Exercici 2.4

Si assumim cache "look-aside" (mentre fa l'accés alhora va a la memòria principal):

a)
$$t_{miss L1} = t_{MP}, \ t_{CPU \ mem} = 5 \ ns, \ hit_{L1} = 99\% \Rightarrow miss_{L1} = 1\%, \ t_{L1} = \frac{1}{400} t_{MP} \Rightarrow t_{MP} = 400 \ t_{L1}$$

$$t_{CPU \ mem} = hit_{L1} t_{L1} + miss_{L1} t_{MP}$$

$$t_{CPU \ mem} = 0.99 \ t_{L1} + 0.01 \cdot 400 \ t_{L1} = 5 \ ns$$

$$t_{L1} = \frac{5 \ ns}{0.99 + 0.01 \cdot 400} = \frac{5 \ ns}{4.99} = 1.002... \ ns$$

b)
$$t_{CPU\ mem} = 2\ ns,\ hit_{L2} = 99\% \Rightarrow miss_{L2} = 1\%,\ t_{miss\ L2} = t_{MP}$$

$$t_{CPU\ mem} = hit_{L1}t_{L1} + miss_{L1}hit_{L2}t_{L2} + miss_{L1}miss_{L2}t_{MP}$$

$$t_{CPU\ mem} = 0.99t_{L1} + 0.01 \cdot 0.99 \cdot t_{L2} + 0.01^2t_{MP} = 2\ ns$$

$$t_{L2} = \frac{2\ ns - 0.99t_{L1} - 0.01^2 \cdot 400}{0.01 \cdot 0.99} = \frac{0.9579...ns}{0.0099} = 96.767...\ ns$$

Si assumim cache "look-through" (fa l'accés i si falla va a la memòria principal):

a)
$$t_{miss L1} = t_{MP}, \ t_{CPU \ mem} = 5 \ ns, \ hit_{L1} = 99\% \Rightarrow miss_{L1} = 1\%, \ t_{L1} = \frac{1}{400} t_{MP} \Rightarrow t_{MP} = 400 \ t_{L1}$$

$$t_{CPU \ mem} = t_{L1} + miss_{L1} t_{MP}$$

$$t_{CPU \ mem} = t_{L1} + 0.01 \cdot 400 \ t_{L1} = 5 \ ns$$

$$t_{L1} = \frac{5 \ ns}{1 + 0.01 \cdot 400} = 1 \ ns$$

b)
$$t_{CPU\ mem} = 2\ ns,\ hit_{L2} = 99\% \Rightarrow miss_{L2} = 1\%,\ t_{miss\ L2} = t_{MP}$$

$$t_{CPU\ mem} = t_{L1} + miss_{L1} (t_{L2} + miss_{L2} t_{MP})$$

$$t_{CPU\ mem} = t_{L1} + 0.01 (t_{L2} + 0.01 t_{MP}) = 2 \text{ ns}$$

$$t_{L2} = \frac{2 \text{ ns} - t_{L1} - 0.01^2 \cdot 400}{0.01} = \frac{0.96 \text{ ns}}{0.01} = 96 \text{ ns}$$