
**11-442 / 11-642:
Search Engines**

Introduction to Search

Jamie Callan
Carnegie Mellon University
callan@cs.cmu.edu

Two Lecture Outline

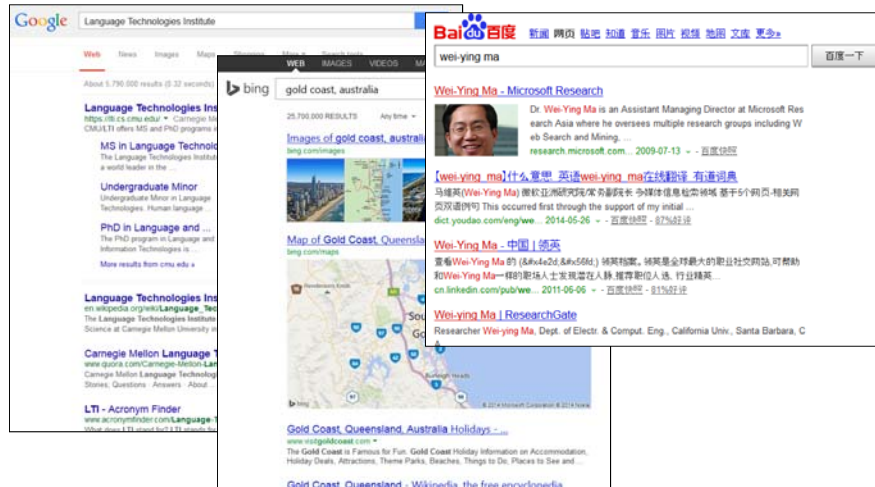
A quick introduction to...

- Ad-hoc retrieval
- Information needs & queries
- Document representation
- Exact match retrieval
 - Unranked Boolean
 - Ranked Boolean
- Indexing
 - Inverted lists
 - Term dictionary
- Query processing
 - TAAT
 - DAAT
- Query operators

Goal: Provide an overview of search (“the Big Picture”)

- Later lectures explore these topics in greater detail

Probably You are an Experienced Search Engine User



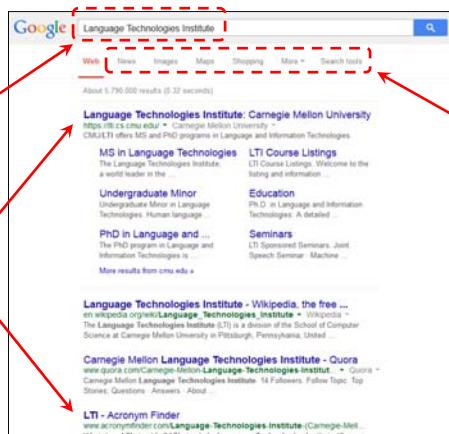
3

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How Does a Search Engine Developer or Researcher View the Search Process?

A query that expresses an information need

Documents (unstructured information)



Vertical search engines

4

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How Does a Search Engine Developer or Researcher View the Search Process?

A person starts with an information need

- The query is an approximate description of the information need

The person searches a corpus of unstructured information

- Documents

Goal: Find documents that satisfy the information need

- Search, retrieval

This lecture and the next present a simple end-to-end solution

- The “big picture”
- Later lectures go into more detail & more advanced material

5

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Simple End-to-End Solutions

Requirements

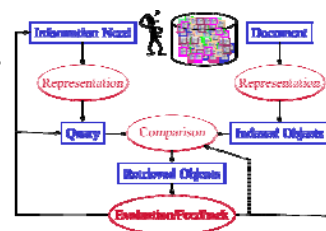
- A way of representing information needs
- A way of representing document content
- A comparison or matching process

Initial solutions

- Boolean queries
- Exact-match retrieval models (unranked and ranked)

These solutions are primitive, but they are still used today

- Fast, easy to build, easy to understand



6

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7

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Representing the Information Need



Exact-match retrieval models assume that a person can describe the information need as a Boolean query

- Relational database systems also make this assumption
- Most people are not good at creating Boolean queries
- Even well-trained people overestimate the quality of their queries



Examples:

- Angelina AND Jolie
- (Angelina AND Jolie) OR (Brad AND Pitt)
- (Angelina NEAR/2 Jolie) OR (Brad NEAR/2 Pitt)
 - NEAR/n is similar to a phrase operator
 - Match if terms are in this order, separated by a distance $\leq n$

8

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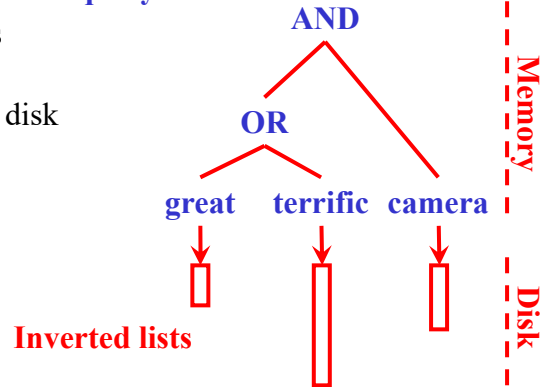
Query Trees



Query: (great OR terrific) AND camera

Search engines represent the query as a tree

- Leaves are index terms
- Leaves are pointers to inverted lists stored on disk



9

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Two Lecture Outline

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- | | |
|-------------------------------|--------------------|
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| • Document representation | – Term dictionary |
| • Exact match retrieval | • Query processing |
| – Unranked Boolean | – TAAT |
| – Ranked Boolean | – DAAT |
| | • Query operators |

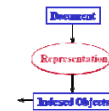
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Representing the Document: An Example Document



A Great Choice.

Review by topjimmy5150

★★★★★ April, 21 2003

I have been looking and looking for a new camera to replace our bulky, but simple and reliable (but only fair picture taker) Sony Mavica FD73. My other choice (Besides the more expensive Nikon Coolpix 3100) was the (also more expensive) Sony Cybershot P72. I recommend any of these cameras, and I was set to buy the Sony, but at the last minute I cheaped out and bought the 2100. No regrets. I bought the camera (along with 128mb memory card (the stock 16mb card will be kept in the bag as a spare) and carrying case) at the new Best Buy in Harrisburg, PA. I also bought a set of 4 Nickle-Metal Hydride rechargeable batteries and charger at Walmart for less than \$20. I keep 2 in the camera and two in the charger/in the camera bag along with the original Lithium battery pack as spares.

Hands down, the best feature of this camera is it's compact design. It is very small. My family likes to go camping during the summer, and last year we found the Mavica too

....

(topjimmy5150, Epinions.com)

11

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Representing the Document



How should the contents of a document be represented?

Today, assume that we will use words from the document

- Free-text indexing: Use just some of the words
 - Developed first, but ... which words?
- Full-text indexing: Use most or all of the words
 - Most search engines do this

Later lectures consider other possibilities

12

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```

graph TD
    Document[Document] --> Representation((Representation))
    Representation --> IndexedObjects[Indexed Objects]
    IndexedObjects --> Search[Search]

```

- Invented first
- Almost never used anymore, but a useful simplification

Corpus
|C|

| | a | abba | abend | ability | able | about | ... | zooms |
|------------------------|---|------|-------|---------|------|-------|-----|-------|
| Doc₁ | 0 | 0 | 0 | 1 | 1 | 1 | ... | 1 |
| Doc₂ | 1 | 1 | 0 | 0 | 1 | 1 | ... | 0 |
| :::: | : | : : | : : | : : | : : | : :: | | : :: |
| Doc_n | 0 | 0 | 1 | 1 | 0 | 1 | ... | 0 |

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```

graph TD
    Document[Document] --> Representation((Representation))
    Representation --> InfernalObjects[Infernal Objects]
    InfernalObjects --> Representation

```

- The document is a “bag of words”
 - Or other features (covered later)

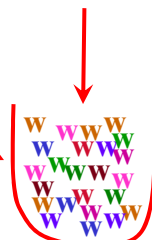
- But...surprisingly effective for search and other tasks (e.g., classification)

Full Review

I have been looking and looking for a new camera to replace our bulky, but simple and reliable Sony Cyber-shot camera (Sony Cyber-shot M20). My other choice (besides the more expensive Canon G12) was the also more expensive Sony Cyber-shot P72. I recommend any of these cameras, and I was set to buy the Sony, but at the last minute I checked out and bought the 2100. No regrets. I bought the camera (along with the "Memory card" (the stock "Mini card" will not hold in the "big" size) and carrying case) at the new Best Buy in Harrisburg, PA. I also bought a set of 2 Nickel-Metal hydride rechargeable batteries and charger for Wal-Mart for less than \$20. I use the camera in the car in the charger (the camera bag along with the original iStock battery pack as spares).

Hands down, the best feature of this camera is its compact design. It is very small. My 14-year-old son is carrying it all summer, and last year we found the M20 too cumbersome to haul around. The 2100 is perfect size. It will easily slip into a shirt pocket. I like the way it looks and I like the way it feels in my hand. It feels perfect.

The photo quality is top notch in the 2mp range. I really want a 3mp camera, but



Frequency-Based Full-Text Representation



Record the frequency of each word in each document

- More effective for search than the binary representation
- The tabular representation is a useful simplification

Corpus Vocabulary |V|

Corpus
|C|

| | a | abba | abend | ability | able | about | ... | zooms |
|------------------|---|------|-------|---------|------|-------|-----|-------|
| Doc ₁ | 0 | 0 | 0 | 7 | 3 | 4 | ... | 2 |
| Doc ₂ | 4 | 5 | 0 | 0 | 1 | 2 | ... | 0 |
| Doc _n | 6 | 0 | 1 | 3 | 0 | 1 | ... | 0 |

15

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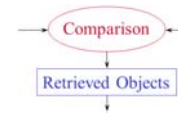
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16

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Retrieval Model #1: Unranked Boolean



Model: Retrieve documents iff they satisfy a Boolean expression

- **Examples:** “michelle AND obama”, “clinton OR trump”
- The query specifies exact relevance criteria
 - Exact match retrieval
- The matching set of retrieved documents is unordered
 - Often sorted by date

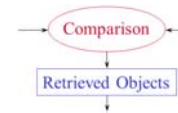
Query operators:

- AND, OR, ANDNOT, NEAR, DATE, ...
- Typically these systems have sophisticated query languages
 - A rich language to describe the set of relevant documents

17

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Retrieval Model #1: Unranked Boolean



**This approach to document retrieval was invented first
...and was the dominant model until the early 1990s
...but it is no longer state-of-the-art**

Why?

- Documents are returned in no particular order

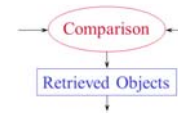
However, it is still used in many systems, and still important

- E.g., WestLaw, PubMed, first pass in Web search engines, ...

18

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Retrieval Model #2: Ranked Boolean



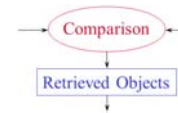
Ranked Boolean addresses a flaw of Unranked Boolean

- Model & operators are the same as for Unranked Boolean
- But ... matching documents are ranked by a document score
 - Unranked Boolean document scores are 0 and 1
 - Ranked Boolean document scores can be anything
 - » Typical Ranked Boolean systems have simple scores

19

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Ranked Boolean: Calculating Scores



What is the score when a query term t occurs in document d ?

- $tf_{t,d}$: The frequency of term t in document d
- $tf_{t,d} \times idf_t = tf_{t,d} \times \log(N / df_t)$: Penalize common terms
 - N : Number of documents in the corpus
 - df_t : The number of documents that contain term t

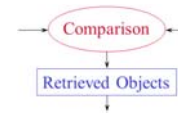
Both types of weights are used

- $tf_{t,d}$: Invented first, easy to implement, only considers the document
- $tf_{t,d} \times idf_t$: More effective
 - Rewards terms that are frequent in this document, but not frequent in the corpus

20

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Ranked Boolean: Calculating Scores



Boolean queries have operators such as AND and OR

- cat AND mouse; john AND paul AND george AND ringo
- rich OR poor; obama OR bush OR clinton OR reagan

A prefix representation makes the query structure more apparent

- AND (cat mouse) AND (john paul george ringo)
- OR (rich poor) OR (obama bush clinton reagan)

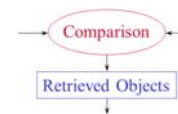
Notation: $q_{\text{operator}}(q_1 \dots q_n)$

- $q_{\text{AND}}(\text{cat mouse})$ $q_{\text{AND}}(\text{john paul george ringo})$
- $q_{\text{OR}}(\text{rich poor})$ $q_{\text{OR}}(\text{obama bush clinton reagan})$

21

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Ranked Boolean: Calculating Scores



What is the score for AND operator $q_{\text{AND}}(q_1 \dots q_n)$ on document j ?

- $\text{score}(q_{\text{AND}}(q_1 \dots q_n), d_j) = \text{MIN}(\text{score}(q_1, d_j), \dots, \text{score}(q_n, d_j))$

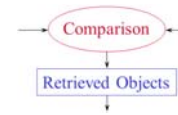
What is the score for OR operator $q_{\text{OR}}(q_1 \dots q_n)$ on document j ?

- $\text{score}(q_{\text{OR}}(q_1 \dots q_n), d_j) = \text{MAX}(\text{score}(q_1, d_j), \dots, \text{score}(q_n, d_j))$
 - Consistent with the AND operator
- $\text{score}(q_{\text{OR}}(q_1 \dots q_n), d_j) = \text{MEAN}(\text{score}(q_1, d_j), \dots, \text{score}(q_n, d_j))$
 - Rewards documents that match many query terms
 - The semantics of an OR operator do not require this behavior
 - But, it is the behavior that people expect
 - Typically a little more effective than MAX

22

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Retrieval Model #2: Ranked Boolean



Advantages

- Very efficient
- Predictable, easy to explain, structured queries
- Works well enough when searchers know exactly what is wanted
- Results ordered by how redundantly a document satisfies a query
- Other term weighting methods can be used, too

Disadvantages

- It's still an Exact-Match model
- Usually it is difficult to get a good balance of Precision and Recall

23

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Exact-Match Retrieval: Unranked vs. Ranked Boolean Retrieval

Query: Trump AND Clinton

| | | | | | |
|----------------------|---|----------------------|--|----------------------|--|
| D₁ | ... Trump ... Clinton Sanders ... | D₂ | Trump ... Clinton... ... Clinton Trump ... | D₃ | ... Trump ... Hillary ... Bill ... Sanders ... |
|----------------------|---|----------------------|--|----------------------|--|

Three retrieval methods

| <u>Unranked Boolean</u> | <u>Ranked Boolean</u> | <u>Best Match</u> |
|-------------------------|-----------------------|-------------------|
| D ₁ | D ₂ | D ₂ |
| D ₂ | D ₁ | D ₁ |
| (arbitrary order) | | D ₃ |

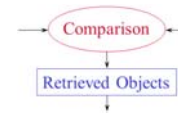
Which ranking is best?

- It depends on the task ... sometimes unranked Boolean is enough

24

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Are Exact-Match Models Still Relevant?



Many people prefer exact-match Boolean models

- Professional searchers (e.g., librarians, paralegals)
- Some Web surfers (e.g., “Advanced Search” feature)
- What do they like? Control, predictability, understandability
- Preferred by 70% of WESTLAW searchers in a 2007 survey
-- James Allan, 2007

Exact-match Boolean is a low-level part of Web search engines

- Massive corpus makes efficiency important
- Massive corpus makes partial matching less important

25

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26


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Data Structures for Index Terms

Search engines use indexes to process queries quickly

- Indexes are data structures that allow things to be found quickly
- Present a key, get back an object

What kinds of lookup does a search engine need?

- Term \rightarrow DocId + “apple” \rightarrow doc₁ doc₁₄ doc₃₂ ...
- Attribute \rightarrow Docid + 2014-08-06 \rightarrow doc₈ doc₁₉ doc₆₃ ...
- Term \rightarrow Corpus statistics “apple” \rightarrow df=3,731; ctf=8,839; ...
- Doc id \rightarrow Attribute doc₁₉ \rightarrow 2014-01-04
- Doc id \rightarrow Term + doc₁₉ \rightarrow “listen” “live” “WYEP” ...
- Doc id \rightarrow Document doc₁₉ \rightarrow 
- ...

27

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Data Structures for Index Terms

Task: Evaluate the query “ability AND about”

One could compare to each document (row)

- Invented first
- Rows are bit vectors
- Complexity is $O(|C| \times |V|)$
- Is this good?

Corpus Vocabulary |V|

| | a | abba | aband | ability | able | about | ... | zooms |
|------------------|---|------|-------|---------|------|-------|-----|-------|
| Doc ₁ | 1 | 0 | 0 | 1 | 1 | 1 | ... | 1 |
| Doc ₂ | 1 | 1 | 0 | 0 | 1 | 1 | ... | 0 |
| ... | : | : | : | : | : | : | : | : |
| Doc _n | 1 | 0 | 1 | 1 | 0 | 1 | ... | 0 |

Corpus |C|

Most terms are rare (occur in few documents)

- The vocabulary V is huge
- Nearly all documents fail to match the query
- Most of the $O(|C| \times |V|)$ effort is wasted effort

28

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Data Structures for Index Terms: Inverted Lists

Task: Evaluate the query “ability AND about”

One could compare to query terms (columns)

- Columns are bit vectors
- Columns are called inverted lists
- Complexity is $O(|C| \times |Q|)$

Corpus

| | a | abba | abnd | ability | able | about | ... | zooms |
|------------------|---|------|------|---------|------|-------|-----|-------|
| Doc ₁ | 1 | 0 | 0 | 1 | 1 | 1 | ... | 1 |
| Doc ₂ | 1 | 1 | 0 | 0 | 1 | 1 | ... | 0 |
| ... | : | : | : | : | : | : | : | : |
| Doc _n | 1 | 0 | 1 | 1 | 0 | 1 | ... | 0 |

**Inverted
Lists**

**Really important
data structure!**

Most terms are rare (occur in few documents)

- Nearly all documents fail to match the query
- More efficient
... but still, most of the $O(|C| \times |Q|)$ effort is wasted effort

29

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Are Fixed-Length Inverted Lists A Good Idea?

Fixed-length inverted lists were used in early search engines

- Simple to manage
- Bit-vector operations are fast and easy to parallelize

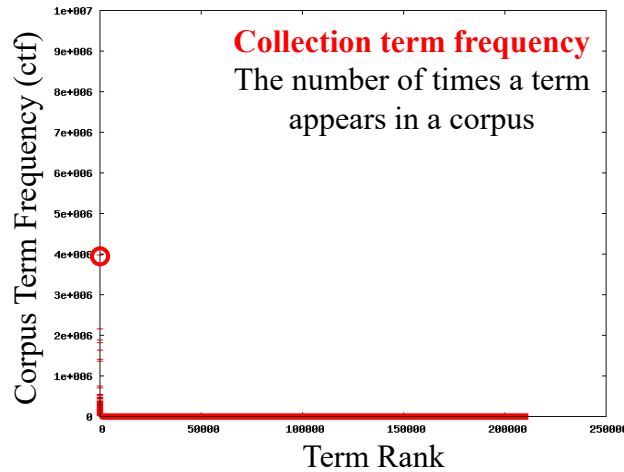
Fixed-length inverted lists are inefficient but ... how inefficient?

- Length: $|C|$ bits
 - The number of documents in the corpus
- Number of bits set to 1 in a typical inverted list: df_{typical}
 - The document frequency of the term with the median term frequency
- How does $|C|$ compare to df_{typical} ?

30

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Term Frequency in the WSJ



Wall Street Journal (1987-1992)

Documents: 174K
Tokens: 69M
Terms (types): 211K
Megabytes: 533

Tokens:

Word occurrences

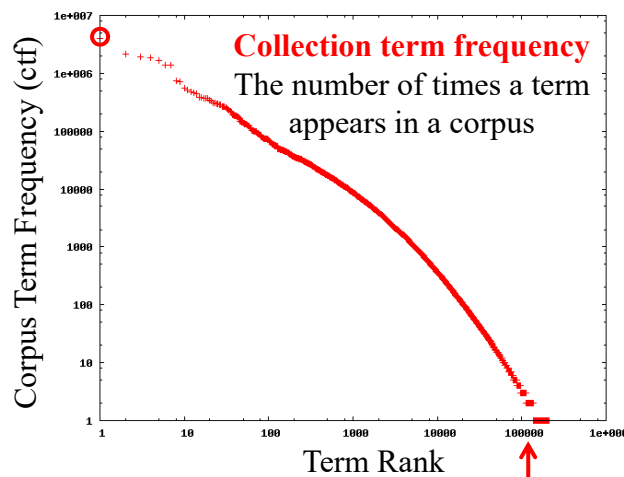
Types:

Unique words

31

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Term Frequency in the WSJ



Wall Street Journal (1987-1992)

Documents: 174K
Tokens: 69M
Terms (types): 211K
Megabytes: 533

Tokens:

Word occurrences

Types:

Unique words

Half of the vocabulary

32

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Are Fixed-Length Inverted Lists A Good Idea?

| Doc | t1 | t2 | t3 | t4 | t5 | t6 | t7 | t8 | t9 | t10 |
|-----|----|----|----|----|----|----|----|----|----|-----|
| 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

Fixed-Length Inverted Lists

In ordinary text, $|C| \gg |df_{\text{median}}|$

- In the Wall Street Journal, $|C| = 174K$ and $df_{\text{median}} = 2$
 - i.e., the median term appears in just two documents

So usually fixed-length inverted lists are very inefficient

- Often used for illustration
- Rarely used in real systems

33

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Sparse Representation of Inverted Lists

Simple approach: Store ids of documents that contain the word

- **Full inverted list:** 10001100100...
 - The i^{th} bit indicates whether the term occurs in the i^{th} document
- **Sparse inverted list:** length=18, docids: 1, 5, 6, 9, ...
 - The term occurs in 18 documents

Usually in this course inverted lists are represented as

- **$df_t=18$, docids 1, 5, 6, 9, ...**
 - df_t :** document frequency (number of documents containing t)
 - docids:** document identifiers

You must know this data structure & more advanced variants

34

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Cyclically Shifting

| | | | | | |
|--|----|----|----|----|--|
| | 2 | 3 | 4 | 5 | |
| | 5 | 6 | 7 | 8 | |
| | 8 | 9 | 10 | 11 | |
| | 11 | 12 | 13 | 14 | |

Inverted Table

- Binary inverted lists

- Frequency inverted lists

- **Positional** inverted lists

- 35

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Figure 1 illustrates the process of generating an inverted index from a document. The document is divided into segments (Doc1, Doc2, Doc3, Doc4) and words (Word1, Word2, Word3, Word4, Word5, Word6, Word7, Word8, Word9, Word10, Word11, Word12, Word13, Word14, Word15, Word16, Word17, Word18, Word19, Word20, Word21, Word22, Word23, Word24, Word25, Word26, Word27, Word28, Word29, Word30, Word31, Word32, Word33, Word34, Word35, Word36, Word37, Word38, Word39, Word40, Word41, Word42, Word43, Word44, Word45, Word46, Word47, Word48, Word49, Word50, Word51, Word52, Word53, Word54, Word55, Word56, Word57, Word58, Word59, Word60, Word61, Word62, Word63, Word64, Word65, Word66, Word67, Word68, Word69, Word70, Word71, Word72, Word73, Word74, Word75, Word76, Word77, Word78, Word79, Word80, Word81, Word82, Word83, Word84, Word85, Word86, Word87, Word88, Word89, Word90, Word91, Word92, Word93, Word94, Word95, Word96, Word97, Word98, Word99, Word100). The inverted index is a table where the rows represent words and the columns represent documents. The words are sorted alphabetically. The documents are sorted by the first word they contain. The inverted index is a table where the rows represent words and the columns represent documents. The words are sorted alphabetically. The documents are sorted by the first word they contain. The inverted index is a table where the rows represent words and the columns represent documents. The words are sorted alphabetically. The documents are sorted by the first word they contain.

| | |
|--------|------|
| df: | 4356 |
| docid: | 42 |
| docid: | 94 |
| : | |

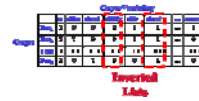
| | |
|--------|------|
| df: | 4356 |
| docid: | 42 |
| tf: | 3 |
| docid: | 94 |
| tf: | 1 |
| : | |

```
df: 4356
docid: 42
tf: 3
locs: 14
      83
      157
docid: 94
tf: 1
locs: 65
      :
```

| | |
|---------|------|
| df: | 4356 |
| docid: | 42 |
| doclen: | 357 |
| tf: | 3 |
| locs: | 14 |
| | 83 |
| | 157 |
| docid: | 94 |
| doclen: | 172 |
| tf: | 1 |
| locs: | 65 |
| | : |

36

Inverted Indexes



After indexing, there are many inverted lists

- One per term in the vocabulary (typically 10^6 to 10^8)
- Very skewed size distribution (Zipf's Law)
- Very skewed access patterns

An inverted index consists of two parts

- Inverted file(s) that contain inverted lists
 - An object database containing the inverted lists
- An access mechanism
 - Term string \rightarrow inverted list
 - Term id \rightarrow inverted list
 - Sometimes combined with the term dictionary

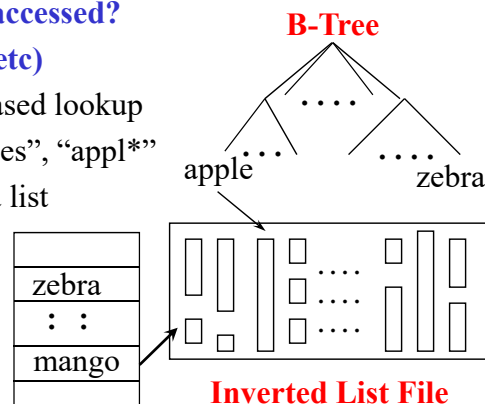
37

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Inverted Indexes: Two Common Access Methods

How is a file of inverted lists accessed?

- **B-Tree (B+ Tree, B* Tree, etc)**
 - Exact-match and range-based lookup
 - » “apple”, “apple – apples”, “appl*”
 - $O(\log n)$ lookups to find a list
 - Usually easy to expand
- **Hash table**
 - Exact-match lookup
 - » “apple”
 - $O(1)$ lookups to find a list
 - May be complex to expand



38

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- Exact match retrieval
 - Unranked Boolean
 - Ranked Boolean
- Indexes
 - Inverted lists
 - Term dictionary
- Query processing
 - TAAT
 - DAAT
- Query operators

Goal: Provide an overview of search (“the Big Picture”)

- Later lectures explore these topics in greater detail

39

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Waitlist Reminder

If you are on the waitlist...

- I will admit some people from the waitlist today or tomorrow
- Be sure to sign the attendance sheet to show that you are here

157

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