# The TwoPhaseInd package: Estimation of gene-treatment interactions in randomized clinical trials exploiting gene-treatment independence

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## 1 Introduction

In randomized clinical trials, there are often ancillary studies that uses outcome-dependent sampling to identify baseline genetic markers that modify treatment effect. The TwoPhaselnd package assembles several functions to estimate gene-treatment interactions in randomized clinical trials exploiting gene-treatment independence in case-control sampling and case-cohort sampling. For case-control sampling, it computes two estimators- semi-parametric maximum likelihood estimator exploiting (SPMLE) and maximum estimated likelihood estimator (MELE), exploiting the treatment-covariate independence resulted from randomization in two-phase randomized trials [1]. For case-cohort sampling, it has a function (acoarm) to estimate parameters in a cox regression model by a two-stage estimation procedure developed for augmented case-only designs [2].

# 2 SPMLE

We took a WHI biomarker study to illustrate our methods. The aforementioned 29 biomarkers were picked by WHI investigators as markers that are possibly associated with either stroke, venous thrombotic disease, or myocardial infarction. A comprehensive analysis of these samples was published by [3]. The results of this particular biomarker example were shown in [1]. The methodologies for estimating SPMLE and EMLE can be found in [1].

- > data(whiBioMarker)
- > dim(whiBioMarker)

[1] 16608 10

> str(whiBioMarker)

```
'data.frame':
                    16608 obs. of 10 variables:
 $ stroke : num 0 0 0 0 0 0 1 0 0 1 ...
 $ hrtdisp: num 1 1 0 1 1 1 1 1 0 1 ...
 $ papbl : num NA ...
          : num 64 62 62 60 54 57 77 68 73 64 ...
 $ age
 $ dias : num 74 70 70 79 70 88 62 60 60 67 ...
 $ hyp
         : Factor w/ 3 levels "Missing", "No", ...: 2 2 2 2 3 3 2 2 2 2 ...
 $ syst : num 116 135 133 133 119 ...
 $ diabtrt: Factor w/ 3 levels "Missing", "No", ...: 2 2 2 2 2 2 2 2 2 ...
 $ lmsepi : Factor w/ 5 levels "2 - <4 episodes per week",..: 5 4 1 4 1 5 5 4 2 2 ...
 $ phase : num 1 1 1 1 1 1 1 1 1 1 ...
Here is an example of estimating SPMLE without exploiting independent and with no
confounding factors:
> spmleNonIndNoExtra <- spmle(data=whiBioMarker, ## dataset
                   response="stroke",
                                              ## response variable
                   treatment="hrtdisp", ## treatment variable
                   BaselineMarker="papbl",
                                                   ## environment variable
                   extra=NULL,
                   phase="phase",
                                          ## phase indicator (1 and 2)
                   ind=FALSE ## independent or non-indepentent
+ )
> spmleNonIndNoExtra
                          beta stder
                                              pVal
(Intercept)
                       -4.4266 0.1147 0.0000000000
hrtdisp (Treatment)
                      0.3185 0.1473 0.0306369775
papbl (BaselineMarker) 2.2603 1.0152 0.0259794031
hrtdisp:papbl
                      -4.2536 1.2880 0.0009584502
  Here is an example of SPMLE with exploiting independent and with no confounding
> spmleIndNoExtra <- spmle(data=whiBioMarker,</pre>
                                                      ## dataset
                response="stroke", ## response variable
                treatment="hrtdisp",
+
                                           ## treatment variable
                BaselineMarker="papbl",
                                                        ## environment variable
+
                extra=NULL,
                phase="phase",
                                      ## phase indicator
+
                ind=TRUE
                                ## independent or non-indepentent
+ )
```

> spmleIndNoExtra

```
beta stder pVal
(Intercept) -4.4198 0.1131 0.0000000000
hrtdisp (Treatment) 0.3077 0.1463 0.0354228673
papbl (BaselineMarker) 1.9063 0.9097 0.0361172352
hrtdisp:papbl -3.9327 1.1533 0.0006499955
```

Here is an example of estimating SPMLE without exploiting independent and with confounding factors:

```
> spmleNonIndExtra <- spmle(data=whiBioMarker,</pre>
                                                       ## dataset
                 response="stroke", ## response variable
                 treatment="hrtdisp",
                                            ## treatment variable
                                                 ## environment variable
                 BaselineMarker="papbl",
+
                 extra=c(
                          "age"
+
                                                ## age
                          ## physical activity levels
                           , "dias"
                                            ## diabetes
                             "hyp"
                                           ## hypertension
                             "syst"
                                            ## systolic
                             "diabtrt"
                                              ## diastolic BP
                             "lmsepi" ## waist:hip ratio
                                         ## extra variable(s)
                               ),
                 phase="phase",
                                        ## phase indicator
+
                 ind=FALSE
                                   ## independent or non-independent
> spmleNonIndExtra
                              beta stder
                                                  pVal
                           -3.9599 0.6756 4.602982e-09
(Intercept)
                            0.3698 0.1599 2.071078e-02
hrtdisp (Treatment)
papbl (BaselineMarker)
                            2.3487 1.0565 2.620678e-02
hrtdisp:papbl
                           -4.1924 1.3313 1.637308e-03
                            1.3736 1.1935 2.497868e-01
age
                           -0.8499 0.9990 3.949167e-01
dias
hypNo
                           -0.7751 0.6229 2.133320e-01
hypYes
                           -0.7607 0.6288 2.263832e-01
                            3.3370 1.2286 6.603730e-03
syst
                            0.8811 0.3707 1.746453e-02
diabtrtYes
lmsepi4+ episodes per week 0.0022 0.3927 9.954563e-01
                           -0.1904 0.6121 7.557121e-01
lmsepiMissing
lmsepiNo activity
                           0.3231 0.4145 4.356103e-01
                           0.0659 0.3522 8.516191e-01
lmsepiSome activity
```

Here is an example of estimating SPMLE with exploiting independent and with confounding factors:

```
> spmleIndExtra <- spmle(data=whiBioMarker,
                                                    ## dataset
              response="stroke", ## response variable
              treatment="hrtdisp",
                                       ## treatment variable
              BaselineMarker="papbl",
+
                                              ## environment variable
              extra=c(
+
                 "age"
                               ## age
                                  ## physical activity levels
                  "dias"
                                ## diabetes
                  "hyp" ## hypertension
                  "syst" ## systolic
                  "diabtrt"
                                   ## diastolic BP
                  "lmsepi" ## waist:hip ratio
                             ## extra variable(s)
              phase="phase", ## phase indicator
+
              ind=TRUE ## independent or non-indepentent
> spmleIndExtra
                              beta stder
                                                 pVal
(Intercept)
                           -3.9647 0.6734 3.923841e-09
hrtdisp (Treatment)
                            0.3102 0.1467 3.440407e-02
papbl (BaselineMarker)
                           1.9058 0.9375 4.206696e-02
hrtdisp:papbl
                           -3.8688 1.1590 8.435226e-04
                            1.7675 1.2051 1.424798e-01
age
dias
                           -0.6402 0.9864 5.163627e-01
hypNo
                           -0.8253 0.6189 1.823384e-01
hypYes
                           -0.8161 0.6244 1.911675e-01
                            3.0481 1.2110 1.183349e-02
syst
                            0.9493 0.3715 1.060836e-02
diabtrtYes
lmsepi4+ episodes per week 0.1714 0.3879 6.586897e-01
lmsepiMissing
                           -0.1447 0.6089 8.121264e-01
lmsepiNo activity
                          0.3950 0.4085 3.336301e-01
lmsepiSome activity
                          0.1540 0.3488 6.588982e-01
```

### 3 MELE

Here is an example of MELE with exploiting independent and with no confounding factors:

```
> melIndNoExtra <- mele(data=whiBioMarker,</pre>
                                                  ## dataset
              response="stroke", ## response variable
              treatment="hrtdisp",
                                       ## treatment variable
              BaselineMarker="papbl",
                                             ## environment variable
+
              extra=NULL,
              phase="phase", ## variable for phase indicator
              ind=TRUE ## independent or non-indepentent
+ )
> melIndNoExtra
                         beta stder
                                             pVal
                      -4.4183 0.1128 0.0000000000
(Intercept)
hrtdisp (Treatment)
                      0.3065 0.1460 0.0357817680
papbl (BaselineMarker) 1.8586 0.8981 0.0385007661
                      -3.8660 1.1464 0.0007450917
hrtdisp:papbl
  Here is an example of MELE without exploiting independent with confounding fac-
tors:
> melNoIndNoExtra <- mele(data=whiBioMarker,</pre>
                                                    ## dataset
                response="stroke", ## response variable
+
                treatment="hrtdisp",
                                          ## treatment variable
+
                BaselineMarker="papbl",
                                               ## environment variable
+
                extra=NULL,
                phase="phase", ## phase indicator
                ind=FALSE ## independent or non-indepentent
+ )
> melNoIndNoExtra
                         beta stder
                                            pVal
(Intercept)
                      -4.4269 0.1148 0.000000000
hrtdisp (Treatment)
                     0.3202 0.1472 0.029616750
papbl (BaselineMarker) 2.2724 1.0199 0.025875181
```

Here is an example of MELE with exploiting independent and with confounding factors:

-4.2016 1.2855 0.001081392

hrtdisp:papbl

```
> melIndExtra <- mele(data=whiBioMarker, ## dataset
+ response="stroke", ## response variable
+ treatment="hrtdisp", ## treatment variable
+ BaselineMarker="papbl", ## environment variable
+ extra=c(</pre>
```

```
"age"
                              ## age
                                   ## physical activity levels
                   "dias"
                                  ## diabetes
                  "hyp" ## hypertension
+
                  "syst"
                                  ## systolic
+
                  "diabtrt"
                                    ## diastolic BP
                , "lmsepi" ## waist:hip ratio
                ),
                          ## extra variable(s)
            phase="phase",
                                   ## phase indicator
+
            ind=TRUE
                            ## independent or non-indepentent
+ )
> melIndExtra
                              beta stder
                                                  pVal
(Intercept)
                           -3.8846 0.7172 6.089906e-08
hrtdisp (Treatment)
                            0.3083 0.1463 3.511160e-02
papbl (BaselineMarker)
                            1.8662 0.9282 4.436775e-02
hrtdisp:papbl
                           -3.7931 1.1548 1.021672e-03
                            1.7872 1.2034 1.375141e-01
age
dias
                           -0.8270 1.0211 4.180127e-01
                           -0.8560 0.6636 1.971193e-01
hypNo
                           -0.9329 0.6739 1.662278e-01
hypYes
                            3.3869 1.2285 5.834062e-03
syst
diabtrtYes
                            0.9363 0.3711 1.164302e-02
lmsepi4+ episodes per week 0.1278 0.3903 7.434100e-01
lmsepiMissing
                           -0.2114 0.6500 7.450406e-01
                            0.4480 0.4086 2.729547e-01
lmsepiNo activity
                          0.1385 0.3515 6.935112e-01
lmsepiSome activity
```

Here is an example of MELE without exploiting independent and with confounding factors:

```
> melNoIndExtra <- mele(data=whiBioMarker,</pre>
                                                  ## dataset
              response="stroke",
                                     ## response variable
              treatment="hrtdisp",
                                       ## treatment variable
+
              BaselineMarker="papbl",
                                             ## environment variable
+
              extra=c(
                  "age"
                                  ## physical activity levels
+
                                   ## diabetes
                   "dias"
                  , "hyp"
                                  ## hypertension
                   "syst"
                                   ## systolic
                  , "diabtrt"
                                    ## diastolic BP
```

```
, "lmsepi" ## waist:hip ratio
                            ## extra variable(s)
              phase="phase",
                                    ## phase indicator
+
              ind=FALSE
                               ## independent or non-indepentent
+ )
> melNoIndExtra
                              beta stder
                                                  pVal
(Intercept)
                           -3.9227 0.7239 5.999024e-08
hrtdisp (Treatment)
                            0.3190 0.1587 4.441772e-02
papbl (BaselineMarker)
                            2.0377 1.0557 5.358469e-02
                           -3.7559 1.3308 4.767720e-03
hrtdisp:papbl
                            1.8170 1.2290 1.392979e-01
age
                           -1.0119 1.0309 3.263064e-01
dias
hypNo
                           -0.7987 0.6694 2.328199e-01
                           -0.9390 0.6790 1.666968e-01
hypYes
                            3.5970 1.2565 4.199987e-03
syst
diabtrtYes
                            0.7687 0.3844 4.551940e-02
lmsepi4+ episodes per week 0.1654 0.3953 6.756095e-01
                           -0.2160 0.6578 7.426848e-01
lmsepiMissing
lmsepiNo activity
                            0.4793 0.4148 2.478730e-01
lmsepiSome activity
                            0.1717 0.3586 6.319940e-01
    ACOARM
4
> data(acodata)
> dim(acodata)
[1] 907 14
> str(acodata)
'data.frame':
                    907 obs. of 14 variables:
                    : int 1442 1489 913 920 1448 1465 377 1274 1472 1463 ...
 $ vacc1_evinf
 $ f_evinf
                    : int 0000000000...
 $ subcoh
                    : logi
                           TRUE FALSE FALSE FALSE TRUE FALSE ...
 $ ptid
                    : int
                          9601 9603 9605 9606 9607 9608 9609 9610 9613 9614 ...
 $ f_treat
                    : int
                           1 1 1 1 0 0 1 1 1 0 ...
 $ fcgr2a.3
                    : num O NA NA NA NA NA NA NA NA ...
 $ f_agele30
                    : int
                          0 0 0 0 1 0 0 0 1 1 ...
 $ f_hsv_2
                    : num 0 1 0 0 0 0 0 0 0 0 ...
 $ f_ad5gt18
                    : int 0000000000...
```

```
$ f_crcm : num 1 1 1 1 1 1 1 1 1 1 1 ...
$ any_drug : num 1 1 1 1 0 0 0 0 1 0 0 ...
$ num_male_part_cat: num 0 0 0 1 0 0 0 0 0 0 ...
$ uias : num 0 1 1 1 1 0 0 0 0 0 0 ...
$ uras : num 0 0 0 0 1 0 0 0 0 0 ...
>
```

For two-arm, placebo-controlled trials with rare failure time endpoints, we can augment the case-only design with random samples of controls from both arms, as in the classical case-cohort sampling scheme, or with a random sample of controls from the active treatment arm only. We show that these designs can identify all parameters in a Cox model and that the efficient case-only estimator can be incorporated in a two-step plug-in procedure[2]. A data example was shown in [2] that incorporating case-only estimators in the classical case-cohort design improves the precision of all estimated parameters; sampling controls only in the active treatment arm attains a similar level of efficiency. Here is an example of ACO using controls from the placebo arm.

```
> rfit0 <- acoarm(data=acodata,</pre>
                    svtime="vacc1_evinf",
+
                    event="f_evinf",
+
                    treatment="f_treat",
+
                    BaselineMarker="fcgr2a.3",
                    id="ptid",
                    subcohort="subcoh",
                    esttype=1,
                    augment=0,
                    extra=c("f_agele30","f_hsv_2","f_ad5gt18","f_crcm","any_drug","num
> rfit0
                              beta stder
                                                 pVal
fcgr2a.3 (BaselineMarker)
                            0.1784 0.3871 0.64494332
f_treat (Treatment)
                            0.6327 0.4938 0.20009115
interatcion
                           -0.2550 0.3821 0.50455514
                            0.3637 0.6260 0.56120036
f_agele30
f_hsv_2
                            1.6177 0.6588 0.01405904
f_ad5gt18
                           -0.2784 0.6874 0.68553494
                            0.5609 1.0100 0.57868519
f_crcm
```

Here is an example of ACO using controls from the active arm

any\_drug

uias

uras

num\_male\_part\_cat

0.9704 0.6623 0.14286876

-1.7869 0.8573 0.03713643

0.7115 0.5203 0.17145652

0.9528 0.6391 0.13596896

```
event="f_evinf",
                    treatment="f_treat",
+
                    BaselineMarker="fcgr2a.3",
                    id="ptid",
+
                    subcohort="subcoh",
                    esttype=1,
                    augment=1,
                    extra=c("f_agele30", "f_hsv_2", "f_ad5gt18", "f_crcm", "any_drug", "num
> rfit1
                              beta stder
                                                 pVal
fcgr2a.3 (BaselineMarker) 0.2360 0.3765 0.53070424
f_treat (Treatment)
                            0.6327 0.4938 0.20009115
                           -0.2550 0.3821 0.50455514
interatcion
f_agele30
                            0.1902 0.5041 0.70593304
f_hsv_2
                            0.8494 0.5389 0.11497257
f_ad5gt18
                            0.3646 0.4553 0.42326823
                           -0.1616 0.5843 0.78213299
f\_crcm
any_drug
                            1.0837 0.5540 0.05047852
                            0.1792 0.6052 0.76711529
num_male_part_cat
uias
                            0.0663 0.4531 0.88368210
                            1.1437 0.4905 0.01972308
uras
   Here is an example of ACO using controls from both arms
> rfit2 <- acoarm(data=acodata,</pre>
                    svtime="vacc1_evinf",
                    event="f_evinf",
                    treatment="f_treat",
                    BaselineMarker="fcgr2a.3",
+
                    id="ptid",
                    subcohort="subcoh",
                    esttype=1,
                    augment=2,
                    extra=c("f_agele30", "f_hsv_2", "f_ad5gt18", "f_crcm", "any_drug", "num
> rfit2
                              beta stder
                                                   pVal
fcgr2a.3 (BaselineMarker) 0.1904 0.3119 0.5414829219
f_treat (Treatment)
                           0.6327 0.4938 0.2000911539
                           -0.2550 0.3821 0.5045551427
interatcion
```

> rfit1 <- acoarm(data=acodata,</pre>

svtime="vacc1\_evinf",

```
f_agele30
                            0.0740 0.3436 0.8293998716
                            1.2066 0.3981 0.0024400419
f_hsv_2
f_ad5gt18
                            0.1039 0.3728 0.7804757254
                            0.1086 0.4375 0.8039160862
f_crcm
                            1.1332 0.3709 0.0022464789
any_drug
                           -0.4866 0.4127 0.2383614665
num_male_part_cat
                            0.2364 0.3324 0.4769372489
uias
uras
                            1.1534 0.3458 0.0008510074
```

## 5 Session Information

The version number of R and packages loaded for generating the vignette were:

```
R version 3.2.2 (2015-08-14)
```

Platform: x86\_64-pc-linux-gnu (64-bit) Running under: Ubuntu 14.04.2 LTS

#### locale:

[1] LC\_CTYPE=en\_US.UTF-8 LC\_NUMERIC=C

[3] LC\_TIME=en\_US.UTF-8 LC\_COLLATE=en\_US.UTF-8
[5] LC\_MONETARY=en\_US.UTF-8 LC\_MESSAGES=en\_US.UTF-8

[7] LC\_PAPER=en\_US.UTF-8 LC\_NAME=C

[9] LC\_ADDRESS=C LC\_TELEPHONE=C

[11] LC\_MEASUREMENT=en\_US.UTF-8 LC\_IDENTIFICATION=C

#### attached base packages:

[1] stats graphics grDevices utils datasets methods base

#### other attached packages:

[1] TwoPhaseInd\_1.1.0

loaded via a namespace (and not attached):

[1] tools\_3.2.2 survival\_2.38-3 splines\_3.2.2

## References

- [1] J. Y. Dai, M. LeBlanc, and C. Kooperberg. Semiparametric estimation exploiting covariate independence in two-phase randomized trials. *Biometrics*, 65(1):178–187, Mar 2009.
- [2] J. Y. Dai, X. C. Zhang, C. Y. Wang, and C. Kooperberg. Augmented case-only designs for randomized clinical trials with failure time endpoints. *Biometrics*, 2015.

[3] C. Kooperberg, M. Cushman, J. Hsia, J. G. Robinson, A. K. Aragaki, J. K. Lynch, A. E. Baird, K. C. Johnson, L. H. Kuller, S. A. Beresford, and B. Rodriguez. Can biomarkers identify women at increased stroke risk? the women's health initiative hormone trials. *PLoS clinical trials*, 2(6):e28, Jun 15 2007.