

Big Book of Antenna Engineering Notes

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Phased Array Antennas

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Discrete Fourier Transform

The array factor of a phased array antenna can be efficiently computed using the Fast Fourier Transform (FFT), which is a method to compute the Discrete Fourier Transform (DFT). This is not only useful in evaluating the performance of the array, but also valuable in gaining intuition on the physics behind certain phenomena in phased array systems, such as the generation of grating lobes, and nonlinear spatial mixing.

Beamforming

Define the steering vector (also known as the array manifold vector) $\vec{v}_{\vec{k}}$ as

$$\vec{v}_{\vec{k}}[n] = e^{j\vec{k} \cdot \vec{r}_n} \quad (1)$$

Where \vec{r}_n is the position of the n^{th} antenna. We can interpret the steering vector as the voltages measured at the positions of the antennas with an unit-amplitude plane wave incident *from* the direction of \vec{k} , or, in the direction of $-\vec{k}$.

In a transmitting array, the total transmitted signal to the direction of \vec{k} is equal to $\vec{w}^\dagger \vec{v}_{\vec{k}}$, where \vec{w} is a vector corresponding to the weights of the antennas.

When $\vec{v}_{\vec{k}}$ is parallel with \vec{w} , the response (transmitted or received power) is maximized. When the two vectors are orthogonal, the array response is minimized.

Conventional Beamformer

The conventional beamformer for a beam towards the direction of \vec{k} has weights equal to

$$\vec{w} = \vec{v}_{\vec{k}} \quad (2)$$

Minimum Variance Distortionless Response (MVDR) Beamformer

Linearly Constrained Minimum Covariance (LCMV) Beamformer

Digital Beamforming

Spatial Multiplexing

Spatial multiplexing refers to the transmission of multiple independent streams of data to different spatial positions or angles, using the same antenna aperture. This is easily achieved through digital beamforming.

Theoretically speaking, the maximum number of independently steerable beams is equal to the number of antenna elements. However in practice, we would not want too many beams, as it increases the peak-to-average ratio of the total emitted signal, which lowers the PA efficiency/increases chance of saturation.

Delay Steering

Dithering

Dithering is a technique whereby random noise is deliberately added to the transmitted signals of each of the antennas in a phased array, in order to spatially decorrelate the quantization noise.

When there is spatial correlation between the quantization errors, the error signal also adds coherently in the direction of the main beam, forming directive radiation.

Dithering decorrelates the quantization error, causing the energy to be spread out (ideally isotopically).

Nonlinearity in Phased Arrays