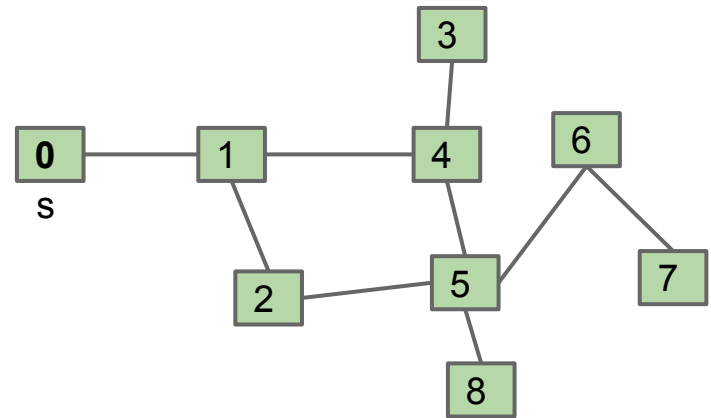


BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | F | - | 0 |
| 1 | F | - | - |
| 2 | F | - | - |
| 3 | F | - | - |
| 4 | F | - | - |
| 5 | F | - | - |
| 6 | F | - | - |
| 7 | F | - | - |
| 8 | F | - | - |



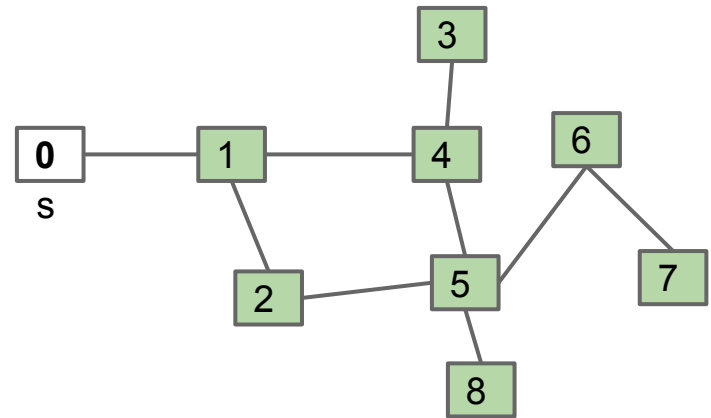
Queue: []

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | F | - | - |
| 2 | F | - | - |
| 3 | F | - | - |
| 4 | F | - | - |
| 5 | F | - | - |
| 6 | F | - | - |
| 7 | F | - | - |
| 8 | F | - | - |



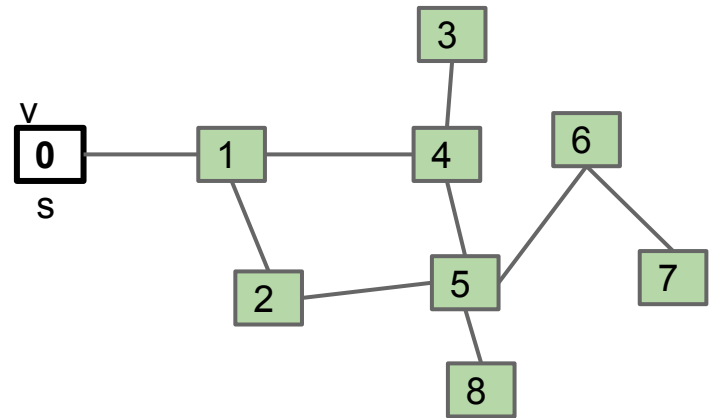
Queue: [0]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | F | - | - |
| 2 | F | - | - |
| 3 | F | - | - |
| 4 | F | - | - |
| 5 | F | - | - |
| 6 | F | - | - |
| 7 | F | - | - |
| 8 | F | - | - |



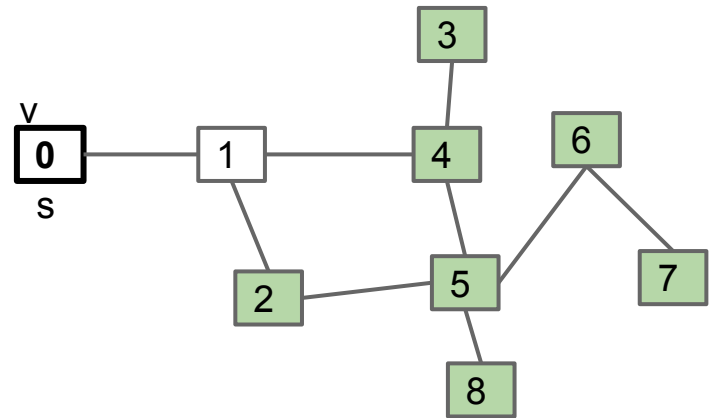
Queue: []

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | F | - | - |
| 3 | F | - | - |
| 4 | F | - | - |
| 5 | F | - | - |
| 6 | F | - | - |
| 7 | F | - | - |
| 8 | F | - | - |



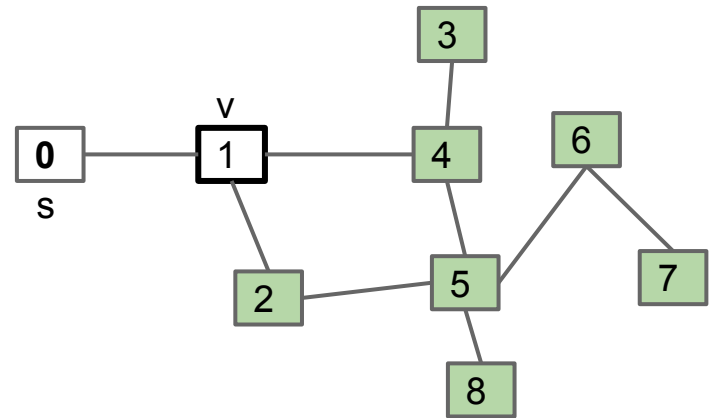
Queue: [1]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | F | - | - |
| 3 | F | - | - |
| 4 | F | - | - |
| 5 | F | - | - |
| 6 | F | - | - |
| 7 | F | - | - |
| 8 | F | - | - |



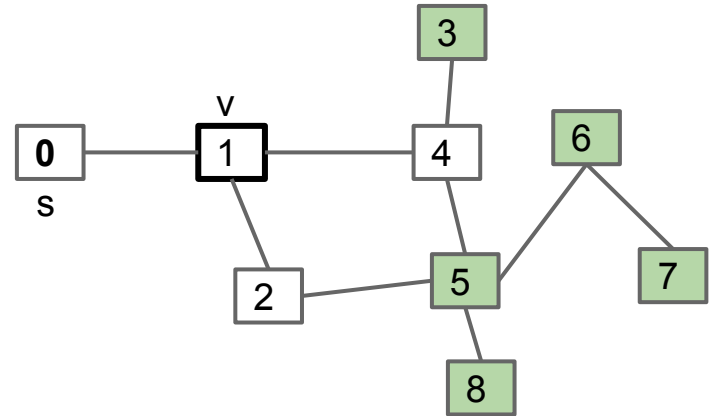
Queue: []

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | F | - | - |
| 4 | T | 1 | 2 |
| 5 | F | - | - |
| 6 | F | - | - |
| 7 | F | - | - |
| 8 | F | - | - |



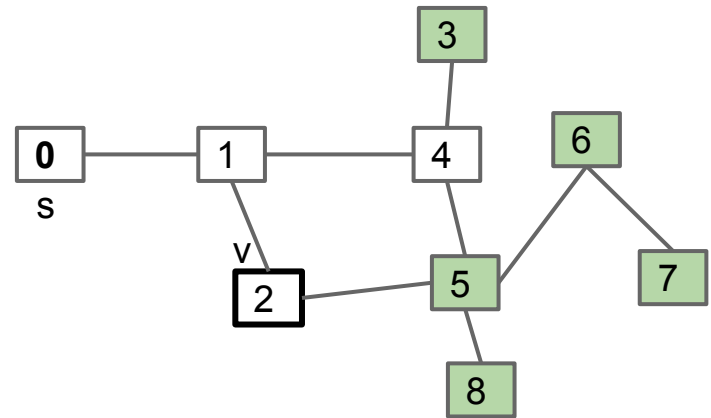
Queue: [2, 4]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | F | - | - |
| 4 | T | 1 | 2 |
| 5 | F | - | - |
| 6 | F | - | - |
| 7 | F | - | - |
| 8 | F | - | - |



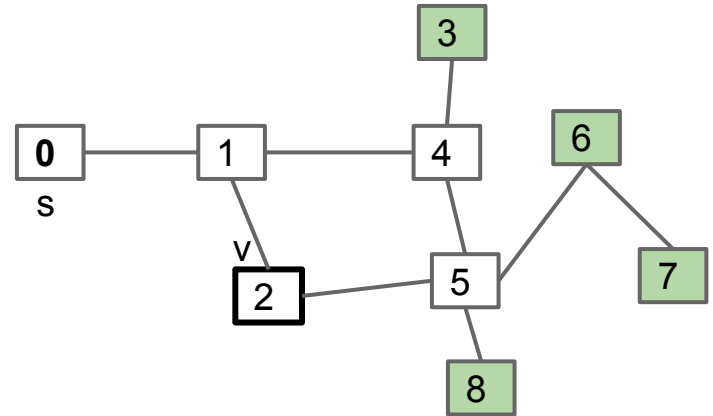
Queue: [4]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | F | - | - |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | F | - | - |
| 7 | F | - | - |
| 8 | F | - | - |

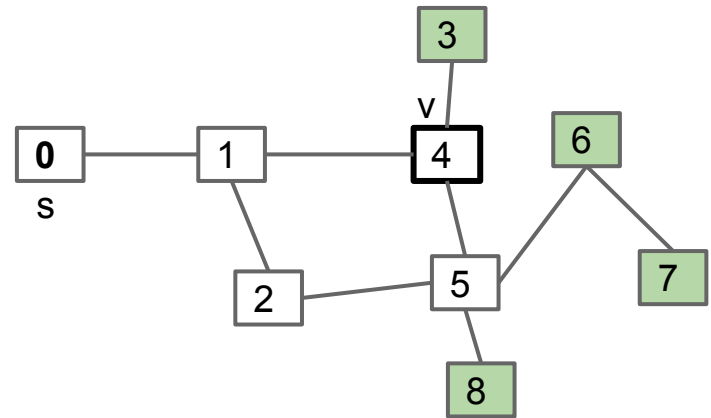


BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | F | - | - |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | F | - | - |
| 7 | F | - | - |
| 8 | F | - | - |



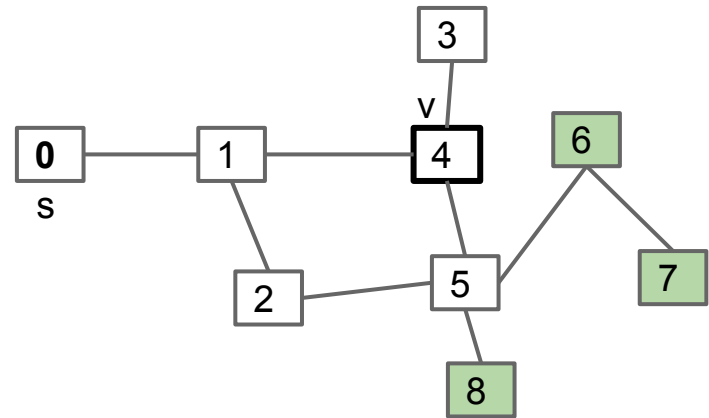
Queue: [5]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | T | 4 | 3 |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | F | - | - |
| 7 | F | - | - |
| 8 | F | - | - |



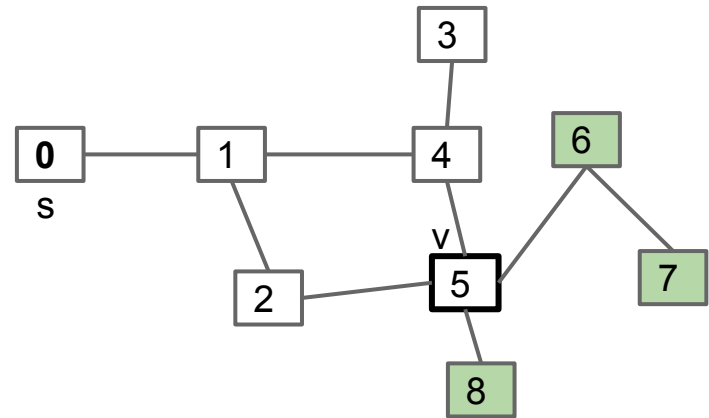
Queue: [5, 3]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | T | 4 | 3 |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | F | - | - |
| 7 | F | - | - |
| 8 | F | - | - |



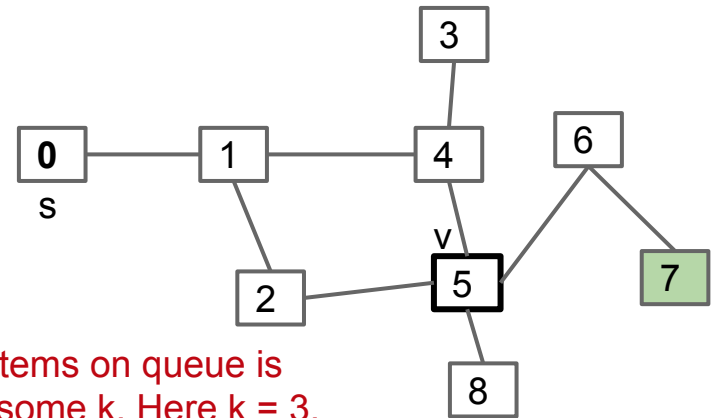
Queue: [3]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | T | 4 | 3 |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | T | 5 | 4 |
| 7 | F | - | - |
| 8 | T | 5 | 4 |



Note: distance to all items on queue is always k or $k + 1$ for some k . Here $k = 3$.

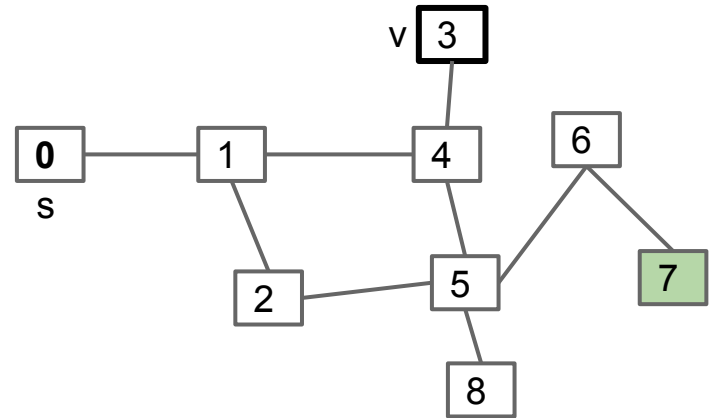
Queue: [3, 6, 8]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | T | 4 | 3 |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | T | 5 | 4 |
| 7 | F | - | - |
| 8 | T | 5 | 4 |



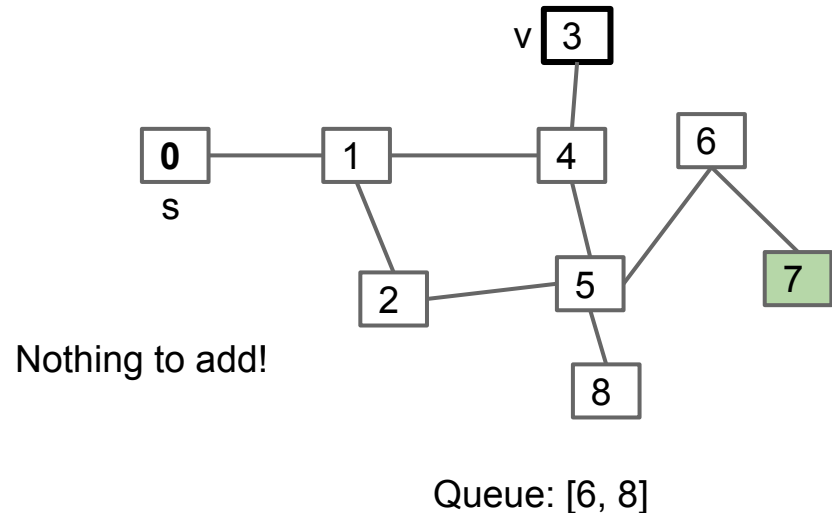
Queue: [6, 8]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | T | 4 | 3 |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | T | 5 | 4 |
| 7 | F | - | - |
| 8 | T | 5 | 4 |

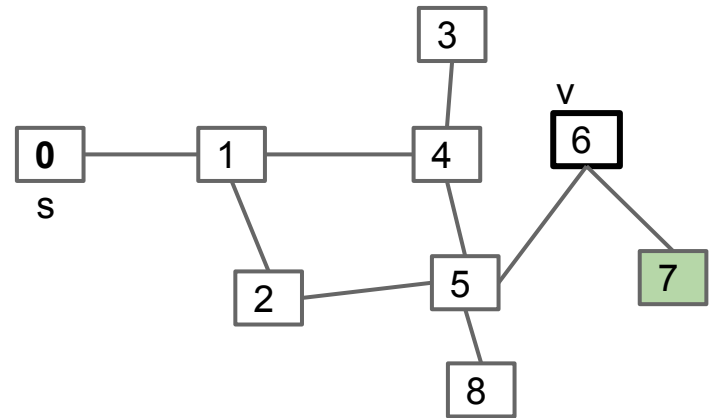


BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | T | 4 | 3 |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | T | 5 | 4 |
| 7 | F | - | - |
| 8 | T | 5 | 4 |



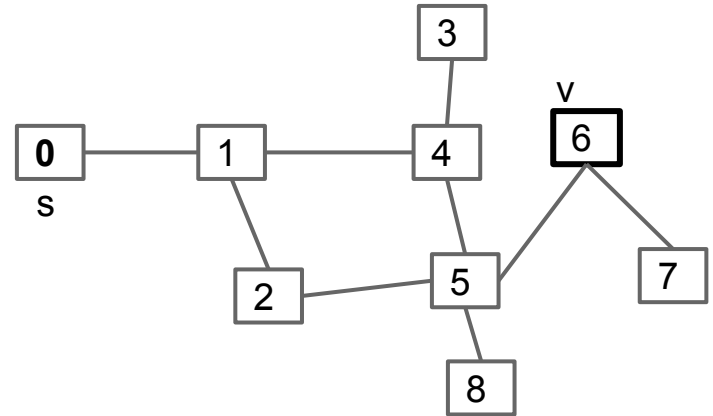
Queue: [8]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | T | 4 | 3 |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | T | 5 | 4 |
| 7 | T | 6 | 5 |
| 8 | T | 5 | 4 |



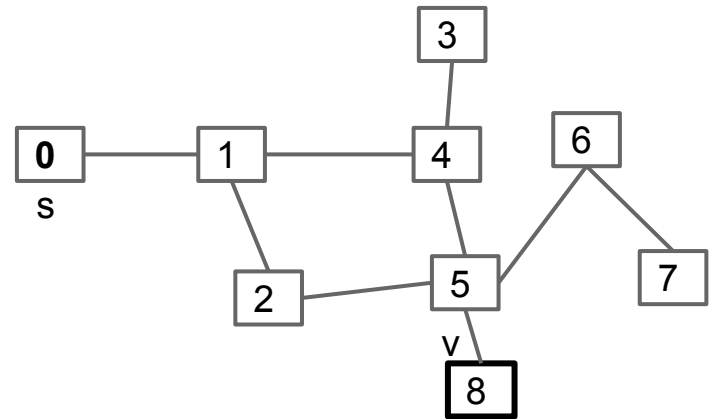
Queue: [8, 7]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | T | 4 | 3 |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | T | 5 | 4 |
| 7 | T | 6 | 5 |
| 8 | T | 5 | 4 |



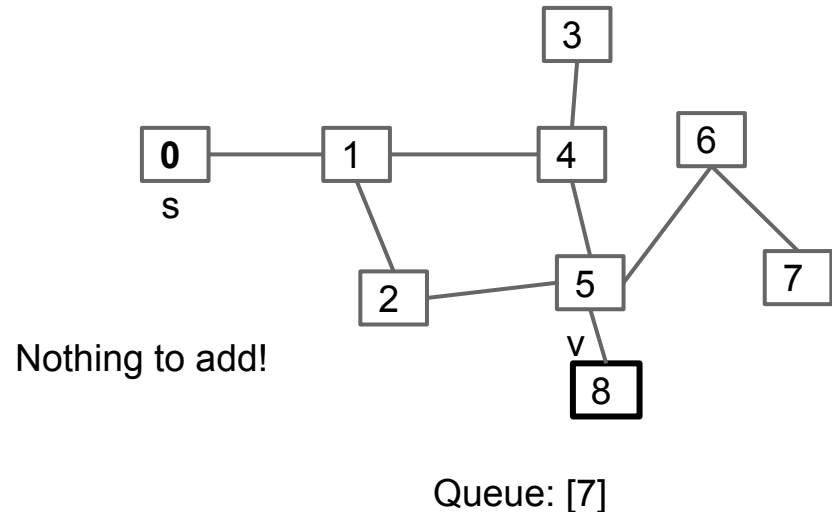
Queue: [7]

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | T | 4 | 3 |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | T | 5 | 4 |
| 7 | T | 6 | 5 |
| 8 | T | 5 | 4 |

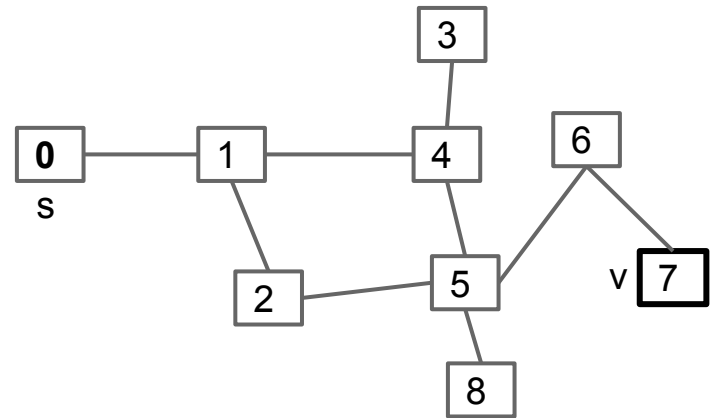


BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | T | 4 | 3 |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | T | 5 | 4 |
| 7 | T | 6 | 5 |
| 8 | T | 5 | 4 |



Queue: []

BreadthFirstPaths Demo

Goal: Find shortest path between s and every other vertex.

- **Initialize the fringe (a queue with a starting vertex s) and mark that vertex.**
- Repeat until fringe is empty:
 - Remove vertex v from fringe.
 - For each unmarked neighbor n of v : mark n , add n to fringe, set $\text{edgeTo}[n] = v$, set $\text{distTo}[n] = \text{distTo}[v] + 1$.

| # | marked | edgeTo | distTo |
|---|--------|--------|--------|
| 0 | T | - | 0 |
| 1 | T | 0 | 1 |
| 2 | T | 1 | 2 |
| 3 | T | 4 | 3 |
| 4 | T | 1 | 2 |
| 5 | T | 2 | 3 |
| 6 | T | 5 | 4 |
| 7 | T | 6 | 5 |
| 8 | T | 5 | 4 |

