Hence, me get a set of solutions. ence, x = 0, y = 2 x = 0, y = -2 x = 2, y = 0 x = -2, y = 0Ans. All the 4 solutions satisfy the constraint n2+y= 4. Also f(0,2) and f (0,-2) = -4 < minima and f(2,0) and f(-2,0) = 4 < maxima. Hence, the above A sets of x and y are the extrema of the function. (b) f(x,y) = xy - logx subject to x+2y=0 Introducing tagrange's multiplier, we get a new function, $\phi(x,y) = n^2y - \log x - \lambda(x+2y)$ Now, differentiating partially wirt x and y, 30(x,y) =0 or 3 (22y - logx - 1 (x+2y))=0 or 2 my - 1 = 0 St = 1 - or 2 2 2 y - 1 - 1 = 0 - (i) = 0 or \frac{0}{04} (x^2y - logx -) (x+2y) = 0 or $n = \pm \sqrt{2} \lambda$

for $\chi'=\frac{1}{2}$ ($\chi=\frac{1}{2}$) we can plugin this value of χ in eqn (i) and get the below: $4\lambda y - \lambda x - 1 = 0 \qquad (7i)$ or x (4y- \(\frac{12}{2}\)=1 or 42y- 12x. x=1 or y = 1+12x.x Now, me replace these values of a & y m the constraint. or $\sqrt{2\lambda} + 2 \times \left(\frac{1 + \sqrt{2\lambda} - \lambda}{2 \times \lambda}\right) = 0$ or 2. 1. 121 + 1+ 121. 1 = 0 3/-12/ =- 1/= ASDIA or $\lambda - \sqrt{2\lambda} = -\frac{1}{3}$ or $\lambda^2 \times 2\lambda = \frac{1}{9}$ or $\lambda^3 = \frac{1}{18}$ or $\lambda = 3\frac{1}{18}$ $\chi = + \sqrt{2} = + \sqrt{2} \times \frac{1}{18} = \sqrt{2} \times \frac{1}{3^{2/5} \times 2^{1/3}}$ $=\sqrt{\left(\frac{2}{3}\right)^{2/3}}$ = $\left(\frac{2}{3}\right)$ = 1 + x h =

For x= (2)113,4 y is always the which mean

constraint 2+2y=0 can't for 22 tre and y2 tre Now, let's calculate y for $x = -\sqrt{2}\lambda$. 4 dy - dx - 1 = 0 from equation (ii) For 2 = - \(\frac{1}{2}\chi \). 4 24 + J2x.x-1=0 y = 1-121.1 Now, putting this value in x+2y=0 $-\sqrt{2}\lambda + 2\times \left(\frac{1-\sqrt{2}\lambda\cdot\lambda}{2}\right)=0$ - VZA. 2 \ + 1 - VZA. \ =0 +31. 12/5 - 1 / 75/1.5 1. V21 = 1 - 48 1-46 or $\lambda \times 2\lambda = \frac{1}{9}$ or $\lambda^3 = \frac{1}{18}$ or $\lambda = 3\frac{1}{18}$ $\frac{2\lambda}{2\lambda} = -3\frac{2}{3} = 1 - \left(\frac{2}{3}\right)^{1/3} \times \left(\frac{1}{18}\right)^{1/3}$ 1+xx =

 $\frac{1}{2}\left(-\frac{1}{3}\right)\times 3$ $(2)^{2/3} (3)^{\frac{1}{3}}$ $\frac{1 \times 2}{2} = \frac{1}{2} \times (2)^{2/3} \times (3)^{1/3}$ $= \frac{1}{2} \times (2)^{2/3} \times (3)^{1/3}$ = $-\left(\frac{2}{3}\right)^{1/3}$ and $y = \frac{1}{2} \times \left(\frac{2}{3}\right)$ the solutions. (App) supposed $-\frac{2}{3}^{1/3} + \frac{2}{3} \times \frac{1}{3} \times \frac{2}{3}^{1/3} = 0$ $x = -\frac{2}{3}$ 1/3 nohich is -ve in f(m, y), $\log(x)$ is not defined this value of x. (negative values) solu exists for this fu

(e) f(x,y) = x2+2my +y2-2x subject to Introducing tagrange's multiplier, the function now becomes, $\phi(x,y) = x^2 + 2xy + y^2 - 2x - \lambda (x^2 + y^2 + 1)$ Partially differentiating $\phi(x,y)$ wit it & & a p(x14) = 2x + 2y - 2 - 2x/=0 or n+y-1-x 1=0 Eli (3) 2 x (1-x) +y =1-(i) 2 d(114) = 2x + 2y + 2y \ = 0 or xty thy =0 or $-y(1+\lambda) = x - (ii)$ Putting this value of x in (i), we get -y(1+x)(1-x) +y=1 or $-y(1-\lambda^2)+y=1$ or -y + y12 +y = 1 or $\lambda^2 = \frac{1}{y}$ or $y = \frac{1}{\lambda^2}$ TEE = X vo Putting this value of me get:

Putting this value of
$$\chi$$
 in the constraint $\chi^2-y^2=-1$, we get
$$\frac{(1+\lambda)^L}{\lambda^4}-\frac{1}{\lambda^4}=-1$$
or
$$\frac{(\lambda^2+2\lambda-1)}{\lambda^4}=-1$$
or
$$\frac{(\lambda^2+2\lambda-1)}{\lambda^4}=-1$$
or
$$\frac{(\lambda^3+\lambda^2+2\lambda-1)}{\lambda^4}=-1$$
or
$$\frac{(\lambda^3+\lambda^2+2\lambda-1)}{\lambda^4}=-1$$
either
$$\lambda=0 \text{ or } (\lambda^3+\lambda+2)=0$$
either
$$\lambda=0 \text{ or } (\lambda^3+\lambda+2)=0$$
or
$$\lambda^3+\lambda+2=0-(iii)$$

$$(-1) \text{ is a root of the eqn } (iii)$$
or
$$\lambda^3+\lambda^2-\lambda^2-\lambda+2\lambda+2=0$$
or
$$\lambda^2-(\lambda+1)-\lambda(\lambda+1)+2(\lambda+1)=0$$
or
$$(\lambda+1)(\lambda^2-\lambda+2)=0$$
for
$$(\lambda+1)(\lambda^2-\lambda+2)=0$$
This equation has or
$$(\lambda+1)(\lambda^2-\lambda+2)=0$$
So,
$$\lambda=-1$$
For
$$\lambda=-1$$
, we
$$y=1|_{\lambda^2}=1$$

So, [2=0, y=1] is a solu of this eqn.

It satisfies constraint $x^2-y^2=0-1$ f(x,y)=0+2+1=23.

So, $[x=0, y=1] \rightarrow Am$.

4