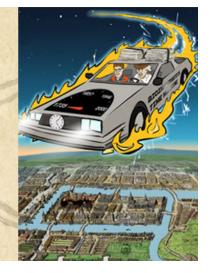


BIOINFORMATICS ALGORITHMS



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Chapter 9: How Do We Locate Disease-Causing Mutations?

(Coursera Week 1)

Does amalgamation of the reference human genome from various individuals cause problems? Can't such amalgamation produce a phenotype that does not occur naturally?

Yes, the reference human genome is a mosaic of various genomes that does not match the genome of any individual human. Since various human genomes differ by only 0.1%, however, the amalgamation does not cause significant problems.

How does the repeated triplet "CAG" affect the severity of Huntington's disease?

Huntington's disease is a rare genetic disease in that it is attributable to a single gene, called *Huntingtin*. This gene includes a trinucleotide repeat "...cagcagcag..." that varies in length. Individuals with fewer than 26 copies of "cag" in their *Huntingtin* gene are classified as unaffected by Huntington's disease, whereas individuals with more than 35 copies carry a large risk of the disease, and individuals with more than 40 copies will be afflicted. Moreover, an unaffected person can pass the disease to a child if the normal gene mutates and increases the repeat length. The reason why many repeated copies of "cag" in *Huntingtin* leads to disease is that this gene produces a protein with many copies of glutamine ("cag" codes for glutamine), which increases the decay rate of neurons.

Would it be better to use multiple reference genomes instead of a single reference genome?

Perhaps in theory, but in practice, biologists still use one reference genome, since comparison against thousands of reference genomes would be time-consuming.

What is the point of appending the "\$" sign to Text when we construct SuffixTrie(Text)?

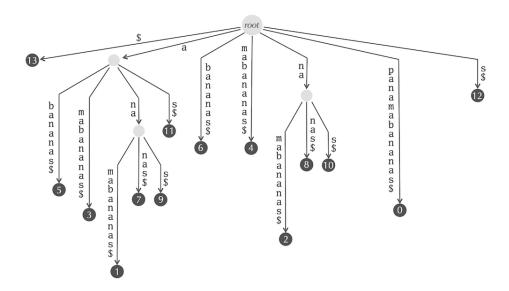
Construct the suffix trie for "papa" and you will see why we have added the "\$" sign – without the "\$" sign, the suffix "pa" will become a part of the path spelled by the suffix "papa".

Why do we need an edge from the root to the leaf in the suffix tree (labeled by the "\$" sign) if this edge is never traversed during pattern matching? Although we indeed do not need this edge, it is included to simplify the description of the suffix tree.

What are the edge labels in the suffix tree for "panamabananas\$"?

The suffix tree for "panamabananas\$" reproduced below contains 17 edges with the following labels (note that different edges may have the same labels):

\$ a bananas\$ mabananas\$ na mabananas\$ s\$ s\$ bananas\$ mabananas\$ na mabananas\$ na mabananas\$ panamabananas\$ s\$



How does storing SuffixTree(Text) require memory on the order of 20·IText| if the number of nodes in the suffix tree does not exceed 2·IText|?

In addition to storing the nodes and edges of the suffix tree, we also need to store the information at the edge labels. Storing this information takes most of the memory allocated for the suffix tree.

How can I construct a suffix tree in linear time?

Suffix trees were introduced by Weiner, 1973. However, the original linear-time algorithm for building the suffix tree was extremely complex. Although the Weiner algorithm was greatly simplified by Esko Ukkonen in 1995, it is still non-trivial. Check out this excellent StackOverflow post by Johannes Goller if you are interested in seeing a full explanation.

Why does the suffix tree for the 3-billion nucleotide human require about 60 GB of memory?

A suffix tree for a string Text has |Text|+1 leaves and up to |Text| other nodes. The last figure in "Charging Station: Constructing a Suffix Tree" illustrates that we need to store two (rather large) numbers for each edge of the suffix tree, each requiring at least 4 bytes for the approximately 3 billion nucleotide human genome. Thus, since there are approximately $2 \cdot |Text|$ edges in the suffix tree of Text, the suffix tree for the human genome requires at least $3 \cdot 10^9 \cdot 2 \cdot (4+4) = 48$ GB. And we have not even taken into account some other things that need to be stored, such as the human genome itself:)

Can I see an example of how PatternMatchingWithSuffixArray works?

We illustrate how **PatternMatchingWithSuffixArray** matches "ana" against the suffix array of "panamabananas\$", reproduced below from the main text (the suffix array is the column on the left).

Starting Positions	Sorted Suffixes
13	\$
5	abananas\$
3	amabananas\$
1	anamabananas\$
7	ananas\$
9	anas\$
11	as\$
6	bananas\$
4	mabananas\$
2	namabananas\$
8	nanas\$
10	nas\$
0	panamabananas\$
12	s\$

- It first initializes minIndex = 0 and maxIndex = |Text| = 13 and computes $midIndex = \lfloor (0+13)/2 \rfloor = 6$. It then compares Pattern with the suffix "as\$" of Text starting at position SuffixArray(6). Since "ana" < "as\$", it assigns maxIndex = midIndex 1 = 5 and computes $midIndex = \lfloor (0+5)/2 \rfloor = 2$.
- Since "ana" is larger than suffix "amabananas\$" of *Text* starting at position *SuffixArray*(2), it assigns *minIndex midIndex* + 1 = 3 and computes $midIndex = \frac{1}{3}(3+5)/2 = 4$.
- Since "ana" is smaller than the suffix "ananas\$" of *Text* starting at position SuffixArray(4), it assigns maxIndex = midIndex 1 = 3 and computes midIndex = |(3+3)/2| = 3.
- Since "ana" is smaller than the suffix "ananas\$" of *Text* starting at position *SuffixArray*(4), it assigns maxIndex = midIndex 1 = 3 and computes $midIndex = \lfloor (3+3)/2 \rfloor = 3$.
- Since "ana" is smaller than the suffix "anamabananas\$" of Text starting at position SuffixArray(3), it assigns maxIndex = midIndex 1 = 2.

The last assignment breaks the first while loop since maxIndex is now smaller than minIndex. As a result, after the first while loop ends, we have maxIndex = 2, minIndex = 3, and

- suffix of *Text* starting at position *SuffixArray*(2) = "amabananas\$" < "ana"
- suffix of *Text* starting at position *SuffixArray*(3) = "anamabananas\$" > "ana"

Therefore, the first index of the suffix array corresponding to a suffix beginning with "ana" is first = 3.

The second while loop finds the last index of the suffix array corresponding to a suffix beginning with "ana".

- PatternMatchingWithSuffixArray first sets minIndex = first = 3, maxIndex = |Text| = 13, and computes $midIndex = \lfloor (minIndex + maxIndex)/2 \rfloor = \lfloor (3+13)/2 \rfloor = 8$.
- Since "ana" does not match the suffix "mabananas\$" of *Text* starting at position *SuffixArray*(8), it assigns *maxIndex* = *midIndex* 1 = 7 and computes *midIndex* = | (3+7)/2 | = 5.
- Since "ana" matches the suffix "anas\$" of *Text* starting at position SuffixArray(5), it assigns minIndex = midIndex + 1 = 6 and computes $midIndex = \lfloor (6+7)/2 \rfloor = 6$.
- Since "ana" does not match the suffix "as\$" of Text starting at position SuffixArray(6), it assigns maxIndex = midIndex 1 = 5.

The last assignment breaks the second while loop and assigs last = maxIndex = 5 as the last index of the suffix array corresponding to a suffix beginning with "ana".

Why does the suffix array for the 3-billion nucleotide human require 12 GB of memory? Is about 3 GB not sufficient?

The suffix array for the human genome indeed has about 3 billion elements. However, since each element represents one of $3 \cdot 10^9$ positions in the human genome, we need 4 bytes to store each element.

(Coursera Week 2)

Is it possible to construct the Burrows-Wheeler Transform in linear time?

Our naive approach to constructing BWT(Text) requires constructing the matrix M(Text) of all cyclic rotations, which requires O(Text) time and space. However, there exist algorithms constructing BWT(Text) in linear time. One such algorithm first constructs the suffix array of Text in linear time and then uses this suffix array to construct BWT(Text).

What is special about the final column of the Burrows-Wheeler matrix? Why not work with some other column?

In short, the last column is the only invertible column of the Burrows-Wheeler matrix. In other words, it is the only column from which we are always able to reconstruct the original string *Text*.

For example, strings 001 and 100 have identical third columns in the Burrows-Wheeler matrix, as shown below.

\$001	\$100
001\$	0\$10
01\$0	00\$1
1\$00	100\$

Doesn't the Last-to-First mapping require a lot of memory?

In practice, it is possible to compute the Last-to-First mapping of a given position of BWT(*Text*) with very low runtime and memory using the array holding the first occurrence of each symbol in the sorted string. Unfortunately, the analysis is beyond the scope of this class. For details, please see Ferragina and Manzini, 2000 (click here for full text).

Why does FirstColumn appear among the arguments in **BWMatching** if it is never used in the **BWMatching** pseudocode?

We indeed do not use *FirstColumn* in **BWMatching**. Although it seemingly does not make sense, we prefer this because we use *FirstColumn* in a modification of of **BWMatching** in a later section.

How does the array FirstOccurrence reduce memory if we still need the larger array FirstColumn to construct FirstOccurrence in the first place?

When we use *FirstColumn* to construct *FirstOccurrence*, we can immediately release the memory taken by *FirstColumn*. Furthermore, there is an alternative way to construct *FirstOccurrence* without using *FirstColumn*.

Why do the first and last occurrences of *symbol* in the range of positions from *top* to *bottom* in *LastColumn* have respective ranks *Count*_{symbol}(*top*, *LastColumn*)+1 and *Count*_{symbol}(*bottom*+1, *LastColumn*)?

Given an index *ind* in the array *LastColumn* (varying from 0 to 13 in the example shown in the text), the number of occurrences of *symbol* before position *ind* (i.e., in positions with indices less than *ind*) is defined by *Count*_{symbol}(*ind*, *LastColumn*). Since the number of occurrences of *symbol* starting before position *ind* is equal to *Count*_{symbol}(*ind*, *LastColumn*), the rank of the first occurrence of *symbol* starting from position *ind* is

 $Count_{symbol}(ind, LastColumn) + 1$

To be more precise, it is $Count_{symbol}(ind, LastColumn) + 1$ if symbol occurs in LastColumn at or after position ind.

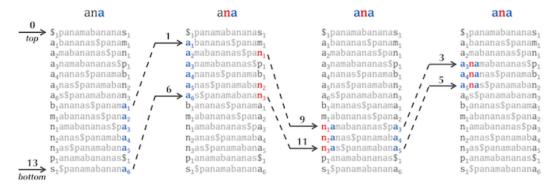
Similarly, the rank of the last occurrence of symbol starting before or at position *ind* is given by

 $Count_{symbol}(ind + 1, LastColumn)$

For example, when ind = 5, the rank of the first occurrence of "n" starting at position 5 is $Count_{"n"}(5, LastColumn) + 1 = 1 + 1 = 2$. On the other hand, the rank of the last occurrence of "p" starting before or at position ind is $Count_{"p"}(6, LastColumn) = 1$.

Would it be possible to match a pattern using the Burrows-Wheeler Transform by moving forward through the pattern instead of moving backward?

Let's match "nam" against *BWT*("panamabananas\$"), but instead of matching backward (like in the figure below, reproduced from the text), let's try to match it forward. We can easily find the three occurrences of "n" in the first column to start this matching, but afterwards we need to match the next symbol "a" in "nam". However, this symbol is "hiding" in the second column, and we have no clue what is in the second column - the Burrows Wheeler Transform does not reveal this information! And there is no equivalent of the "First-Last Property" for the second column to help us.



Is **BetterBWMatching** guaranteed to terminate?

The condition " $top \le bottom$ " is a **loop invariant**, or a property that holds before and after each iteration of the loop. In this case, if pattern matches have been found, the number of matches is equal to bottom - top + 1. If pattern matches are not found, then at some point in the loop, bottom becomes equal to top - 1, in which case $top \le bottom$ and the loop terminates.

Would **BetterBWMatching** work properly if *Pattern* contains symbols that do not appear in *Text*?

No; however, you can easily modify **BetterBWMatching** by first checking whether *Pattern* contains symbols not present in *Text* and immediately returning 0 in this case.

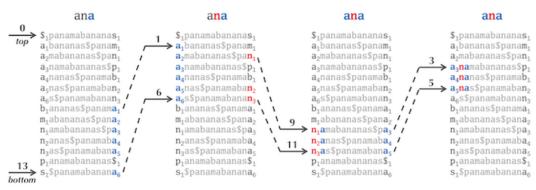
In the main text, you illustrated walking backward in **BetterBWMatching** with the pattern "ana", which is a palindrome. How can we match a non-palindromic pattern?

Try "walking backwards" to find the one pattern match of "ban" in "panamabananas\$".

(Coursera Week 3)

How do we select the constant *K* for constructing the partial suffix array?

Selecting a large value of K reduces the memory allocated to the partial suffix array by a factor of K but increases the time needed to "walk backward" during the pattern matching process (see the figure below, reproduced from the main text). This backward walk may take up to K-1 steps ((K-1)/2 steps on average). Thus, it makes sense to select the minimum value of K that allows fitting the BWT pattern matching code into the memory on your machine.



It seems as though the partial suffix array will require using the *LastToFirst* mapping. But we got rid of the *LastToFirst* mapping in order to speed up pattern matching and save memory! Why do we do this?

We indeed got rid of the LastToFirst array; however, in the same section we saw how the Count arrays can be used as a substitute for LastToFirst.

What modifications of **BetterBWMatching** are needed to make it work with checkpoint arrays instead of count arrays?

To explain how to modify **BetterBWMatching** for working with checkpoint arrays, we explain how to quickly compute each value in the count array given the checkpoint arrays and *LastColumn*.

To compute $Count_{symbol}(i, LastColumn)$, we represent i as $t \cdot K + j$, where j < K. We can then compute $Count_{symbol}(i, LastColumn)$ as $Count_{symbol}(t \cdot K, LastColumn)$ (contained in the checkpoint arrays) plus the number of occurrences of symbol in positions $t \cdot K + 1$ to i in LastColumn.

How do biologists determine the maximum allowable number of mismatches while mapping reads to the human genome?

Biologists usually set a small threshold for the maximum number of mismatches, since otherwise read mapping becomes too slow.

Can reads that "fall off the edges of the text" form approximate matches?

For example, does Pattern = "TTACTG" match Text = "ACTGCTGCTG" with d = 2 mismatches? Not according to the statement of the Multiple Approximate Pattern Matching Problem, since there is no *starting position* in Text where Pattern appears as a substring with at most d mismatches. However, if you want to count approximate matches falling off the edges of Text, you can simply add short strings formed by "\$" signs before the start and after the end of Text.

What is the running time of approximate pattern matching using the Burrows Wheeler Transform?

Unfortunately, the running time scales roughly as A^k , where A is the alphabet size and k is the number of mismatches. This is why the existing read matching tools based on the Burrows Wheeler Transform become prohibitively slow when the number of mismatches increases. For more details, see N. Zhang, A. Mukherjee, D.Adjeroh, T. Bell. "Approximate Pattern Matching using the Burrows-Wheeler Transform." Data Compression Conference, 2003, 458.

How does BLAST extend the seeds that it identifies? Does it not require constructing an optimal alignment, thus significantly slowing down the algorithm?

BLAST does construct an alignment in a narrow band starting from each end of the seed. However, since the band is narrow, the algorithm for constructing this alignment is fast.

How can I modify the approximate pattern matching with the Burrows-Wheeler transform to account for patterns whose last symbols do not appear in Text?

The algorithm illustrated in the epilogue would fail to find an approximate match of "nad" because the final symbol of "nad" does not appear in "panamabananas\$". To address this complication, we can modify the algorithm for finding a pattern of length m with up to k mismatches as follows.

We first run the algorithm described in the main text to find all approximate instances of a *Pattern* of length k against Text. However, this algorithm does not actually find all approximate matches of Pattern – since we do not allow mismatched strings in the early stages of **BetterBWMatching**, we miss those matches where the last letter of Pattern does not match Text. To fix this shortcoming, we can simply find all locations in Text where the prefix of Text and Text where the last two letters of Text where the last two letters of Text where the last two letters of Text where the prefix of Text of length Text of length Text where the prefix of Text of length Text where the prefix of Text of length Te

When we approximately match patterns with the Burrows-Wheeler transform, we consider possibilities of mismatches in all positions but the first one. Wouldn't this strategy fail to match a read with an error at the first position?

Yes, this strategy would fail to match a read with an error at the first position. However, as noted in the main text, if we start considering mismatches at the first position, the running time will significantly increase. As is, the running time explodes with the increase in the maximum number of errors. If one wants to allow mismatches at the first position, a more sensible strategy would be to trim the first position of the read.

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