

US Spine Simulation and Results

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MBP rotation
Sept 8-Oct 14

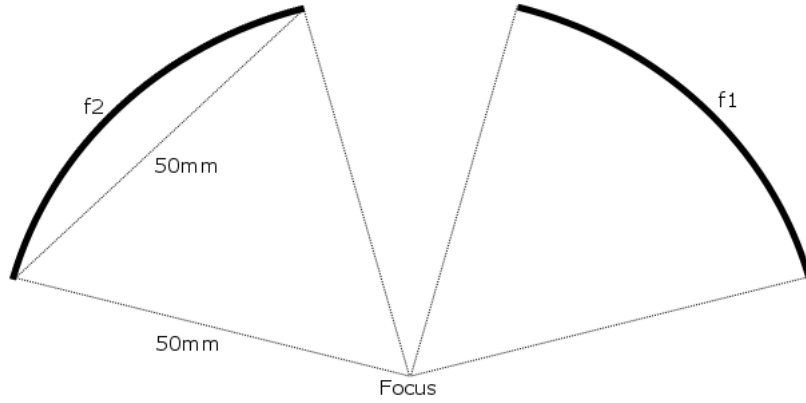
September 16, 2016

1 Introduction

This document will outline my ultrasound code and results. I have constructed a simple two-dimensional simulation using existing code from the k-wave package to construct a two-transistor system.

2 System 1: Homogeneous Medium, Two Elements, Two Frequencies

The first system I created was a system of two curved transducers, each with a radius of curvature of 50mm, and each subtending $\pi/2$ radians. The two transducers are driven at frequencies f_1 and f_2 . The focal point of the two transducers are the same. I create the transducers by defining source points at a 50mm radius for $\pi/12 \leq \Theta_1 \leq 5\pi/12$ and $7\pi/12 \leq \Theta_2 \leq 11\pi/12$. The system setup is shown in the following figure.



2.1 Half-Maximum Profiles

The first test was to vary the frequency f_1 of the right hand side transducer, while keeping the frequency of the second transducer constant $f_2 = 0.25\text{MHz}$. Implementing multiple frequencies in k-wave require that each source point have its frequency assigned to it. In the current implementation, then I've simply looped over all points, and set the frequency of the source points on the left half of the computational box to f_2 and those on the right half to f_1 . Take care with the current code if you move the transducers around. It may be advisable to write a foolproof version of the frequency assignment part of the code.

We are interested in the pressure profile of the system near the focal point, for different frequencies $0.15\text{MHz} \leq f_1 \leq 0.35\text{MHz}$, tested in increments of 10kHz. The following figures show the 2D root-mean-square pressure profiles. The points of half-maximum pressure are outlined in black.

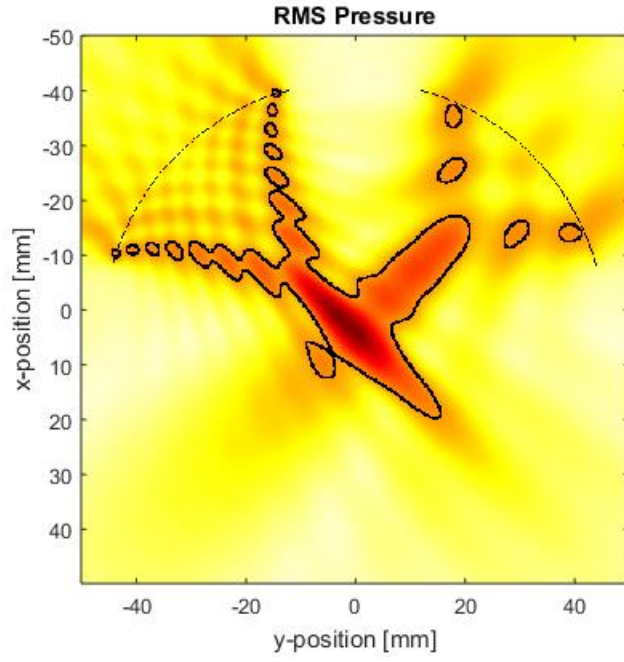


Figure 1: RMS pressure profile for $f_1 = 0.15\text{MHz}$, $f_2 = 0.25\text{MHz}$

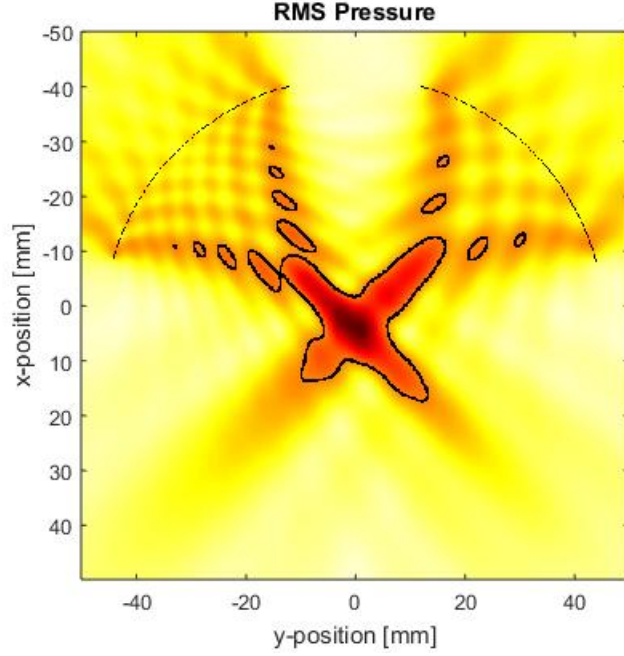


Figure 2: RMS pressure profile for $f_1 = 0.16\text{MHz}$, $f_2 = 0.25\text{MHz}$

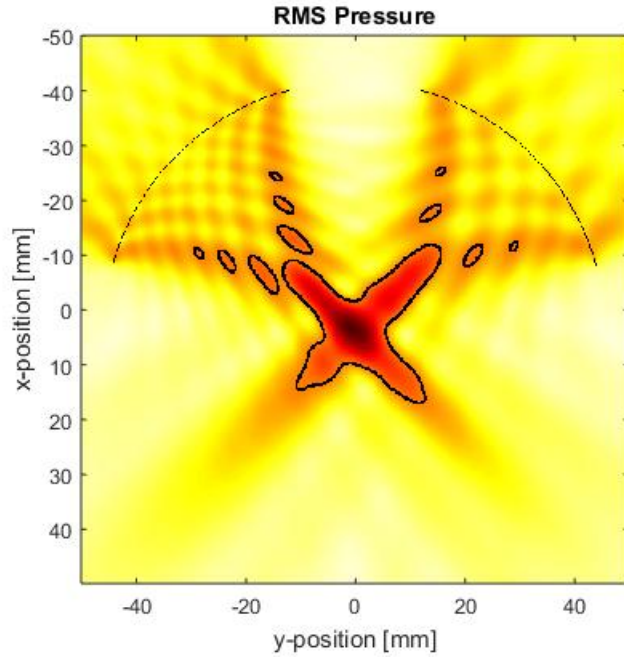


Figure 3: RMS pressure profile for $f_1 = 0.17\text{MHz}$, $f_2 = 0.25\text{MHz}$

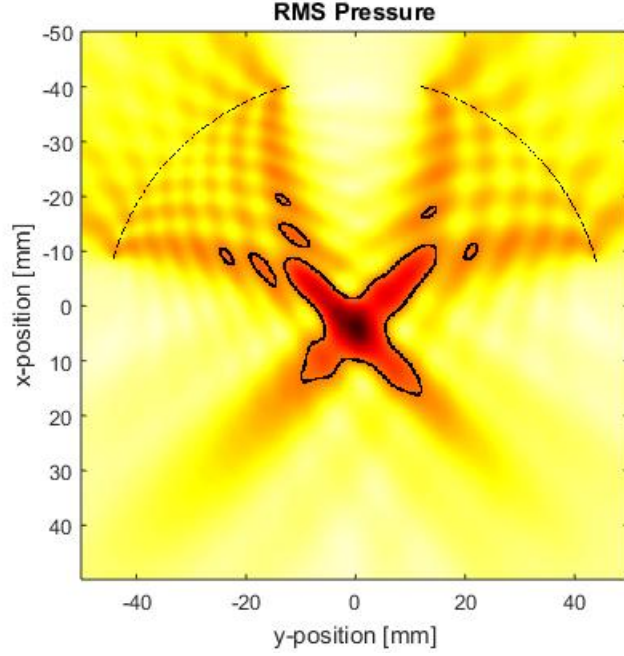


Figure 4: RMS pressure profile for $f_1 = 0.18\text{MHz}$, $f_2 = 0.25\text{MHz}$

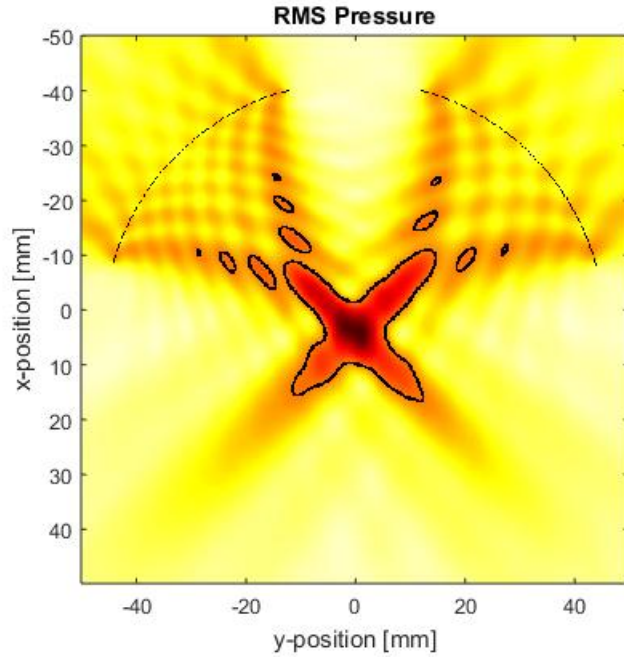


Figure 5: RMS pressure profile for $f_1 = 0.19\text{MHz}$, $f_2 = 0.25\text{MHz}$

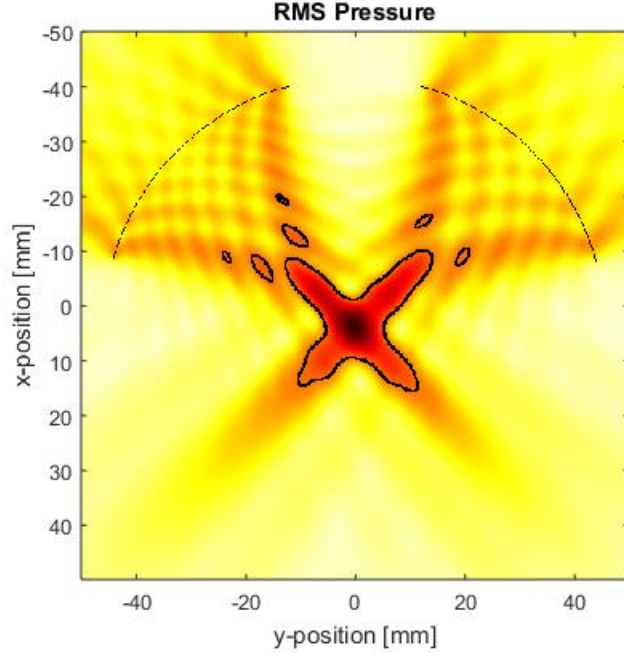


Figure 6: RMS pressure profile for $f_1 = 0.20\text{MHz}$, $f_2 = 0.25\text{MHz}$

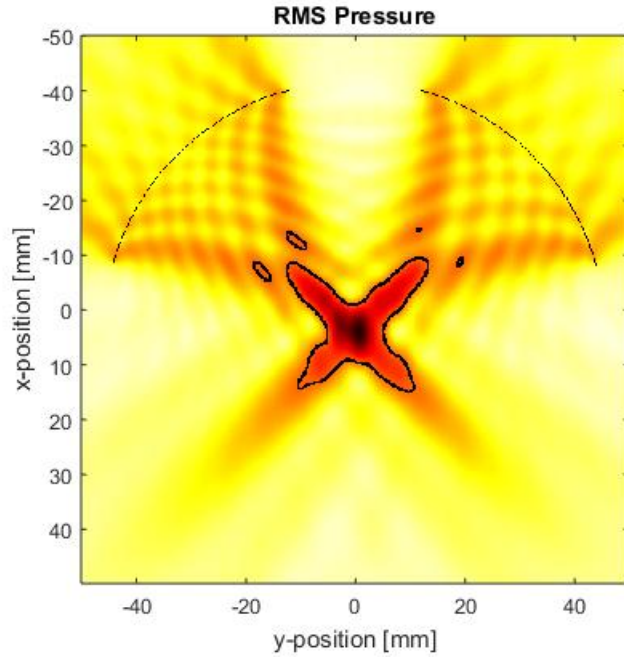


Figure 7: RMS pressure profile for $f_1 = 0.21\text{MHz}$, $f_2 = 0.25\text{MHz}$

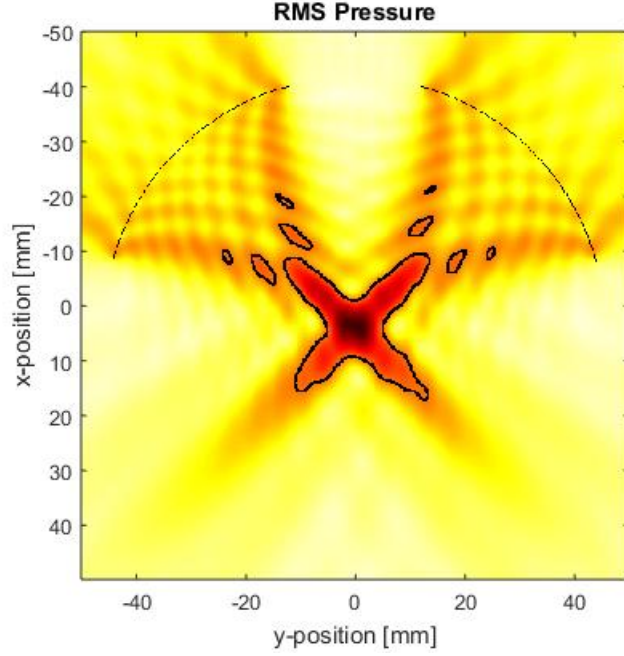


Figure 8: RMS pressure profile for $f_1 = 0.22\text{MHz}$, $f_2 = 0.25\text{MHz}$

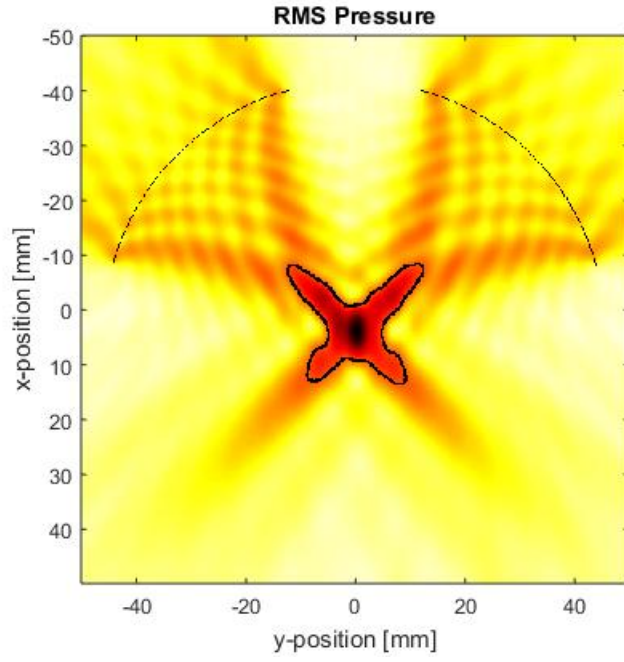


Figure 9: RMS pressure profile for $f_1 = 0.23\text{MHz}$, $f_2 = 0.25\text{MHz}$

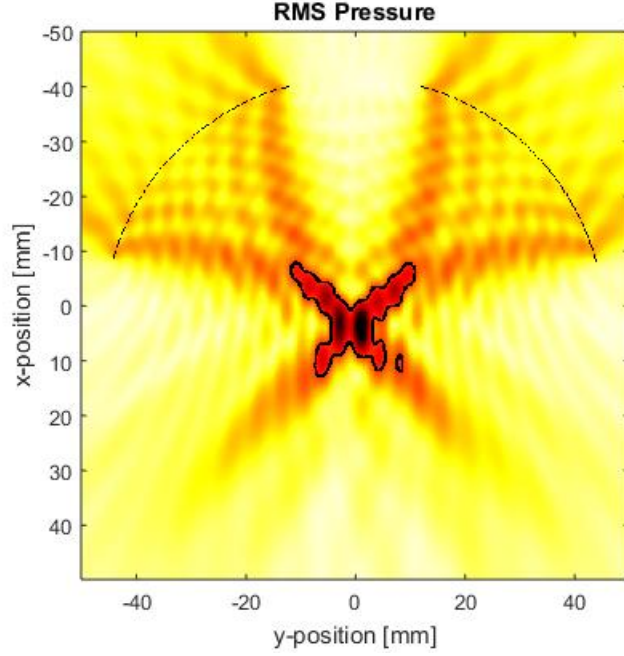


Figure 10: RMS pressure profile for $f_1 = 0.24\text{MHz}$, $f_2 = 0.25\text{MHz}$

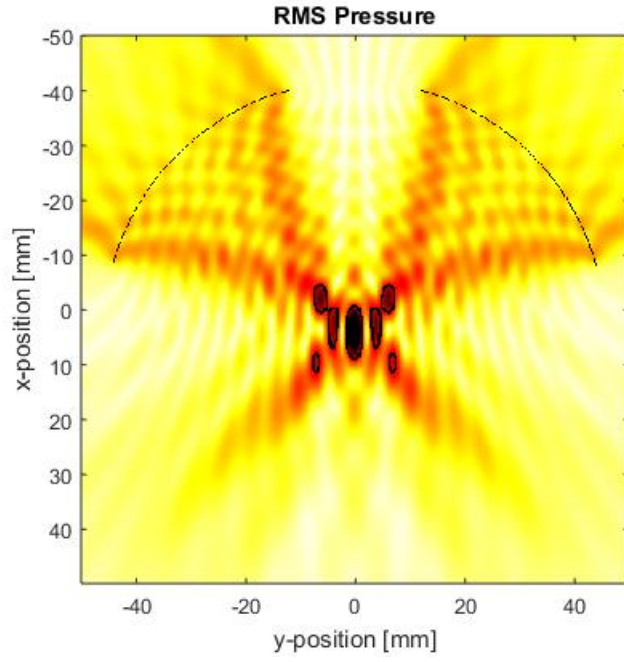


Figure 11: RMS pressure profile for $f_1 = 0.25\text{MHz}$, $f_2 = 0.25\text{MHz}$

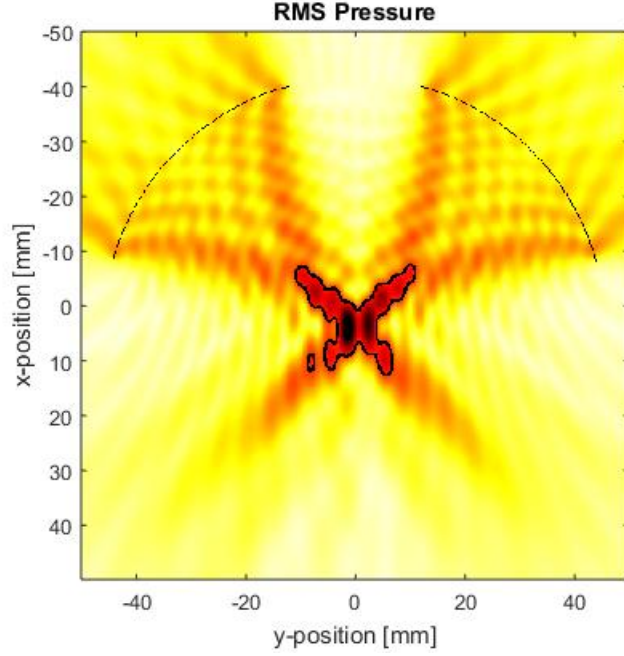


Figure 12: RMS pressure profile for $f_1 = 0.26\text{MHz}$, $f_2 = 0.25\text{MHz}$

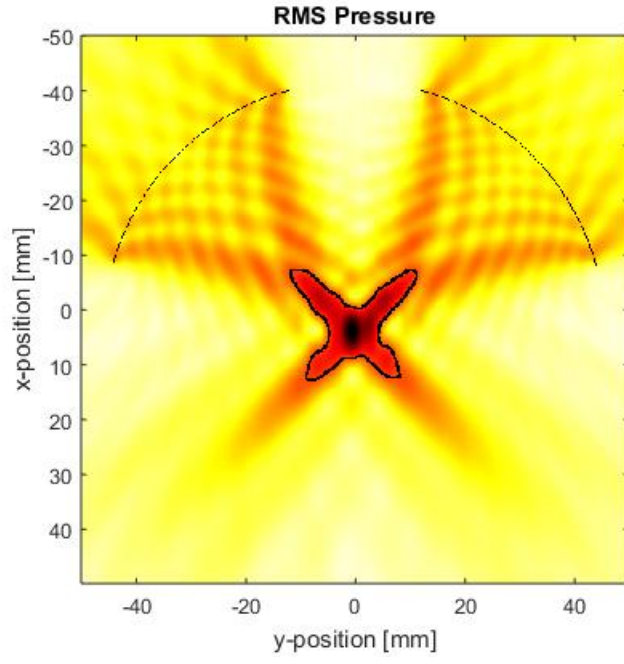


Figure 13: RMS pressure profile for $f_1 = 0.27\text{MHz}$, $f_2 = 0.25\text{MHz}$

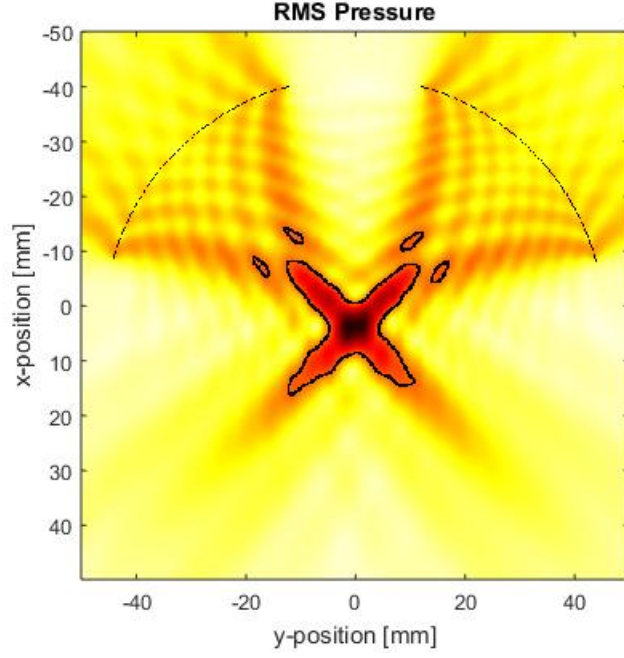


Figure 14: RMS pressure profile for $f_1 = 0.28\text{MHz}$, $f_2 = 0.25\text{MHz}$

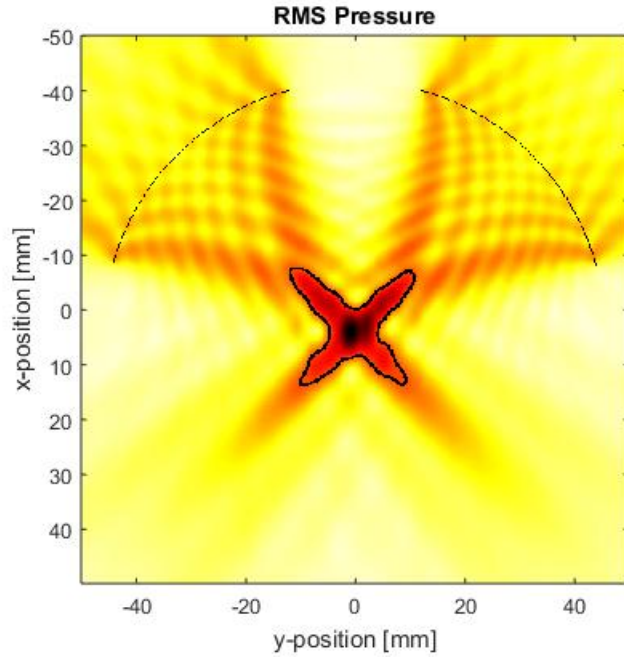


Figure 15: RMS pressure profile for $f_1 = 0.29\text{MHz}$, $f_2 = 0.25\text{MHz}$

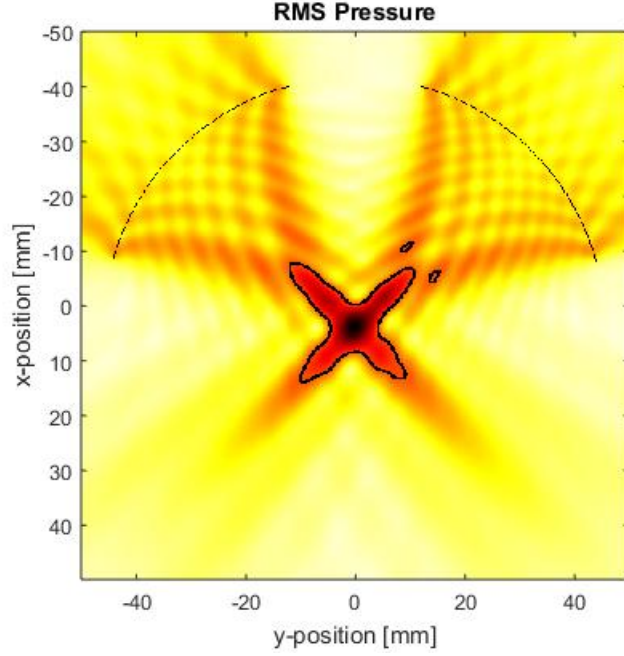


Figure 16: RMS pressure profile for $f_1 = 0.30\text{MHz}$, $f_2 = 0.25\text{MHz}$

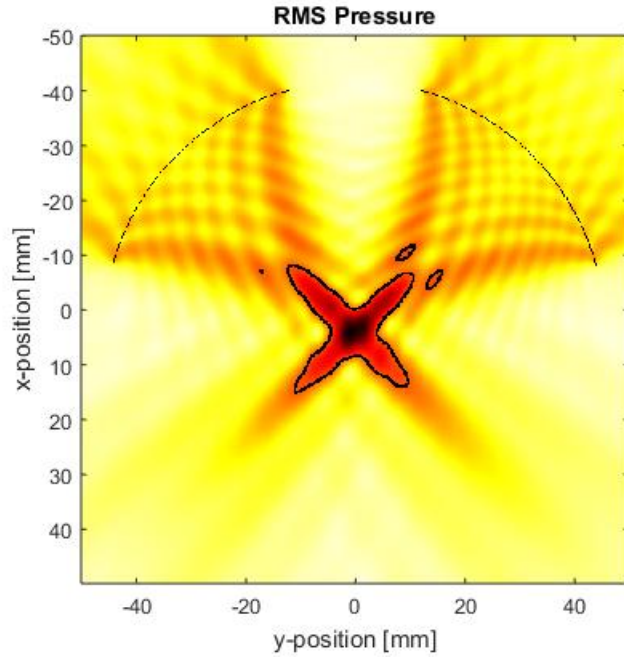


Figure 17: RMS pressure profile for $f_1 = 0.31\text{MHz}$, $f_2 = 0.25\text{MHz}$

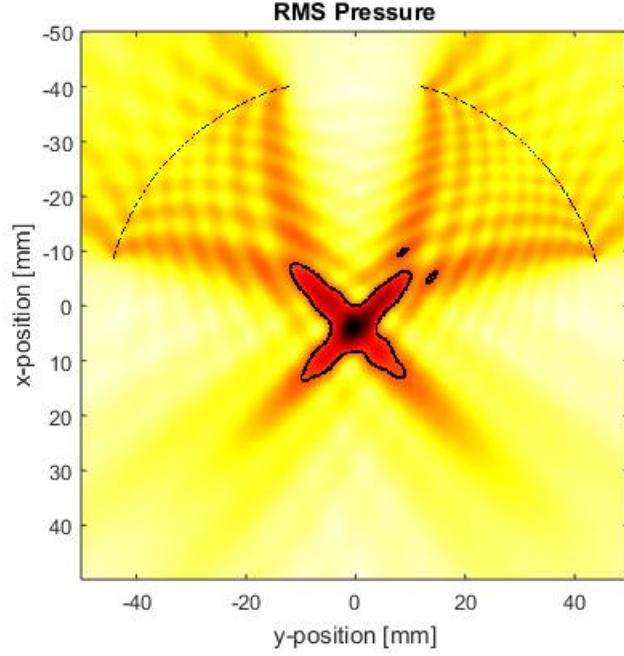


Figure 18: RMS pressure profile for $f_1 = 0.32\text{MHz}$, $f_2 = 0.25\text{MHz}$

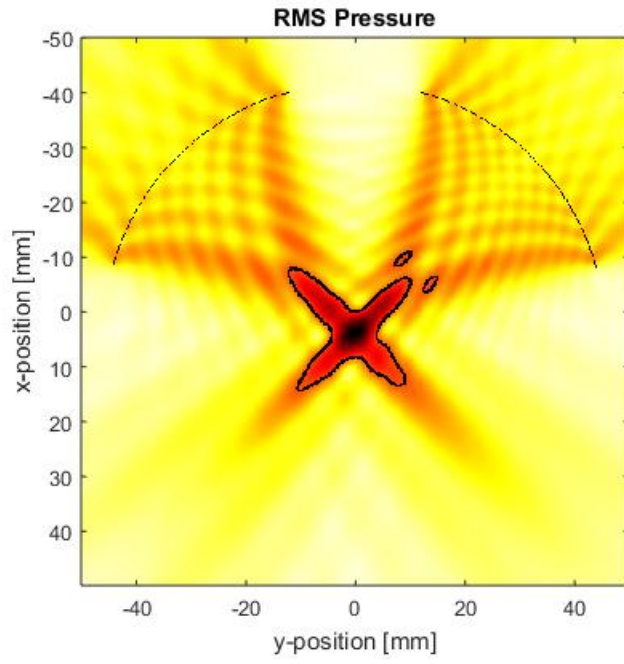


Figure 19: RMS pressure profile for $f_1 = 0.33\text{MHz}$, $f_2 = 0.25\text{MHz}$

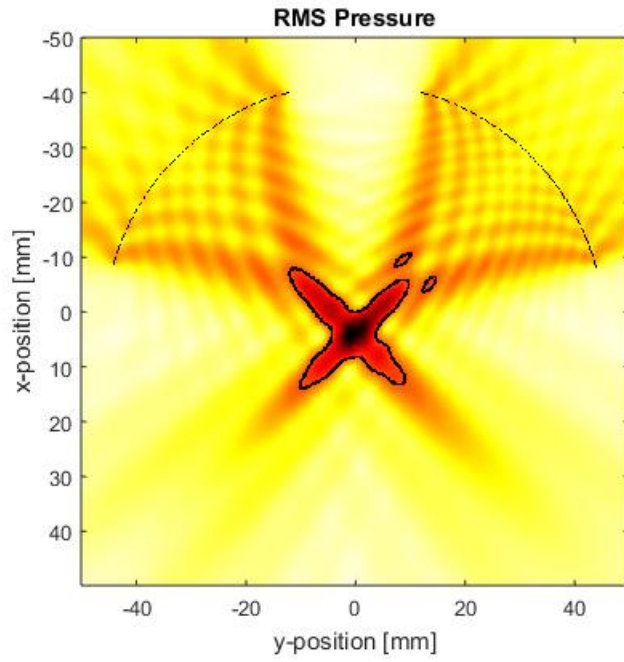


Figure 20: RMS pressure profile for $f_1 = 0.34\text{MHz}$, $f_2 = 0.25\text{MHz}$

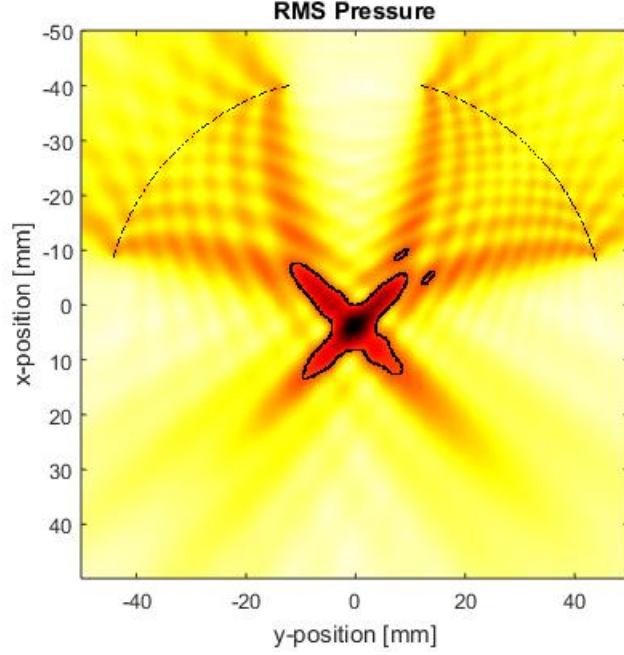


Figure 21: RMS pressure profile for $f_1 = 0.35\text{MHz}$, $f_2 = 0.25\text{MHz}$

2.2 FWHM for different frequencies

Another informative metric can be the FWHM of the profile. However, this is more useful for pressure profiles that are approximately Gaussian. The method I used for finding the points with half maximum pressure returns coordinates for all points, not just those around the central maximum. This is remediable, but the profiles remain non-circular. The FWHM of the distributions can easily be calculated from the coordinates (x_{HM}, y_{HM}) by first calculating the coordinate of the centre of the HM points (x_{HMc}, y_{HMc}) :

$$x_{HMc} = \frac{1}{N} \sum_{i=1}^N x_{HM_i} \cdot dx, \quad y_{HMc} = \frac{1}{N} \sum_{i=1}^N y_{HM_i} \cdot dy \quad (1)$$

where N is the number of HM points. We can calculate the average distance d of the HM points from the HM centre using:

$$d = \frac{1}{N} \sum_{i=1}^N \sqrt{(x_{HM_i} - x_{HMc})^2 + (y_{HM_i} - y_{HMc})^2} \cdot dx \quad (2)$$

The FWHM is then approximately equal to two times the average distance between an HM point and the centre of the HM point distribution. For HM distributions that are highly non-Gaussian, then there is little purpose in calling it the FWHM - it's simply the average width of the half-maximum RMS pressure profile. Despite this, I'll continue calling it FWHM for the time being. The FWHM is shown for $200\text{kHz} \leq f_1 \leq 300\text{kHz}$ in Figure 2.2.

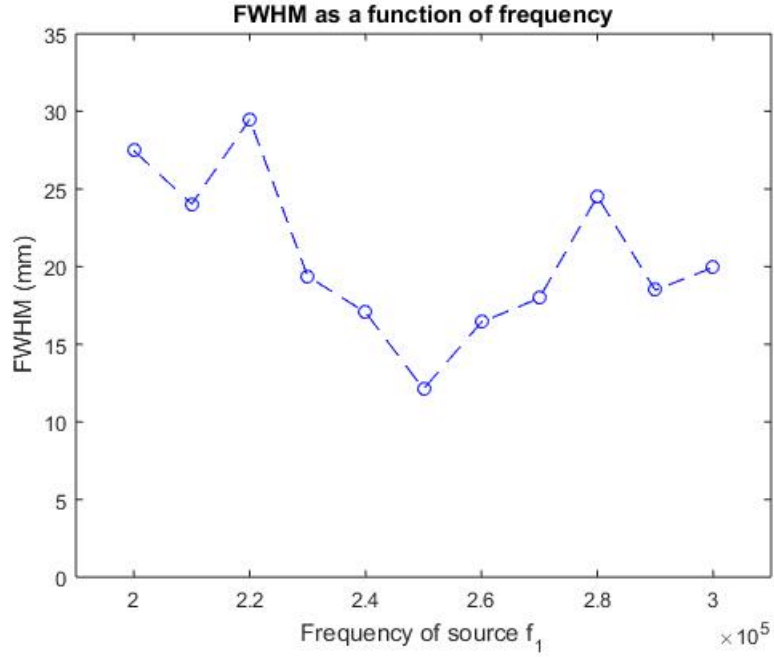


Figure 22: The FWHM of the RMS pressure distribution for $200\text{kHz} \leq f_1 \leq 300\text{kHz}$, $f_2 = 250\text{kHz}$.

2.3 Centre of HM profile

I've included this for curiosity's sake. Here I plot the centre of the FWHM profile, for $200\text{kHz} \leq f_1 \leq 300\text{kHz}$.

2.4 Maximum RMS Pressure

We are also interested in the location of the maximum RMS intensity for different frequencies. These are shown in the following Figure 2.4.

There does not appear to be any pattern in the location of the maximum RMS pressure coordinates. In the x-dimension, the maxima are confined to within three computational grid points, approximately +4mm away from the focal point of the independent transducers. In the y-dimension, the maxima remain closely clustered around the focal point.

3 Adding Inclusions to the Simulation

3.1 Results from Cadavers

3.2 Acoustic Properties

3.3 Simulation

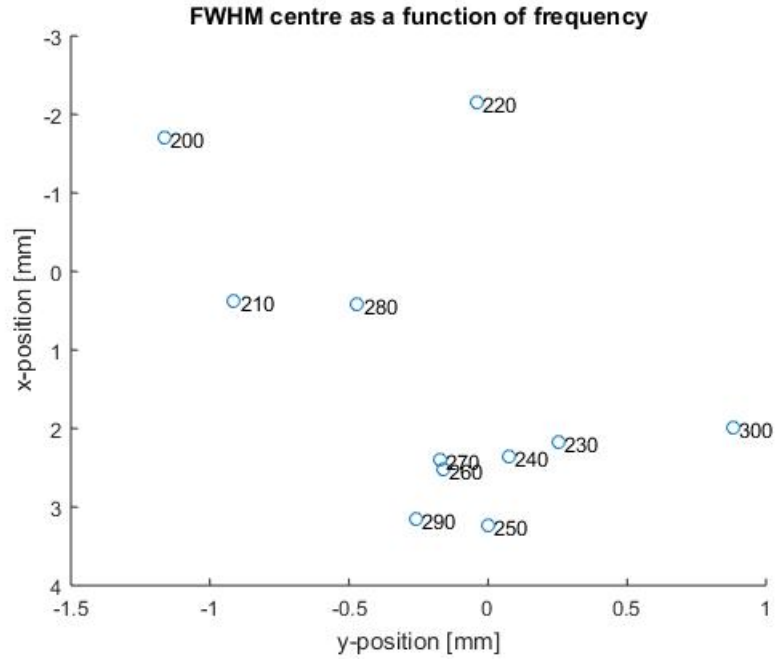


Figure 23: The coordinates of the centre of the FWHM profile of the RMS pressure distribution for $200\text{kHz} \leq f_1 \leq 300\text{kHz}$, $f_2 = 250\text{kHz}$.

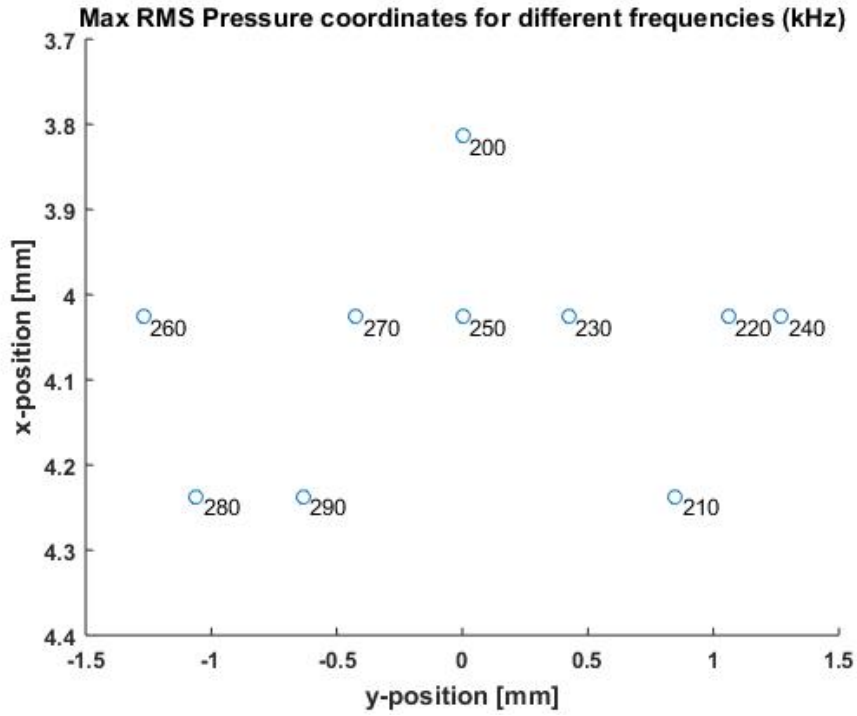


Figure 24: The Maximum RMS pressure for $200\text{kHz} \leq f_1 \leq 300\text{kHz}$.