# **Biological Physics II: Dynamics in Biological Systems**

- I. Deterministic dynamics
- 1. Qualitative analysis of dynamical systems

Strogatz, Chapter 2; Murray I, Section 1.1

- 1.1 Dynamical systems
- 1.2 Logistic growth
- 1.3 Flows on the line
- 1.4 Bifurcations

Strogatz, Chapter 3; Murray I, Section 1.6

- 1.5 Higher-dimensional flows
- 2. Dynamics of interacting populations
- 2.1 Predator-prey dynamics Murray I, Sections 3.1 and 3.3; Hofbauer & Sigmund, Chapter 2
- 2.2 Competetive exclusion *Murray I, Section 3.5; Hofbauer & Sigmund, Chapter 3*
- 2.3 Epidemic modeling Murray I, Section 10.2

## 3. Nonlinear dynamics in gene regulation

Molecular mechanisms of gene regulation; genetic switches and genetic oscillators

#### 4. Chaos in biological systems

Characteristics of chaotic dynamics; logistic map; chaos in microbial communities

#### II. Stochastic dynamics

#### 5. Elementary stochastic processes

Poisson distribution and Poisson process; birth-death processes; branching processes; Markov chains; Langevin equations

#### 6. Noise in gene expression

Bursty expression dynamics; Fano factor and statistical kinetics; functional significance of expression noise: bet hedging

## 7. Exclusion models of cellular transport

The asymmetric simple exclusion process; exlusion models of translation and transscription; pore transport; transport by motor proteins

## III. Spatiotemporal dynamics

## 8. Biological waves

Fisher waves; velocity selection; pulled and pushed fronts; effects of noise

**Books** (\*) available as e-books

- M. Cross and H. Greenside: Pattern formation and dynamics in nonequilibrium systems. Cambridge University Press 2009 (\*)
- J.H. Hofbauer and K. Sigmund: Evolutionary Games and Replicator Dynamics. Cambridge University Press 1998 (\*)
- J.D. Murray: Mathematical Biology I: An Introduction. Springer 2002
- J.D. Murray Mathematical Biology II: Spatial models and biomedical applications. Springer 2002
- A. Schadschneider, D. Chowdhury and K. Nishinari: Stochastic transport in complex systems: from molecules to vehicles. Elsevier 2011 (\*)
- K. Sneppen: Models of Life. Cambridge University Press 2014 (\*)
- S.H. Strogatz: Nonlinear dynamics and chaos. CRC Press 2018 (\*)
- N. van Kampen: Stochastic Processes in Physics and Chemistry. North Holland 2007 (\*)