

$$1. (a) W_1 = \begin{bmatrix} 2 & 0 & 1 \\ -0.5 & 2 & -2.5 \\ 0.5 & -2 & 0.5 \end{bmatrix} \quad W_2 = \begin{bmatrix} 0 & -1.5 & -1 & 1 \\ 1 & 2 & -3 & -2 \end{bmatrix}$$

$$W_1 \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix} = \begin{bmatrix} 3 \\ 1.25 \\ -3 \end{bmatrix} \Rightarrow \begin{bmatrix} 3.25 \\ 1.25 \\ 0 \end{bmatrix} \quad W_2 \begin{bmatrix} 3 \\ 1.25 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} -0.805 \\ 3.5 \end{bmatrix} \Rightarrow \begin{bmatrix} 0 \\ 3.5 \end{bmatrix}$$

$$(b) S_i = 1 \times (0 \times 0 + 1 \times 3.5) = 3.5$$

$$S_j = 1 \times (1.5 \times 0 + 2 \times 3.5) = 7$$

$$S_k = 0$$

$$S_{ep} = 5 - 0 = 5$$

$$S_p = 0$$

$$S_{eq} = 7 - 3.5 = 3.5$$

$$S_q = 1 \times 3.5 = 3.5$$

$$(c) W_1 = \begin{bmatrix} r & 1.4 & 1.7 \\ 0.7 & s & -0.85 \\ 0.5 & -2 & t \end{bmatrix}, \quad W_2 = \begin{bmatrix} 0 & m & -1 & 1 \\ 3.1 & n & -3 & -1.2 \end{bmatrix}$$

$$\Delta r = 0.2 \times 1 \times 3.5 = 0.7 \quad r = 2 + 0.7 = 2.7$$

$$\Delta s = 0.2 \times 2 \times 7 = 2.8 \quad s = 2 + 2.8 = 4.8$$

$$\Delta t = 0.2 \times 1 \times 0 = 0 \quad t = 0.5$$

$$\Delta m = 0.2 \times 1.25 \times 0 = 0 \quad m = 0 - 1.5 = -1.5$$

$$\Delta n = 0.2 \times 1.25 \times 3.5 = 0.875 \quad n = 2 + 0.875 = 2.875$$

$$z. (a) \begin{cases} i = \sqrt{3} + 1 = 1 \\ j = \sqrt{2} - 1 = 0.5 \\ k = 1 - \sqrt{3} + 1 = -1 \end{cases} \quad \begin{bmatrix} 0 & -1.5 & -1 \\ 1 & 2 & -3 \end{bmatrix} \begin{bmatrix} 0.5 \\ -1 \\ 1 \end{bmatrix} = \begin{bmatrix} -0.75 + 1 + 1 \\ 1.1 + 3 - 2 \end{bmatrix} = \begin{bmatrix} 1.25 \\ 3 \end{bmatrix}$$

$$p = \sqrt{2} - 1 = 0.5$$

$$q = \sqrt{3} + 1 = 1$$

$$(b) : \delta i = g'(3) \times (0 + 1 \times 1.5) = 0.375$$

$$\delta j = g'(1.25) \times (1.5 \times 1.5 + 2 \times 1.5) = 0.25$$

$$\delta k = g'(-3) \times (-1 \times 1.5 + -3 \times 1.5) = -1.5$$

$$\delta p = 4.5 \times g'(1.25) = 1.5$$

$$\delta q = 6 \times g'(3) = 1.5$$

$$(c) W = \begin{bmatrix} r & 0.15 & 1.075 \\ -0.45 & s & -2.2 \\ 0.2 & -2.6 & t \end{bmatrix}, W_2 = \begin{bmatrix} 0.3 & m & -1.3 & 1.3 \\ 1.3 & n & -3.3 & -1.7 \end{bmatrix}$$

$$\Delta r = 0.2 \times$$

$$r = 0.2 \times 1 \times 0.375 + 2 = 2.075$$

$$\Delta s = 0.2 \times$$

$$s = 0.2 \times 2 \times 0.25 + 2 = 2.1$$

$$\Delta t = 0.2 \times$$

$$t = 0.2 \times 1 \times -1.5 + 0.5 = 0.2$$

$$\Delta m = 0.2 \times$$

$$m = 0.2 \times 0.5 \times 1.5 + (-1.3) = -1.35$$

$$\Delta n = 0.2 \times$$

$$n = 0.2 \times 0.5 \times 1.5 + 2 = 2.15$$