w \le 500$  shown in (c) and (d), respectively.

Wall shear type	$\Gamma_{\perp}$	$Re_w$	Nu	Re	$(Nu-Nu_0)/Nu_0$	$(Re - Re_0)/Re_0$
-	$\begin{array}{c} 1/8 \\ 1/4 \end{array}$	0	$34.80 \\ 32.38$	258.39 282.32	- -	- -
(1, 1) type	1/8 1/8 1/4 1/4	100 3000 100 3000	35.18 82.44 34.32 86.39	280.65 741.02 357.81 854.66	$\begin{array}{c} 1.1\% \\ 136.9\% \\ 6.0\% \\ 166.8\% \end{array}$	8.6% $186.8%$ $26.7%$ $202.7%$
(2, 1) type	1/8 1/8 1/4 1/4		35.86 112.15 36.05 113.75	273.78 761.90 351.58 910.96	3.0% 222.2% 11.3% 251.3%	6.0% $194.9%$ $24.5%$ $222.7%$
(1, 2) type	1/8 1/8 1/4 1/4	100 3000 100 3000	34.62 68.83 33.16 67.95	265.11 784.14 298.15 935.05	-0.5% $97.8%$ $2.4%$ $109.9%$	2.6% $203.5%$ $5.6%$ $231.2%$

Table 2. Heat transfer efficiency and global flow strength in the 3-D cases. The columns from left to right indicate the following: imposed wall shear type ('-' denotes convection without wall shear), cell aspect ratio ( $\Gamma_{\perp}$ ) in the plane perpendicular to the LSC, wall shear strength ( $Re_w$ ), Nusselt number (Nu), Reynolds number (Re), heat transfer enhancement ( $Nu - Nu_0$ )/ $Nu_0$ , global flow strength enhancement ( $Re - Re_0$ )/ $Re_0$ . Here,  $Nu_0$  and  $Re_0$  are the Nusselt and Reynolds numbers in the absence of wall shear at the same  $\Gamma_{\perp}$ , respectively.

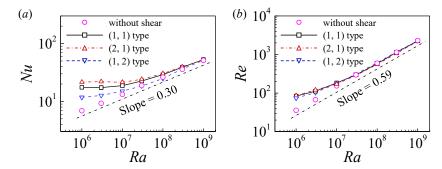


FIGURE 5. (a) Nusselt number, (b) Reynolds number as a function of Rayleigh number for various types of wall shear in the 2-D cases, when the wall shear Reynolds number is fixed as  $Re_w = 100$ .

We further quantitatively investigate the influence of different types of wall shear on the temperature distribution. Figure 6 shows the probability density functions (PDFs) of the normalized temperature  $(T - \mu_T)/\sigma_T$  in the bulk region of the 2-D cell (i.e.,  $0.4L \le x \le 0.6L$  and  $0.4H \le y \le 0.6H$ ), where  $\mu_T$  and  $\sigma_T$  are the mean and standard deviation of the temperature. In the absence of wall shear, the PDFs of temperature in the bulk show a stretched exponential behavior. Under the (1, 1) type wall shear, the temperature in the bulk is well-mixed and the PDFs are symmetric at different  $Re_w$  (see figure 6a). With imposed external wall shear, the PDFs at different  $Re_w$  collapse and they deviate significantly from that in the absence of wall shear. The narrowed PDF tails imply that fewer plumes pass through the bulk region and the temperature fluctuation is suppressed. Under the (2, 1) type wall shear, the PDF is negatively skewed at smaller  $Re_w$  (see figure 6b), which is due to cold plumes descend through the central region. However, as  $Re_w$  increases, the skewness of the temperature PDFs decreases, and their tails become narrower, implying that temperature is better mixed and fewer cold fluids pass through the central region. Under the (1, 2) type wall shear, the PDFs are symmetric (see figure 6c) due to the top-down symmetry of the convection cell, both hot and cold plumes pass through the central region. As the strength of the wall shear increases, the heads of the PDFs gradually exhibit a bi-modal shape (e.g., the inset shown in figure 6c), suggesting the top cold and bottom hot subregions are gradually separated; meanwhile, all the tails of the PDFs exhibit Gaussian shape and their profiles collapse for different  $Re_w$ . The collapse of PDF indicates a similar flow pattern in the bulk region because the functional form of the temperature PDF is determined by the coherence of plumes (Solomon & Gollub 1990; Xia & Lui 1997).

We now investigate how the local heat transfer properties are influenced by different types of wall shear. In figure 7, we show the vertical convective heat flux field  $v \cdot \delta T$ , where the temperature fluctuation is  $\delta T = T - (T_{hot} + T_{cold})/2$ . At small wall shear strength of  $Re_w = 100$  (see figures 7a-c for 2-D cases and 7g-i for 3-D cases), the heat is mainly transported by the moving thermal plumes and the magnitudes of vertical convective heat flux are relatively weak. Under the (1, 1) type wall shear (see figures 7a and 7g), plumes that carry heat mainly go up and down near the sidewalls; under the (2, 1) type wall shear (see figures 7b and 7h), plumes can also penetrate vertically in the bulk region of the cell, thus forming additional convection channels between the cold top wall and the hot bottom wall; under the (1, 2) type wall shear (see figures 7c and 7i), plumes that penetrate the bulk region of the cell exhibit horizontal motion at the mid-height of the cell. At large wall shear strength of  $Re_w = 4000$  (see figures 7d-f for 2-D

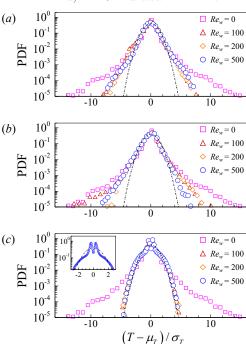


FIGURE 6. The probability density functions (PDFs) of the temperature measured in the bulk region of the 2-D cells (i.e.,  $0.4L \le x \le 0.6L$  and  $0.4H \le y \le 0.6H$ ) under (a) the (1, 1) type wall shear, (b) the (2, 1) type wall shear, (c) the (1, 2) type wall shear, when the flow is in turbulent state. The dotted-dashed line represents a Gaussian distribution. The inset in (c) magnifies the head of the PDF at  $Re_w = 500$ .

cases) and  $Re_w = 3000$  (see figures 7j-l for 3-D cases), the vertical convective heat flux forms much more stable and regular convection channels, and their magnitudes are much stronger. It should be noted that there are small regions of negative convective heat flux immediately adjacent to the regions of large positive convective heat flux, which is known as counter-gradient local heat transport (Gasteuil et al. 2007; Huang & Zhou 2013). The counter-gradient local heat transport essentially describes that both the LSC and the corner flows may contribute to heat transport in the 'wrong' direction: hot (or cold) plumes can be brought back to the hot (or cold) plate by either the corner flows or the LSC. The counter-gradient local heat transport is ubiquitous and can be found in 2D and 3D systems, either turbulent or laminar states. An interesting finding is that under the (1, 2) type wall shear in the 2-D case (see figures 7f), there exists strong negative vertical convective heat flux along the right vertical wall, which is opposite to the temperature gradient of the system. Under the external wall shear, hot (or cold) fluids are forced to form a circulation in the bottom (or top) subregion of the cell. When the hot (or cold) fluids fall (or rise) along the right vertical wall, they do not exchange heat with the other and do not lose their thermal energy at all, thus hot (or cold) fluids are swept back to the hot (or cold) walls and exhibit counter-gradient heat transport behavior. Previously, Blass et al. (2020, 2021) observed that by adding the Couette type shear, the increase of heat transfer efficiency is due to elongated streaks generating vertical crossstream motion. While in our work, adding the (m,n) type wall shear mainly facilitates a more coherent flow structure and forms more stable and stronger convection channels, particularly in the cases of laminar flows when the wall shear strength is strong.

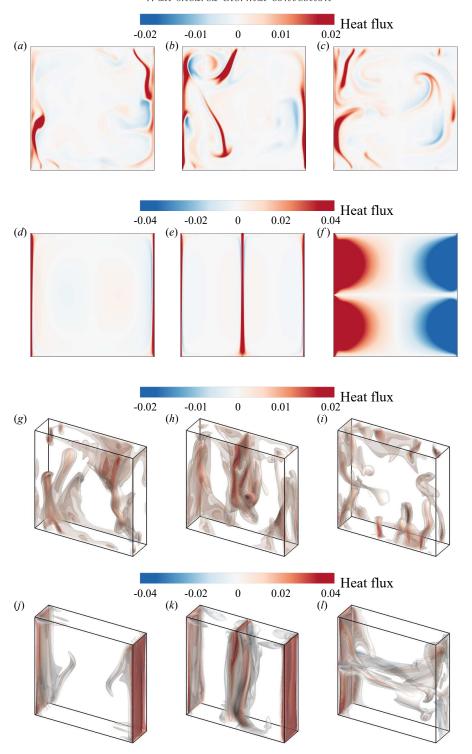


Figure 7. Snapshots of vertical convective heat flux field at (a-c)  $Re_w=100$ , (d-f)  $Re_w=4000$ , (g-i)  $Re_w=100$  and  $\Gamma_\perp=1/4$ , (j-l)  $Re_w=3000$  and  $\Gamma_\perp=1/4$ , under (left column) the  $(1,\ 1)$  type, (middle-column) the  $(2,\ 1)$  type and (right-column) the  $(1,\ 2)$  type wall shear.

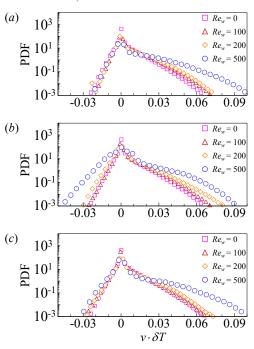


FIGURE 8. The PDFs of the heat flux measured in the whole cells for 2-D cases under (a) the (1, 1) type wall shear, (b) the (2, 1) type wall shear, (c) the (1, 2) type wall shear, when the flow is in turbulent state.

In figure 8, we further plot the PDFs of the vertical convective heat flux  $v \cdot \delta T$  in the whole cell for 2-D cases. All the PDFs have longer positive tails and shorter negative tails, implying strong upward convective heat transfer, yet there exist counter-gradient convective heat transfer (Huang & Zhou 2013). Under the wall shear, the strength of the upward convective heat transfer is enhanced with the increase of wall shear strength in the whole cell; meanwhile, we checked the PDFs of convective heat flux in the bulk region (not shown here for clarity), and found that their shapes are much narrower, implying that heat exchange is weak in the bulk region, and hotter (or colder) fluids tend to flow upward (or downward) along the sidewalls. Such strong counter-gradient convective heat transfer is consistent with our qualitative observation shown in figure 7.

In this work, we designed the (m,n) type wall shear to facilitate the flow structure with m rolls in the x-direction and n rolls in the y-direction. Under the imposed wall shear, to quantitatively evaluate whether the expected flow structure is dominated or not, we perform Fourier mode decomposition on the velocity field. The Fourier mode decomposition is a powerful tool to extract coherent structure in turbulent convection (Petschel et al. 2011; Chandra & Verma 2011, 2013; Chong et al. 2018; Wang et al. 2018). Specifically, the instantaneous velocity field (u, v) is projected onto the Fourier basis  $(\hat{u}^{m,n}, \hat{v}^{m,n})$  as

$$u(x, y, t) = \sum_{m,n} A_x^{m,n}(t) \hat{u}^{m,n}(x, y)$$
(3.1)

$$v(x, y, t) = \sum_{m,n} A_y^{m,n}(t)\hat{v}^{m,n}(x, y)$$
(3.2)

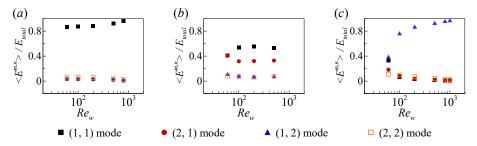


FIGURE 9. Time-averaged energy contained in the first four Fourier modes as functions of  $Re_w$  under (a) the (1, 1) type wall shear, (b) the (2, 1) type wall shear, (c) the (1, 2) type wall shear. Note the Fourier mode decomposition is only applied when the flow is in turbulent state for 2-D cases (refer to the phase diagram of flow states in figure 3).

Here, the Fourier basis  $(\hat{u}^{m,n}, \hat{v}^{m,n})$  is chosen as

$$\hat{u}^{m,n}(x,y) = 2\sin(m\pi x)\cos(n\pi y) \tag{3.3}$$

$$\hat{v}^{m,n}(x,y) = -2\cos(m\pi x)\sin(n\pi y) \tag{3.4}$$

The instantaneous amplitude of the Fourier mode is then calculated as

$$A_x^{m,n}(t) = \langle u(x,y,t), \hat{u}^{m,n}(x,y) \rangle = \sum_i \sum_j u(x_i, y_i, t) \hat{u}^{m,n}(x_i, y_i)$$
 (3.5)

$$A_y^{m,n}(t) = \langle v(x, y, t), \hat{v}^{m,n}(x, y) \rangle = \sum_i \sum_j v(x_i, y_i, t) \hat{v}^{m,n}(x_i, y_i)$$
 (3.6)

where  $\langle u, \hat{u} \rangle$  and  $\langle v, \hat{v} \rangle$  denote the inner product of u and  $\hat{u}$ , v and  $\hat{v}$ , respectively. The energy in each Fourier mode is calculated as  $E^{m,n}(t) = \sqrt{[A_x^{m,n}(t)]^2 + [A_y^{m,n}(t)]^2}$ , the total energy is calculated as  $E_{total} = \sum_{m,n} \langle E^{m,n} \rangle$ , and  $\langle \cdots \rangle$  denotes the time average. In figure 9, we plot the time-averaged energy as functions of  $Re_w$  for various types of wall shear when the flow is in the turbulent state for 2-D cases. Here, we consider m and n=1,2, namely the first four Fourier modes. From figure 9(a) we can see that under the (1, 1) type wall shear, the (1, 1) Fourier mode is indeed dominant. Similarly, under the (1, 2) type wall shear, the (1, 2) Fourier mode is the dominant flow mode (see figure 9c). However, under the (2, 1) type wall shear, despite the energy percentage in the (2, 1)mode being much larger compared to that in the absence of wall shear, the (2, 1) mode does not contain the highest percentage of energy. We can see from figure 9(b) that the (1, 1) Fourier mode contains more energy than the expected (2, 1) mode. To explain the discrepancy, we check the snapshots of the flow fields and the heat flux fields (see figures 2b and 7b) and observe that some hot (or cold) plumes lose their energy before reaching the cold top (or hot bottom) wall. The plumes then fall (or turn back up) to form small rolls, thus substructures emerge inside the left-side big roll (Chen et al. 2019). When the unstable small rolls inside the left-side big roll shrink their size, the Fourier mode decomposition that captures flows in the bulk region implies the (1, 1) mode (i.e., one big roll in the whole cell) prevails.

#### 3.2. Stabilizing thermal turbulence via wall movement

The original objective of imposing the (m, n) type wall shear is to adjust the internal flow mode and control heat transfer properties. While we found that by increasing the wall shear strength, the thermal turbulence is relaminarized, and more surprisingly, the heat transfer efficiency of the convection cell in the laminar state is higher than that in

the turbulent state. In the previous section, we have explained that the enhancement of heat transfer efficiency at the laminar regime is due to the formation of more stable and stronger convection channels. Below, we further discuss the origin of thermal turbulence laminarization. We start by examining the turbulent kinetic energy (TKE) equation of incompressible thermal convection, which is written as

$$\frac{\partial \|}{\partial t} + \overline{u_j} \partial_j \| = -\overline{u_i' u_j'} \partial_j \overline{u_i} 
+ \partial_j \left( -\overline{p' u_j'} + \sqrt{\frac{Pr}{Ra}} \partial_j \| - \frac{1}{2} \overline{u_i' u_i' u_j'} \right) - \sqrt{\frac{Pr}{Ra}} \overline{(\partial_j u_i')^2} + \overline{T'v'}$$
(3.7)

In the above, the subscripts i and j are dummy indices.  $\| = \overline{u_i' u_i'}/2$  denotes the TKE and the superscript (') denotes the fluctuation part of an instantaneous flow variable. The term  $-u'_iu'_i\partial_i\overline{u_i}$  represents shear-produced TKE, and the term  $\overline{T'v'}$  represents buoyancyproduced TKE. Because the flow remains laminar in a smaller range of  $Re_w$  for 3-D cases, we mainly discuss the results for 2-D cases below. In figure 10, we show the shearproduced, the buoyancy-produced, and the total TKE production under the (1, 1) type wall shear as an example. With increasing the wall shear strength, the shear-produced TKE is increasingly concentrated near the top-left and bottom-right corners of the convection cells (see figures 10a and 10d), where rising hot (or falling cold) plumes impact the cold (or hot) boundary layers. Compared to the shear-produced TKE, the buoyancyproduced TKE is more intense (see figures 10b and 10e) and contributes a dominant part of the total TKE production (see figures 10c and 10f); meanwhile, with increasing the wall shear strength, the buoyancy-produced TKE becomes weaker. Previously, in the absence of wall shear, Xia et al. (2003) quantitatively described that the TKE largely comes from the buoyant motions of thermal plumes based on the particle image velocimetry (PIV) results. With the aid of direct numerical simulation,  $\overline{T'v'}$  is directly obtained in the whole convection cell, we now provide direct evidence that thermal plumes are mainly responsible for the TKE production.

After analyzing the TKE production, we now turn to the TKE dissipation. In figures 11(a) and 11(b), we show the TKE dissipation under the (1, 1) type wall shear as an example. We can see that intense TKE dissipation occurs in the top-right and bottomleft corners, namely, in the regions of plumes detachment. Meanwhile, with increasing the wall shear strength, the TKE dissipation becomes weaker. It should be noted that here we considered the dissipation term of  $\sqrt{Pr/Ra}(\partial_j u_i')^2$  in the TKE equation, which is known as pseudo-dissipation by Pope (2000). Previously, Zhang et al. (2017) and Bhattacharya et al. (2018) analyzed the statistics of TKE dissipation in terms of  $\frac{1}{2}\sqrt{Pr/Ra}(\partial_j u_i' + \partial_i u_j')^2$  in the canonical RB convection without wall shear. We checked that the numerical differences between  $\sqrt{Pr/Ra}(\partial_j u_i')^2$  and  $\frac{1}{2}\sqrt{Pr/Ra}(\partial_j u_i' + \partial_i u_i')^2$ are indeed very small. We then plot the volume-averaged TKE and the volume-averaged TKE dissipation as functions of  $Re_w$  for various types of wall shear in figures 11(c) and 11(d). With the increase of wall shear strength, the volume-averaged TKE is indeed decreasing, eventually, the TKE vanishes, and the thermal turbulence is relaminarized. However, the decreased TKE and the corresponding thermal turbulence laminarization are not caused by the viscous dissipation, which is evident from figure 10(d) that the volume-averaged TKE dissipation is also decreasing.

The above analysis suggests that the plume plays a key role in thermal turbulence production and dissipation. To identify the mechanism responsible for the thermal turbulence laminarization, we then analyze the spatial and temporal distributions of plumes. In figures 12(a-c), we show the typical snapshots of instantaneous plume field under the

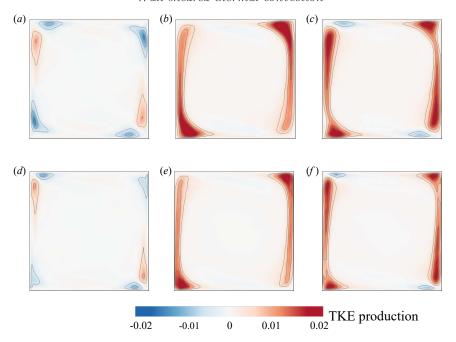


FIGURE 10. (a,d) The shear-produced turbulent kinetic energy (TKE), (b,e) the buoyancy-produced TKE, and (c,f) the total TKE production, under the (1, 1) type wall shear for (a-c)  $Re_w = 200$ , (d-f)  $Re_w = 500$ .

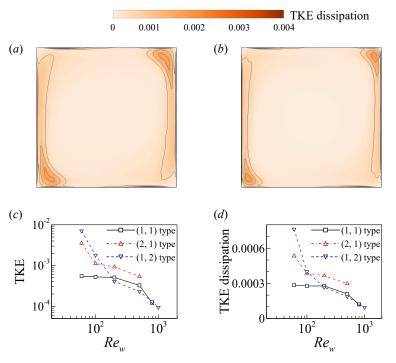


FIGURE 11. The TKE dissipation for (a)  $Re_w = 200$  and (b)  $Re_w = 500$  under the (1, 1) type wall shear; (c) the volume-averaged TKE, and (d) the volume-averaged TKE dissipation as functions of  $Re_w$  for various types of wall shear.

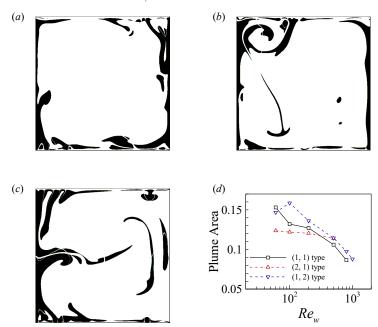


FIGURE 12. Typical snapshots of plume field at  $Re_w = 100$  for (a) the (1, 1) type wall shear, (b) the (2, 1) type wall shear, (c) the (1, 2) type wall shear. (d) Time-averaged plume area in the cell as functions of  $Re_w$  under three types of wall shear.

three types of wall shear. Here, the criteria to quantitatively identify thermal plumes are similar to those used in (Huang *et al.* 2013; van der Poel *et al.* 2015; Zhang *et al.* 2017), which is

$$|T(\mathbf{x},t) - \langle T(\mathbf{x}) \rangle| > c \langle T_{rms}(\mathbf{x}) \rangle, \quad \sqrt{Pr \cdot Ra} |v(\mathbf{x},t)T(\mathbf{x},t)| > cNu$$
 (3.8)

Here, c is an empirical constant and its value can be chosen as  $0.8 \le c \le 1.2$ , and we adopt the value of c=1. This criterion assumes that plumes occur in regions of local temperature maximum (or minimum), as well as regions where local convective heat flux is larger than the spatial and temporal averaged one. We can see from figures 12(a-c), this empirical criterion can extract the plume structures reasonably well in the sheared convection. We also calculate the time-averaged plume area in the cell and plot the plume areas as functions of  $Re_w$ . From figure 12(d), we can see that with the increase of wall shear strength, plume areas generally decrease under all three types of wall shear. Because thermal plumes are mainly responsible for TKE production, a reduced number of plumes indicates reduced TKE production.

We then examine the flow field during the laminarization process, as shown in figure 13, and the corresponding video can be viewed in the supplementary movie 2. Initially, an instantaneous flow field obtained at  $Re_w = 200$  for the 2-D case and  $Re_w = 100$  for the 3-D case (i.e., the turbulent state) is used to start the simulation, in which the shear effects are relatively weak and the flow is buoyancy dominated. We can see plumes self-organize into the LSC, and large magnitudes of velocity vectors appear near the region where plumes erupt (see figure 13a for the 2-D case). When the wall shear strength increases to  $Re_w = 2000$  for the 2-D case, the plumes have less chance to detach from the boundary layers near the top and bottom walls, and they will be swept along the walls (see figure 13b). Because the organization of plume motions leads to the LSC in the turbulent RB

convection cell (Xi et al. 2004), suppressing plume detachment will weaken the LSC. In addition, hot (or cold) plumes are forced to sweep to the cold top (or hot bottom) wall (see figures 13c and 13d) and thermal plumes exchange heat near the walls, while the temperature in the bulk region of the cell is more uniform and well-mixed (see figure 13e). Eventually, one regular big roll is formed, and hot and cold fluids flow along the wall, which is completely influenced by the external wall shear (see figure 13f). We can also see from figures 13(g-l) that, the turbulence relaminarization process in similar for both 2-D and 3-D cases; however, it is noteworthy that due to prominent shear instability effects in 3-D, the turbulence relaminarization is rare and occurs in a smaller range of wall shear Reynolds number for 3-D cases.

#### 3.3. Expenditure of mechanical energy due to external wall shear

We manipulated the internal flow modes via imposing external wall shear, and the corresponding heat transfer efficiency enhancement requires the expenditure of mechanical energy. To evaluate whether such mechanical energy expenditure is worthy or not, we calculate the ratio between the enhanced heat flux  $\delta Q$  (which is further normalized by heat flux  $Q_0$  in the absence of wall shear) and the required mechanical energy  $W_s$  due to wall shear (which is further normalized by energy dissipation due to viscosity  $W_0$  in the absence of wall shear) as

$$\eta = \frac{\delta Q/Q_0}{W_s/W_0} \tag{3.9}$$

Here,  $\delta Q = Q_{\mathbf{u}_w} - Q_0$ . Generally, the heat flux  $Q_{\mathbf{u}_w}$  is calculated as

$$Q_{\mathbf{u}_w} = \left\langle \int_0^L \left( -\kappa \frac{\partial T}{\partial \mathbf{n}} \right) dx \right\rangle_t \tag{3.10}$$

In the above,  $\kappa$  denotes thermal conductivity of the fluids, and  $\langle \cdots \rangle_t$  denotes the time average. To impose the wall shear, an additional external mechanical energy  $W_s$  is required, which is calculated as

$$W_s = \left\langle \oint_{\mathbf{l}} \left| \mu \frac{d\mathbf{u}_w}{d\mathbf{n}} \cdot \mathbf{u}_w \right| d\mathbf{l} \right\rangle_t \tag{3.11}$$

Here, the integration  $\oint_{\mathbf{l}}(\cdots)$  is performed along all the shear wall. In the absence of wall shear, the energy dissipation due to viscosity in the convection cell is

$$W_0 = \left\langle \int_V \frac{\mu}{2} \sum_{i,j} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) dV \right\rangle_t$$
 (3.12)

The ratio between enhanced heat flux and imposed mechanical energy can be regarded as a metric that describes the efficiency of facilitating heat transport via external shearing. From figure 14, we can see that for the (1, 1) and (2, 1) types of wall shear, the efficiency  $\eta$  decreases monotonously with the increase of  $Re_w$ . Recall that from figures 4(a) and 4(c), we found the Nu increases monotonously with the increase of  $Re_w$ , thus the enhanced Nu requires a larger expenditure of mechanical energy at a larger  $Re_w$ . For the (1, 2) type wall shear, the efficiency  $\eta$  is negative at  $Re_w \leq 200$ , because the Nu is weakened in that range, as shown in figures 4(a) and 4(c); at larger  $Re_w$ , the efficiency  $\eta$  is positive, yet it does not exhibit monotonous behavior with the increase of  $Re_w$ . Among the three types of wall shear, the (2, 1) type results in the highest efficiency  $\eta$ , because the flow is more coherent in the corresponding (2, 1) flow mode. At the largest  $Re_w$ , all three types of wall shear exhibit very small values of efficiency  $\eta$ , implying heat transfer enhancement

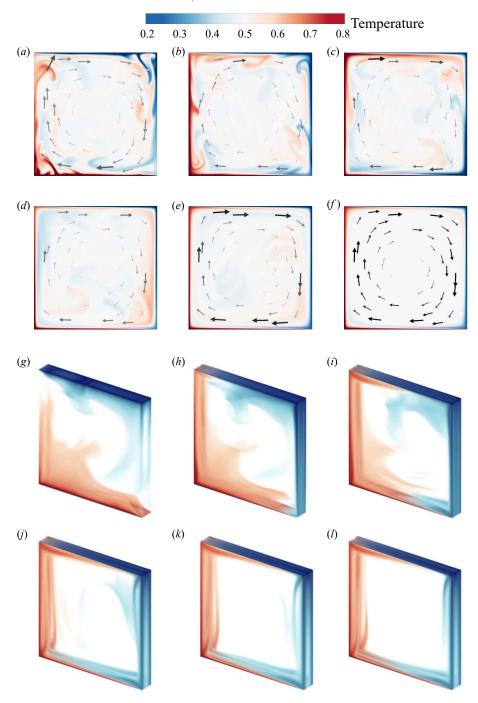


FIGURE 13. Turbulence relaminarization process: time evolution of instantaneous flow fields (temperature contours and velocity vectors in 2-D, volume rendering of temperature field in 3-D). (a-f) Snapshots for the the 2-D case at t=0, 2, 4, 8, 22 and 354  $t_f$ , respectively, with wall shear strength  $Re_w=2000$ . (g-l) Snapshots for the 3-D case at t=0, 2, 4, 8, 11 and 158  $t_f$ , respectively, with  $Re_w=3000$ . Initially, an instantaneous flow field obtained at  $Re_w=200$  for the 2-D case and  $Re_w=100$  for the 3-D case, is used to start the simulation, respectively.

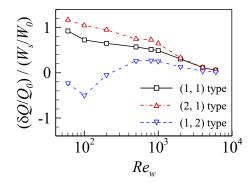


FIGURE 14. The ratio between enhanced heat flux and imposed mechanical energy as a function of shear Reynolds number for various types of wall shear in the 2-D cases.

comes at a very high price. We deduce that further increase the wall shear strength, the efficiency  $\eta$  would approach the limit of zero (but non-negative) value because the heat transfer increases monotonously at large  $Re_w$ .

#### 4. Conclusions

In this work, we have performed direct numerical simulations of thermal convection under three different (m, n) types of wall shear. The (m, n) type wall shear is imposed to facilitate m rolls in the horizontal direction and n rolls in the vertical direction. Under the (1, 1) type, the (2, 1) type, and the (1, 2) type wall shear, we can observe the single-roll, the horizontally stacked double-roll, and the vertically stacked double-roll flow modes, respectively, are generally prevail flow modes in the convection cell. With the increase of  $Re_w$ , we generally found enhanced heat transfer efficiency and global flow strength for all three types of wall shear. However, even with the same magnitude of flow strength, the heat transfer efficiency of the convection cell varies significantly under different types of wall shear. Specifically, the (2, 1) type wall shear results in the largest magnitude of heat transfer efficiency, and the (1, 2) type wall shear results in the smallest one, which is consistent with our expectation that facilitating the horizontally stacked double-roll flow modes is efficient for heat transfer, yet facilitating the vertically stacked double-roll is inefficient for heat transfer.

The original objective of imposing the wall shear was to manipulate flow mode to control heat transfer efficiency. While it is found that by increasing the wall shear strength, the thermal turbulence is relaminarized, and more surprisingly, the heat transfer efficiency of the convection in the laminar state is higher than that in the turbulent state. By examining the flow field and the convective heat flux field, we found the enhancement of heat transfer efficiency at the laminar regime is due to the formation of more stable and stronger convection channels.

We explained the origin of thermal turbulence laminarization in the sheared convection cell. Analysis of the shear-produced TKE (i.e.,  $-\overline{u_i'u_j'}\partial_j\overline{u_i}$ ) and the buoyancy-produced TKE (i.e.,  $\overline{T'v'}$ ) provide direct evidence that thermal plumes are mainly responsible for the TKE production. We then quantitatively measure the changes in plume areas under the wall shear and found that plumes are swept away by the wall shear once they are detached from the top cold and bottom hot walls, and such a reduced number of thermal plumes decreases the TKE production in the bulk cell.

We evaluated whether the mechanical energy expenditure by wall shear is worthy or

not. We used the ratio between the enhanced heat flux and the required mechanical energy to quantify the efficiency of facilitating heat transport via external shearing. We found that at a larger  $Re_w$ , although the heat transfer efficiency increases, it comes at a price of a larger expenditure of mechanical energy.

Finally, we emphasize that in turbulent wall-sheared thermal convection, the heat transfer may not always monotonically increase with increasing shear. For example, in the RB system with a Couette-type wall shear, Blass et al. (2020, 2021) found with increasing wall shear, the heat transfer first decreases (due to the breakup of the thermal convection rolls) and then increases. In our study, the heat transfer enhancement is a consequence of the moving adiabatic side walls advecting fluid in the vertical direction, thus facilitating the formation of stable and strong convection channels between the top cold wall and the bottom hot wall.

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#### 6. Declaration of interests

The authors report no conflict of interest.

## 7. Supplementary movies

Supplementary movies are available at https://doi.org/10.1017/jfm.xxxxxx.

# 8. Appendix A. Flow and heat transfer patterns in the canonical RB convection

In figure 15, we show the typical instantaneous temperature and flow fields, as well as vertical convective heat flux field for the canonical RB convection in the absence of wall shear. In the 2-D case, we can see that there exists a well-defined LSC, together with counter-rotating corner rolls (figure 15a). The LSC is in the form of a tilted ellipse, sitting along a diagonal of the flow cell with two secondary corner vortices that exist along the other diagonal. Strong positive heat flux occurs in regions of rising hot (or falling cold) plumes (see figure 15d). In the 3-D case, the very confined cell with  $\Gamma_{\perp} = 1/8$  exhibits similar flow and heat transfer pattern to that of the 2-D case, with persistent LSC [see figures 15b and 15e]. When the cell aspect ratio  $\Gamma_{\perp}$  increases to 1/4, the LSC is less stable and its shape becomes distorted [see figures 15c and 15f].

# 9. Appendix B. Determination of flow states via time recordings and its power spectrum density

In figure 16, we give examples of temperature series at the location of (0.25, 0.5) in the 2-D convection cell under (1, 1) type wall shear. We also show the power spectrum density (PSD) of the corresponding temperature series. At  $Re_w = 100$  and 500, the temperature fluctuates randomly around 0.5 [see figure 16(a) and 16(c)], and the corresponding PSD [see figure 16(b) and 16(d)] exhibit continuous spectra; thus, we determine the flow states as the turbulent state. At  $Re_w = 1000$ , the fluctuation of the temperature series is within a smaller range [see figure 16(e) and its inset], and the corresponding PSD

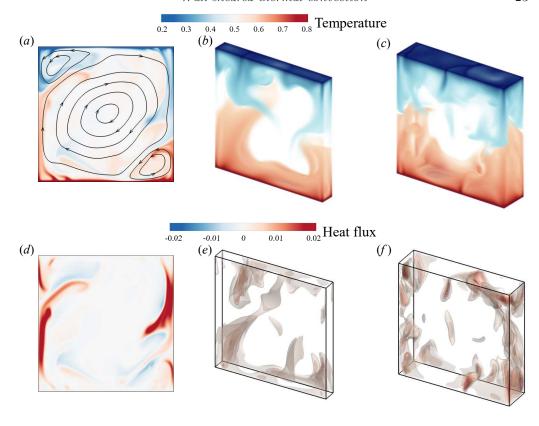


FIGURE 15. Typical instantaneous (a-c) temperature field and (d-f) vertical convective heat flux field for the canonical RB convection at  $Ra=10^8$  and Pr=5.3: (a,d) 2-D case, (b,e) 3-D case at  $\Gamma_{\perp}=1/8$ , (c,f) 3-D case at  $\Gamma_{\perp}=1/4$ .

exhibits characteristic peaks, suggesting the flow is quasi-periodic; thus, we determine the flow states as the laminar state. At  $Re_w = 4000$ , the temperature series gradually approaches a steady value of 0.5 [see figure 16(f)], thus, we also determine the flow states as the laminar state.

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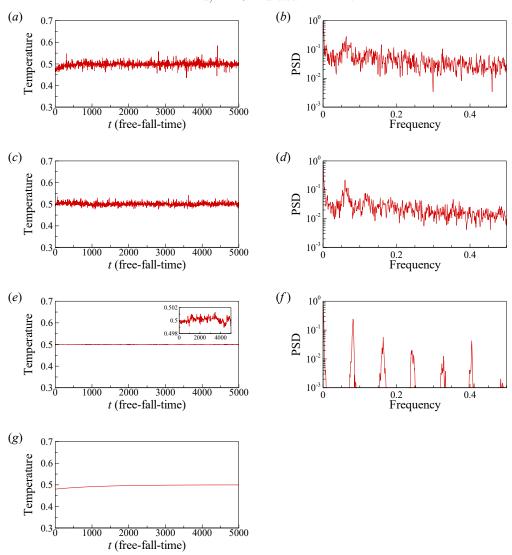


FIGURE 16. (Left-column) Temperature series at the location of (0.25, 0.5) in the 2-D convection cell under (1, 1) type wall shear, and (right-column) the power spectrum density (PSD) of the corresponding temperature series, at (a, b)  $Re_w = 100$ , (c, d)  $Re_w = 500$ , (e, f)  $Re_w = 1000$ , (g)  $Re_w = 4000$ . Note for the temperature series shown in (g), it eventually approaches a steady value, thus we did not calculate the corresponding PSD.

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