

Econometrics Assignment 5
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$$Pr[resp_i = 1] = \frac{\exp(\beta_0 + \beta_1 male_i + \beta_2 active_i + \beta_3 age_i + \beta_4 (age_i/10)^2)}{1 + \exp(\beta_0 + \beta_1 male_i + \beta_2 active_i + \beta_3 age_i + \beta_4 (age_i/10)^2)}$$

Variable	Coefficient
Intercept	-2.488
Male	0.954
Active	0.914
Age	0.070
(Age/10) ²	-0.069

(a) For a 50 year old active male customer

$$\frac{Pr[resp_i = 0]active_i\beta_2}{(1 - Pr[resp_i = 1])active_i\beta_2} = \frac{1}{1 + \exp(-2.488 + 0.954 + 0.914 + 0.070 * 50 - 0.069 * 25)}^{(0.914 * 1)} = 0.229$$

For a 50 year old inactive male customer

$$\frac{1}{1 + \exp(-2.488 + 0.954 + 0.070 * 50 - 0.069 * 25)}^{(0.914 * 0)} = 0$$

(b) Let $Z = \exp(\beta_0 + \beta_1 male_i + \beta_3 age_i + \beta_4 (age_i/10)^2)$

then $\exp(\beta_2)Z = \exp(\beta_0 + \beta_1 male_i + \beta_2 + \beta_3 age_i + \beta_4 (age_i/10)^2)$

$$\begin{aligned} & \frac{Pr[resp_i = 1|active_i = 1] - Pr[resp_i = 1|active_i = 0]}{Pr[resp_i = 1|active_i = 0]} \\ &= \frac{\frac{\exp(\beta_2)Z}{1 + Z\exp(\beta_2)} - \frac{Z}{1 + Z}}{\frac{Z}{1 + Z}} \\ &= \left(\frac{1 + Z}{Z}\right) \frac{\exp(\beta_2)Z}{1 + Z\exp(\beta_2)} - \left(\frac{1 + Z}{Z}\right) \frac{Z}{1 + Z} \\ &= \frac{(1 + Z)\exp(\beta_2)}{1 + Z\exp(\beta_2)} - 1 \\ &= \frac{Z\exp(\beta_2) + \exp(\beta_2) - 1 - Z\exp(\beta_2)}{1 + Z\exp(\beta_2)} \\ &= \frac{\exp(\beta_2) - 1}{1 + Z\exp(\beta_2)} \\ &= (\exp(\beta_2) - 1) \frac{1}{1 + Z\exp(\beta_2)} \end{aligned}$$

$$\text{Using } Pr[resp_i = 0|active_i = 1] = 1 - Pr[resp_i = 1|active_i = 1] = \frac{1}{1 + Z\exp(\beta_2)}$$

$$(exp(\beta_2) - 1)Pr[resp_i = 0|active_i = 1]$$

$$(c) \ (exp(\beta_2) - 1)Pr[resp_i = 0|active_i = 1]$$

$$(exp(0.914) - 1) \frac{1}{1 + exp(-2.488 + 0.954 + 0.914 + 0.070 * 50 - 0.069 * 25)}$$

0.365