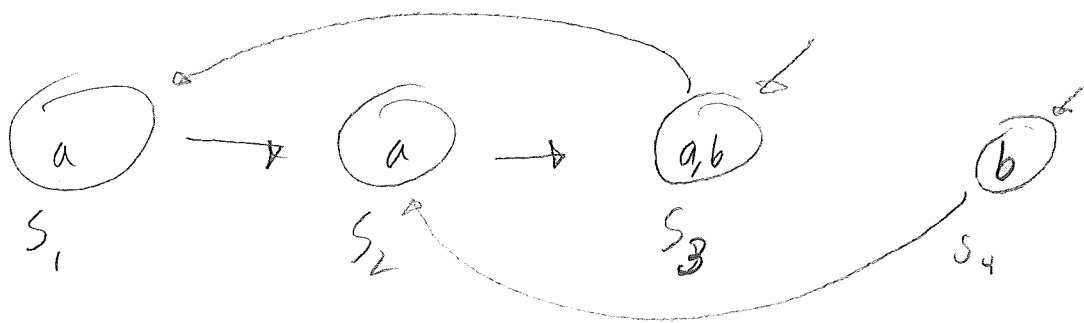


1)



- $Xa = \{s_1, s_2, s_3\}$
- $XXXa = \{s_1, s_2, s_3, s_4\}$
- $[] b = \{s_3, s_4\}$
- $[] < a = \{s_1, s_2, s_3, s_4\}$
- $[] b \cup a = \{s_4, s_3, s_1, s_2\}$
- $< b \cup a = \{s_4, s_3, s_1, s_2\}$

2)

- Any door will not open unless the elevator is present
 - $P = \{ \text{door open, elevator present} \}$
 - $L+L = [] \neg (\text{door open} \wedge \neg \text{elevator present})$
- Requested floor will be served eventually.
 - $P = \{ \text{Requested, served} \}$
 - $L+L = [] \neg (\text{Requested} \wedge \neg \text{served})$
- The elevator repeatedly returns to floor 0
 - $P = \{ 0 \}$ - Meaning floor position
 - $L+L = [] \wedge < 0$
- Top floor is served immediately
 - $P = \{ R_{\text{top}}, S_{\text{top}} \}$ request served
 - $L+L = [] \neg (R_{\text{top}} \wedge \neg X S_{\text{top}})$

3)

- Number of items in a buffer may not exceed N
 - Safety

$$-CTL^* = [\Box A \neg N+1]$$

$$P = \{1, 2, 3, \dots, N, N+1\}$$

current buffer count

- If a process reaches a location l_i just before a critical section, it should not be blocked forever

$$P = \{l_i, \text{critical}\}$$

- Liveness

$$-CTL^* = [\Box A \neg (l_i \wedge \neg \langle \rangle \text{critical})]$$

- Clients may not retain resources forever

$$P = \{\text{obtain}, \text{release}\}$$

- Liveness

$$-CTL^* = [\Box A \neg (\text{obtain} \wedge \neg \langle \rangle \text{release})]$$

- it is always cloudy before it rains

- Safety cloudy, Rain

$$-P = \{C, R\}$$

$$[\Box A (\neg R \cup C)]$$

- 4) Transition $!_p \rightarrow p$ will happen at most once

$$([\Box \neg p] \cup [\Box p]) \vee [\Box \neg p]$$

- 5) Infinitely many transitions from $!_p$ to p .

$$\neg (p \wedge \neg \langle \rangle \neg p) \wedge \neg (\neg p \wedge \neg \langle \rangle p)$$

$$p \rightarrow \neg p \wedge \neg p \rightarrow \neg p$$

$$b) ((r \rightarrow p \vee y) \wedge (y \rightarrow y \vee g) \wedge (g \rightarrow g \vee r))$$

$$!(r \wedge !r \vee y) \wedge !(y \wedge !y \vee g) \wedge !(g \wedge !g \vee r)$$

assuming $r \rightarrow y \rightarrow g \rightarrow r$ not
 $g \rightarrow y \rightarrow r \rightarrow g$

$$\Rightarrow q \rightarrow \neg p \vee r$$

↓

$$!(q \vee \neg(\neg p \vee r))$$

