

Signal & System 2022 期末考模擬

- 手做答案可以手寫拍照。
- 程式考題寫出程式碼以及列印執行結果。
- 一並彙整為一個pdf檔上傳。
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- 將請助教開一個 E-Learning 作業於考試當天(6月17日)限時(2.5小時)之內上傳。
- 正式考試為第17周上課時間(6月17日15:00~18:00)

(1)

What is a linear chirp signal? Write down its mathematical function.

(2)

Write a function called myChirp(), it can generate a chirp signal.

- input:
 - a time sequence: $ts = [0, 0.0001, 0.0002, \dots, T]$ in (sec)
 - a start frequency f_0 (Hz),
 - a ending frequency f_1 (Hz).
- output:
 - the chirp sequence: $ys = \text{myChirp}(ts)$

```
def myChirp(ts, f0=100, f1=400):
```

```
    #  
    # your code ...  
    #  
    return ys
```

```
# 1. generate a time sequence from 0 sec to 10 sec  
# 2. test your function.
```

(3) what is DFT (Discrete Fourier Transform), and IDFT (Inverse Discrete Fourier Transform), write down their mathematical definition.

(4) Given a time-domain sequence $x[n] = [1, 1, 1, 1]$, please calculate the DFT $X[k]$. and also compute $y[n]$, which is the IDFT of $X[k]$.

(5)

Write a function called myDft(), it can compute the DFT of any signal $x[n]$ or the IDFT of any spectrum $X[k]$.

- input:
 - a time-domain signal: $x = [x_0, x_1, \dots, x_{N-1}]$
 - or a frequency-domain spectrum: $X = [X_0, X_1, \dots, X_{N-1}]$
- output:

- a spectrum $X[k]$ or a signal $x[n]$

```
def myDft(x, inverst=False):
    #
    # your code ...
    #
    #
    #
    return X
```

```
# 1. generate a time-domain signal  $x[n]$  or a time-domain spectrum  $X[k]$ 
# 2. test your function.
```

(6) If x is a Cosine signal with frequency = 100 Hz, generate a discrete signal with sampling frequency, $F_s = 1000$ samples/sec, for 10 sec. compute the spectrum $X[k]$ of the the signal $x[n]$ and plot $X[k]$, what does it look like?

(7) what is convolution of 2 signal $x[n]$ and $y[n]$, please write down their mathematical definition.

(8) if $x = [1,1,1,1]$, $y = [1,2,3,4,5]$, what is their convolution $z = x*y$?

(9) write a function called `myConvolution()`, which can compute the convolution of two signal.

```
def myConvolution(x,y):
    #
    # your code to implement
    #  $z = x * y$ 
    #
    return z
```

(10) what is the convolution theorem?

(11) Verify the convolution theorem by using `myDft()` and `myConvolution()`

In []: