

# Binary Search Trees: Introduction

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Data Structures  
Data Structures and Algorithms

# Learning Objectives

- Provide examples of the sorts of problems we hope to solve with Binary Search Trees.
- Show why data structures that we have already covered are insufficient.

# Outline

1 Local Search

2 Attempts

# Dictionary Search

Find all words that start with some given string.



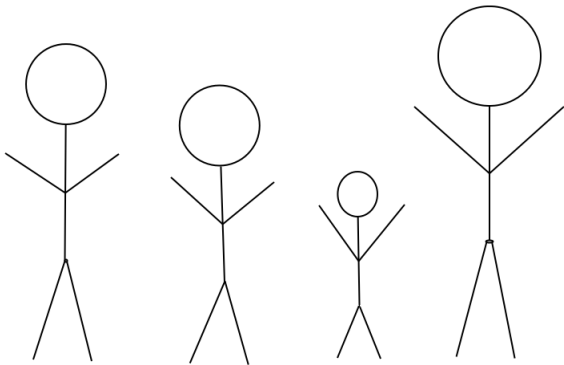
# Date Ranges

Find all emails received in a given period.

Inbox				
FROM	KNOW	TO	SUBJECT	SENT TIME ▾
"lawiki.i2p admin" <J5uF>		Bote User <uhOd>	hi	Unknown
anonymous		Bote User <uhOd>	Sanders 2016	Aug 30, 2015 3:27 PM
anonymous		Bote User <uhOd>	I2PCon 2016	Aug 30, 2015 3:25 PM
Anon Developer <gvbM>		Bote User <uhOd>	Re: Bote changess	Aug 30, 2015 2:54 PM
I2P User <uUUX>		Bote User <uhOd>	Hello World!	Aug 30, 2015 2:51 PM

# Closest Height

Find the person in your class whose height is closest to yours.



# Local Search

## Definition

A **Local Search Datastructure** stores a number of elements each with a **key** coming from an ordered set. It supports operations:

- **RangeSearch( $x, y$ )**: Returns all elements with keys between  $x$  and  $y$ .
- **NearestNeighbors( $z$ )**: Returns the element with keys on either side of  $z$ .

## Example

1	4	6	7	10	13	15
---	---	---	---	----	----	----



## Example

1	4	6	7	10	13	15
---	---	---	---	----	----	----

RangeSearch(5, 12)

1	4	6	7	10	13	15
---	---	---	---	----	----	----

## Example

1	4	6	7	10	13	15
---	---	---	---	----	----	----

RangeSearch(5, 12)

1	4	6	7	10	13	15
---	---	---	---	----	----	----

NearestNeighbors(3)

1	4	6	7	10	13	15
---	---	---	---	----	----	----

# Dynamic Data Structure

We would also like to be able to modify the data structure as we go.

- `Insert( $x$ )`: Adds a element with key  $x$ .
- `Delete( $x$ )`: Removes the element with key  $x$ .

## Example

1	4	6	7	10	13	15
---	---	---	---	----	----	----

## Example

1	4	6	7	10	13	15
---	---	---	---	----	----	----

Insert(3)

1	3	4	6	7	10	13	15
---	---	---	---	---	----	----	----

## Example

1	4	6	7	10	13	15
---	---	---	---	----	----	----

Insert(3)

1	3	4	6	7	10	13	15
---	---	---	---	---	----	----	----

Delete(10)

1	3	4	6	7	13	15
---	---	---	---	---	----	----

# Problem

If an empty data structure is given these commands what does it output at the end?

- `Insert(3)`
- `Insert(8)`
- `Insert(5)`
- `Insert(10)`
- `Delete(8)`
- `Insert(12)`
- `NearestNeighbors(7)`

Answer

3	5	<del>8</del>	10	12
---	---	--------------	----	----



# Outline

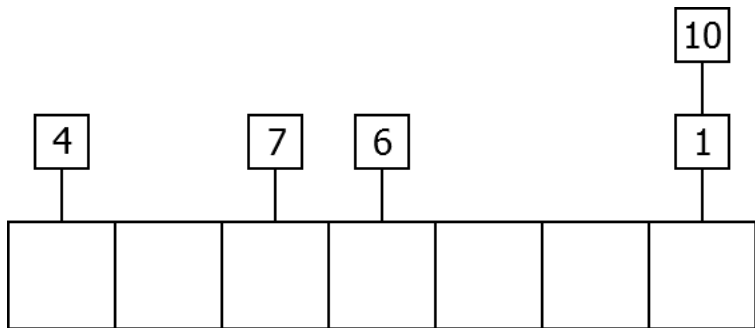
① Local Search

② Attempts

# Hash Table

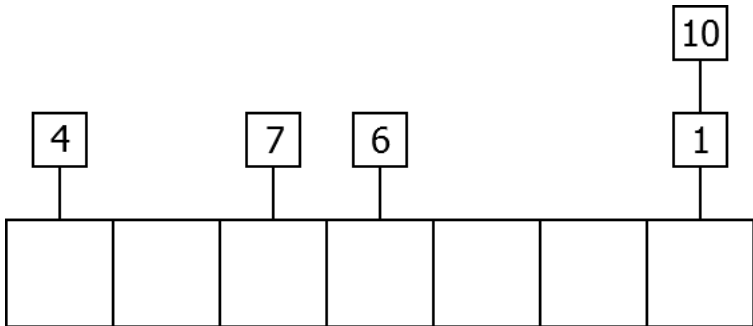
■ RangeSearch:

Impossible ✕



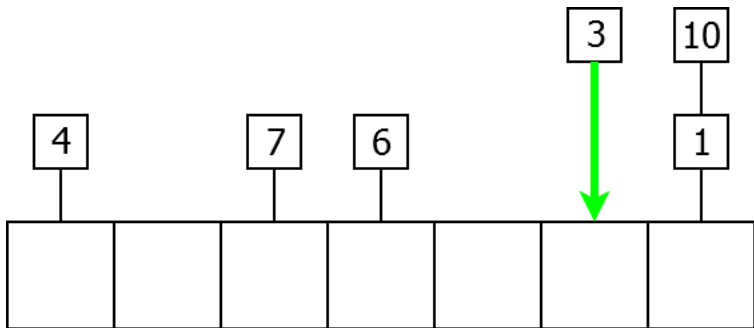
# Hash Table

- RangeSearch: Impossible ✕
- NearestNeighbors: Impossible ✕



# Hash Table

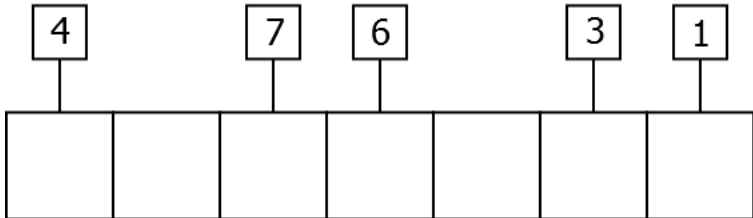
- RangeSearch: Impossible ✗
- NearestNeighbors: Impossible ✗
- Insert:  $O(1)$  ✓



# Hash Table

- RangeSearch: Impossible ✗
- NearestNeighbors: Impossible ✗
- Insert:  $O(1)$  ✓
- Delete:  $O(1)$  ✓

~~10~~



# Array

■ RangeSearch:

$O(n)$  ✗

7	10	4	13	1	6	15
---	----	---	----	---	---	----

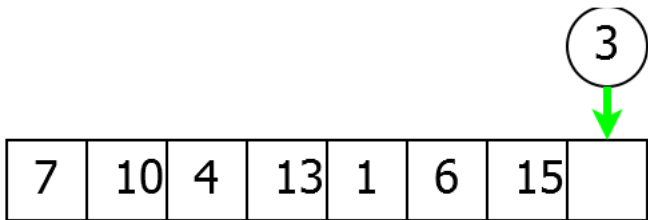
# Array

- RangeSearch:  $O(n)$  ✗
- NearestNeighbors:  $O(n)$  ✗

7	10	4	13	1	6	15
---	----	---	----	---	---	----

# Array

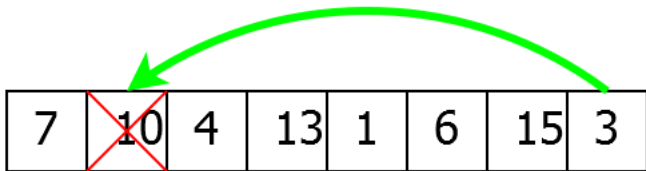
- RangeSearch:  $O(n)$  ✗
- NearestNeighbors:  $O(n)$  ✗
- Insert:  $O(1)$  ✓





# Array

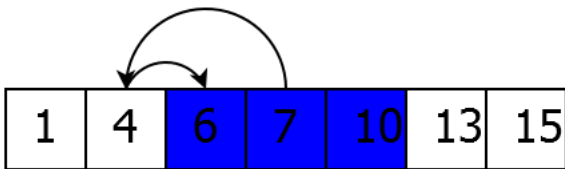
- RangeSearch:  $O(n)$  ✗
- NearestNeighbors:  $O(n)$  ✗
- Insert:  $O(1)$  ✓
- Delete:  $O(1)$  ✓



# Sorted Array

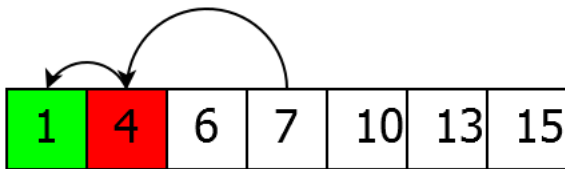
■ RangeSearch:

$O(\log(n))$  ✓



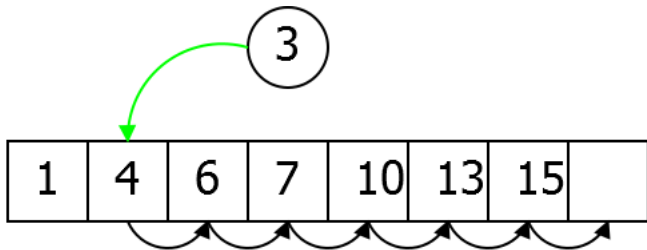
# Sorted Array

- RangeSearch:  $O(\log(n))$  ✓
- NearestNeighbors:  $O(\log(n))$  ✓



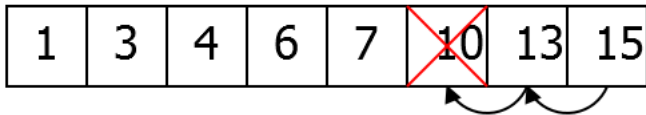
# Sorted Array

- RangeSearch:  $O(\log(n))$  ✓
- NearestNeighbors:  $O(\log(n))$  ✓
- Insert:  $O(n)$  ✗



# Sorted Array

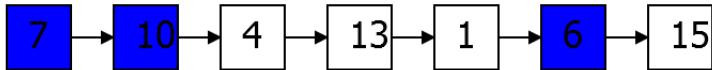
- RangeSearch:  $O(\log(n))$  ✓
- NearestNeighbors:  $O(\log(n))$  ✓
- Insert:  $O(n)$  ✗
- Delete:  $O(n)$  ✗



# Linked List

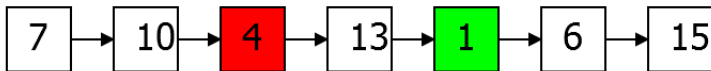
■ RangeSearch:

$O(n)$  ✗



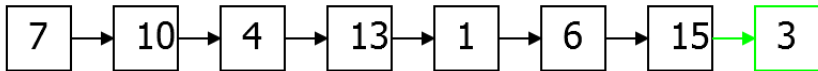
# Linked List

- RangeSearch:  $O(n)$  ✗
- NearestNeighbors:  $O(n)$  ✗



# Linked List

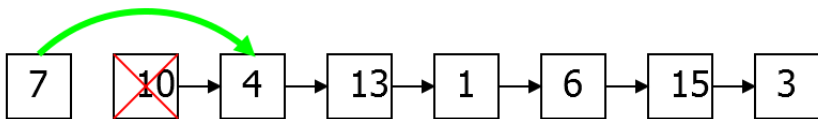
- RangeSearch:  $O(n)$  ✗
- NearestNeighbors:  $O(n)$  ✗
- Insert:  $O(1)$  ✓





# Linked List

- RangeSearch:  $O(n)$  ✗
- NearestNeighbors:  $O(n)$  ✗
- Insert:  $O(1)$  ✓
- Delete:  $O(1)$  ✓



# Need Something New

## Problem

Previous data structures won't work. We need something new.