

# Biostatistics

Week #13

5/26/2020



# Ch 11 – Comparison of Two Means



# Introduction

- In previous chapter we learned how to compare the unknown mean of a ***single*** population to some fixed, known value  $\mu_0$ .
- In practical applications, it is common to compare the means of ***TWO*** populations where both means are not known.
- ***Matched pair comparison*** is important in many scientific aspects.
- The idea is to draw a conclusion about their similarities or differences.

# Example 1

- We are interested in knowing the relationship between the use of ***oral contraceptives (OC)*** and the level of ***blood pressure (bp)*** in women.
- Two different experiment designs can be used to assess this relationship – ***longitudinal*** study and ***cross-sectional*** study.

# Longitudinal Study

- Identify a group of women who are not currently OC users and measure their bp.
- Rescreen these (same) women 1 year later and ascertain a subgroup who have become OC users. Measure their bp. This approach is often called a ***follow-up*** study.
- Compare these bps for the same women.

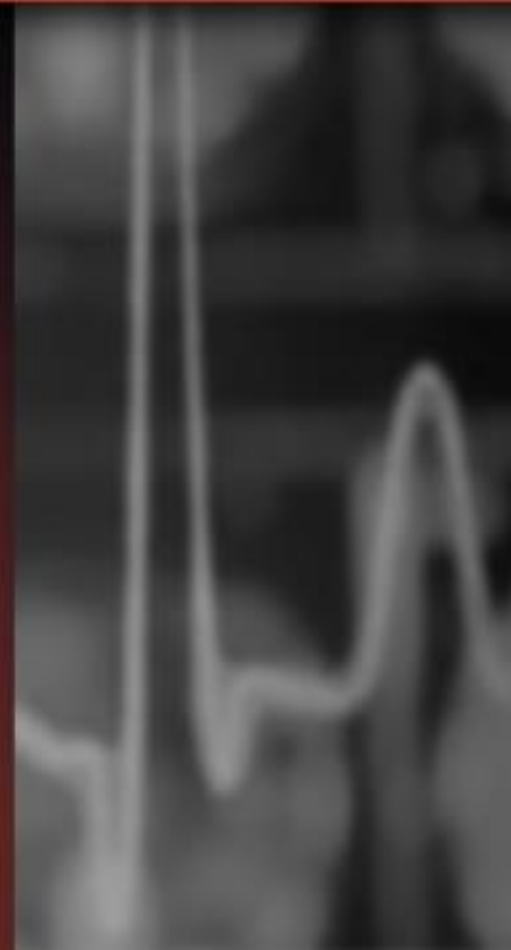
# Cross-Sectional Study

- Identify both a group of OC users and a group of non-OC users. Measure their bps.
- Compare their bps.

# Comments

- Longitudinal study uses paired samples. It is more **definitive**, since most confounding factors that influence the women's bp will be present both in the screening and the follow-ups.
- Cross-sectional study uses independent samples, which is usually considered **suggestive** only, because of possible confounding factors.

# 11.1 Paired Samples





## Example 2

- It was suspected that the amount of carbon monoxide CO (一氧化碳) in the air could increase the carboxyhemoglobin (一氧化碳血紅素) level for patients with coronary artery (冠狀動脈) disease, which might cause angina (心絞痛) .
- We wish to perform a hypothesis testing on the assumption that *indeed the increased CO level would be a threat to patients with coronary artery disease.*

# Study design

- Same individuals for taking the experiment (a longitudinal study).
  - ***Control group*** for having them breathe in normal air.
  - ***Experiment group*** for having them breathe in CO-rich air.
- Which group would have a ***quicker onset*** of angina. That is, the ***time elapse to angina onset*** is ***shorter***.

Note that 'group' here means different breathing conditions, not different people.

# Cont'd

- 63 patients are randomly selected to measure *the percent decreases in time to angina* (our random variable) for each of the following two occasions. (See next slide)
- More decrease in time to angina means quicker onset, which is more threatening.

- Occasion #1 (control group):
  - On a given day, each individual exercises on a treadmill (跑步機) until the patient experiences angina, for which the onset time for angina  $t_1$  was recorded.
  - The same patient (after experiencing angina at  $t_1$ ) is exposed to plain room air for approximately 1 hour, followed by performing a second exercise test until the onset time for another angina  $t_2$  was recorded.
  - Usually  $t_2$  will be smaller than  $t_1$ , so  $t_1 - t_2$  would be a positive number.

- Occasion #2 (experiment group):
  - On another day, each individual again exercises on a treadmill (跑步機) until the patient experiences angina, for which the onset time for angina  $t_1$  was recorded.
  - The same patient (after experiencing angina at  $t_1$ ) is exposed to room air abundant with carbon monoxide (CO) for approximately 1 hour, followed by performing a second exercise test until the onset time for another angina  $t_2$  was recorded.

- We are interested in the “percent decrease in time”
- For example, if a patient was recorded  $t_1 = 983$  and  $t_2 = 957$  seconds in control group, we will have this value

$$\frac{983 - 957}{983} = 0.026 = 2.6\%$$

- The same individual in experiment group has  $t_1 = 991$  and  $t_2 = 900$ , then

$$\frac{991 - 900}{991} = 0.092 = 9.2\%$$

*Larger means more threatening...*

- It is also possible that the two random variables are  $(+,-)$ ,  $(-,+)$  and  $(-,-)$ .
- For example, if a patient was recorded  $t_1 = 983$  and  $t_2 = 957$  seconds in control group, we will have this value

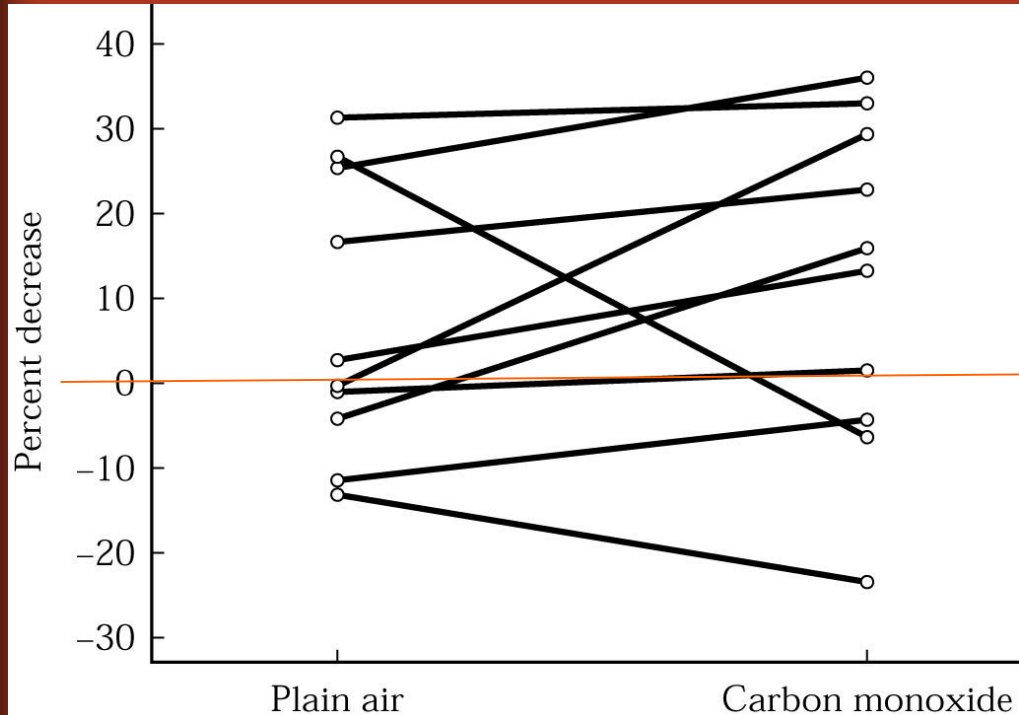
$$\frac{983 - 957}{983} = 0.026 = 2.6\%$$

- The same individual in experiment group has  $t_1 = 991$  and  $t_2 = 999$ (吸了CO變得更強!!), then

$$\frac{991 - 999}{991} = -0.008 = -0.8\%$$

*Larger means more threatening...*

# The matched pairs experiment



**FIGURE 11.1**

Percent decrease in time to angina on two different occasions for each of ten men with coronary artery disease

- It looks like most of the pairs have the “percent decrease” up (i.e., earlier onset of angina in CO environment) instead of down.

- ***Is such increase significant?***

***Larger means more threatening...***



# Matched Pairs Experiment – initial statement

- Compare two populations of percent decreases in time to angina.
- The parameter tested is  $\mu_1 - \mu_2$

Sample 1	Sample 2
$x_{11}$	$x_{12}$
$x_{21}$	$x_{22}$
$x_{31}$	$x_{32}$
$\vdots$	$\vdots$
$x_{n1}$	$x_{n2}$

*Negative means threatening. More negative, more threatening...*

$\mu_1$  The population mean of percent decreases exposed to plain air

$\mu_2$  The population mean of percent decreases exposed to carbon Monoxide (CO)

# The Null Hypothesis

- We'd like to know whether indeed the increased CO level would be a threat to patients with coronary artery disease.
- A threat can be interpreted as a quicker onset of second angina (a larger “percent decrease in time”, or  $\mu_2$  is greater than  $\mu_1$ ).
- Let the null hypothesis be the following:

$$H_0: (\mu_1 - \mu_2) \geq 0$$

*1: plain air*

*2: carbon monoxide*

## Cont'd

- This null hypothesis states that observations in sample 1 would be in general matching or greater than in sample 2.
- Rejecting it would suggest otherwise. That is, sample 2 indeed gives significantly larger values of “percent decrease in time”

$$H_0: (\mu_1 - \mu_2) \geq 0$$

$$H_A: (\mu_1 - \mu_2) < 0$$

# The problem is...

- *How would we evaluate  $\mu_1 - \mu_2$  as a random variable?*
- Computing  $\mu_1$  from sample #1 and  $\mu_2$  from sample #2 will not serve this purpose.  
[because it is a single observation, not a random variable]
- We need to define a random variable representing the difference of “percent decrease in time” between two samples.

# Matched Pairs Experiment – changing statement

- Since the difference of the means is equal to the mean of the differences, we can rewrite the hypotheses in terms of  $\delta$  (the mean of the differences) rather than in terms of  $\mu_1 - \mu_2$ .

## Difference $d$

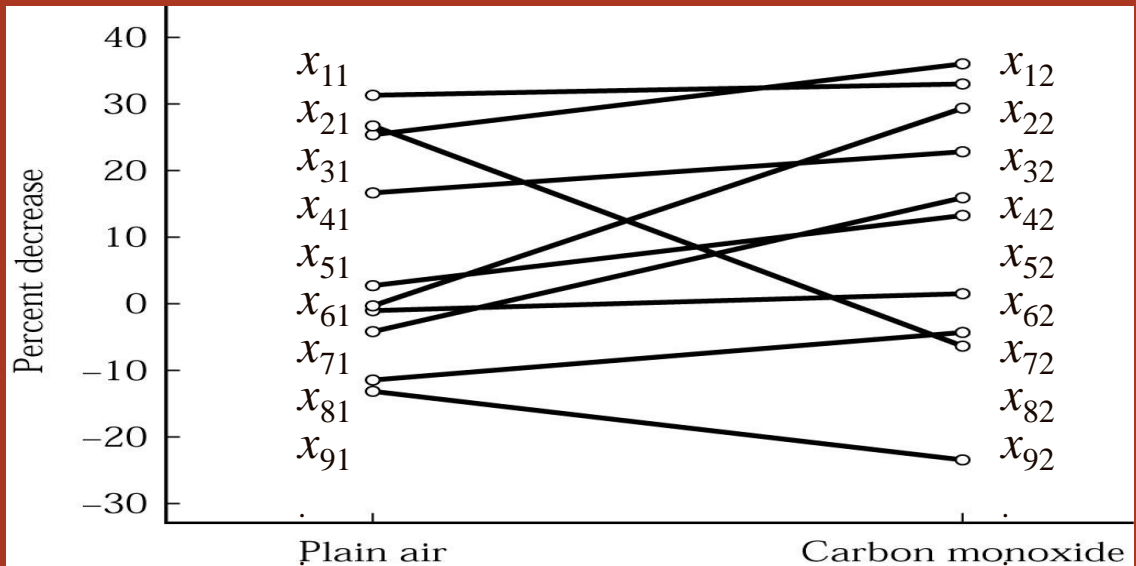
$$d_1 = x_{11} - x_{12}$$

$$d_2 = x_{21} - x_{22}$$

$$d_3 = x_{31} - x_{32}$$

...

$$d_n = x_{n1} - x_{n2}$$



**FIGURE 11.1**

Percent decrease in time to angina on two different occasions for each of ten men with coronary artery disease

# The paired t-test

- Solution

- $\delta = \mu_1 - \mu_2$  is the “percent decrease in time”

- The hypotheses:

- $H_0: \bar{d} = \delta (=0)$  (i.e., no difference of angina onset)

- $H_A: \delta < 0$  (scenario #2 has bigger “percent decrease in time”, or early onset of angina)

- The  $t$  statistic:

$$t = \frac{\bar{d} - \delta}{s_d / \sqrt{n}}$$

*Note that we changed  $\delta \geq 0$  to  $\delta = 0$  here!*

# The paired *t*-test

## The *t*-statistics

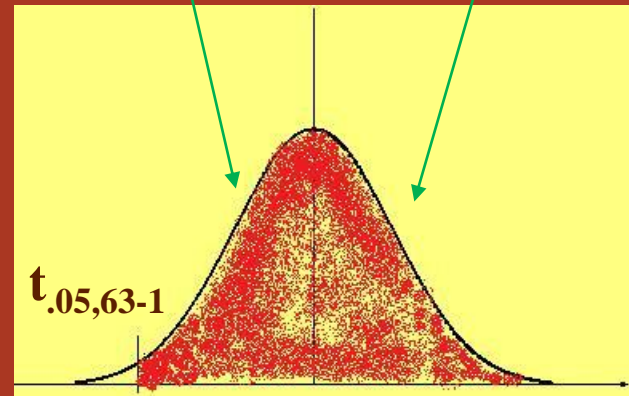
$$t = \frac{\bar{d} - \delta}{s_d / \sqrt{n}}$$

For the null hypothesis to match  $\delta = 0$ , a negative mean value of  $d$  would result in a negative  $t$  towards the left tail. Further into the left tail would suggest to reject the null hypothesis that  $\delta = 0$ .

**This is a one-sided test with a left-tail.**

*Mean values only slightly less than 0 would suggest  $\mu_1$  and  $\mu_2$  are comparable.*

*Mean values greater than 0 wouldn't serve our purpose to show CO threat.*

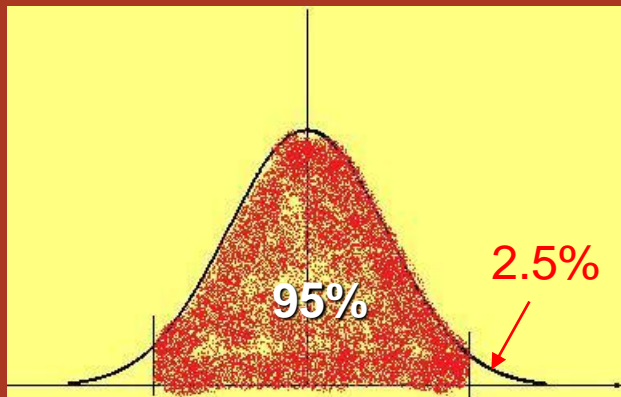


The rejection region is  
 $t < t_{.05,63-1}$

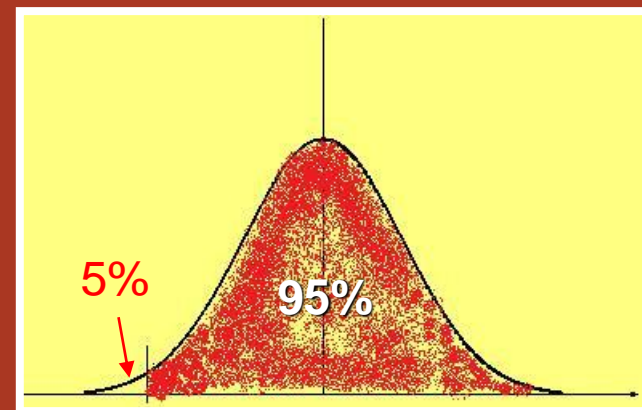
Degrees of freedom =  $n - 1$

# Computing $t_{.05,63-1}$

- Recall that earlier we had the MATLAB function `TINV` giving this value  $t$ .
- Note that we had a 2-tailed test then (left).
- Now we have a one-sided test (right).



```
>> tinv(0.975,62)  
ans = 1.9990
```

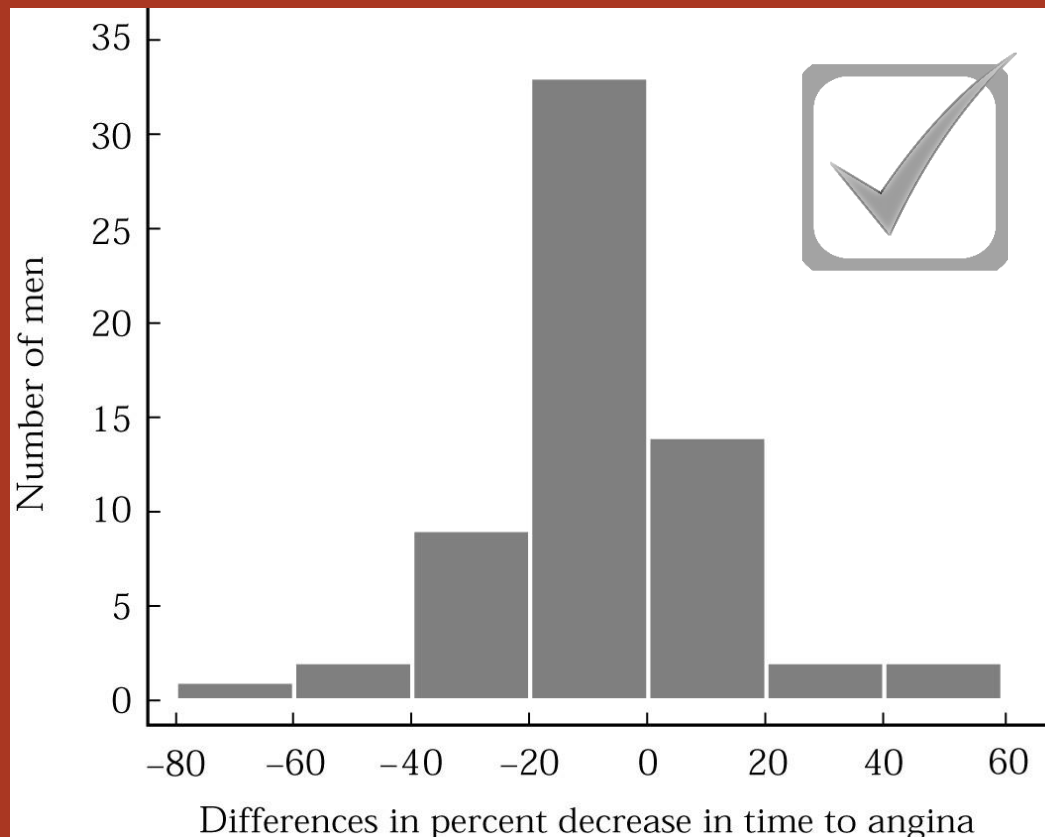


```
>> tinv(0.05,62)  
ans = -1.6698
```



# Checking the required conditions for the paired observations case

- The validity of the results depends on the normality of the differences. Indeed we have a fairly normal distribution here!



# Matched Pairs Experiment – implementation

- Solution (given the following statistics)

$$\bar{d} = \frac{\sum_{i=1}^{63} d_i}{63} = -6.63$$
$$s_d = 20.29$$

*It is a negative value, which is good. But is it negative enough to reject the null hypothesis, so that we may ascertain that CO-environment promotes angina onset?*

– Calculate t

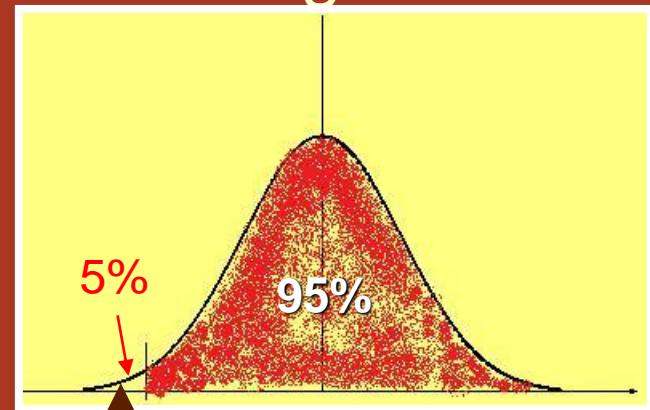
$$t = \frac{\bar{d} - \delta}{s_d / \sqrt{n}} = \frac{-6.63 - 0}{20.29 / \sqrt{63}} = -2.59$$

**Rejecting the null hypothesis, since it is further to the left tail of t=-1.6698.**

# Computing $p=P(t < -2.59)$

- Although we can immediately know to reject the hypothesis when obtaining  $t = -2.59$  which is smaller than  $t_{.05,62} = -1.6698$ , we can still use MATLAB to compute the p-value for this sample.
- Below we use MATLAB in performing this computation.

```
>> tcdf(-2.59,62)  
ans =  
    0.0060
```



```
>> tinvcdf(0.05,62)  
ans = -1.6698
```

# Matched Pairs Experiment – Conclusion

- There is a significance difference of the mean percent decreases in time to angina between two exposures. [statistically different~~~]
- Sample 2 apparently delivers larger percent decreases in time, suggesting patients exposed to CO would likely to have a quicker onset of angina.

$$H_0: (\mu_1 - \mu_2) \geq 0$$

$$H_A: (\mu_1 - \mu_2) < 0$$

# Example 3 – BP changes upon using OC?

N	Systolic bp with no OC ( $x_1$ )	Systolic bp with OC ( $x_2$ )	$d = x_2 - x_1$
1	115	128	13
2	112	115	3
3	107	106	-1
4	119	128	9
5	115	122	7
6	138	145	7
7	126	132	6
8	105	109	4
9	104	102	-2
10	115	117	2

```
>> x1=[115 112 107 119 115 138 126 105 104 115];  
>> x2=[128 115 106 128 122 145 132 109 102 117];  
>> d=x2-x1 =  
13 3 -1 9 7 7 6 4 -2 2
```

- The null hypothesis would be  $d=0$ .
- This is a ***2-tailed test***.
- This is a t-test since no population standard deviation is available.
- Degree of freedom is  $10-1=9$ .
- Level of significant  $\alpha = 0.05$ .

```
>> mu=mean(d)
mu = 4.8000

>> std=std(d)
std = 4.5656

>> t=(mu-0)/(std/sqrt(10))
t = 3.3247

>> 2*(1-tcdf(t,9))
ans = 0.0089

>>
```

Since  $p$  is smaller than 0.05, we conclude that  $bp$  will change significantly (regardless increasing or decreasing) when using OC.

# Comments

- This example problem asked “whether BP changes upon using OC”. This is a 2-sided test since we did not ask whether BP will drop or rise.
- If the problem asked “whether BP rises upon using OC”, then this would be a 1-sided test with a p-value half of what we obtained earlier. Still we’d reject the null hypothesis that the BP change equals to zero.

# A Brief Summary

- Here we covered “Chapter 11.1 – Paired Samples”:
  - For each observation on the first group, there is a corresponding observation in the second group. So we may reduce the problem to a one-sample test problem (using one difference of the mean, instead of two means from two samples).
  - In this case, the two samples are paired (or dependent).



## 11.2 Independent Samples

- In many cases, however, the two groups of measurements of interests are not paired. 【cross-sectional study...】
- For example, we are interested in the serum iron level of two groups of children:
  - One group healthy (with mean  $\mu_1$ )
  - The other group suffering from cystic fibrosis (囊腫性纖維化) (with mean  $\mu_2$ )
  - Two types of populations are independent and normally distributed.

# The Null Hypothesis

- We wonder if the two population means are equal. (That is, if the difference of serum iron level would attribute to this hereditary disease or not).
- So the null hypothesis would be

$$H_0 : \mu_1 - \mu_2 = 0$$

or

$$H_0 : \mu_1 = \mu_2$$

		Group 1	Group 2
Population	Mean	$\mu_1$	$\mu_2$
	Standard Deviation	$\sigma_1$	$\sigma_2$
Sample	Mean	$\bar{x}_1 = 18.9$	$\bar{x}_2 = 11.9$
	Standard Deviation	$s_1 = 5.9$	$s_2 = 6.3$
	Sample Size	$n_1 = 9$	$n_2 = 13$

- Two samples each was drawn from these two normally distributed populations, each with its own mean, STD and sample size.
- We'd like to perform a *t*-test on the proposed null hypothesis

$$H_0 : \mu_1 - \mu_2 = 0$$

## 11.2.1 Equal Variances

- We first assume that the two population variations are identical (i.e.,  $\sigma_1 = \sigma_2 = \sigma$ )
- By central limit theorem, we can perform the following conversion where the normally distributed  $\bar{x}$  would become a standard normal distribution  $z$ .

$$z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$$

# Cont'd

- Since we are dealing with the samples from two independent normal distribution, we utilize **an extension of the central limit theorem** that the difference in means  $\bar{x}_1 - \bar{x}_2$  is approximately normal with mean  $\mu_1 - \mu_2$  and standard error  $\sqrt{\sigma_1^2/n_1 + \sigma_2^2/n_2}$
- Since  $\sigma_1 = \sigma_2 = \sigma$ , we now have the z conversion as

$$z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$$

Before...

$$\begin{aligned} z &= \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\sigma^2/n_1 + \sigma^2/n_2}} \\ &= \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\sigma^2[(1/n_1) + (1/n_2)]}} \end{aligned}$$

## Cont'd

- If the population variance  $\sigma^2$  is known, we may use this z-statistics to test the proposed null hypothesis, as we have done before.

$$z = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\sigma^2/n_1 + \sigma^2/n_2}}$$
$$= \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\sigma^2[(1/n_1) + (1/n_2)]}}$$

$$\frac{\sigma}{\sqrt{n}}$$

$$\frac{\sigma}{\sqrt{n_1 + n_2}}$$

Note the correct formula for the denominator (分母)

# Using t-statistics

- As noted earlier, it is much more common that the true value of  $\sigma^2$  is not known. In this case, we use t-statistics instead of z-statistics:

$$t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{s_p^2 [(1/n_1) + (1/n_2)]}}$$

where the new quantity  $s_p$  is a “pooled” estimate of the variance, which replaces  $\sigma^2$  used in the z-statistics.

# Computing $s_p^2$

- The pooled estimate of the variance combines information from both samples to produce a more reliable estimate for the variance  $\sigma^2$ . (Recall we still assume that the two population variations are identical)
- If we know all measurements in the samples, we may compute it by

$$s_p^2 = \frac{\sum_{i=1}^{n_1} (x_{i1} - \bar{x}_1)^2 + \sum_{j=1}^{n_2} (x_{j2} - \bar{x}_2)^2}{n_1 + n_2 - 2}$$

1

Similar to the formula of variance given before.



## Cont'd

- If the two standard variations ( $s_1$  and  $s_2$ ) of two samples are known, the previously formula can be easily replaced by

$$s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$$

2

One can see that this is actually a **weighted average** of the two sample variances  $s_1^2$  and  $s_2^2$ .

# Example 4

- Consider the two-group children example mentioned earlier:

		Group 1	Group 2
Population	Mean	$\mu_1$	$\mu_2$
	Standard Deviation	$\sigma_1$	$\sigma_2$
Sample	Mean	$\bar{x}_1 = 18.9$	$\bar{x}_2 = 11.9$
	Standard Deviation	$s_1 = 5.9$	$s_2 = 6.3$
	Sample Size	$n_1 = 9$	$n_2 = 13$

We'd like to test whether children with cystic fibrosis (group 2) would have a level of iron in their blood on average as healthy children (group 1). There we test the null hypothesis that the two population means are identical.

# Solution

- The null hypothesis states that there is no difference in the underlying population mean iron levels for the two groups of children.
- **Two-sided t-test** will be performed, with a preset level of significance  $\alpha=0.05$ .

$$H_0 : \mu_1 - \mu_2 = 0$$

- We first compute the pooled estimate of the variance using formula 2 we have seen earlier.

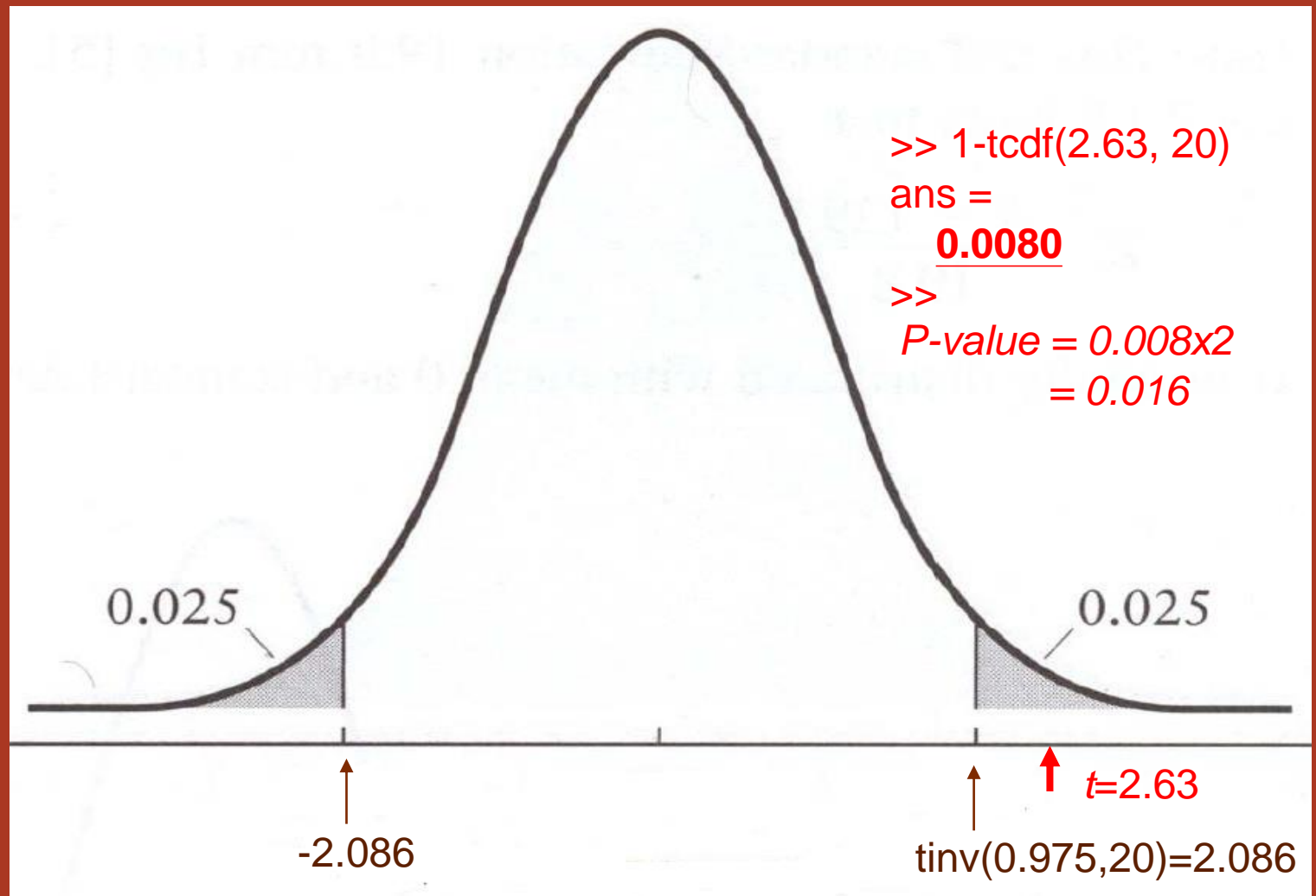
$$\begin{aligned}s_p^2 &= \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2} \\&= \frac{(9 - 1)(5.9)^2 + (13 - 1)(6.3)^2}{9 + 13 - 2} \\&= \frac{(8)(34.81) + (12)(39.69)}{20} \\&= 37.74.\end{aligned}$$

Effective degree of freedom when using t-correction

- With this, we can now compute for the t-statistics:

$$\begin{aligned} t &= \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{s_p^2 [(1/n_1) + (1/n_2)]}} \\ &= \frac{(18.9 - 11.9) - 0}{\sqrt{(37.74)[(1/9) + (1/13)]}} \\ &= 2.63. \end{aligned}$$

# Two-sided distribution (df=20)



# Conclusion

- We computed for a p-value of 0.016. **This is smaller than  $\alpha=0.05$  for us to reject the null hypothesis.**
- That is, the **difference** between the mean serum iron level of healthy children (group 1) and ones with cystic fibrosis (group 2) is **statistically significant**.
- Based on these samples, it appears that children with cystic fibrosis **suffer** from an iron deficiency.

## Estimating 95% CI for this difference of mean

$$P\left(-2.086 \leq \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{s_p^2 [(1/n_1) + (1/n_2)]}} \leq 2.086\right) = 0.95.$$

So the 95% CI for  $\mu_1 - \mu_2$  can be computed as

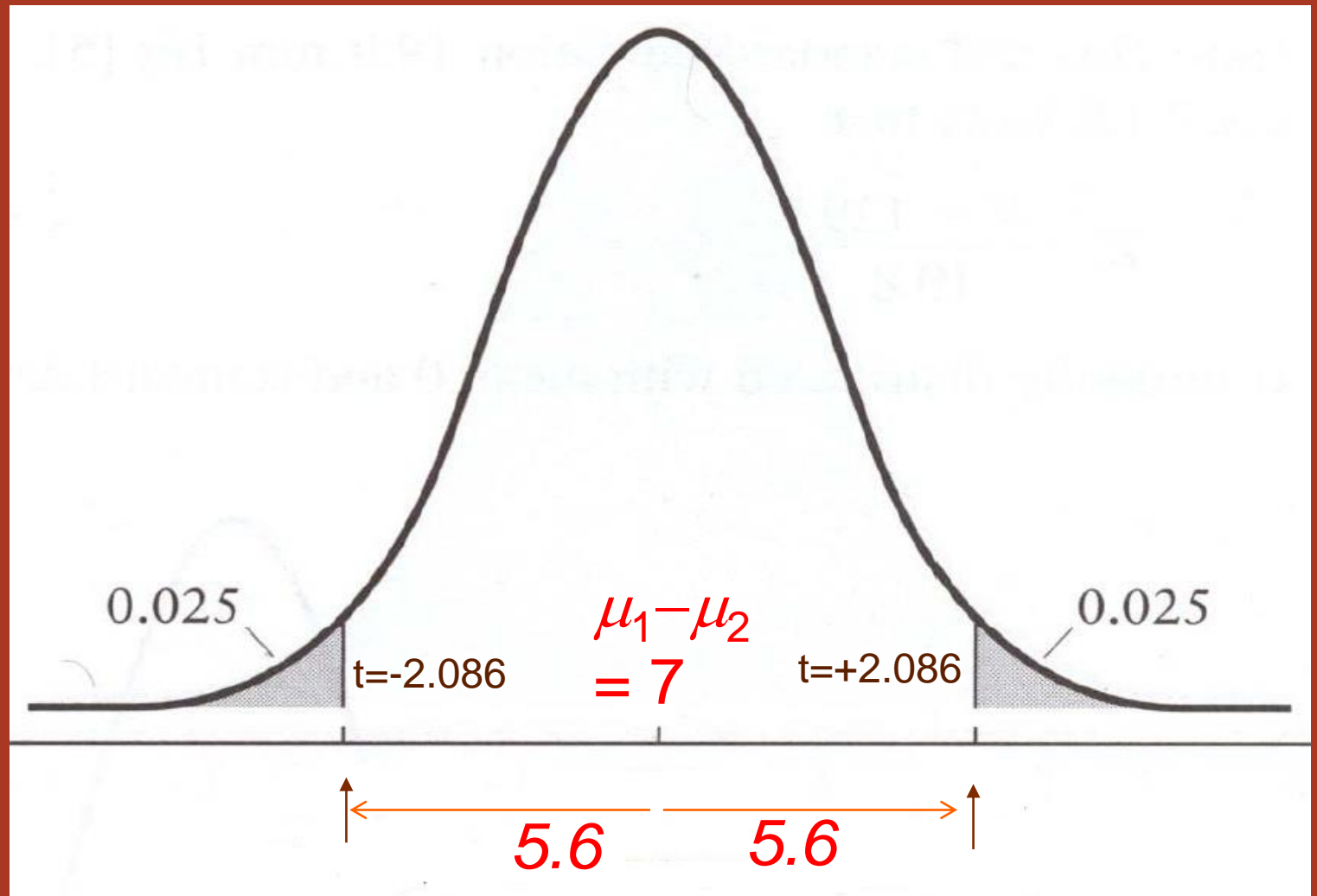
$$(\bar{x}_1 - \bar{x}_2) \pm (2.086) \sqrt{s_p^2 \left[ \frac{1}{n_1} + \frac{1}{n_2} \right]}, \text{ or}$$

$$(18.9 - 11.9) \pm (2.086) \sqrt{(37.74) \left[ \frac{1}{9} + \frac{1}{13} \right]}.$$



## Cont'd

- That is, we are 95% confident that the interval (1.4, 12.6) covers  $\mu_1 - \mu_2$ , the true difference in mean serum iron levels for the two populations of children.
- Note that the interval does not contain the value 0 (meaning that  $\mu_1 \neq \mu_2$ ), which is consistent with the result from the hypothesis testing we performed earlier.



# Summary

- The analysis we have seen in this lecture will pave way into Chapter 12, where we will do analysis of variance comparing two or more populations of interval data.
- This is an extension of the two-sample  $t$ -test we have seen here to three or more samples.

## 11.2.2 Unequal Variances?

- What if the two datasets do not have equal variance?
- In other words, earlier mentioned using  $s_p^2$  as an estimate of the common variance  $\sigma^2$  won't be valid.

$$\begin{aligned} z &= \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\sigma_1^2/n_1 + \sigma_2^2/n_2}} \\ &= \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\sigma^2[(1/n_1) + (1/n_2)]}} \end{aligned}$$

- A  $t$ -test must be used, and the standard error term now uses  $s_1$  and  $s_2$  rather than  $\sigma_1$  and  $\sigma_2$ .
- The exact  $t$ -distribution is difficult to derive, and an approximation must be used to compute the “**effective**” degree of freedom to use the conventional  $t$ -distribution..

$$t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{(s_1^2/n_1) + (s_2^2/n_2)}}.$$

- The value of  $v$  below is rounded to the nearest integer, which will serve as the degree of freedom when we approximate this distribution to a t-distribution.

$$v = \frac{[(s_1^2/n_1) + (s_2^2/n_2)]^2}{[(s_1^2/n_1)^2/(n_1 - 1) + (s_2^2/n_2)^2/(n_2 - 1)]};$$

# Example 5

- Effect of an anti-hypertensive drug against persons  $\geq 60$  yr who suffered from systolic blood pressure over 160 mmHg.
- Group 1
  - subjects receiving active drug for one year.
  - Mean systolic BP =  $\mu_1$ , unknown variation.
- Group 2
  - subjects receiving placebo for one year
  - Mean systolic BP =  $\mu_2$ , unknown variation and is different from group 1.

- $H_0: \mu_1 = \mu_2$

- $H_A: \mu_1 \neq \mu_2$

		Group 1	Group 2
Population	Mean	$\mu_1$	$\mu_2$
	Standard Deviation	$\sigma_1$	$\sigma_2$
Sample	Mean	$\bar{x}_1 = 142.5$	$\bar{x}_2 = 156.5$
	Standard Deviation	$s_1 = 15.7$	$s_2 = 17.3$
	Sample Size	$n_1 = 2308$	$n_2 = 2293$



Compute the test statistics:

$$\begin{aligned} t &= \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{(s_1^2/n_1) + (s_2^2/n_2)}} \\ &= \frac{(142.5 - 156.5) - 0}{\sqrt{[(15.7)^2/2308] + [(17.3)^2/2293]}} \\ &= -28.74. \end{aligned}$$

# Compute the “effective” degree of freedom:

$$\begin{aligned}v &= \frac{[(s_1^2/n_1) + (s_2^2/n_2)]^2}{[(s_1^2/n_1)^2/(n_1 - 1) + (s_2^2/n_2)^2/(n_2 - 1)]} \\&= \frac{[(246.49/2308) + (299.29/2293)]^2}{[(246.49/2308)^2/(2308 - 1) + (299.29/2293)^2/(2293 - 1)]} \\&= 4550.5. \quad \Rightarrow \quad 4550 \text{ (rounding down to nearest integer)}\end{aligned}$$

- We know t-distribution of df=4550 is practically the same as normal distribution.
- $t = -28.74$  is far left to  $z = -1.96$  which cuts the left tail at 2.5%. This concludes the difference is significant.

- One may now compute twice the value of  $\text{tcdf}(-28.74, 4550)$ , which is the p-value for this test. The result is zero.
- This concludes the patients receiving the drug do have a lower mean systolic blood pressure than those receiving placebo.
- We may compute the 95% confidence interval of the difference of BP between these two samples as  $(-15.0, -13.0)$ . [Verify this by yourself!!!]
- This too helps in rejecting the hypothesis that two means are equal.

		Group 1	Group 2
Population	Mean	$\mu_1$	$\mu_2$
	Standard Deviation	$\sigma_1$	$\sigma_2$
Sample	Mean	$\bar{x}_1 = 142.5$	$\bar{x}_2 = 156.5$
	Standard Deviation	$s_1 = 15.7$	$s_2 = 17.3$
	Sample Size	$n_1 = 2308$	$n_2 = 2293$

- Note that the sample sizes are big. This effectively raises DF and the absolute value of t (ideal conditions to reject the null hypothesis).
- ***What if the sample sizes are small, say, 10 each?***

```
>> x1=142.5; x2=156.5; s1=15.7; s2=17.3;  
>> t=((x1-x2)-0)/sqrt(s1^2/10+s2^2/10)  
t = -1.8950
```

```
>>  
v=((s1^2/10+s2^2/10)^2)/((s1^2/10)^2/9+(s2^2/10  
)^2/9)  
v = 17.8331
```

```
>> 2*tcdf(t,v)  
ans = 0.0744
```

*With this p-value, we cannot ascertain the two samples are having different mean values.*