

## Assignment # 4

1/ (a)  $f(x, y) = x^2 - y^2$  subject to  $x^2 + y^2 = 4$ .

Introducing Lagrange's multiplier  $\lambda$ , we get,  
a new function,

$$L(x, y, \lambda) = x^2 - y^2 - \lambda(x^2 + y^2 - 4)$$

Now, partially differentiating this function,  
we get,

$$\frac{\partial L}{\partial x} = 2x - 2x\lambda = 0 \quad \text{--- (i)}$$

$$\frac{\partial L}{\partial y} = -2y - 2y\lambda = 0 \quad \text{--- (ii)}$$

From (i), we get,

$$x(1 - \lambda) = 0$$

So, either,  $x = 0$  or  $(1 - \lambda) = 0$  or  $\lambda = 1$

From (ii), we get,

$$y(1 + \lambda) = 0$$

$$y = 0 \text{ or } \lambda = -1$$

$x = 0$  and  $y = 0$  cannot be a soln as it doesn't satisfy the constraint  $x^2 + y^2 = 4$ .

~~When  $\lambda = 1$ , putting  $\lambda = 1$  in (ii), we get~~

~~(i)  $\Rightarrow 0 = 0$~~   
When  $x = 0$ ,  $0 + y^2 = 4$  or  $y = \pm 2$ .

$$\left. \begin{array}{l} x = 0, y = 2 \\ x = 0, y = -2 \end{array} \right\} \text{ are solutions.}$$

When  $y = 0$ ,  $x = \pm 2$

$$\left. \begin{array}{l} \text{So, } x = 2, y = 0 \\ x = -2, y = 0 \end{array} \right\} \text{ are solutions}$$