Faster generic CCA secure KEM transformation using encrypt-then-MAC

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Abstract. Abstract needs to be rewritten because ML-KEM is not a suitable candidate. Instead, section 3 will be about the proof, section 4 will be a survey of existing public-key encryption schemes and a discussion of which ones are suitable, and section 5 will be about implementation and performance analysis with classic McEliece

Keywords: First keyword · Second keyword · Another keyword.

1 Introduction

Introduction will need to be re-written. I will get back to it after writing section 2, 3, 4, 5

2 Preliminaries

2.1 Public-key encryption scheme

Syntax. A public-key encryption scheme $\texttt{PKE}(\texttt{KeyGen}, \texttt{Enc}, \texttt{Dec})$ is a collection of three routines defined over some plaintext space $\mathcal{M}$ and some ciphertext space $\mathcal{C}$. Key generation $(\texttt{pk}, \texttt{sk}) \xleftarrow{\$} \texttt{KeyGen}()$ is a randomized routine that returns a keypair. The encryption routine $\texttt{Enc} : (\texttt{pk}, m) \mapsto c$ encrypts the input plaintext m under the input public key $\texttt{pk}$ and produces a ciphertext c. The decryption routine $\texttt{Dec} : (\texttt{sk}, c) \mapsto m$ decrypts the input ciphertext c under the input secret key $\texttt{sk}$ and produces a plaintext m. Where the encryption routine is randomized, we denote the randomness by a coin $r \in \mathcal{R}$, where $\mathcal{R}$ is called the coin space. The decryption routine is assumed to always be deterministic.

Correctness. Following the definition in [4], a PKE is δ-correct if:

$$E\left[\max_{m \in \mathcal{M}} P\left[\texttt{Dec}(\texttt{sk}, c) \neq m \mid c \xleftarrow{\$} \texttt{Enc}(\texttt{pk}, m)\right]\right] \leq \delta.$$

Where the expectation is taken with respect to the probability distribution of all possible keypairs $(\texttt{pk}, \texttt{sk}) \xleftarrow{\$} \texttt{PKE.KeyGen()}$. For many lattice-based cryptosystems, including ML-KEM, decryption failures could leak information about the secret key, although the probability of a decryption failure is low enough that

classical adversaries cannot exploit decryption failure more than they can defeat the underlying lattice problem.

Security. The security of public-key encryption is conventionally discussed within the context of adversarial games played between a challenger and an adversary [6]. There are two main types of games: i) in the one-wayness (OW-ATK) game, the adversary is given a random encryption, then asked to produce the correct decryption; ii) in the indistinguishability (IND-ATK) game, the adversary is given the encryption of one of two adversary-chosen plaintexts, then asked to decide which of the plaintexts corresponds with the given encryption. Depending on the attack model, the adversary may have access to various oracles. Within the context of public-key cryptography, adversaries are always assumed to have the public key with which they can mount chosen-plaintext attack (CPA). If the adversary has access to a plaintext-checking oracle (PCO) [12] then it can mount plaintext-checking attack (PCA). Where the adversary has access to a decryption oracle, it can mount chosen-ciphertext attacks (CCA).

OW-ATK Game

$(\mathtt{pk}, \mathtt{sk}) \xleftarrow{\$} \mathtt{KeyGen}(1^\lambda)$
$m^* \xleftarrow{\$} \mathcal{M}$
$c^* \xleftarrow{\$} \mathtt{Enc}(\mathtt{pk}, m^*)$
$\hat{m} \xleftarrow{\$} A^{\mathcal{O}_{\mathtt{ATK}}}(1^\lambda, \mathtt{pk}, c^*)$
return $[\![\hat{m} = m^*]\!]$

IND-ATK Game

$(\mathtt{pk}, \mathtt{sk}) \xleftarrow{\$} \mathtt{KeyGen}(1^\lambda)$
$(m_0, m_1) \xleftarrow{\$} A^{\mathcal{O}_{\mathtt{ATK}}}(1^\lambda, \mathtt{pk})$
$b \xleftarrow{\$} \{0, 1\}$
$c^* \xleftarrow{\$} \mathtt{Enc}(\mathtt{pk}, m_b)$
$\hat{b} \xleftarrow{\$} A^{\mathcal{O}_{\mathtt{ATK}}}(1^\lambda, \mathtt{pk}, c^*)$
return $[\![\hat{b} = b]\!]$

$\mathcal{O}_{\mathtt{PCO}}(m, c)$
return $[\![m = \mathtt{Dec}(\mathtt{sk}, c)]\!]$

$\mathcal{O}_{\mathtt{Dec}}(c)$
return $\mathtt{Dec}(\mathtt{sk}, c)$

Fig. 1: The one-way game, indistinguishability game, plaintext-checking oracle (PCO), and decryption oracle. $\mathtt{ATK} \in \{\mathtt{CPA}, \mathtt{PCA}, \mathtt{CCA}\}$

The advantage of an adversary in the OW-ATK game is the probability that it outputs the correct decryption. The advantage of an adversary in the IND-ATK game is defined below. A PKE is OW-ATK/IND-ATK secure if no efficient adversary has non-negligible advantage in the corresponding security game.

$$\mathtt{Adv}_{\mathtt{IND\text{-}ATK}}(A) = \left| P\left[A^{\mathcal{O}_{\mathtt{ATK}}}(1^\lambda, \mathtt{pk}, c^*) = b\right] - \frac{1}{2} \right|.$$

2.2 Key encapsulation mechanism (KEM)

Syntax. A key encapsulation mechanism $\mathtt{KEM}(\mathtt{KeyGen}, \mathtt{Encap}, \mathtt{Decap})$ is a collection of three routines defined over some ciphertext space $\mathcal{C}$ and some key space $\mathcal{K}$. The key generation routine takes the security parameter 1^λ and outputs a

keypair $(\mathtt{pk}, \mathtt{sk}) \xleftarrow{\$} \mathtt{KeyGen}(1^\lambda)$. $\mathtt{Encap}(\mathtt{pk})$ is a probabilistic routine that takes a public key $\mathtt{pk}$ and outputs a pair of values (c, K) where $c \in \mathcal{C}$ is the ciphertext (also called encapsulation) and $K \in \mathcal{K}$ is the shared secret (also called session key). $\mathtt{Decap}(\mathtt{sk}, c)$ is a deterministic routine that takes the secret key $\mathtt{sk}$ and the encapsulation c and returns the shared secret K if the ciphertext is valid. Some KEM constructions use explicit rejection, where if c is invalid then $\mathtt{Decap}$ will return a rejection symbol $\perp$; other KEM constructions use implicit rejection, where if c is invalid then $\mathtt{Decap}$ will return a fake session key that depends on the ciphertext and some other secret values.

Security. The security of a KEM is similarly discussed in adversarial games (Figure 2), although the win conditions differ slightly from the win conditions of a PKE indistinguishability game. In a KEM's indistinguishability game, an adversary is given the public key and a challenge ciphertext, then asked to distinguish a pseudorandom shared secret K_0 associated with the challenge ciphertext from a truly random bit string of equal length.

$\mathtt{IND\text{-}ATK}$ game

1: $(\mathtt{pk}, \mathtt{sk}) \xleftarrow{\$} \mathtt{KeyGen}(1^\lambda)$
2: $(c^*, K_0) \xleftarrow{\$} \mathtt{Encap}(\mathtt{pk})$
3: $K_1 \xleftarrow{\$} \mathcal{K}$
4: $b \xleftarrow{\$} \{0, 1\}$
5: $\hat{b} \xleftarrow{\$} A^{\mathcal{O}_{\mathtt{ATK}}}(1^\lambda, \mathtt{pk}, c^*, K_b)$
6: **return** $[\![\hat{b} = b]\!]$

$\mathcal{O}_{\mathtt{Decap}}(c)$

1: **return** $\mathtt{Decap}(\mathtt{sk}, c)$

Fig. 2: $\mathtt{IND\text{-}ATK}$ game for KEM and decapsulation oracle $\mathcal{O}_{\mathtt{Decap}}$

The decapsulation oracle $\mathcal{O}^{\mathtt{Decap}}$ takes a ciphertext c and returns the output of the $\mathtt{Decap}$ routine using the secret key. The advantage of an IND-CCA adversary $\mathcal{A}_{\mathtt{IND\text{-}CCA}}$ is defined by the adversary's ability to correctly distinguish the two cases beyond a blind guess:

$$\mathtt{Adv}_{\mathtt{IND\text{-}CCA}}(A) = \left| P[A^{\mathcal{O}_{\mathtt{Decap}}}(a^\lambda, \mathtt{pk}, c^*, K_b) = b] - \frac{1}{2} \right|.$$

A KEM is $\mathtt{IND\text{-}ATK}$ secure if no efficient adversary has non-negligible advantage in the corresponding security game.

2.3 Message authentication code (MAC)

Syntax. A message authentication code $\mathtt{MAC}(\mathtt{KeyGen}, \mathtt{Sign}, \mathtt{Verify})$ is a collection of routines defined over some key space $\mathcal{K}$, some message space $\mathcal{M}$, and

some tag space $\mathcal{T}$. The signing routine $\texttt{Sign}(k, m)$ authenticates the message m under the secret key k by producing a tag t (also called digest) (we define the process that generates an authentication tag t over message m a *signing routine* in this paper). The verification routine $\texttt{Verify}(k, m, t)$ takes the triplet of secret key k, message m, and tag t, and outputs `1` if the message-tag pair is valid under the secret key, or `0` otherwise. Many MAC constructions are deterministic. For these constructions it is simpler to denote the signing routine by $t \leftarrow \texttt{MAC}(k, m)$ and perform verification using a simple comparison.

Security. The security of a MAC is defined in an adversarial game in which an adversary, with access to a MAC oracle that can answer signing queries $\texttt{MAC}(k, m) \leftarrow \mathcal{O}_{\texttt{MAC}}(m)$, tries to forge a new valid message-tag pair that has never been queried before. The ability to access a MAC oracle is called *chosen-message attack (CMA)*. The ability to produce a valid tag on some arbitrary message is called *existential forgery*. The existential unforgeability under chosen message attack (EUF-CMA) game is shown below:

EUF-CMA game
1: $k^* \xleftarrow{\$} \mathcal{K}$
2: $(\hat{m}, \hat{t}) \xleftarrow{\$} \mathcal{A}^{\mathcal{O}_{\texttt{MAC}}}()$
3: **return** $[\![\texttt{Verify}(k^*, \hat{m}, \hat{t}) \wedge (\hat{m}, \hat{t}) \notin \mathcal{O}_{\texttt{MAC}}]\!]$

MAC oracle $\mathcal{O}_{\texttt{MAC}}(m)$
1: **return** $\texttt{MAC}(k^*, m)$

Fig. 3: The existential forgery game and the MAC oracle

The advantage $\texttt{Adv}_{\texttt{EUF-CMA}}$ of the existential forgery adversary is the probability that it wins the EUF-CMA game. Some MACs are one-time existentially unforgeable, meaning that each secret key can be used to authenticate only a single message. The corresponding security game is modified such that the MAC oracle will only answer a single signing query.

3 The encrypt-then-MAC transformation

Our technique. We introduce our encrypt-then-MAC transformation that transforms a OW-PCA secure PKE and an one-time existentially unforgeable MAC into an IND-CCA secure KEM. Our scheme mainly differs from DHIES in its versatility and input requirement. Whereas the IND-CCA security of DHIES reduces specifically to the Gap Diffie-Hellman assumption, the chosen-ciphertext security of the encrypt-then-MAC KEM reduces more generally to the OW-PCA security [12] of the input scheme. In addition, we propose that because each call to encapsulation samples a fresh PKE plaintext, the encrypt-then-MAC KEM can be instantiated with one-time secure MAC such as Poly1305 for further performance improvements (Abdalla, Rogaway, and Bellare originally proposed to

use HMAC and CBC-MAC, which are many-time secure MAC but less efficient than one-time MAC, see Section 5.1). The encapsulation data flow is illustrated in Figure 4.

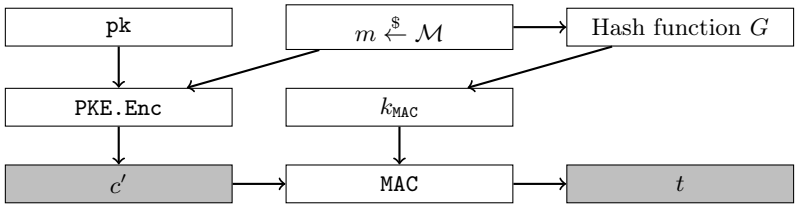

Fig. 4: Combining PKE with MAC using encrypt-then-MAC to ensure ciphertext integrity

In Section 3.2 we reduce the IND-CCA security of the KEM tightly to the OW-PCA security of the underlying PKE, and non-tightly to the unforgeability of the MAC. In Section **??**, we show that DHIES is a special case of the encrypt-then-MAC transformation by reducing the OW-PCA security of the ElGamal cryptosystem to the Gap Diffie-Hellman assumption.

3.1 The generic KEM construction

Let $\mathcal{B}^*$ denote the set of finite bit strings. Let $\mathtt{PKE}(\mathtt{KeyGen}, \mathtt{Enc}, \mathtt{Dec})$ be a public-key encryption scheme defined over message space $\mathcal{M}$ and ciphertext space $\mathcal{C}$. Let $\mathtt{MAC} : \mathcal{K}_{\mathtt{MAC}} \times \mathcal{B}^* \to \mathcal{T}$ be a deterministic message authentication code that takes a key $k \in \mathcal{K}_{\mathtt{MAC}}$, some message $m \in \mathcal{B}^*$, and outputs a tag $t \in \mathcal{T}$. Let $G : \mathcal{M} \to \mathcal{K}_{\mathtt{MAC}}$ be a hash function that maps from PKE's plaintext space to MAC's key space. Let $H : \mathcal{B}^* \to \mathcal{K}_{\mathtt{KEM}}$ be a hash function that maps bit strings into the set of possible shared secrets. The encrypt-then-MAC transformation $\mathtt{EtM}[\mathtt{PKE}, \mathtt{MAC}, G, H]$ constructs a key encapsulation mechanism $\mathtt{KEM}_{\mathtt{EtM}}(\mathtt{KeyGen}, \mathtt{Encap}, \mathtt{Decap})$, whose routines are described in Figure 5.

$\mathtt{KEM}_{\mathtt{EtM}}.\mathtt{KeyGen}()$

1: $(\mathtt{pk}, \mathtt{sk}') \xleftarrow{\$} \mathtt{PKE.KeyGen}()$
2: $z \xleftarrow{\$} \mathcal{M}$
3: $\mathtt{sk} \leftarrow (\mathtt{sk}', z)$
4: **return** $(\mathtt{pk}, \mathtt{sk})$

$\mathtt{KEM}_{\mathtt{EtM}}.\mathtt{Encap}(\mathtt{pk})$

1: $m \xleftarrow{\$} \mathcal{M}$
2: $k \leftarrow G(m)$
3: $c' \xleftarrow{\$} \mathtt{PKE.Enc}(\mathtt{pk}, m)$
4: $t \leftarrow \mathtt{MAC}(k, c')$
5: $c \leftarrow (c', t)$
6: $K \leftarrow H(m, c)$
7: **return** (c, K)

$\mathtt{KEM}_{\mathtt{EtM}}.\mathtt{Decap}(\mathtt{sk}, c)$

1: $(c', t) \leftarrow c$
2: $(\mathtt{sk}', z) \leftarrow \mathtt{sk}$
3: $\hat{m} \leftarrow \mathtt{PKE.Dec}(\mathtt{sk}', c')$
4: $\hat{k} \leftarrow G(\hat{m})$
5: **if** $\mathtt{MAC}(\hat{k}, c') = t$ **then**
6: $\quad K \leftarrow H(\hat{m}, c)$
7: **else**
8: $\quad K \leftarrow H(z, c)$
9: **end if**
10: **return** K

Fig. 5: The encrypt-then-MAC transformation builds a KEM, denoted by $\mathtt{KEM}_{\mathtt{EtM}}$, using a $\mathtt{PKE}(\mathtt{KeyGen}, \mathtt{Enc}, \mathtt{Dec})$, a $\mathtt{MAC}$, and two hash functions G, H

Since the encrypt-then-MAC transformation removes re-encryption in decapsulation, there is no longer the need for fixing the pseudorandom coin r in the PKE's encryption routine. If the input PKE is already rigid, then the shared secret may be derived from hashing the PKE plaintext alone. However, if the input PKE is not rigid, then the shared secret must be derived from hashing both the PKE plaintext and the PKE ciphertext.

Security analysis. The CCA security of the encrypt-then-MAC scheme can be intuitively argued through an adversary's inability to learn additional information from the decapsulation oracle. For an adversary A to produce a valid tag t for some unauthenticated ciphertext c' under the symmetric key $k \leftarrow G(\mathtt{Dec}(\mathtt{sk}', c'))$ implies that A must either know the symmetric key k or produce a forgery. Under the random oracle model, A also cannot know k without knowing its pre-image $\mathtt{Dec}(\mathtt{sk}', c')$, so A must either have produced c' honestly, or have broken the one-way security of $\mathtt{PKE}$. This means that the decapsulation oracle will not give out information on decryption that the adversary does not already know.

However, a decapsulation oracle can still give out some information: for a known plaintext m, all possible encryptions $c' \xleftarrow{\$} \mathtt{Enc}(\mathtt{pk}, m)$ can be correctly signed, while ciphertexts that don't decrypt back to m cannot be correctly signed. This means that a decapsulation oracle can be converted into a plaintext-

checking oracle, so every chosen-ciphertext attack against the KEM can be converted into a plaintext-checking attack against the underlying PKE.

On the other hand, if the underlying PKE is OW-PCA secure and the underlying MAC is one-time existentially unforgeable, then the encrypt-then-MAC KEM is IND-CCA secure:

Theorem 1. *For every* $\mathit{IND\text{-}CCA}$ *adversary* A *against* $\mathit{KEM}_{\mathit{EtM}}$ *that makes* q *decapsulation queries, there exists an* $\mathit{OW\text{-}PCA}$ *adversary* B *who makes at least* q *plaintext-checking queries against the underlying* PKE*, and an one-time existential forgery adversary* C *against the underlying* MAC *such that*

$$\mathit{Adv}_{\mathit{IND\text{-}CCA}}(A) \leq q \cdot \mathit{Adv}_{\mathit{OT\text{-}MAC}}(C) + 2 \cdot \mathit{Adv}_{\mathit{OW\text{-}PCA}}(B).$$

3.2 Proof of Theorem 1

We will prove Theorem 1 using a sequence of game. A summary of the the sequence of games can be found in Figure 6 and 7. From a high level we made three incremental modifications to the IND-CCA game for $\mathtt{KEM}_{\mathtt{EtM}}$:

1. Replace the true decapsulation oracle with a simulated decapsulation oracle
2. Replace the pseudorandom MAC key $k^* \leftarrow G(m^*)$ with a truly random $k^* \xleftarrow{\$} \mathcal{K}_{\mathtt{MAC}}$
3. Replace the pseudorandom shared secret $K_0 \leftarrow H(m^*, c)$ with a truly random shared secret $K_0 \xleftarrow{\$} \mathcal{K}_{\mathtt{KEM}}$

A OW-PCA adversary can then simulate the modified IND-CCA game for the KEM adversary, and the advantage of the OW-PCA adversary is associated with the probability of certain behaviors of the KEM adversary.

IND-CCA game for $\mathtt{KEM}_{\mathtt{EtM}}$

$(\mathtt{pk}, \mathtt{sk}) \xleftarrow{\$} \mathtt{KEM}_{\mathtt{EtM}}.\mathtt{KeyGen}()$
$m^* \xleftarrow{\$} \mathcal{M}$
$c' \xleftarrow{\$} \mathtt{PKE.Enc}(\mathtt{pk}, m^*)$
$k^* \leftarrow G(m^*)$ ▷ Game 0-1
$k^* \xleftarrow{\$} \mathcal{K}_{\mathtt{MAC}}$ ▷ Game 2-3
$t \leftarrow \mathtt{MAC}(k^*, c')$
$c^* \leftarrow (c', t)$
$K_0 \leftarrow H(m^*, c^*)$ ▷ Game 0-2
$K_0 \xleftarrow{\$} \mathcal{K}_{\mathtt{KEM}}$ ▷ Game 3
$K_1 \xleftarrow{\$} \mathcal{K}_{\mathtt{KEM}}$
$b \xleftarrow{\$} \{0, 1\}$
$\hat{b} \leftarrow A^{\mathcal{O}^{\mathtt{Decap}}}(\mathtt{pk}, c^*, K_b)$ ▷ Game 0
$\hat{b} \leftarrow A^{\mathcal{O}_1^{\mathtt{Decap}}}(\mathtt{pk}, c^*, K_b)$ ▷ Game 1-3
return $[\![\hat{b} = b]\!]$

Hash oracle $\mathcal{O}^G(m)$

if $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = m$ **then**
  return $\tilde{k}$
end if
$k \xleftarrow{\$} \mathcal{K}_{\mathtt{MAC}}$
$\mathcal{L}^G \leftarrow \mathcal{L}^G \cup \{(m, k)\}$
return k

Decap oracle $\mathcal{O}^{\mathtt{Decap}}(c)$

$(c', t) \leftarrow c$
$\hat{m} = \mathtt{Dec}(\mathtt{sk}', c')$
$\hat{k} \leftarrow G(\hat{m})$
if $\mathtt{MAC}(\hat{k}, c') = t$ **then**
  $K \leftarrow H(\hat{m}, c)$
else
  $K \leftarrow H(z, c)$
end if
return K

$\mathcal{O}_1^{\mathtt{Decap}}(c)$

$(c', t) \leftarrow c$
if $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = \mathtt{Dec}(\mathtt{sk}', c') \wedge \mathtt{MAC}(\tilde{k}, c') = t$ **then**
  $K \leftarrow H(\tilde{m}, c)$
else
  $K \leftarrow H(z, c)$
end if
return K

$\mathcal{O}^H(m, c)$

if $\exists(\tilde{m}, \tilde{c}, \tilde{K}) \in \mathcal{L}^H : \tilde{m} = m \wedge \tilde{c} = c$ **then**
  return $\tilde{K}$
end if
$K \xleftarrow{\$} \mathcal{K}_{\mathtt{KEM}}$
$\mathcal{L}^H \leftarrow \mathcal{L}^H \cup \{(m, c, K)\}$
return K

Fig. 6: Sequence of games in the proof of Theorem 1

$B(\mathtt{pk}, c'^*)$

1: $z \xleftarrow{\$} \mathcal{M}$
2: $k \xleftarrow{\$} \mathcal{K}_{\mathtt{MAC}}$
3: $t \leftarrow \mathtt{MAC}(k, c'^*)$
4: $c^* \leftarrow (c'^*, t)$
5: $K \xleftarrow{\$} \mathcal{K}_{\mathtt{KEM}}$
6: $\hat{b} \leftarrow A^{\mathcal{O}_B^{\mathtt{Decap}}, \mathcal{O}_B^G, \mathcal{O}_B^H}(\mathtt{pk}, c^*, K)$
7: **if** $\mathtt{ABORT}(m)$ **then**
8: **return** m
9: **end if**

$\mathcal{O}_B^{\mathtt{Decap}}(c)$

1: $(c', t) \leftarrow c$
2: **if** $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \mathtt{PCO}(\tilde{m}, c') = 1 \wedge \mathtt{MAC}(\tilde{k}, c') = t$ **then**
3: $K \leftarrow H(\tilde{m}, c)$
4: **else**
5: $K \leftarrow H(z, c)$
6: **end if**
7: **return** K

$\mathcal{O}_B^H(m, c)$

if $\mathtt{PCO}(m, c'^*) = 1$ **then**
$\mathtt{ABORT}(m)$
end if
if $\exists(\tilde{m}, \tilde{c}, \tilde{K}) \in \mathcal{L}^H : \tilde{m} = m \wedge \tilde{c} = c$ **then**
return $\tilde{K}$
end if
$K \xleftarrow{\$} \mathcal{K}_{\mathtt{KEM}}$
$\mathcal{L}^H \leftarrow \mathcal{L}^H \cup \{(m, c, K)\}$
return K

$\mathcal{O}_B^G(m)$

1: **if** $\mathtt{PCO}(m, c'^*) = 1$ **then**
2: $\mathtt{ABORT}(m)$
3: **end if**
4: **if** $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = m$ **then**
5: **return** $\tilde{k}$
6: **end if**
7: $k \xleftarrow{\$} \mathcal{K}_{\mathtt{MAC}}$
8: $\mathcal{L}^G \leftarrow \mathcal{L}^G \cup \{(m, k)\}$
9: **return** k

Fig. 7: OW-PCA adversary B simulates game 3 for IND-CCA adversary A in the proof for Theorem 1

Proof. *Game 0* is the standard KEM IND-CCA game. The decapsulation oracle $\mathcal{O}^{\mathtt{Decap}}$ executes the decapsulation routine using the challenge keypair and return the results faithfully. The queries made to the hash oracles $\mathcal{O}^G, \mathcal{O}^H$ are recorded to their respective tapes $\mathcal{L}^G, \mathcal{L}^H$.

Game 1 is identical to game 0 except that the true decapsulation oracle $\mathcal{O}^{\mathtt{Decap}}$ is replaced with a simulated oracle $\mathcal{O}_1^{\mathtt{Decap}}$. Instead of directly decrypting c' as in the decapsulation routine, the simulated oracle searches through the tape $\mathcal{L}^G$ to find a matching query $(\tilde{m}, \tilde{k})$ such that $\tilde{m}$ is the decryption of c'. The simulated oracle then uses $\tilde{k}$ to validate the tag t against c'.

If the simulated oracle accepts the queried ciphertext as valid, then there is a matching query that also validates the tag, which means that the queried ciphertext is honestly generated. Therefore, the true oracle must also accept the queried ciphertext. On the other hand, if the true oracle rejects the queried ciphertext, then the tag is simply invalid under the MAC key $k = G(\mathtt{Dec}(\mathtt{sk}', c'))$.

Therefore, there could not have been a matching query that also validates the tag, and the simulated oracle must also rejects the queried ciphertext.

This means that from the adversary A's perspective, game 1 and game 0 differ only when the true oracle accepts while the simulated oracle rejects, which means that t is a valid tag for c' under $k = G(\mathtt{Dec}(\mathtt{sk}', c'))$, but k has never been queried. Under the random oracle model, such k is a uniformly random sample of $\mathcal{K}_{\mathtt{MAC}}$ that the adversary does not know, so for A to produce a valid tag is to produce a forgery against the MAC under an unknown and uniformly random key. Furthermore, the security game does not include a MAC oracle, so this is a zero-time forgery. While zero-time forgery is not a standard security definition for a MAC, we can bound it by the advantage of a one-time forgery adversary C:

$$P\left[\mathcal{O}^{\mathtt{Decap}}(c) \neq \mathcal{O}_1^{\mathtt{Decap}}(c)\right] \leq \mathtt{Adv}_{\mathtt{OT\text{-}MAC}}(C).$$

Across all q decapsulation queries, the probability that at least one query is a forgery is thus at most $q \cdot P\left[\mathcal{O}^{\mathtt{Decap}}(c) \neq \mathcal{O}_1^{\mathtt{Decap}}(c)\right]$. By the difference lemma:

$$\mathtt{Adv}_{G_0}(A) - \mathtt{Adv}_{G_1}(A) \leq q \cdot \mathtt{Adv}_{\mathtt{OT\text{-}MAC}}(C).$$

Game 2 is identical to game 1, except that the challenger samples a uniformly random MAC key $k^* \xleftarrow{\$} \mathcal{K}_{\mathtt{MAC}}$ instead of deriving it from m^*. From A's perspective the two games are indistinguishable, unless A queries G with the value of m^*. Denote the probability that A queries G with m^* by $P[\mathtt{QUERY\ G}]$, then:

$$\mathtt{Adv}_{G_1}(A) - \mathtt{Adv}_{G_2}(A) \leq P\left[\mathtt{QUERY\ G}\right].$$

Game 3 is identical to game 2, except that the challenger samples a uniformly random shared secret $K_0 \xleftarrow{\$} \mathcal{K}_{\mathtt{KEM}}$ instead of deriving it from m^* and t. From A's perspective the two games are indistinguishable, unless A queries H with $(m^*, \cdot)$. Denote the probability that A queries H with $(m^*, \cdot)$ by $P[\mathtt{QUERY\ H}]$, then:

$$\mathtt{Adv}_{G_2}(A) - \mathtt{Adv}_{G_3}(A) \leq P\left[\mathtt{QUERY\ H}\right].$$

Since in game 3, both K_0 and K_1 are uniformly random and independent of all other variables, no adversary can have any advantage: $\mathtt{Adv}_{G_3}(A) = 0$.

We will bound $P[\mathtt{QUERY\ G}]$ and $P[\mathtt{QUERY\ H}]$ by constructing a OW-PCA adversary B against the underlying PKE that uses A as a sub-routine. B's behaviors are summarized in Figure 7.

B simulates game 3 for A: receiving the public key pk and challenge encryption c'^*, B samples random MAC key and session key to produce the challenge encapsulation, then feeds it to A. When simulating the decapsulation oracle, B uses the plaintext-checking oracle to look for matching queries in $\mathcal{L}^G$. When simulating the hash oracles, B uses the plaintext-checking oracle to detect when $m^* = \mathtt{Dec}(\mathtt{sk}', c'^\star)$ has been queried. When m^* is queried, B terminates A and returns m^* to win the OW-PCA game. In other words:

$$P\left[\texttt{QUERY G}\right] \leq \texttt{Adv}_{\texttt{OW-PCA}}(B),$$
$$P\left[\texttt{QUERY H}\right] \leq \texttt{Adv}_{\texttt{OW-PCA}}(B).$$

Combining all equations above produce the desired security bound.

4 Applications

In this section we will survey a number of existing public-key encryption schemes and discuss the applicability of the encrypt-then-MAC transformation to these schemes.

4.1 RSA

RSA [13] is a public-key cryptosystem proposed by Rivest, Shamir, and Adleman in 1978. A summary of its subroutines can be found in Figure 8.

RSA `KeyGen`	RSA `Enc`	RSA `Dec`

Fig. 8: Textbook RSA

In its original formulation (typically referred to as "textbook RSA"), the RSA cryptosystem is one-way secure against chosen-plaintext attack (OW-CPA) under the conjectured intractability of the RSA problem [13] (Definition 1). Furthermore, it is easy to show that the RSA cryptosystem is a trapdoor permutation on the multiplicative group $\mathbb{Z}_N^*$. In other words, under a given keypair $\texttt{pk} = (N, e), \texttt{sk} = d$, $m^e = c \mod N$ if and only if $c^d \mod N$. Consequently, textbook RSA is one-way secure against plaintext-checking attack, because the plaintext-checking oracle can be perfectly simulated using only the public key, which means that access to a plaintext-checking oracle offers no additional advantage.

Definition 1 (RSA problem). *Let $N = pq$ be the product of two prime numbers. Let e be an integer that is relatively prime to $\phi(N) = (p-1)(q-1)$, and let $d = e^{-1} \mod \phi(N)$. Let m be a uniformly random sample in $\mathbb{Z}_N^*$ and let $c = m^e \mod N$. Given N, e, c, find m.*

Although textbook RSA is OW-PCA secure and thus a suitable candidate for the encrypt-then-MAC transformation, there exists simpler and faster CCA secure KEM transformation. For example, one can apply the $U_m^{\not\perp}$ variant of the modular Fujisaki-Okamoto transformation, which encapsulates the shared secret by directly hashing a randomly sampled plaintext. The resulting KEM

(Figure 9) is largely identical to the RSA-KEM proposed by Victor Shoup in [14]. Compare to the encrypt-then-MAC transformation, RSA-KEM offers identically tight security bound while it removes the need for deriving the MAC key and computing the MAC tag.

RSA-KEM KeyGen	RSA-KEM Enc	RSA-KEM Dec

Fig. 9: RSA-KEM

4.2 ElGamal

We show that the DHAES/DHIES hybrid encryption scheme is a special case of the encrypt-then-MAC transformation. Specifically, we will sketch a proof of the following lemma:

Lemma 1. *For every OW-PCA adversary A against the ElGamal cryptosystem, there exists a Gap Diffie-Hellman problem solver B such that:*

$$Adv_{GapDH}(B) = Adv_{OW\text{-}PCA}(A).$$

In other words, ElGamal is OW-PCA secure under the Gap Diffie-Hellman assumption.

Each ElGamal cryptosystem [5] is parameterized by a cyclic group $G = \langle g \rangle$ of prime order $q > 2$. A summary of the routine is shown in Figure 10:

`KeyGen()`	`Enc`($\mathtt{pk} = g^x, m \in G$)	`Dec`($\mathtt{sk} = x, c = (w, v) \in G^2$)
1: $x \xleftarrow{\$} \mathbb{Z}_q$ 2: $\mathtt{sk} \leftarrow x$ 3: $\mathtt{pk} \leftarrow g^x$ 4: **return** $(\mathtt{pk}, \mathtt{sk})$	**Require:** $m \in G$ 1: $y \xleftarrow{\$} \mathbb{Z}_q$ 2: $w \leftarrow g^y$ 3: $v \leftarrow m \cdot (g^x)^y$ 4: **return** $c = (w, v)$	1: $\hat{m} \leftarrow (w^x)^{-1} \cdot v$ 2: **return** $\hat{m}$

Fig. 10: ElGamal cryptosystem

The security of ElGamal cryptosystem reduces to the conjectured intractability of the computational and decisional Diffie-Hellman problem:

Definition 2 (computational Diffie-Hellman problem). *Let* $x, y \xleftarrow{\$} \mathbb{Z}_q$ *be uniformly random samples. Given* (g, g^x, g^y)*, compute* g^{xy}*.*

Definition 3 (decisional Diffie-Hellman problem). *Let $x, y, z \xleftarrow{\$} \mathbb{Z}_q$ be uniformly random samples. Let $h \xleftarrow{\$} \{g^z, g^{xy}\}$ be randomly chosen between g^z and g^{xy}. Given (g, g^x, g^y, h), determine whether h is g^{xy} or g^z*

It is also conjectured in [1] (and later extensively studied in [11]) that for certain choice of cyclic group G, the computational Diffie-Hellman problem remains intractable even if the adversary as access to a restricted decisional Diffie-Hellman oracle. This assumption is captured in the Gap Diffie-Hellman problem:

Definition 4 (Gap Diffie-Hellman problem). *Let $G = \langle g \rangle$ be a cyclic group of prime order $q > 2$. Let $x, y \xleftarrow{\$} \mathbb{Z}_q$ be uniformly random samples. Given (g, g^x, g^y) and a restricted DDH oracle $\mathcal{O}^{DDH} : (u, v) \mapsto [\![u^x = v]\!]$, compute g^{xy}.*

We now present the proof for Lemma 1.

Proof. We will prove by a sequence of games. A summary can be found in Figure 11

$G_0 - G_2$

1: $x \xleftarrow{\$} \mathbb{Z}_q$
2: $m^* \xleftarrow{\$} G$
3: $y \xleftarrow{\$} \mathbb{Z}_q, w \leftarrow g^y$
4: $v \leftarrow m^* \cdot (g^x)^y$ ▷ G_0 - G_1
5: $v \xleftarrow{\$} G$ ▷ G_2
6: $c^* \leftarrow (w, v)$
7: $\hat{m} \xleftarrow{\$} A^{\mathtt{PCO}}(g^x, c^*)$ ▷ G_0
8: $\hat{m} \xleftarrow{\$} A^{\mathtt{PCO}_1}(g^x, c^*)$ ▷ G_1 - G_2
9: **return** $[\![\hat{m} = m^*]\!]$ ▷ G_0 - G_1
10: **return** $[\![\hat{m} = w^{-x} \cdot v]\!]$ ▷ G_2

$\mathtt{PCO}(m, c = (w, v))$

1: **return** $[\![m = (w^x)^{-1} \cdot v]\!]$

$\mathtt{PCO}_1(m, c = (w, v))$

1: **return** $[\![(w^x) = m^{-1} \cdot v]\!]$

Fig. 11: The sequence of games in proving Lemma 1

Game 0 is the OW-PCA game. Adversary A has access to the plaintext-checking oracle $\mathtt{PCO}$ and wins the game if it can correctly recover the challenge plaintext m^*.

Game 1 is identical to game 0, except that the formulation of the $\mathtt{PCO}$ is changed. When servicing the plaintext-checking query $(m, c = (w, v))$, $\mathtt{PCO}_1$ checks whether w^x is equal to $m^{-1} \cdot v$. Observe that in the cyclic group G, the algebraic expressions in $\mathtt{PCO}$ and $\mathtt{PCO}_1$ are equivalent, which means that $\mathtt{PCO}_1$ behaves identically to $\mathtt{PCO}$.

Game 2 is identical to game 1 except for two modifications: first, when computing the challenge ciphertext, v is no longer computed from m^* but is randomly sampled; second, the win condition changed from $\hat{m} = m^*$ to $\hat{m} = w^{-x} \cdot v$. It is easy to verify that Game 0 through Game 2 are algebraically equivalent:

$$\mathtt{Adv}_0(A) = \mathtt{Adv}_1(A) = \mathtt{Adv}_2(A).$$

The Gap Diffie-Hellman adversary B can perfectly simulate game 2 for A (see Figure 12): B receives as the Gap Diffie-Hellman problem inputs g^x and g^y. g^x simulates an ElGamal public key, where as g^y simulates the first component of the challenge ciphertext. As in game 2, the second component of the challenge ciphertext can be randomly sampled. Finally, the $\mathtt{PCO}_1$ from game 2 can be perfectly simulated using the restricted DDH oracle $\mathcal{O}^{\mathrm{DDH}}$.

$B^{\mathcal{O}^{\mathrm{DDH}}}(g, g^x, g^y)$

1: $w \leftarrow g^y$
2: $v \xleftarrow{\$} G$
3: $c^* \leftarrow (w, v)$
4: $\hat{m} \xleftarrow{\$} A^{\mathtt{PCO}_2}(g^x, c^*)$
5: **return** $\hat{m}^{-1} \cdot v$

$\mathcal{O}^{\mathrm{DDH}}(u, v)$

1: **return** $[\![u^x = v]\!]$

$\mathtt{PCO}_2(m, c = (w, v))$

1: **return** $\mathcal{O}^{\mathrm{DDH}}(w, m^{-1} \cdot v)$

Fig. 12: Gap Diffie-Hellman adversary B simulates game 2 for A

If A wins game 2, then its output is $\hat{m} = w^{-x} \cdot v = g^{-xy} \cdot v$, so $m^{-1} \cdot v$ is g^{xy}, the correct answer to the Gap Diffie-Hellman problem. In other words, B solves its Gap Diffie-Hellman problem if and only if A wins the simulated game 2: $\mathtt{Adv}_2(A) = \mathtt{Adv}_{\mathrm{GapDH}}(B)$.

4.3 Lattice-based cryptosystems

Applying the encrypt-then-MAC transformation to the PKE subroutines of Kyber/ML-KEM (which we will call KyberPKE for short) will not produce CCA secure KEM. This is because KyberPKE is not one-way secure against plaintext checking attack. An abundance of literature [17,16,8] described plaintext-checking attacks that can recover the complete secret key using a few thousand oracle queries. Here we review the key-recovery plaintext-checking attack presented in [8].

Let $q = 3329, n = 256$, let $R_q = \mathbb{Z}_q[x]/\langle x^n + 1\rangle$. The secret key of KyberPKE is $\mathtt{sk} = \mathbf{s} \in R_q^k$ where $k = 2, 3, 4$ for depending on the security level. The coefficients of the secret key are sampled from centered binomial distribution

CBD_{η_1}. The ciphertext takes the form $c = (\mathbf{u} \in R_q^k, v \in R_q)$. The decryption routine is described in Figure 13

$\texttt{KyberPKE.Dec}(\texttt{sk}, c)$

Require: $c = (\mathbf{u}, v)$
Require: $\texttt{sk} = \mathbf{s}$
1: $w \leftarrow v - \langle \mathbf{s}, \mathbf{u} \rangle$
2: $m = \texttt{Round}(w)$ ▷ $m \in Z_2[x]/\langle x^n + 1 \rangle$
3: **return** m

Fig. 13: KyberPKE decryption routine

For $1 \leq i \leq k, 0 \leq j \leq n-1$ denote the i-th entry in a polynomial vector $\mathbf{s} \in R_q^k$ by s_i and the coefficient of the j-th power term of a polynomial $v \in R_q$ by $v[j]$. For some fixed i, j, an adversary can learn some information about $s_i[j]$ by crafting malformed ciphertext $\tilde{c} = (\tilde{\mathbf{u}}, \tilde{v})$ where $\tilde{u}_i[1], \tilde{v}[j]$ are chosen by the adversary, and all other coefficients are set to 0. When decrypting this malformed ciphertext, $w[j] = \tilde{v}[j] - s_i[j]\tilde{u}_i[0]$ and all other coefficients of w are 0s. With specific choices of values for $\tilde{u}_i[0], \tilde{v}[j]$, whether $w[j]$ will round to 1 or 0 will depend on the value of $s_i[j]$. This can be used to perform a binary search that recovers the value of $s_i[j]$ in $\lceil \log_2(2 \cdot \eta_1 + 1) \rceil$ plaintext-checking queries. See Table 1 for an example of plaintext-checking query strategy. Such a binary search can then be repeated $n \cdot k$ times to completely recover the secret key.

$u_i[0]$	$v[j]$	if $m[j] = 1$	if $m[j] = 0$
208	416	$s_i[j] \in \{-3\}$	$s_i[j] \in \{-2, -1, 0, 1, 2, 3\}$
208	624	$s_i[j] \in \{-3, -2\}$	$s_i[j] \in \{-1, 0, 1, 2, 3\}$
208	832	$s_i[j] \in \{-3, -2, -1\}$	$s_i[j] \in \{0, 1, 2, 3\}$
208	1040	$s_i[j] \in \{-3, -2, -1, 0\}$	$s_i[j] \in \{1, 2, 3\}$
208	1248	$s_i[j] \in \{-3, -2, -1, 0, 1\}$	$s_i[j] \in \{2, 3\}$
208	1456	$s_i[j] \in \{-3, -2, -1, 0, 1, 2\}$	$s_i[j] \in \{3\}$
208	-1456	$s_i[j] \in \{-2, -1, 0, 1, 2, 3\}$	$s_i[j] \in \{-3\}$
208	-1248	$s_i[j] \in \{-1, 0, 1, 2, 3\}$	$s_i[j] \in \{-3, -2\}$
208	-1040	$s_i[j] \in \{0, 1, 2, 3\}$	$s_i[j] \in \{-3, -2, -1\}$
208	-832	$s_i[j] \in \{1, 2, 3\}$	$s_i[j] \in \{-3, -2, -1, 0\}$
208	-624	$s_i[j] \in \{2, 3\}$	$s_i[j] \in \{-3, -2, -1, 0, 1\}$
208	-416	$s_i[j] \in \{3\}$	$s_i[j] \in \{-3, -2, -1, 0, 1, 2\}$

Table 1: Plaintext-checking query strategy for Kyber512: $\eta_1 = 3, d_u = 10, d_v = 4$

4.4 Code-based cryptosystems

4.5 Other cryptosystems

5 Application to Classic McEliece

In this section, we instantiate the encrypt-then-MAC KEM transformation using the subroutines of classic McEliece and a variety of MAC implementations. We will discuss the modifications and their rationale, as well as the performance implications.

Classic McEliece is a IND-CCA secure post-quantum KEM submitted to NIST's Post Quantum Cryptoraphy (PQC) standardization project and is currently one of three viable round 4 candidate. Classic McEliece is primarily based on the McEliece cryptosystem first proposed by Robert McEliece in 1978 (citation!) and later improved by Harald Niederreiter in 1986. For a high-level summary, Classic McEliece generates the secret key by sampling a random binary Goppa code, then computes the systematic form of the canonical parity check matrix as the public key. The message space is the set of all codewords with fixed Hamming weight. Each plaintext message is encrypted by multiplying it with the row-reduced parity check matrix, and the resulting syndrome is returned as the ciphertext. For decryption, the secret key, which contains the decoding algorithm, recovers the locations of the errors from the syndrome, which is then used to reconstruct the original codeword.

The PKE subroutines described in the previous paragraph is OW-CPA secure under the conjectured intractability of the Syndrome Decoding Problem (SDP) for random binary Goppa code. However, because the encryption routine is deterministic, the PKE routine does not have indistinguishability. Instead, Classic McEliece applies a non-standard Fujisaki-Okamoto transformation in which the decryption routine checks ciphertext integrity using re-encryption. Finally, indistinguishability is achieved using implicit rejection: the decryption routine will output fake session key on invalid ciphertext that an adversary cannot distinguish from true session key any more than the adversary can recover the decryption without the secret key.

Whether the PKE subroutines of Classic McEliece is OW-PCA secure remains unproven: although the encryption routine is deterministic, the decryption routine might not be injective. Whether the decryption routine is injective likely depends on the choice of binary Goppa decoder. Classic McEliece currently implements syndrome decoding using the Berlekamp-Massey algorithm, which is inherently not injective (there are distinct infinite sequences that correspond to the same shortest LFSR). However, there have been many attempts at constructing plaintext-checking attacks on Classic McEliece using side channels [17][16], but there is no known plaintext-checking attacks to date.

Under the conjectured OW-PCA security of the PKE subroutines Classic McEliece, we speculate that applying the encrypt-then-MAC transformation to the PKE subroutines should result in a CCA secure KEM, which we will call `mceliece+`. A summary of `mceliece+`'s routines can be found in figure 14

`mceliece+ KeyGen`

Fig. 14: `mceliece+`'s routines

5.1 Choosing a message authentication code (MAC)

In Figure **??**, while H, G and KDF are instantiated by SHA3-256, SHA3-512 and Shake256, respectively, there could be various choices of standardized and well-analyze MAC algorithms. For implementation, we instantiated the MAC with a selection that covered a wide range of MAC designs, including Poly1305 [2], GMAC [10], CMAC [9][3], and KMAC [7]. All MACs are parameterized with a 256-bit key to ensure that MAC keys are at least as hard to guess as the underlying PKE plaintext. On the other hand, all MACs use a 128-bit tag except for KMAC, which can have a variable tag length. We suspect that a 128-bit tag might be insufficient for the 192-bit and 256-bit security levels, so for instantiation with the higher security levels, we only use KMAC with 192-bit and 256-bit tag length outputs.

Poly1305 and GMAC are both Carter-Wegman style MACs [18] that compute the tag using finite field arithmetic. Generically speaking, Carter-Wegman MAC operates by breaking the message into message blocks that can then be parsed into finite field elements. The tag is computed by evaluating a polynomial whose coefficients are the message blocks and whose indeterminate is the secret key (also called a *hash key*). Specifically, Poly1035 operates in the prime field $\mathbb{F}_q$ where $q = 2^{130} - 5$ whereas GMAC operates in the binary field $\mathbb{F}_{2^{128}}$.

CMAC is based on the CBC-MAC with the block cipher instantiated from AES-256. To compute a CMAC tag, the message is first broke into 128-bit blocks with appropriate padding. Each block is first XORed with the previous block's output, then encrypted under AES using the symmetric key. The final output is XORed with a sub key derived from the symmetric key, before being encrypted for one last time.

KMAC is based on the SHA-3 family of sponge functions [15]. We chose KMAC-256, which uses Shake256 as the underlying extendable output functions. KMAC is the only MAC to support variable key and tag length, though we fixed the key length at 256 bits. On the other hand, we chose the appropriate tag length for the corresponding security level: when instantiated with ML-KEM-512, the tag length is 128 bits; with ML-KEM-768, the tag length is 192 bits; with ML-KEM-1024, the tag length is 256 bits.

We implemented `mceliece+` by modifying the reference implementation. MAC implementations are taken from OpenSSL. C code is compiled using Apple Clang 15.0.0. Performance measurement is run on Apple Silicon M1 chip. CPU

clock is measured using kernel clock `mach_absolute_time`. Each rouine is run 10000 times, with median time reported in Table 2.

KEM	Enc	Dec	Enc + Dec
mceliece348864	215	2471	2686
mceliece348864 + poly1305	316 (+46.98%)	2074 (-16.07%)	2390 (-11.02%)
mceliece348864 + gmac	335 (+55.81%)	2087 (-15.54%)	2422 (-9.83%)
mceliece348864 + cmac	340 (+58.14%)	2092 (-15.34%)	2432 (-9.46%)
mceliece348864 + kmac256	304 (+41.40%)	2093 (-15.30%)	2397 (-10.76%)

KEM	Enc	Dec	Enc + Dec
mceliece460896	487	6694	7181
mceliece460896 + poly1305	514 (+5.54%)	5784 (-13.59%)	6298 (-12.30%)
mceliece460896 + gmac	565 (+16.02%)	5809 (-13.22%)	6374 (-11.24%)
mceliece460896 + cmac	544 (+11.70%)	5905 (-11.79%)	6449 (-10.19%)
mceliece460896 + kmac256	570 (+17.04%)	5760 (-13.95%)	6330 (-11.85%)

KEM	Enc	Dec	Enc + Dec
mceliece6688128	816	7500	8316
mceliece6688128 + poly1305	889 (+8.95%)	6509 (-13.21%)	7398 (-11.04%)
mceliece6688128 + gmac	890 (+9.07%)	6521 (-13.05%)	7411 (-10.88%)
mceliece6688128 + cmac	900 (+10.29%)	6540 (-12.80%)	7440 (-10.53%)
mceliece6688128 + kmac256	901 (+10.42%)	6546 (-12.72%)	7447 (-10.45%)

KEM	Enc	Dec	Enc + Dec
mceliece6960119	699	7262	7961
mceliece6960119 + poly1305	735 (+5.15%)	6389 (-12.02%)	7124 (-10.51%)
mceliece6960119 + gmac	753 (+7.73%)	6450 (-11.18%)	7203 (-9.52%)
mceliece6960119 + cmac	763 (+9.16%)	6428 (-11.48%)	7191 (-9.67%)
mceliece6960119 + kmac256	765 (+9.44%)	6303 (-13.21%)	7068 (-11.22%)

KEM	Enc	Dec	Enc + Dec
mceliece8192128	858	7464	8322
mceliece8192128 + poly1305	955 (+11.31%)	6547 (-12.29%)	7502 (-9.85%)
mceliece8192128 + gmac	957 (+11.54%)	6550 (-12.25%)	7507 (-9.79%)
mceliece8192128 + cmac	945 (+10.14%)	6546 (-12.30%)	7491 (-9.99%)
mceliece8192128 + kmac256	957 (+11.54%)	6574 (-11.92%)	7531 (-9.50%)

Table 2: Performance comparison between Classic McEliece and `mceliece+`

6 Conclusion

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