

HW1

$$1. P(ZB | \text{Underperformer}) = 5\%^2 = 0.25\%$$

$$P(ZB | \text{In-line}) = 5\%^2 = 25\%$$

$$P(ZB | \text{Outperformer}) = 70\%^2 = 49\%$$

$$2. P(ZB) = 0.25\% \times 10\% + 25\% \times 80\% + 49\% \times 10\% \\ = 24.925\%$$

$$3. P(\text{Underformer} | ZB) = \frac{P(ZB | \text{Underformer}) P(\text{Underformer})}{P(ZB)} = \frac{0.25\% \times 10\%}{24.925\%} \\ \approx 0.001$$

$$P(\text{In-line} | ZB) = \frac{P(ZB | \text{In-line}) P(\text{In-line})}{P(ZB)} = \frac{25\% \times 80\%}{24.925\%} \approx 0.802$$

$$P(\text{Outperformer} | ZB) = \frac{P(ZB | \text{Outperformers}) P(\text{Outperformer})}{P(ZB)}$$

$$= \frac{49\% \times 10\%}{24.925\%} = 0.197$$