

$a = "12345"$ ,  $b = 7$  say.

Now to calculate <sup>(a % b)</sup> we can start like this

$$\begin{aligned} & ((0 \times 10) + 1) \% 7 = 1 \% 7 = 1 \\ \rightarrow & ((1 \times 10) + 2) \% 7 = 12 \% 7 = 5 \\ \rightarrow & ((5 \times 10) + 3) \% 7 = 53 \% 7 = 4 \\ \rightarrow & ((4 \times 10) + 4) \% 7 = 44 \% 7 = 2 \\ \rightarrow & ((2 \times 10) + 5) \% 7 = 25 \% 7 = 4 \end{aligned}$$

which is correct as  $12345 \% 7 = 4$

Thought process:-

① we can write 1 as 1 and take  $1 \% 7 = 1$  and  $1 \% 7 = 1$

② we can write 12 as  $10 \times 1 + 2$   
 $(10 \times 1 + 2) \% 7 = (10 \% 7 \times 1 \% 7 + 2 \% 7) \% 7$   
 $= (3 \times 1 + 2) \% 7$   
 $= (3 + 2) \% 7 = 5$

③ we can write 123 as  $12 \times 10 + 3$   
 $123 \% 7 = ((12 \% 7) \times (10 \% 7) + (3 \% 7)) \% 7$   
 $= ((5 \times 3) + 3) \% 7$   
 $= (15 + 3) \% 7 = 4$

④ 1234 can be written as  $123 \times 10 + 4$   
 $1234 \% 7 = ((123 \% 7) \times (10 \% 7) + 4 \% 7) \% 7$   
 $= ((4 \times 3) + 4) \% 7 = 2$

⑤ 12345 can be written as  $1234 \times 10 + 5$   
 $12345 \% 7 = ((1234 \% 7) \times (10 \% 7) + 5 \% 7) \% 7$   
 $= 4$

do as you can see that  
value calculated on a  
lower step is used on next  
step.

target