



# **BRNO UNIVERSITY OF TECHNOLOGY**

VYSOKÉ UČENÍ TECHNICKÉ V BRNĚ

## **FACULTY OF MECHANICAL ENGINEERING**

FAKULTA STROJNÍHO INŽENÝRSTVÍ

## **INSTITUTE OF SOLID MECHANICS, MECHATRONICS AND BIOMECHANICS**

ÚSTAV MECHANIKY TĚLES, MECHATRONIKY A BIOMECHANIKY

## **PREDICTIVE MAINTENANCE OF PNEUMATIC PISTONS**

MOŽNOSTI PREDIKTIVNÍ ÚDRŽBY PNEUMATICKÝCH PÍSTŮ

### **MASTER'S THESIS**

DIPLOMOVÁ PRÁCE

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**BRNO 2021**

# Assignment Master's Thesis

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Degree program: Applied Sciences in Engineering  
Branch: Mechatronics  
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Academic year: 2020/21

As provided for by the Act No. 111/98 Coll. on higher education institutions and the BUT Study and Examination Regulations, the director of the Institute hereby assigns the following topic of Master's Thesis:

## Predictive maintenance of pneumatic pistons

### Brief Description:

With the ever-increasing degree of automation in the industry, a widespread effort to measure, record, and exploit information and signals related to the state of a given machine and its production quality, is becoming more relevant. Predictive Maintenance (PM) is a relatively new method, which builds on and further expands the ideas of the already established Fault Detection and Analysis (FDA). The purpose of this work is to demonstrate various approaches to Predictive Maintenance (e.g., signal-based and model-based) using the Matlab/Simulink software tools on a double-acting pneumatic piston as a case-study.

### Master's Thesis goals:

1. Conduct research in the area of Predictive Maintenance, Fault Detection and Analysis, and related approaches and try to define their similarities and differences. Provide a practical demonstration for each of the approaches.
2. Create a simulation model of the demonstration device, including models of the sensors. Test different methods to create the model (e.g., software simulation, physical properties, black-box identification, etc.) and identify the models with real data.
3. Apply Predictive Maintenance techniques to a test dataset without using a simulation model.
4. Apply Predictive Maintenance techniques to a test dataset using a simulation model.
5. Evaluate the suitability of each approach for the application of PM and FDA.

### Recommended bibliography:

PRITCHARD, Philip J. Introduction to Fluid Mechanics, 9th edition, Wiley, ISBN 978-1118921876.

NELLES, Oliver. Nonlinear system identification: from classical approaches to neural networks and fuzzy models. Berlin: Springer, 2011. ISBN 978-364-2086-748.

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NOSKIEVIČ, Petr. Modelování a identifikace systémů. Ostrava: Montanex, 1999. ISBN 80-722-50-0-2.

Deadline for submission Master's Thesis is given by the Schedule of the Academic year 2020/21

In Brno,

L. S.

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## Abstrakt

...Abstrakt...

## Summary

...anglicky...

## Klíčová slova

...klicova slova...

## Keywords

...anglicky...

## Bibliographic citation

VORONIN, A. *Predictive maintenance of pneumatic pistons* . Brno: Brno University of Technology, Faculty of Mechanical Engineering, 2021. ?? pages, Master's thesis supervisor: Martin Brable.

Prohlášení...

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Brno . . . . .

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Poděkování..

**Artyom Voronin**

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# 1 Introduction

## 2 Theoretical Survey (10-13 pages)

Why FDA and PdM are useful? Similarities/Differences? The relative arrangement PdM and FDI methods representing in following figure 2.1

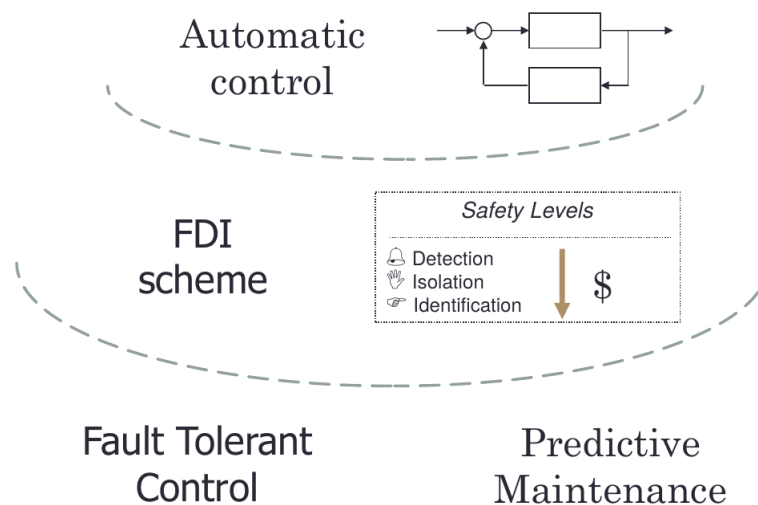


Figure 2.1: PM and FDI

### 2.1 Problem Definition

In practice, many types of machinery require some calibration for adequately working, and online monitoring and classification algorithms can find the problem.

Smart systems = Sensors, but sensors only not doing the system smart. Smart is combination of sensors, processing signals, extraction useful information and some decision based on this information.

What kind of sensors to use and which sensor is the best based on cost/technical efficient perspective.

- Fault
- Failure
- Malfunction

#### 2.1.1 Types of Faults

- Plant
- Sensor

- Combination

### 2.1.2 Types of Maintenance

- Reactive (fixes than fail)
- Preventative (schedules)
- Condition-based (based on assessment of system)
- Predictive (based on model that predicts failure)

## 2.2 Fault Detection and Analysis (FDA)

Fault Detection and Analysis, FDA. (Fault detection and isolation, FDI)

**FD not new** FD exists from 60th.

### 2.2.1 Goals

- Fault detection: Detect malfunctions in real time, as soon and as surely as possible
- Fault isolation: Find the root cause, by isolating the system components whose operation mode is not nominal
- Fault identification: Estimation the magnitude (size) and type or nature of the fault

### 2.2.2 Methods

Figure 2.2 introduces 2 main approaches:

- Model-based FDI (compare data with healthy-model)
- Signal processing based FDI (using math methods to extract information about the fault from data)

#### Signal-Based methods

- Limit Checking and Trend Checking
- Data Analysis (PCA)
- Spectral Analysis
- Parametric Signal Models
- Pattern Recognition (kNN, ANN, SOM)

**Model-Based methods** We know system structure. Faults modeled as some system variables changes. Parameter estimation

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<sup>0</sup>**Fault** - not acceptable deviation of at least one characteristic or parameter of the system from the standard condition.

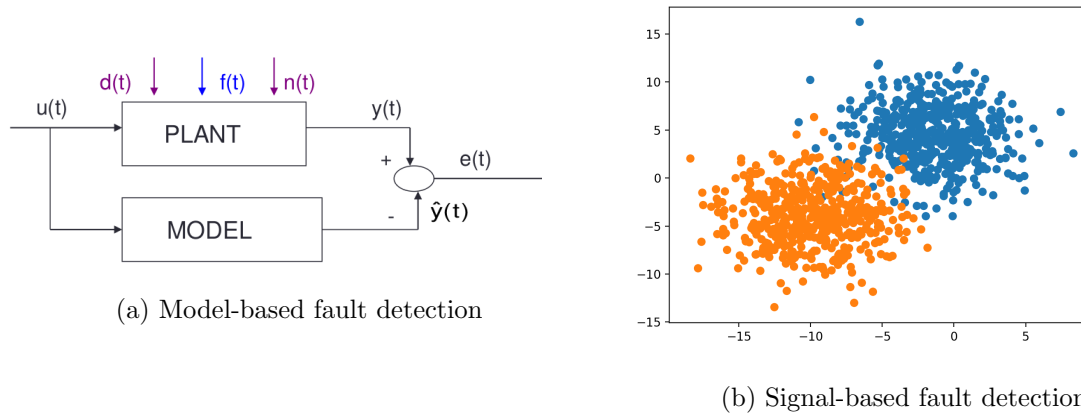


Figure 2.2: Fault detection common approaches

**Knowledge-Based methods** We know some Expert Knowledge about system behavior. Fuzzy, confidence-numbers, probability density functions, logic fault-symptom-tree, if-then rules.

The result of FDI is the detection and identification of faults that occur during the operation of the device. Subsequently data is processed using Fault Tolerance and Predictive maintenance methods.

**Fault Tolerance:** Provide the system with the hardware architecture and software mechanisms which will allow, if possible to achieve a given objective not only in normal operation, but also in given fault situations.

### 2.2.3 Condition Monitoring

Answer to question: "How does system operate now?" CM gives Diagnostic methods that provides alarm or warning, but not prognostic forecast about the future behavior (Not RUL).

But collected Condition Monitoring information can give information about system degradation.

There is a optimization between technical and financial possibilities in a specific situation.

FMECA (Failure Mode, Effect and Criticality Analysis)

FTA (Fault Tree Analysis)

RCA (Root Cause Analysis)

## 2.3 Predictive maintenance (PdM)

**Predictive maintenance (PdM)** is cost-effective maintenance strategy that predicts time to failure and warns of an anticipated location where this could occur.

### 2.3.1 Goals

The are two main goals of Predictive maintenance, RUL (remaining useful life) estimation and identification where the future failure can appear, or what is the reason of decreasing RUL. As a result of PdM is RUL representing of number cycles, days, or some time period before fault occurred. And probability where this fault can appear.

Predict where, when and what is the reason of failure (identify primary factors).

**Predictive maintenance development sequence:**

1. Collect data (using sensors, math model)
2. Process data (clean up data)
3. Identify Condition Indicators CI
  - Signal-based CI
  - Model-based CI
4. Fit model (ML techniques)
5. Deploy monitoring and integrate
6. Dashboard (UI)

### 2.3.2 Methods

There are couples of signal processing and analyzing methods that used in both PdM and FDI. For example:

**Signal-Based** approach is suitable in situation when we have measurements from system in different operating conditions. But there is a problem that Signal-Based approach enable to classify and learn patterns observed in training dataset.

**Model-Based** approach is to use physical failure models. This models do not require a large dataset of failure data. And they can work in situations never observed before.

### 2.3.3 Condition Indicators

Features in PdM field are called Condition Indicators or CI. Condition Indicators are features extracted from the signals, representing some system behavior and hides some information about system processing.

Condition indicators represented by three main domain. There are Time domain, Frequency domain, Time-Frequency domain Condition Indicators.

- Time-domain
- Frequency-domain
- Time-frequency

### 2.3.4 Fault Classification

### 2.3.5 Remaining useful life

RUL goal is remaining time before machine requires maintenance. Not only predict but provide a confidence bound.

## **RUL Models :**

Inputs are condition indicators and models depends on data: 1. Lifetime, Run-to-failure, known threshold for CI.

- Similarity model
- Survival model
- Degradation model

## **2.4 Digital twin**

Digital twin is digital representation of the real life system. Can be represented as a component, a system of components, or as a system of system.

**Updating digital twin with incoming data** Digital twin can be updated with incoming data from sensors. Fitting model to new data, digital twin represents the current condition state of the real world object.

Digital twin can hold historical data about behavior of a system and can be used for simulation system operation in different conditions, for designing control and simulate future behavior. (RUL, "What-if")

Digital Twins are helpful in the field of Anomaly Detection and Predictive Maintenance.

Mathematical model of the real world system can be created using different approaches. Modeling based on Physical modeling (Simscape) data-driven modeling where system is represented as a "Black box" or some combination of this approaches. Model with estimated parameters uses for simulation system behavior in different working conditions and with different faults during working process.

### **2.4.1 Using Digital Twin in PdM**

Measured data, Generated data from mathematical model, or Synthetic data (Combination of measured and generated) can be used for assessment of Condition Indicators.

## **2.5 Comparison PdM and FDA approaches**

- Compare similarities and differences in FDA and PdM

## **2.6 Application field**

- Answer to question where FDA and PdM can be suitable.

# 3 First Principle Modeling (15 pages)

## First Principles (White-Box)

Simplification, Linearization, Reduction, Parameter Estimation.  
SimScape (Physical modeling), Simulink (Differential equations).

## Data-Driven modeling (Black-Box)

Measurements, Identification.

### 3.1 Pneumatic piston system overview

### 3.2 General physical principles

**Equation of state** Generally  $pV = nR_mT$  but for air, using ideal gas constant  $R = 287.1[Jkg^{-1}K^{-1}]$  state equation can be rewrite as 3.1.

$$pV = mRT \quad (3.1)$$

**Isothermal process** For isothermal process 3.2:

$$p_1V_1 = p_2V_2 = const \quad (3.2)$$

**Adiabatic process** Adiabatic process 3.3:

$$p_1V_1^\kappa = p_2V_2^\kappa = const \quad (3.3)$$

where  $\kappa = c_p/c_v$  is a heat capacity ratio. Another important equation is Mayer's relation  $c_p = c_v + R$ .

**Bernoulli's principle** Bernoulli's principle 3.4:

$$H_1 + \frac{mw_1^2}{2} + mgz_1 + Q = H_2 + \frac{mw_2^2}{2} + mgz_w + W_T \quad (3.4)$$

$$H_1 - H_2 = - \int_1^2 V dp = c_p(T_1 - T_2) = c_pT_1(1 - \frac{T_2}{T_1}) \quad (3.5)$$

Differential form:

$$\nu dp + wdw + gdz + dw_T = 0 \quad (3.6)$$

**Fluid mechanics** Continuity equation 3.7:

$$\dot{m} = S_1w_1\rho_1 = S_2w_2\rho_2 = const \quad (3.7)$$

**Air expansion from tank** Assuming  $W_T = 0, z_1 = z_2, Q = 0$  conditions and combine with 3.4 we will get 3.8 equation:

$$w_2 = \sqrt{2(H_1 - H_2)} \quad (3.8)$$

$$w_2 = \sqrt{2RT_1 \left( \frac{\kappa}{\kappa - 1} \right) \left( 1 - \left( \frac{p_2}{p_1} \right)^{\frac{\kappa-1}{\kappa}} \right)} \quad (3.9)$$

$$\rho_2 = \frac{p_1}{RT_1} \left( \frac{p_2}{p_1} \right)^{\frac{1}{\kappa}} \quad (3.10)$$

Together 3.7 3.9 3.10:

$$\dot{m} = Sp_1 \sqrt{\frac{2}{RT_1}} \cdot \sqrt{\frac{\kappa}{\kappa - 1} \left( \left( \frac{p_2}{p_1} \right)^{\frac{2}{\kappa}} - \left( \frac{p_2}{p_1} \right)^{\frac{\kappa+1}{\kappa}} \right)} \quad (3.11)$$

where:

$$\psi \left( \frac{p_2}{p_1} \right) = \sqrt{\frac{\kappa}{\kappa - 1} \left( \left( \frac{p_2}{p_1} \right)^{\frac{2}{\kappa}} - \left( \frac{p_2}{p_1} \right)^{\frac{\kappa+1}{\kappa}} \right)} \quad (3.12)$$

Finally 3.13:

$$\dot{m} = Sp_1 \sqrt{\frac{2}{RT_1}} \psi \left( \frac{p_2}{p_1} \right) \quad (3.13)$$

**Critical flow velocity** Speed of sound:

$$c = \sqrt{\frac{dp}{d\rho}} = \sqrt{\frac{\kappa p}{\rho}} = \sqrt{\kappa RT} \quad (3.14)$$

Assume  $c = w_2$  (3.9, 3.14) we will get the critical flow velocity:

$$c_2 = w_k = \sqrt{\kappa RT} = \sqrt{2RT_1 \frac{\kappa}{\kappa - 1} - 2w_k^2 \frac{1}{\kappa - 1}} \quad (3.15)$$

$$w_k^2 = 2RT_1 \frac{\kappa}{\kappa - 1} - 2w_k^2 \frac{1}{\kappa - 1} \quad (3.16)$$

$$w_k = \sqrt{2RT_1 \frac{\kappa}{\kappa - 1}} = \sqrt{2p_1 \nu_1 \frac{\kappa}{\kappa + 1}} \quad (3.17)$$



For calculating critical pressure ratio assume  $w_k = w_2$  3.17 3.9:

$$\sqrt{2RT_1 \frac{\kappa}{\kappa-1}} = \sqrt{2RT_1 \frac{\kappa}{\kappa-1} \left(1 - \left(\frac{p_2}{p_1}\right)^{\frac{\kappa+1}{\kappa}}\right)} \quad (3.18)$$

$$\left(\frac{p_2}{p_1}\right)^{\frac{\kappa-1}{\kappa}} = \frac{2}{\kappa+1} \quad (3.19)$$

$$(3.20)$$

$$\left(\frac{p_2}{p_1}\right)_k = \left(\frac{p_k}{p_1}\right) = \left(\frac{2}{\kappa+1}\right)^{\frac{\kappa}{\kappa-1}} = \beta_k \quad (3.21)$$

Critical pressure condition is  $p_k = p_1 \beta_k$ .

Applying 3.21 to 3.12:

$$\psi_{max}(\beta_k) = \left(\frac{2}{\kappa+1}\right)^{\frac{\kappa}{\kappa-1}} \sqrt{\frac{\kappa}{\kappa+1}} \quad (3.22)$$

For air  $\beta_k = 0.528$ ,  $\psi_{max} = 0.484$

Final equation for  $\psi$ :

$$\psi\left(\frac{p_2}{p_1}\right) = \begin{cases} \sqrt{\frac{\kappa}{\kappa-1} \left( \left(\frac{p_2}{p_1}\right)^{\frac{2}{\kappa}} - \left(\frac{p_2}{p_1}\right)^{\frac{\kappa+1}{\kappa}} \right)} & 0.528 < \frac{p_2}{p_1} \leq 1 \\ \left(\frac{2}{\kappa+1}\right)^{\frac{1}{\kappa+1}} \sqrt{\frac{\kappa}{\kappa+1}} & 0 \geq \frac{p_2}{p_1} \leq 0.528 \end{cases} \quad (3.23)$$

### 3.3 Pressure model

|                        |                   |                                  |
|------------------------|-------------------|----------------------------------|
| $p_A, p_B$             | $Pa$              | pressure in chamber A, B         |
| $\dot{m}_A, \dot{m}_B$ | $kg \cdot s^{-1}$ | mass flow on way to chamber A, B |
| $S_A, S_B$             | $m^2$             | piston area                      |
| $V_A, V_B$             | $m^3$             | volume of chamber A,B            |
| $V_{0A}, V_{0B}$       | $m^3$             | "dead" volume of chamber A,B     |
| $m$                    | $kg$              | piston mass                      |
| $F_{load}$             | $N$               | load                             |
| $x$                    | $m$               | piston position                  |
| $l$                    | $m$               | maximum piston position          |

There are different approaches how to model thermal processes in pneumatic system. Isothermal, adiabatic, polytropic models are suitable in different technical applications.

#### Isothermal model of pressure in cylinder

$$m = \rho V \quad (3.24)$$

$$\dot{m} = \dot{\rho} V + \rho \dot{V} \quad (3.25)$$

Applying 3.1:

$$\rho = \frac{p}{RT} \quad (3.26)$$

$$\dot{\rho} = \frac{\dot{p}}{RT} \quad (3.27)$$

Finally get 3.28:

$$\dot{p} = -\frac{p}{V}\dot{V} + \frac{RT}{V}\dot{m} \quad (3.28)$$

**Adiabatic model of pressure in cylinder** Assume adiabatic process. For simple adiabatic model following equation can be used 3.29:

$$\dot{p} = -\frac{\kappa p}{V}\dot{V} + \frac{\kappa RT}{V}\dot{m} \quad (3.29)$$

$$\dot{p}_A = \frac{\kappa}{S_A x + V_{0A}} (-p_A S_A \dot{x} + RT_A \dot{m}_A) \quad (3.30)$$

$$\dot{p}_B = \frac{\kappa}{S_B(l-x) + V_{0B}} (p_B S_B \dot{x} + RT_B \dot{m}_B) \quad (3.31)$$

Volumes of chambers:

$$V_A = S_A x + V_{0A} \quad (3.32)$$

$$V_B = S_B(l-x) + V_{0B} \quad (3.33)$$

$$\dot{V}_A = S_A \dot{x} \quad (3.34)$$

$$\dot{V}_B = -S_B \dot{x} \quad (3.35)$$

## 3.4 Mass flow model

### 3.4.1 Input/Output mass flows

$$\dot{m}T = \dot{m}_{in}T_s - \dot{m}_{out}T_{A/B} \quad (3.36)$$

### 3.4.2 Valve model

|           |       |                            |
|-----------|-------|----------------------------|
| $S_{eq}$  | $m^2$ | Equivalent cross section   |
| $S_{max}$ | $m^2$ | Maximum cross section      |
| $Cd$      | —     | Coefficient of contraction |
| $u$       | —     | Regulation variable        |

**Valve flow model with simply input control signal** For regulation flow this model used input control signal directly without spool mechanics.

Coefficient of contraction 3.37:

$$C_d = \frac{S_{eq}}{S_{max}} \quad (3.37)$$

For flow control regulation  $u \in \langle -1, 1 \rangle$  can be used.

$$u = \begin{cases} u \in \langle -1, 0 \rangle & \text{discharge the chamber} \\ u = 0 & \text{valve closed} \\ u \in (0, 1) & \text{filling the chamber} \end{cases} \quad (3.38)$$

$$\dot{m} = u S_{max} C_d p_1 \sqrt{\frac{2}{RT_1}} \cdot \psi \left( \frac{p_2}{p_1} \right) \quad (3.39)$$

**For filling the chamber:**

- $p_1 = p_s$
- $p_2 = p_A$  or  $p_B$
- $T_1 = T_s$

**For discharge the chamber:**

- $p_1 = p_A$  or  $p_B$
- $p_2 = p_0$
- $T_1 = T_A, T_B$

where  $p_s$  is supply pressure.  $p_0$  atmospheric pressure. As  $T_i$  - atmospheric temperature using according to isothermal process.

$$\dot{m}_A = \begin{cases} u S_v C_d p_s \sqrt{\frac{2}{RT_s}} \cdot \psi \left( \frac{p_A}{p_s} \right) & , u \in (0, 1) \\ 0 & , u = 0 \\ u S_v C_d p_A \sqrt{\frac{2}{RT_A}} \cdot \psi \left( \frac{p_0}{p_A} \right) & , u \in \langle -1, 0 \rangle \end{cases} \quad (3.40)$$

$$\dot{m}_B = \begin{cases} u S_v C_d p_s \sqrt{\frac{2}{RT_s}} \cdot \psi \left( \frac{p_B}{p_s} \right) & , u \in (0, 1) \\ 0 & , u = 0 \\ u S_v C_d p_A \sqrt{\frac{2}{RT_B}} \cdot \psi \left( \frac{p_0}{p_B} \right) & , u \in \langle -1, 0 \rangle \end{cases} \quad (3.41)$$

**Valve flow with spool mechanic included** With respect to valve spool modeled as 1DOF system 3.48 and mechanical and geometrical properties following equation were used.

**Valve flow with spool** In this model we accept a spool displacement  $x_s$ , controlled by input voltage  $u$ .

$$\dot{m}(P_u, P_d) = \begin{cases} C_f A_v \left( \frac{\kappa}{R} \left( \frac{2}{\kappa-1} \right) \right)^{\frac{1}{2}} \cdot \frac{P_u}{\sqrt{T}} \left( \frac{P_d}{P_u} \right)^{\frac{1}{\kappa}} \cdot \sqrt{1 - \left( \frac{P_d}{P_u} \right)^{\frac{\kappa-1}{\kappa}}} & , \text{ if } \frac{P_d}{P_u} > P_{cr} \text{ (subsonic)} \\ C_f A_v \frac{P_u}{\sqrt{T}} \cdot \sqrt{\frac{\kappa}{R} \left( \frac{2}{\kappa+1} \right)^{\frac{\kappa+1}{\kappa-1}}} & , \text{ if } \frac{P_d}{P_u} \leq P_{cr} \text{ (sonic)} \end{cases} \quad (3.42)$$

where  $C_f$  is discharge coefficient,  $A_v$  is the effective are of valve orifice.

$$A_v = \frac{\pi x_s^2}{4} \quad (3.43)$$

$$x_s = C_v u \quad (3.44)$$

where  $C_v$  is the valve constant.

**Valve model by Endler** Require fitting constants and generally system identification. Mass flow rates are given by following equations:

$$\begin{aligned} \dot{m}_A(u, p_A) &= g_1(p_A, \text{sign}(u)) \arctg(2u) \\ \dot{m}_B(u, p_B) &= g_2(p_B, \text{sign}(u)) \arctg(2u) \end{aligned} \quad (3.45)$$

where  $g_1, g_2$  are signal functions given:

$$\begin{aligned} g_1(p_A, \text{sign}(u)) &= \beta \Delta p_A = \begin{cases} (p_s - p_A) \beta^{ench} & , \text{ if } u \geq 0 \\ (p_A - p_0) \beta^{esv} & , \text{ if } u < 0 \end{cases} \\ g_2(p_B, \text{sign}(u)) &= \beta \Delta p_B = \begin{cases} (p_s - p_B) \beta^{ench} & , \text{ if } u < 0 \\ (p_B - p_0) \beta^{esv} & , \text{ if } u \geq 0 \end{cases} \end{aligned} \quad (3.46)$$

where  $\beta^{ench}, \beta^{esv}$  are constant coefficients. For fitting model stop piston (speed of piston is null). This mean that volume is constant. We can measure flow rate  $\dot{m}$  versus input voltage  $u$  with given pressure difference.

**Valve dead-zone** For more precision control and modeling of the valve system, valve dead-zone can be used 3.47.

$$u_z = \begin{cases} g_z(u) < 0 & , \text{ if } u \leq u_n \\ 0 & , \text{ if } u_n < u < u_p \\ h_z(u) > 0 & , \text{ if } u \geq u_p \end{cases} \quad (3.47)$$

## 3.5 Mechanical assembly

### 3.5.1 Equation of motion

The motion of the pneumatic piston mechanism describes in terms of the general 1dof dynamical equation 3.48.

$$m\ddot{x} + b\dot{x} + kx = u \quad (3.48)$$

In the case of the pneumatic piston, the equation 3.48 transforms into an equation 3.49.

$$(M + M_L)\ddot{x} + F_{damp} + F_g + F_{hs} = F_p \quad (3.49)$$

Where  $M$  represents a mass of the all moveable part of the piston,  $M_L$  is load mass,  $F_g$  gravity force acting to mechanical moving assembly,  $F_{hs}$  - models endpoints (hard stop),  $F_{damp}$  represents shock absorbers acted at endpoints,  $F_p$  is a force produced by the pneumatic piston 3.50.

$$F_p = P_A S_A - P_B S_B - P_0 S_0 \quad (3.50)$$

### 3.5.2 Hard stop

Hard stop can be represented as spring and dumps:

$$F_{HS} = \begin{cases} K_p(x - g_p) + D_p v & \text{for } x \geq g_p \\ 0 & \text{for } g_n < x < g_p \\ K_n(x - g_n) + D_n v & \text{for } x \leq g_n \end{cases} \quad (3.51)$$

### 3.5.3 Shock Absorbers

### 3.5.4 Friction

Friction force can be modeled in the different ways.

TO MUCH 3.52.

$$F_f = \begin{cases} C\dot{x} + \left( f_c + (f_s - f_c)e^{-\left(\frac{\dot{x}}{v_s}\right)^\delta} \right) \text{sign}(\dot{x}) & , \text{ if } \dot{x} \leq v_e \\ \mu\dot{x} & , \text{ if } \dot{x} > v_e \end{cases} \quad (3.52)$$

where  $C$  - viscous friction coefficient,  $f_c$  - Coulomb friction,  $f_s$  - maximum static friction,  $\mu$  - dynamic friction factor,  $v_s$  - Stribeck velocity,  $\delta$  - arbitrary index,  $v_e$  critical velocity.

## 3.6 Sensors Modeling

- Sensors models

## 3.7 Parameter identification

### 3.7.1 Mechanical assembly

In mechanical system there is  $F_f$  force represented by frictions accruing in the system. This force can be modeled by different friction models with respect to  $\dot{x}$ . Friction force parameters can be estimated using "gray-box" method. Using  $\dot{m}$  mass flow data versus  $x$  position measured on real assembly and use these data as an input and output, we can fit  $F_f$ . Simplify model can contain TODO:

- $F_C$  static friction
- $C_v$  viscous
- $C_p$  Pressure difference

### 3.7.2 Cylinder

Dead volume:  $p_1 V_1^n = p_2 V_2^n$  or datasheet.

### 3.7.3 Valve

For valve system there are two parameters that need to be estimated. According to equation 3.53 with constant  $p_1$  (pressure supply) and  $p_2$  (atmospheric pressure), we can estimate  $C$  if we neglect Valve Spool dynamic. If in experiment we determine that spool dynamic necessary to include. We provide same experiment with spool model including to "Gray-box" fitting model.

$$\dot{m} = \mathbf{u}(x_s) C p_1 \sqrt{\frac{2}{RT_1}} \cdot \psi\left(\frac{p_2}{p_1}\right) \quad (3.53)$$

## 4 Models comparison (2-3 pages)

### 4.1 First Principle Model

This model 4.1 was developed with respect to equations represented before.

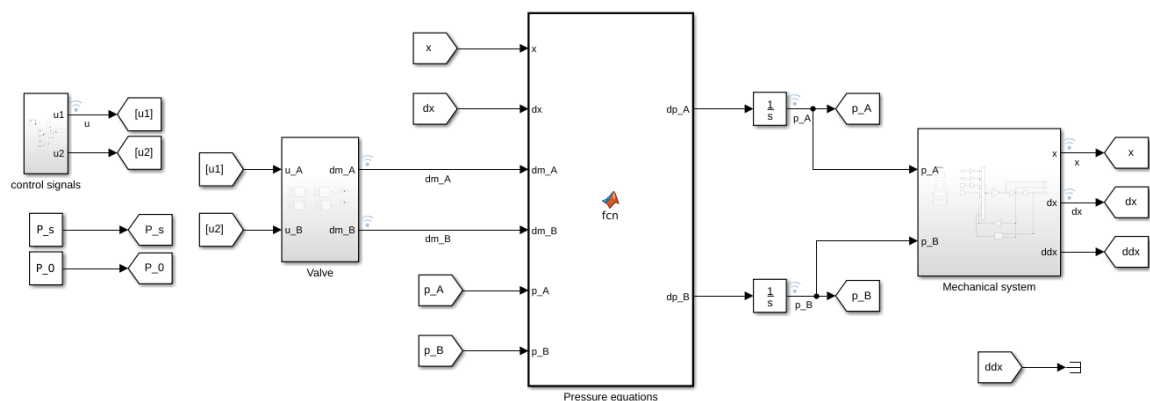


Figure 4.1: Simulink model based on equations

### 4.2 Alternative Modeling Techniques (3 pages)

Generally with dataset of input-output signals approximation model can be fit. Using System Identification Toolbox and modeled as Black-Box or Gray-Box models. This section attempted to fit some models using data from SimScape and Equation model presented before.

Fit approximation model make sense only if we know what to fit. Using signal process techniques and identify dominant signals that providing best classification features we will train models with respect to this signals.

#### 4.2.1 Physical Model (SimScape)

Working, very slow. Equations are faster for estimation parameters. Model 4.2 was developed using SimScape toolbox.

#### 4.2.2 State-space/ARX Models

Not working, Nonlinearities.

#### 4.2.3 Hammerstein-Wiener Model

Working only for Position.

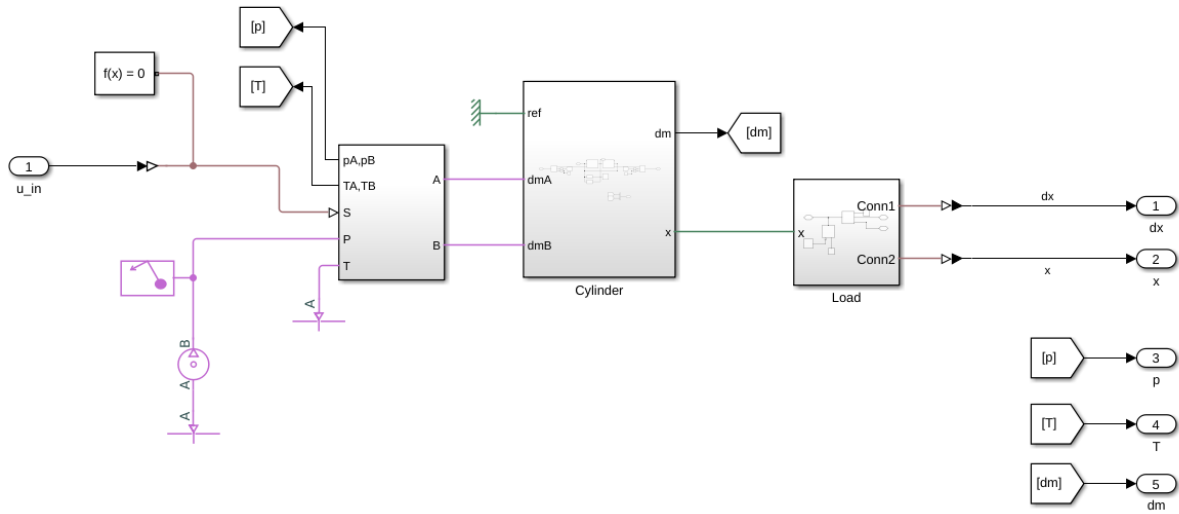


Figure 4.2: Simulink model using SimScape Toolbox

#### 4.2.4 Nonparametric model (ANN)

Working. Can be used as "Normal operation" model.

### 4.3 Comparison

Following figure 4.3 represent comparison of 2 models (Simscape and based on equations) using same parameters for simulation: There is slight difference between models causing Valve dynamics simplifications in model based on equations.

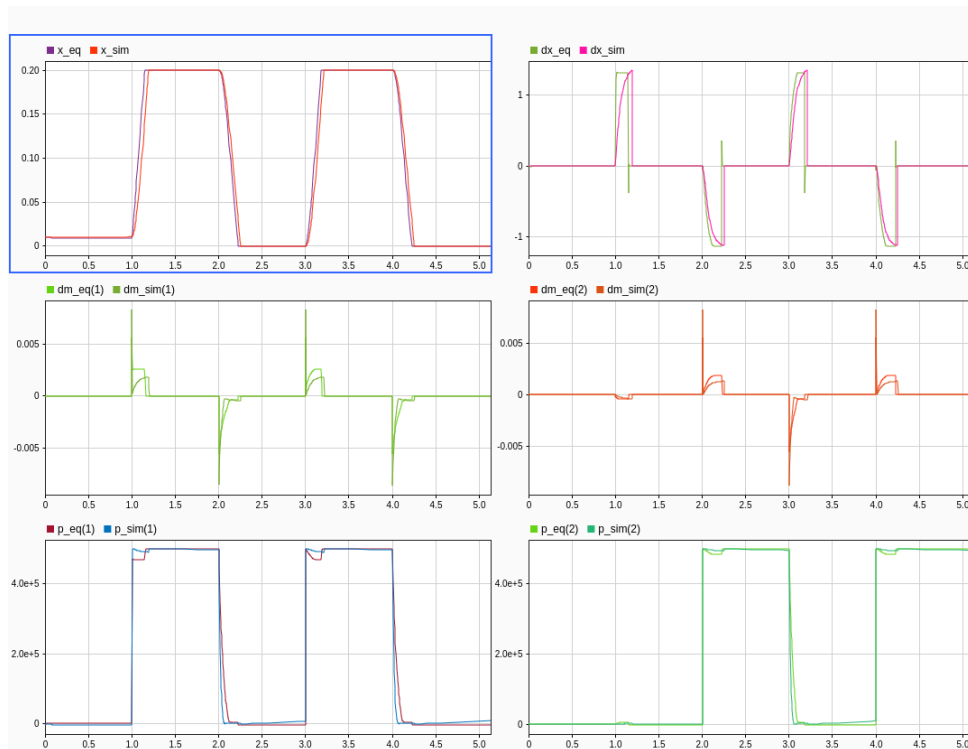


Figure 4.3: Comparison of simscape and model based on equations



## 5 Signal-Based PdM (15 pages)

Signal-Based Predictive Maintenance.

### General

### Workflow

## 5.1 Sensors

Sensors comparison, cost.

## 5.2 Data exploring

Data has been collect from 8 types of sensors corresponding table 5.1:

| Signal name               | Description        |
|---------------------------|--------------------|
| FlowExtrusin              | Flow sensor        |
| FlowContraction           | Flow sensor        |
| AirPressure               | Pressure sensor    |
| AccelerometerMoving_axisY | Accelerometer      |
| AccelerometerMoving_axisZ | Accelerometer      |
| AccelerometerStat_axisY   | Accelerometer      |
| AccelerometerStat_axisZ   | Accelerometer      |
|                           | Temperature sensor |
|                           | Proximity sensor   |
|                           | Strain gauge       |
|                           | Microphones        |

Table 5.1: Measured signals

There are 660 measurements with different parameters system parameters 5.2.

|                   |  |
|-------------------|--|
| Adjusting valve 1 |  |
| Adjusting valve 2 |  |

Table 5.2: Device parameters

Dataset was divided to 5 main categories.

Data has been accumulated to ".mat" files. Each file contains signals from sensors during 10 seconds measurements with different pneumatic actuator configuration. Example results from one experiment are represented in figures ??, ??.

## 5.3 Data management

**Data Ensembles** Data files have been reshaped to Data Ensembles format used for Condition monitoring purposes. This format allows processing data without copying the whole dataset to memory at once but processes them one by one. In large datasets it gives an option to manipulate with data without problems with allocated memory.

Divided to 3 datasets:

- Train data
- Validation data
- Test data

## 5.4 Preprocessing

Measured signals require preprocessing concerning the preservation of the information base. For smoothing data Moving Average function were used. As an example, the figure ?? is shown the "raw" and filtered signals. The whole dataset of preprocessed data is relatively big. For time-saving, parallel computing was used for all computationally demanding parts of the code.

## 5.5 FDI methods

### 5.5.1 Line checking

We can use Proximity sensor time delay between input signal and upper proximity sensor signal to evaluate if there is some fault.

Same with Position, if not reach some end position, there is a fault.

Flow sensor, check if the float mean value is under some threshold, there is fault.

## 5.6 Condition Indicators extraction

For classification task purpose from the signals have been extracted statistical features such as mean, median, peak to peak value, etc. As a condition "FaultCode" variable were used. This variable represent configuration of pneumatic actuator during the measurement.

All calculated features were added to the dataset and were ranked by Kruskal-Wallis ANOVA algorithm. Following table ?? contain 5 first best features ranked for classification purpose.

Kruskal-Wallis is very suitable to ranking features before using PCA or SVD.

**Selecting Condition Indicators** There is a problem if we will deploy classification task with large features dataset. There are different possibilities to reduce data before train classification model or do a prediction. One of them is to rank a features by Analysis of Variation algorithm to evaluate a good representation features.

### 5.6.1 Microphones

Cheap, good results, but maybe problems with real life integration (noise from another machines). Another problem cannot be modeled in simulation system. For predictive

purposes require data from real model.

### **5.6.2 Encoder**

Good results, useful in simulations and compare results with Digital Twin. Can be used in Model-Based CI. Digital twin can generate fault data, that will be applicable with encoder sensor.

### **5.6.3 Acceleration sensors**

Not good, not bad. Can be used for classification task. But encoder has more accuracy information.

### **5.6.4 Proximity Sensors**

Cheap. Very correlated features. Can not be used for classification. But suitable to detect binary classification (Health, Failed). Only statistical features, no Frequency domain.

### **5.6.5 Flow Sensors**

Very expensive sensors. Not so good results.

### **5.6.6 Air Pressure**

This sensor always used, to control pressure valve. But not good results. Maybe in combination with another sensor.

### **5.6.7 Strain Gauge**

Expensive, Normal results of classification. But not suitable for Simulation Model.

### **5.6.8 Temperature**

No interesting information. No classification results, not interesting as Independent or Condition Variable.

## **5.7 Classification Task**

The main goal of the classification task is to train a model that can predict the "Fault-Code", or "Label" signalized about pneumatic actuator behavior by calculated features.

Using Kuskal-Wallis one way analysis of variance, features were ranked by importance with respect to correlation. This gives opportunity to reduce number of features before PCA analysis.

Principal component analysis (PCA) has been used to reduce the number of features and chose the best representants.

The trained model has been exported to **models/** directory.

## 6 PdM using a Simulation Model (10-15 pages)

### 6.1 Differences between Model-Based PdM and PdM using Digital Twin

There is a difference between using Model-Based PdM and using Simulation Model as a Digital Twin.

### 6.2 Using Digital Twin to Generate Fault Data

We can use Digital Twin to model situations that were not captured in the original dataset or if it is hard to model some cases with real-world hardware. As an example, we can model sensors fault such as sensor drift or complete signal loss.

### 6.3 Model-Based Condition Indicators

Model-Based approach is suitable when it's difficult to identify condition indicators using only signals. In some cases it's useful to fit some model from data and extract condition indicators as some system parameter.

#### 6.3.1 Static and Dynamic Models

If the system behavior can be fit from the data as a static model, than we can extract condition variables from this model. For example, if model was fitting to a polynomial model, than polynomial coefficients can be use as condition indicators.

Signals showing dynamic behavior can be fitted to dynamic models such as State-Space or AR, ARX, NLARX (Nonlinear auto recursive model) and so on. Then condition indicators can be extracted as poles, zeros damping coefficients from estimated model.

#### 6.3.2 Using Hammerstain-Weiner Model

Demo using Hammerstain-Wiener Model. Fit model to position signal and extract coefficients from model as Condition indicators. Classification.

### 6.4 Using Simulation Model for Residuals Estimation

Another option is using the Simulink model with **prediction error minimization function** to compute difference between Simulink model and measured data. From this difference we can separate fault condition and healthy operation.

### 6.4.1 Comparison with Nominal System Model

Same thing as section 6.4

Compare actual system behavior with system model. This will generate some error  $e(t) = y(t) - \hat{y}(t)$ . From this error residual can be generated in form  $r(t) = \Phi(u_t, y_t, \varepsilon_t, v_t, d)$  and after some decision.

## 6.5 Using Digital Twin to Generate Prognostic Data

Another option is to use Digital Twin to generate a system degradation process. We can evaluate CI from sensor signal by changing a system's mechanical properties as friction or mass flow leakage. Another advantage is that we can design experiments on the model to evaluate what type of data we require from a real-world system to develop a robust algorithm.

## 6.6 RUL

Demo RUL using generated from model degradation dataset.

## 7 Conclusion