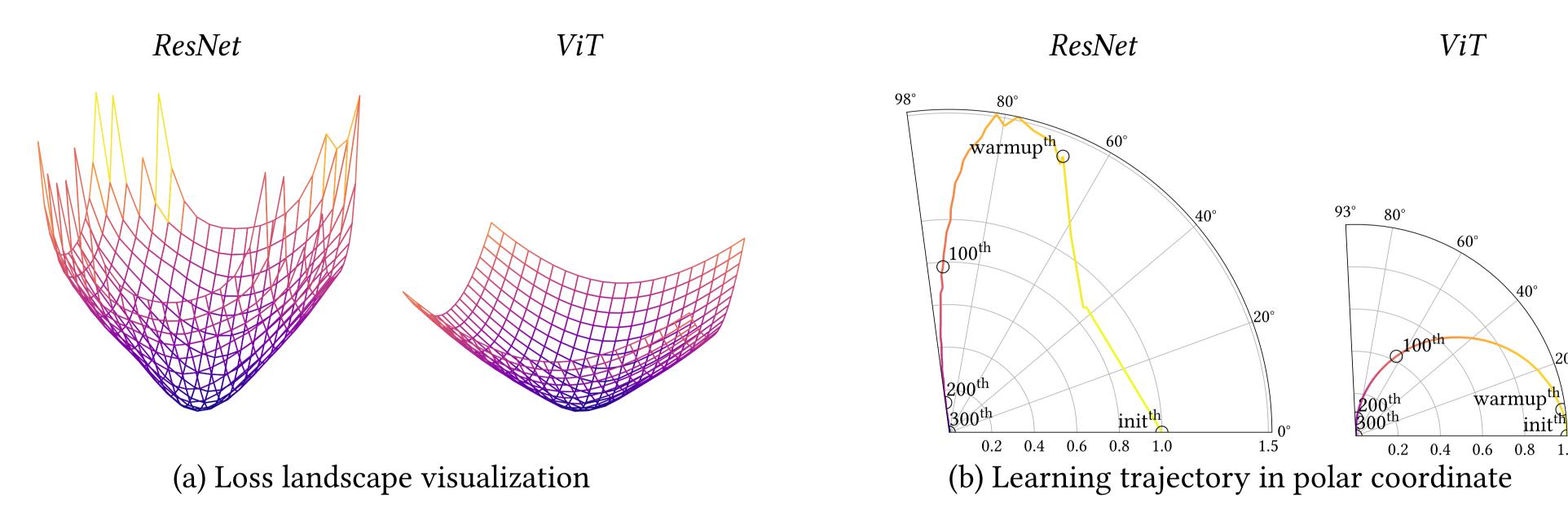
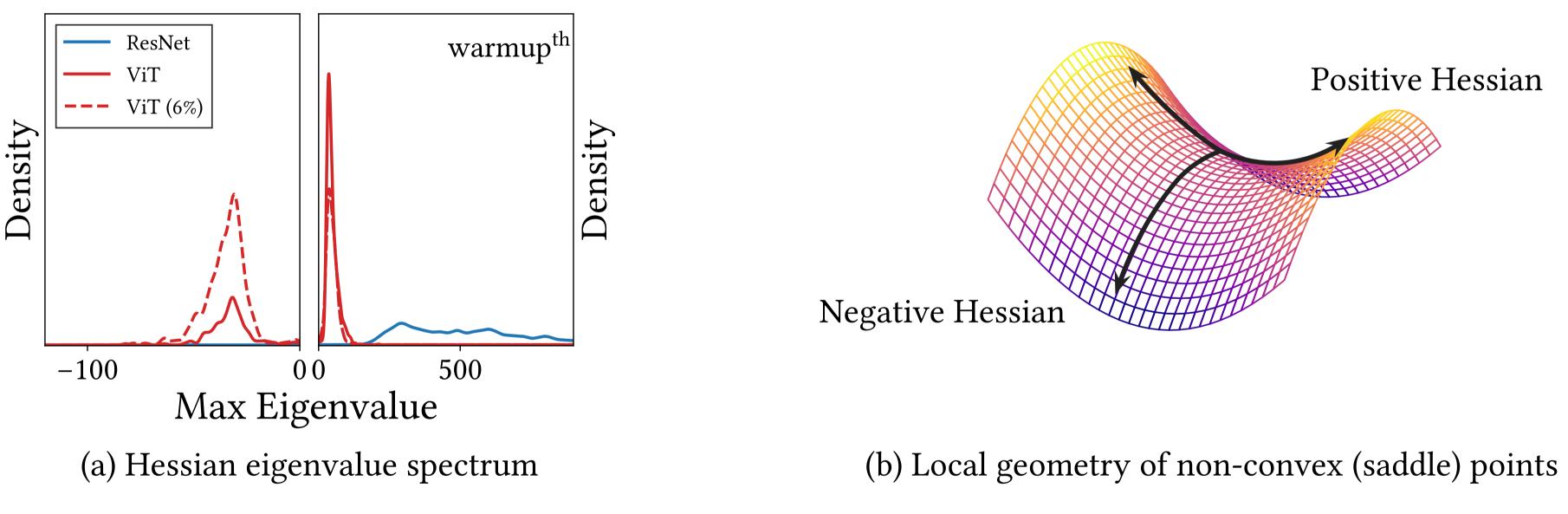
What Properties of Self-Attentions Do We Need?

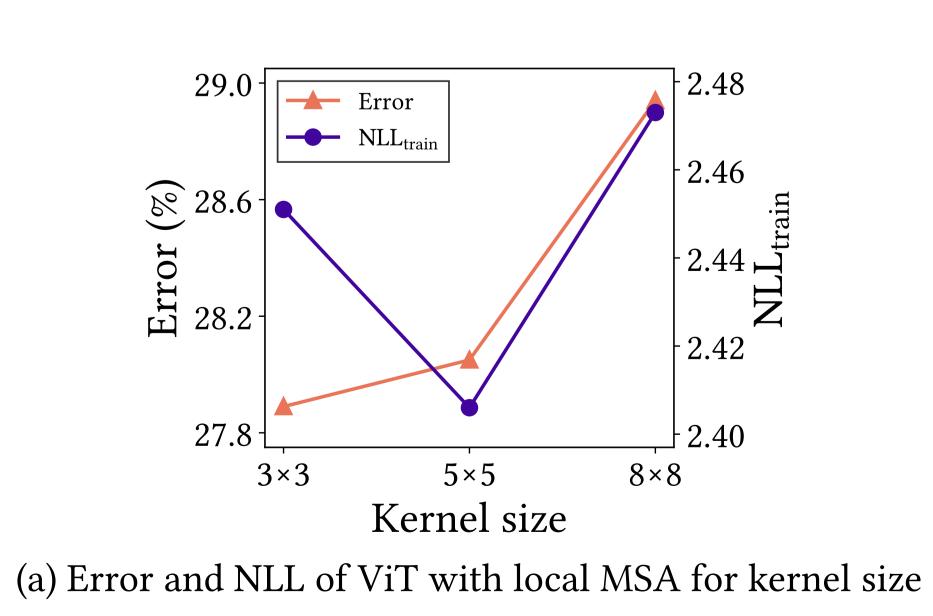
MSAs (multi-head self-attention) have flat but non-convex losses. In contrast, Convs have convex but sharp losses.

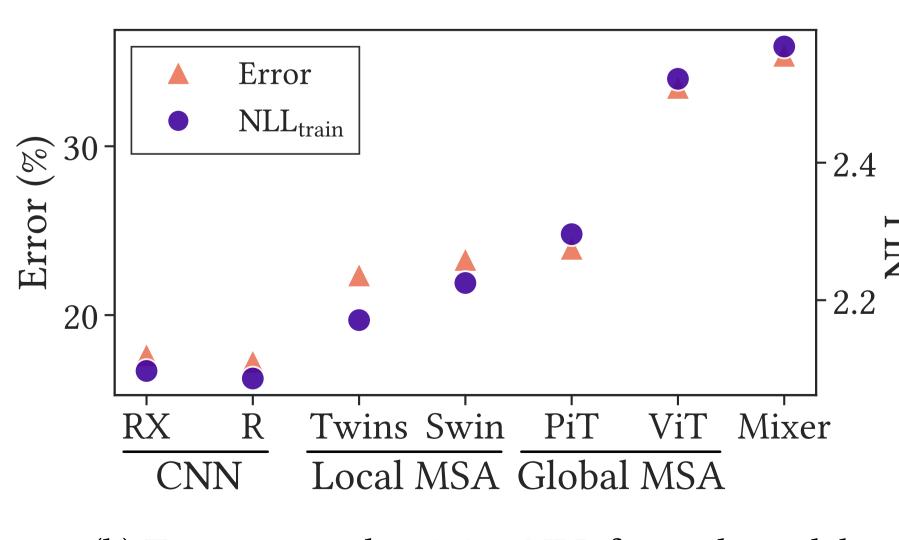


Loss landscape visualization (*Left*) show that ViT has a flatter loss than ResNet. Learning trajectory visualization (*Right*) shows that ViT converges to the optimum along a smooth trajectory.



Hessian max eigenvalue spectra show that MSAs have their pros and cons. ViT has a number of negative Hessian eigenvalues, while ResNet only has a few. The magnitude of ViT's positive Hessian eigenvalues is small.



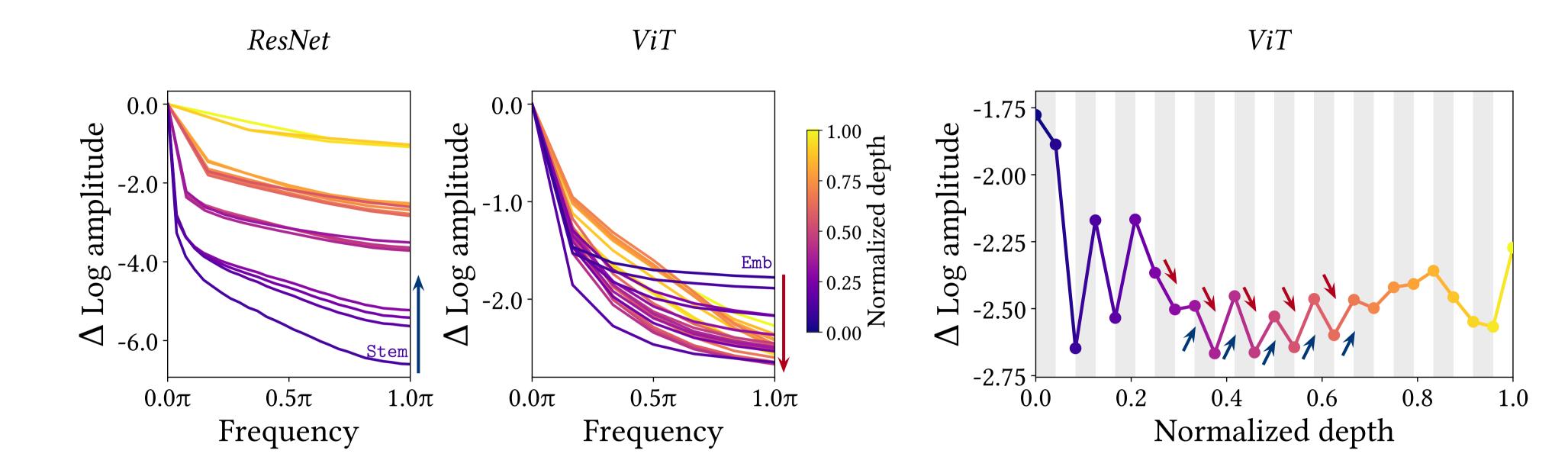


(b) Test error and training NLL for each model

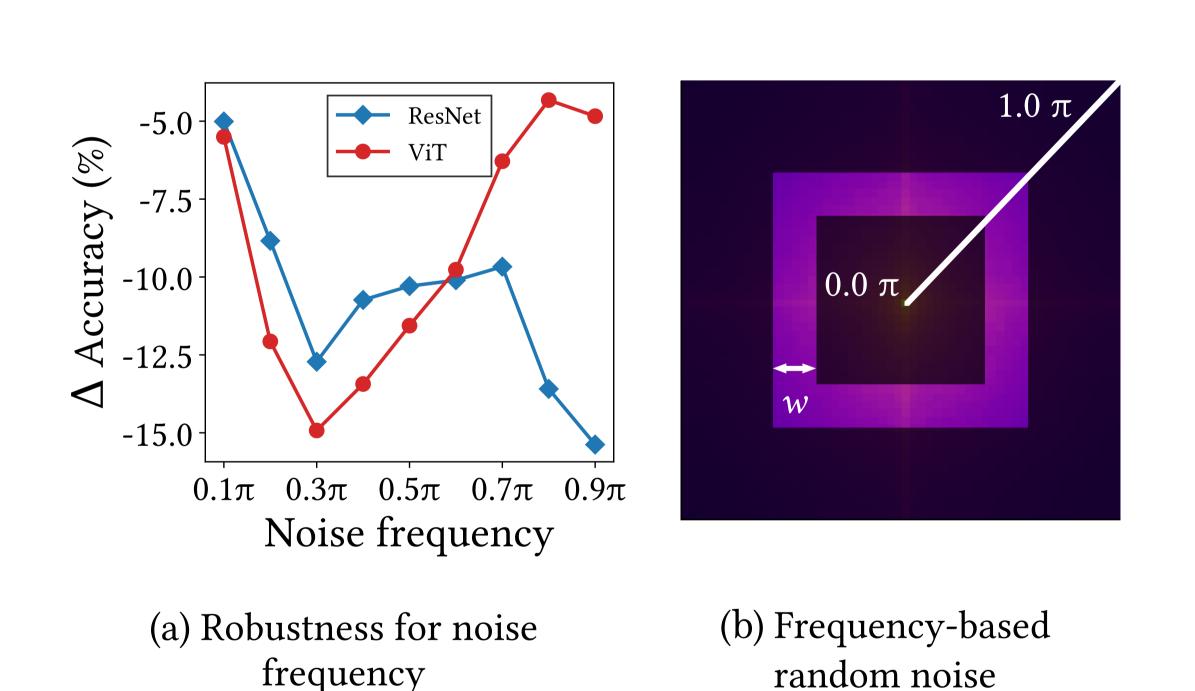
The key feature of MSA is data specificity, not long-range dependency. *Left*: Convolutional ViT demonstrates that locality constraint improves ViT. *Right*: Weak inductive bias (e.g. long-range dependency) disturbs NN optimization.

Do Self-Attentions Act Like Convs?

MSAs are low-pass filter, but Convs are high-pass filter. It suggests that MSAs are shape-biased, whereas Convs are texture-biased.

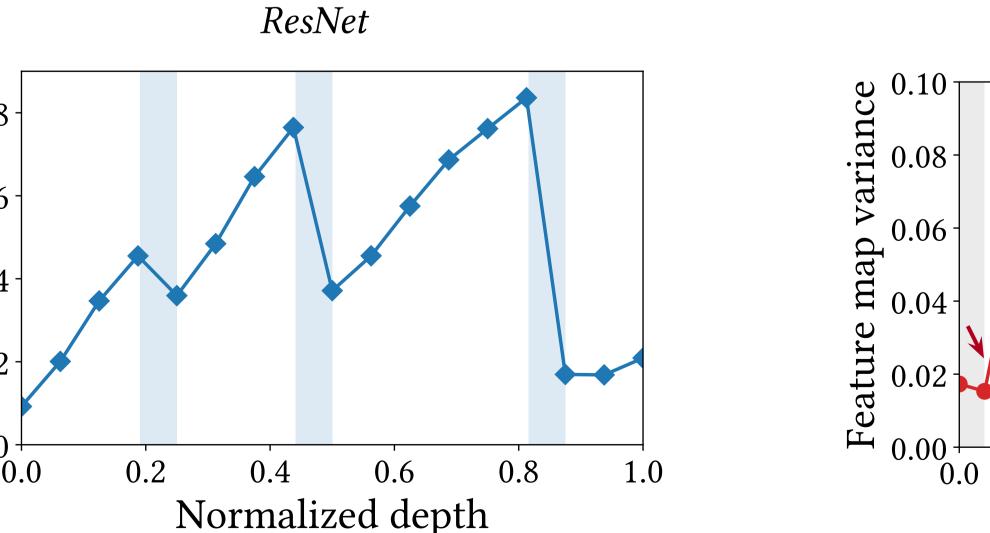


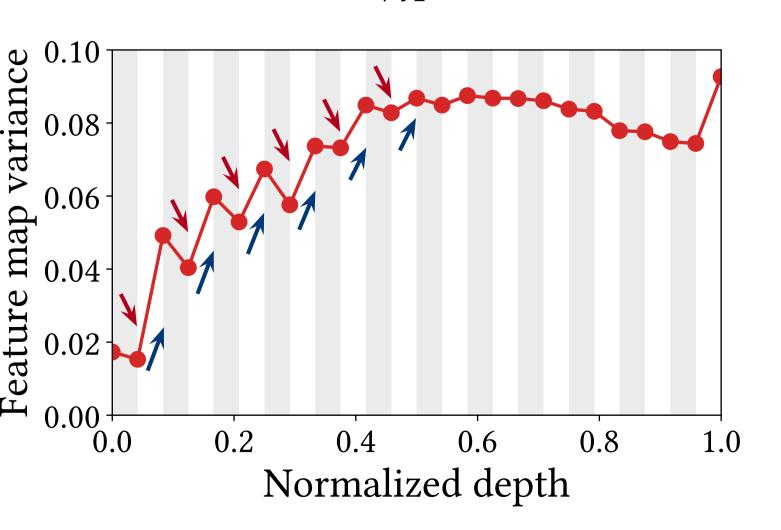
Relative log amplitudes of **Fourier transformed feature map** show that **ViT** tend to reduces high-frequency signals, while ResNet amplify them. *Left*: In ViT, MSAs (gray area) generally reduce the high-frequency (1.0π) component of feature map, and Conv/MLPs (white area) amplify it.



We measure the decrease in accuracy against frequency-based random noise. ViT is robust against high-frequency noise, while ResNet is vulnerable to them.

It suggests that low-frequency signals and high-frequency signals are informative to MSAs and Convs.

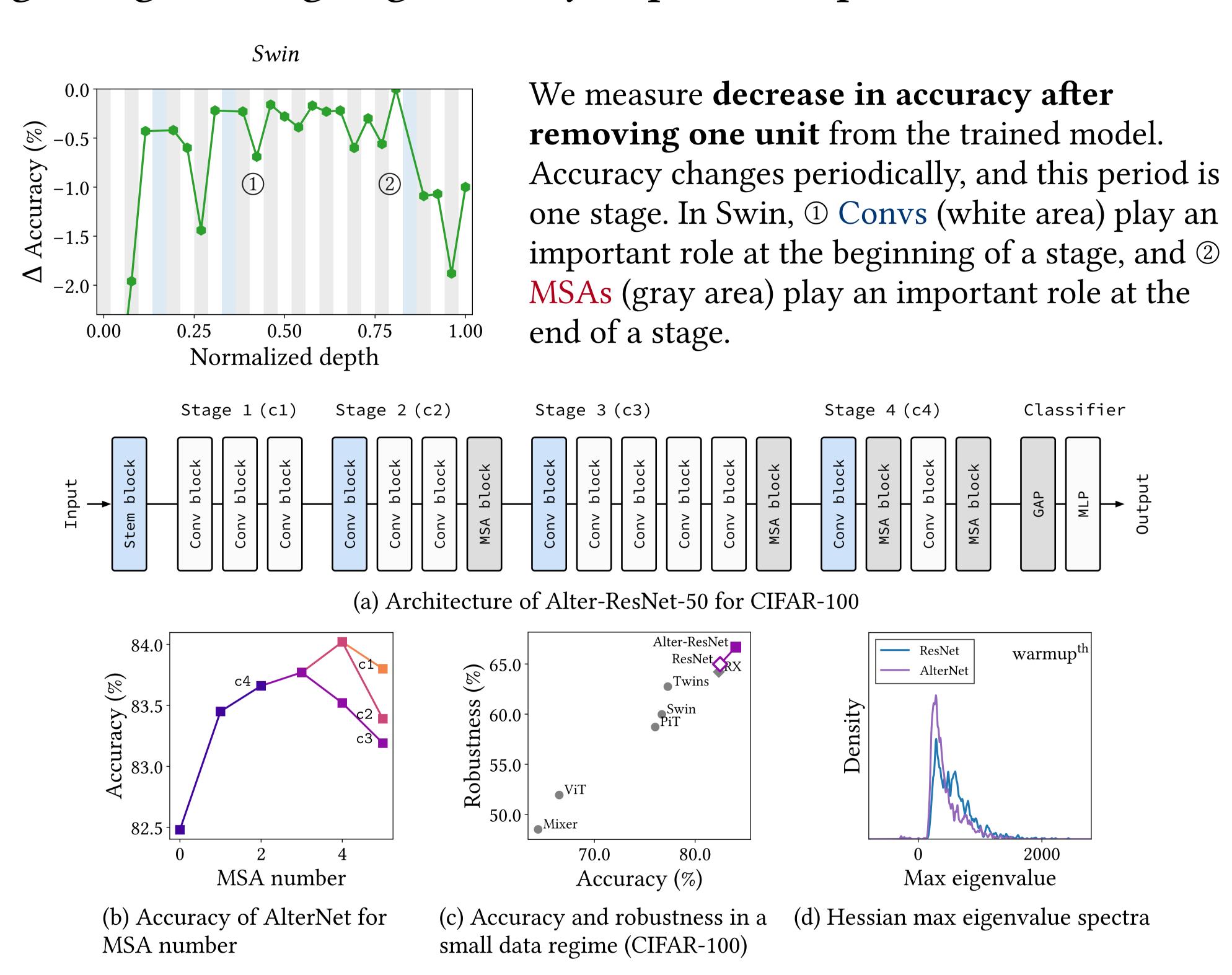




MSAs (gray area) reduce **the variance of feature map points**, but Convs/MLPs (white area) increase the variance. The blue area is subsampling layer. The results implies that MSAs aggregate feature maps, and Convs convert them.

How Can We Harmonize Self-Attentions with Convs?

MSAs closer to the end of a stage (not a model) and Convs at the beginning of a stage significantly improve the performance.



We propose *AlterNet*, a model in which Conv blocks at the end of *a stage* are replaced with MSA blocks. AlterNet outperforms CNNs even in small data regimes.

In summary, appropriate inductive biases improves NN optimization, and self-attentions have a spatial smoothing inductive bias.

	Self-Attention	Convolution
Loss Landscape	Flat but non-convex	Convex but sharp
Fourier Analysis	Low-pass filter (shape-biased)	High-pass filter (texture-biased)
Best Practice	The end of a stage	The beginning of a stage