

# SS-model:

$$x(t+T_s) = Ax(t) + Bu(t) + Ke(t)$$

$$y(t) = Cx(t) + Du(t) + e(t)$$

$$A \in \mathbb{R}^{n \times n}, B \in \mathbb{R}^{n \times m}, C \in \mathbb{R}^{1 \times n}, D \in \mathbb{R}^{1 \times m}$$

$$x(t) \in \mathbb{R}^n, y(t) \in \mathbb{R}, u(t) \in \mathbb{R}^m,$$

$$K \in \mathbb{R}^{n \times m}$$

$e(t)$  - difference between measured and predicted output of the model.

Parameter estimation using PEM

□ ARX model (possible best choice)

□ ARMAX model

□ OE model

□ BJ model

# Models description:

1) Define state parameters :

$$x_1 = x$$

$$x_2 = dx$$

$$x_3 = p_A$$

$$x_4 = p_B$$

$$x(t) = f(x(t), u(t))$$

# Models identification

Mechanical assembly:

$F_f$  parameter represent Friction forces.

1) input data :  $\dot{m}_A, \dot{m}_B$  - flows that can be measured.

output data :  $x$  - position

2) input data :  $\dot{m}_A, \dot{m}_B$  - flows  
output data :  $\ddot{x}$  - accelerometer data.

Depends how to model, but generally:

- $C$  - viscous friction coefficient
- $f_c$  - Coulomb friction
- $f_s, f_d$  - static, dynamic friction factor.

Cylinder:

— All parameters can be measured or taken from datasheet.

Valve:

With respect to equation for mass flow

$$\dot{m} = u(x_s) \underbrace{C \sqrt{\frac{2}{RT}} \psi\left(\frac{p_2}{p_1}\right)}_{\text{const}}$$

where  $p_1$  - supply pressure

$p_2$  - atmospheric pressure

1)  $C$  is valve coefficient that need to be identified.

in 1st experiment we