

Homework 3 Solutions

Ex 1, Page 125

- a) $\{-1, 1\}$
- b) $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\}$
- c) $\{0, 1, 4, 9, 16, 25, 36, 49, 64, 81\}$
- d) $\{\}$ or \emptyset

Ex 2, Page 125

- a) $\{x \mid x = 3i, \text{ and } x \text{ is a non-negative integer and } x < 13\}$
- b) $\{x \mid -3 \leq x \leq 3, x \in \mathbb{Z}\}$
- c) $\{x \mid x \text{ is a letter of the alphabet and } m \leq x \leq p\}$

Ex 5, Page 125

- a) The two sets are equal since order and repetition don't matter
- b) The two sets are not equal, the one contains 1 while the other does not
- c) The two sets are not equal. The one has 1 element in it while the other one is empty

Ex 6, Page 125

$$A = \{2, 4, 6\}, \quad B = \{2, 6\}, \quad C = \{4, 6\}$$
$$D = \{4, 6, 8\}$$

$$B \subseteq A, \quad C \subseteq A, \quad C \subseteq D$$

Ex 7, Page 125

- a) Yes
- b) No
- c) Yes
- d) No
- e) No
- f) No

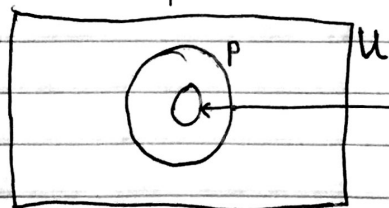
Ex 11, Page 125

- a) True
- b) True
- c) False
- d) True
- e) True
- f) False

Ex 12, page 125

Let U be the set of all integers.

Let P : positive integers not exceeding 10

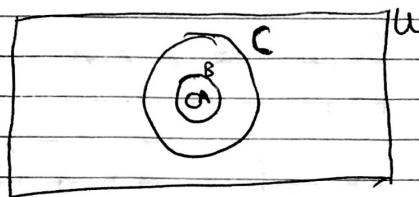


The subset of odd integers in the set of P



Exercise 14, page 126

$$A \subseteq B \quad B \subseteq C$$



Exercise 18, page 126

$$A \in B \quad \text{and} \quad A \subseteq B$$

$$\text{let } A = \emptyset \quad \text{and} \quad B = \{\emptyset\}$$

Exercise 20, page 126

- a) 0
- b) 1
- c) 2
- d) 3

Exercise 21, page 126

- a) $\mathcal{P}(\{a\}) = \{\emptyset, \{a\}\}$
- b) $\mathcal{P}(\{a, b\}) = \{\emptyset, \{a\}, \{b\}, \{a, b\}\}$
- c) $\mathcal{P}(\{\emptyset, \{\emptyset\}\}) = \{\emptyset, \{\emptyset\}, \{\{\emptyset\}\}, \{\emptyset, \{\emptyset\}\}\}$

Ex 27 , page 126

$$A = \{a, b, c, d\} \quad , \quad B = \{y, z\}$$

$$a) \quad A \times B = \{(a, y), (a, z), (b, y), (b, z), (c, y), (c, z), (d, y), (d, z)\}$$

$$b) \quad B \times A = \{(y, a), (y, b), (y, c), (y, d), (z, a), (z, b), (z, c), (z, d)\}$$