QF620 Stochastic Modelling in Finance Assignment 3/4

Due Date: 25-Oct-2023

1. Find the mean and variance of X_t if

(a)

$$dX_t = \mu dt + \sigma dW_t.$$

(b)

$$dX_t = \mu X_t dt + \sigma X_t dW_t.$$

(c)

$$dX_t = \kappa(\theta - X_t)dt + \sigma dW_t.$$

2. Consider the two stochastic differential equations below:

$$dX_t = rX_t dt + \sigma X_t dW_t$$

$$dY_t = rY_t dt + \sigma Y_t d\tilde{W}_t$$

Use Itô's formula to derive the stochastic differential equation for $Z_t = \frac{X_t}{Y_t}$, is

- (a) W_t and \tilde{W}_t are independent.
- (b) W_t and \tilde{W}_t have a correlation of 1.
- (c) W_t and \tilde{W}_t have a correlation of ρ .