# **Big Book of RF Engineering Notes**

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# **RF Engineering**

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### **Noise in RF Systems**

Thermal noise floor is  $kT_0B$ , which is the noise power produced by a matched resistor at the IEEE reference temperature  $T_0=290K$  over a bandwidth of B. If the bandwidth is 1Hz, then the thermal noise floor is -174dBm/Hz.

IEEE definition of noise figures (NF) or noise factor (F) are as follows:

$$F = \frac{SNR_{in}}{SNR_{out}}$$

$$NF = 10 \log_{10}(F)$$
(1)

$$NF = 10\log_{10}(F) \tag{2}$$

where  $SNR_{in}$  is the signal-to-noise ratio at the device input, when the input noise is thermal-limited. In other words, the input noise power is equal to the noise power produced by a matched resistor at a physical temperature of  $T_0 = 290K$ .

#### **Example: Measurement of Amplifier Noise Figure Using Cold Source**

In this section, we discuss the noise figure measurement of an RF low-noise amplifier using the cold source method. We will use the TinySA spectrum analyzer and the NanaVNA vector network analyzer. The device under test is the Nooelec LaNA HF, which is an LNA covering the 50kHz to 150MHz band.

With the cold source method, we first measure the gain of the amplifier using the VNA.

Next, we measure the noise power generated by the amplifier. We first put a  $50\Omega$  termination directly at the input port of the TinySA. We measure a noise floor of  $-169.3 \mathrm{dBm/Hz}$ . Since the thermal noise floor is  $10 \log_{10} (1.38 \times 10^{-23} \times 10^3 \times 290) = -173.9 dBm/Hz$ , we conclude that the noise generated by the internal circuitry of the TinySA increased the total noise power by approximately  $4.6 \mathrm{dBm/Hz}$ . This means the noise figure of TinySA is about 4.6dB. Alternatively, we can say it has an effective noise temperature of approximately  $290\left(10^{4.6/10}-1\right)=546.4\mathrm{K}$ , referred to the inputs.

Having characterize the noise properties of the TinySA, we can now measure the DUT cascaded with its internal receiver. We will then remove the added noise of the TinySA from the overall measurements, to obtain the noise figure of the DUT itself.

#### **Noise Cascade**

When multiple noisy stages are cascaded, the total effective noise temperature referred to the input of the first stage is given by:

$$T_{sys} = T_1 + \frac{T_2}{G_1} + \frac{T_3}{G_1 G_2} + \cdots$$
 (3)

Where  $T_n$  is the effective noise temperature of the  $n^{th}$  stage, *referred to its own input*. Moving the reference location of an effective noise temperature value can be done by simply multiplying/dividing the gains of the appropriate stages. In [3], it can be seen that the noise temperature of the very first stage dominates the total temperature, if there is large gain afterwards. Hence in a receiver it is desirable to put an LNA as close to the antenna as possible, to reduce the impact of noise in the later stages.

We can also calculate the noise figure of the entire system. Each stage of the system will have its own specified noise figure. Remember that the noise figure [2] is defined for when the input noise power is equal to exactly  $kT_0B$ . So we cannot simply cascade the noise figures of the individual components together, because the input to the latter stages are no longer a matched resistor. Instead, it is safer to calculate the effective noise temperature of each stage using its specified noise figure, cascade the temperatures together using [3], then convert the total temperature back to a total noise figure:

$$F_{sys} = F_1 + \frac{F_2 - 1}{G_1} + \frac{F_3 - 1}{G_1 G_2} + \cdots$$
(4)

# **Signal Distortion in RF Systems**

Sources of nonlinear signal distortion:

- Gain compression
- Intermodulation

#### **Oscillators**

Model for a noisy oscillator

$$v(t) = A(t)\cos\left[\omega_c t + \phi_n(t)\right] \tag{5}$$

where A(t) captures amplitude noise, and  $\phi_n(t)$  captures the phase noise.

We can interpret phase noise as phase modulation of the desired ideal oscillator output signal  $\cos(\omega_c t)$ , except that the modulation signal is pure noise. For simplicity, let us first consider the case when the phase modulation is a single-tone sinusoid. This is a helpful example, since we can interpret a noisy signal as the summation of infinitely many sinusoids all with random amplitudes and phases.

#### **Effect of Phase Noise on EVM**

#### **White Phase Noise**

Consider the case where  $\phi_n(t)$  is Gaussian distributed with zero mean and standard deviation  $\sigma_{rms}$ . This means the probability density function of  $\phi_n(t)$  is given by

$$f(\phi) = \frac{1}{\sqrt{2\pi\sigma_{rms}}} e^{-\frac{\phi^2}{2\sigma_{rms}^2}} \tag{6}$$

### **Oscillator Pulling**

Oscillator pulling happens when a strong (undesired) signal couples to a resonator, causing its resonance frequency to change. It is also called **injection locking** or **injection pulling**.

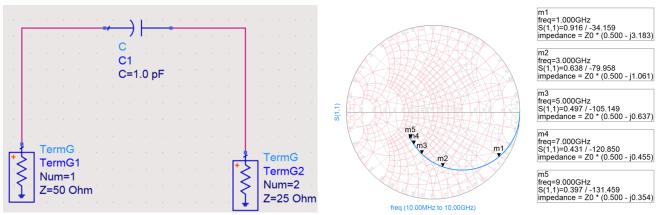
### **Impedance Matching**

#### **LC Components on Smith Chart**

This section describes how shunt and series LC components behave on the smith chart, which can be used to intuitively derive potential matching network topologies.

#### **Series Capacitor**

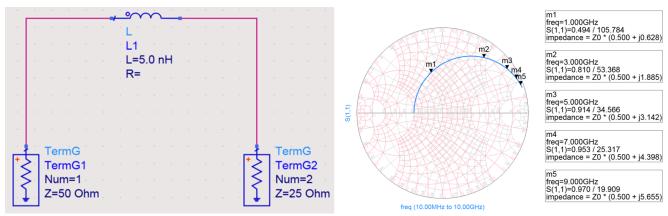
As the frequency increases from DC to infinity, the input impedance swings from open circuit (OC) to the terminating resistance.



Frequency response of series capacitor on the Smith chart.

Note that the series capacitor is a high pass circuit. This means its effect on the impedance is stronger at low frequencies, and weaker at high frequencies. This can be seen from the impedance plot on the Smith chart. The high-frequency points are far away from the right side of the Smitch chart, where any tiny movement represents a huge change in impedance, as can be seen by the axis ticks.

#### **Series Inductor**

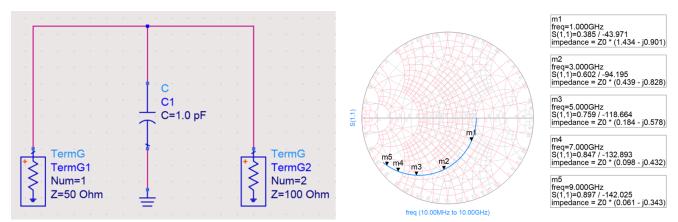


Frequency response of series inductor on the Smith chart.

At DC, the series inductor behaves as a perfectly conducting wire; hence the input impedance is just that of the terminating resistance. As the frequency increases to infinity, the input impedance swings towards OC.

The series inductor is a low pass circuit, meaning it has stronger effect to the input impedance at high frequencies. In the plot above, we see that the low frequency points are far away from the right side of the Smith chart, while the high frequency points are clustered on the right side, where any small movements represents huge deviations in the impedance.

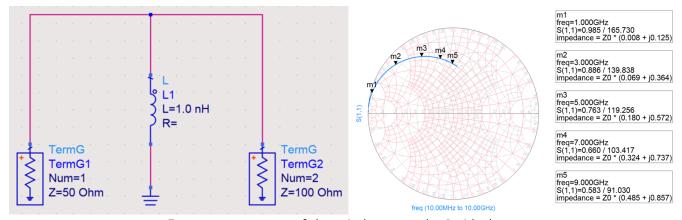
#### **Shunt Capacitor**



Frequency response of shunt capacitor on the Smith chart.

The shunt capacitor is a low pass circuit, meaning it will have larger impact on the admittance of the admittance of the circuit at high frequencies. On the Smith chart, the high frequency points are clustered to the left side, where any small movements correspond huge changes in admittance.

#### **Shunt Inductor**



Frequency response of shunt inductor on the Smith chart.

#### **Series RLC Resonator**

#### **Shunt RLC Resonator**

### **Broadband Matching Techniques**

#### **Reducing Q-factor Using LC**

The idea here is to twist the  $S_{11}$  trace on the Smith chart by adding components that affect the two ends, such that they become closer to the real axis. This lowers the Q factor of the network and allows us to match it over a broader bandwidth.

## **Modulation and Coding**

Different modulation formats and code rates will require different SINAD (signal-to-noise and distortion).

## **Mixed Signal Systems**

# **Antenna Engineering**

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- 2. Microstrip Patch Antenna
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## **Wire Antenna**

## **Microstrip Patch Antenna**

## Parabolic Antenna

# **Phased Array Antennas**

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- 1. Beamforming
- 2. <u>Digital Beamforming</u>
- 3. Nonlinearity in Phased Arrays

## **Beamforming**

Define the steering vector (also known as the array manifold vector)  $\overline{v}_{\vec{k}}$  as

$$\bar{v}_{\vec{k}}[n] = e^{j\vec{k}\cdot\vec{r}_n} \tag{7}$$

Where  $\vec{r}_n$  is the position of the  $n^{th}$  antenna. We can interpret the steering vector as the voltages measured at the positions of the antennas with an unit-amplitude plane wave incident from the direction of  $\vec{k}$ , or, in the direction of  $-\vec{k}$ .

In a transmitting array, the total transmitted signal to the direction of  $\vec{k}$  is equal to  $\bar{w}^\dagger \bar{v}_{\vec{k}}$ , where  $\bar{w}$  is a vector corresponding to the weights of the antennas.

When  $\bar{v}_{\vec{k}}$  is parallel with  $\bar{w}$ , the response (transmitted or received power) is maximized. When the two vectors are orthogonal, the array response is minimized.

#### **Conventional Beamformer**

The conventional beamformer for a beam towards the direction of  $ec{k}$  has weights equal to

$$\bar{w} = \bar{v}_{\vec{k}} \tag{8}$$

Minimum Variance Distortionless Response (MVDR) Beamformer
Linearly Constrained Minimum Covariance (LCMV) Beamformer

## **Digital Beamforming**

### **Spatial Multiplexing**

Spatial multiplexing refers to the transmission of multiple independent streams of data to different spatial positions or angles, using the same antenna aperture. This is easily achieved through digital beamforming.

Theoretically speaking, the maximum number of independently steerable beams is equal to the number of antenna elements. However in practice, we would not want too many beams, as it increases the peak-to-average ratio if the total emitted signal, which lowers the PA efficiency/increases chance of saturation.

#### **Delay Steering**

## **Nonlinearity in Phased Arrays**

# **Digital Signal Processing**

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1. Polyphase Signal Processing

# **Polyphase Signal Processing**