Econ 8307 Assignment 2 (Spring 2019)

Jonah Coste, Fred Xu George Washington University

Question 1

```
1 beta = .97;
2 Δ = .1;
3 theta = .3;
4 steady=@(x) [ x(1) + beta*x(1)*(theta * x(2)^(theta 1) + 1 Δ);
5 x(2)^theta Δ*x(2) x(1)];
6
7 initial_guess=[1;1];
8
9
10 steady_state=fsolve(steady,initial_guess)
```

Prints the steady state solution. Thew first entry is steady state consumption and the second entry is steady state capital.

```
1 steady_state =
2
3    1.0998
4    3.2690
```

Question 2

1. Define E as a row matrix with two variables. Each variable is an indicator for employed

or unemplyed i.e. E = [1,0] if employed and E = [0,1] if unemployed. This is the state variable. Value function becomes Value(E) = EV where V is a 1x2 column vector: $V = [value\ if\ employed; value\ if\ unemployed]$.

```
Value(E) = EV = EU + \beta * ETV
```

Where T is a transition matrix: $T = [pi_e, 1 - pi_e; 1 - pi_u, pi_u]$, and U is the column matrix $U = [u(w_h); u(w_l)]$

Prints value function vector.

```
1 V =
2
3 0.6871
4 1.2597
```

```
3.

1 steady2=@(x) (1 pi_e) * (1 x) + pi_u*x x;

2 initial_guess2=.5;

3 unemployment_rate=fsolve(steady2,initial_guess2)
```

Prints steady state unemployment rate.

```
unemployment_rate =

unem
```

Question 3

$$n^*(z) = (\frac{w}{z\alpha})^{\frac{1}{\alpha-1}}$$

Let $S_{it} = [s_{it1}; s_{it2}; ...; s_{itN}]$ be a Nx1 column vector where $s_{itx} = 1$ if $z_{it} = z_x$ and 0 otherwise. Therefore, $S_{it}Z = z_{it}$. S'it is the state variable.

The value function is: $Value(S) = SV = S\pi + \beta(1-\lambda)STV$ Where T is the NxN transition matrix i.e. $T_{jk} = f(z_{i,t+1} = k|z_{it} = j)$ and π is the optimal profit row vector $[\pi_1, \pi_2, ..., \pi_N]$ where $\pi_x = z_x n^*(z_x)^{\alpha} - wn^*(z_x)$

Question 4

```
N = 5;
   p = .8;
   w = 1;
   alpha = .7;
   beta = .95;
   lambda = .1;
   Z = zeros(1,N);
   T = zeros(N);
   nstar = zeros(N, 1);
   pi = zeros(N, 1);
   I = eye(N);
   T=T+(1p)/(N1)+eye(N)*(p(1p)/(N1));
13
   for i =1:N
14
       Z(i) = i/N;
       nstar(i) = (w/(Z(i)*alpha))^(1/(alpha 1));
16
       pi(i)=Z(i)*nstar(i)^alpha w*nstar(i);
17
   end
18
19
   V = inv(I beta*(1 lambda)*T)*pi
```

Prints value vector V^*

```
1 V = 2
```

```
3 0.1851

4 0.2005

5 0.2496

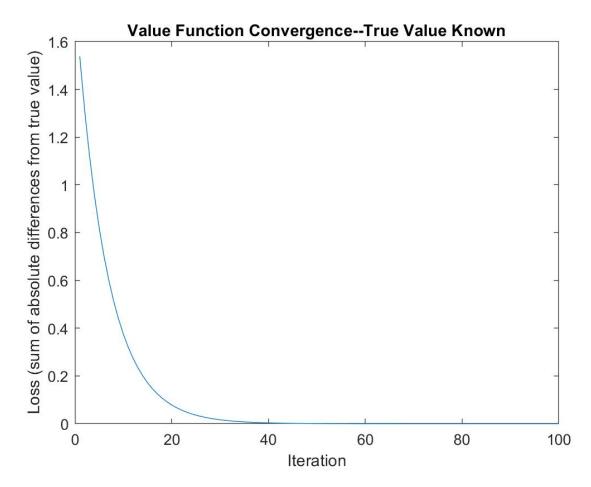
6 0.3563

7 0.5472
```

Prints 2000th iteration.

```
1 Vguess =
2
3 0.1851
4 0.2005
5 0.2496
6 0.3563
7 0.5472
```

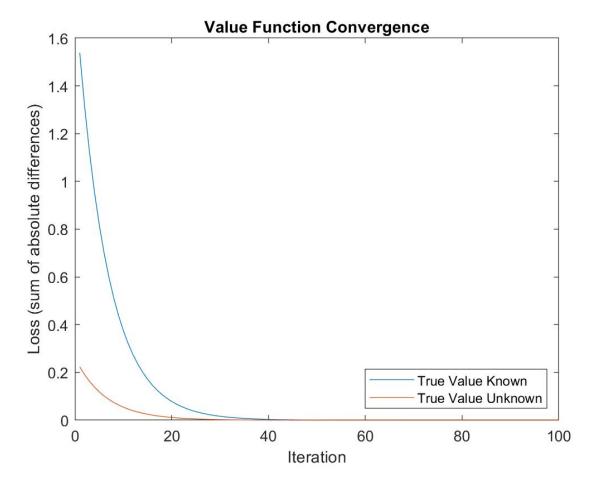
```
iterations = 100;
2 loss = zeros(iterations,1);
3 Vguess = zeros(5,1);
  for j =1:5
       loss(1) = loss(1) + abs(V(j) Vguess(j));
  end
  for i= 1:iterations 1
       Vguess = pi + beta*(1 lambda)*T*Vguess;
       for j =1:5
          loss(i+1) = loss(i+1) + abs(V(j) Vguess(j));
10
11
       end
  end
12
13
  plot(loss)
14
  title('Value Function Convergence True Value Known')
15
  xlabel('Iteration')
```



Around 67 iterations gives a fairly precise estimate of the value function. Note 67 is the first iteration where loss function rounds to .0000.

```
loss2 = zeros(iterations,2);
   Vold = zeros(5,1);
2
   Vnew = zeros(5,1);
    for i= 1:iterations
        loss2(i,1) = loss(i);
5
        Vold=Vnew;
6
        Vnew = pi + beta*(1 lambda)*T*Vold;
        for j = 1:5
           loss2(i,2) = loss2(i,2) + abs(Vnew(j) Vold(j));
        end
10
    end
11
12
   plot(loss2)
```

```
title('Value Function Convergence')
xlabel('Iteration')
ylabel('Loss (sum of absolute differences)')
legend({'True Value Known', 'True Value ...
Unknown'}, 'Location', 'southeast')
```



Now around 55 iterations appears to give a fairly precise estimate of the value function. Note 55 is the first iteration where the new loss function rounds to .0000.