# ARTICLE IN PRESS

YNIMG-11237; No. of pages: 17; 4C: 13, 14

NeuroImage xxx (2014) xxx-xxx



Contents lists available at ScienceDirect

# NeuroImage

journal homepage: www.elsevier.com/locate/ynimg



# Testing for association with multiple traits in generalized estimation equations, with application to neuroimaging data

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#### ARTICLE INFO

- Article history:
- 8 Accepted 23 March 2014
- 9 Available online xxxx
- 10 Keywords:
- 11 aSPU test
- 12 GEE

36 **39** 39

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- 13 GWAS14 Neuroimaging genetics
  - Score test
- 16 Statistical power
- 17 Sum of powered score (SPU) test

#### ABSTRACT

There is an increasing need to develop and apply powerful statistical tests to detect multiple traits-single locus 18 associations, as arising from neuroimaging genetics and other studies. For example, in the Alzheimer's Disease 19 Neuroimaging Initiative (ADNI), in addition to genome-wide single nucleotide polymorphisms (SNPs), thou- 20 sands of neuroimaging and neuropsychological phenotypes as intermediate phenotypes for Alzheimer's disease, 21 have been collected. Although some classic methods like MANOVA and newly proposed methods may be applied, 22 they have their own limitations. For example, MANOVA cannot be applied to binary and other discrete traits. In 23 addition, the relationships among these methods are not well understood. Importantly, since these tests are not 24 data adaptive, depending on the unknown association patterns among multiple traits and between multiple 25 traits and a locus, these tests may or may not be powerful. In this paper we propose a class of data-adaptive 26 weights and the corresponding weighted tests in the general framework of generalized estimation equations 27 (GEE). A highly adaptive test is proposed to select the most powerful one from this class of the weighted tests 28 so that it can maintain high power across a wide range of situations. Our proposed tests are applicable to various 29 types of traits with or without covariates. Importantly, we also analytically show relationships among some 30 existing and our proposed tests, indicating that many existing tests are special cases of our proposed tests. Exten- 31 sive simulation studies were conducted to compare and contrast the power properties of various existing and our 32 new methods. Finally, we applied the methods to an ADNI dataset to illustrate the performance of the methods. 33 We conclude with the recommendation for the use of the GEE-based Score test and our proposed adaptive test 34 for their high and complementary performance.

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## Introduction

Published genome-wide association studies (GWAS) have shown that single nucleotide polymorphisms (SNPs) associated with common diseases and complex traits are not easily detected. The main reason is due to their small effect sizes: the odds ratios from the identified associations are often only 1.1–1.3. It is also realized that using only one single phenotype may not suffice to identify the underlying genetic mechanism, as a complex disease may exhibit its occurrence or progression in several syndromes. Thus, multivariate trait analysis is being increasingly recognized as a potentially useful strategy in genetic studies (Zhu and Zhang, 2009). However, a dilemma in joint analysis of multiple

\* Corresponding author at: Division of Biostatistics, MMC 303, School of Public Health, University of Minnesota, Minneapolis, MN 55455-0392, USA. Fax: +1 612 626 0660. E-mail address: weip@biostat.umn.edu (W. Pan). traits is the inevitable power loss as more and more non-associated 52 traits are being included; in practice, there is no guarantee that multiple 53 traits being analyzed are all simultaneously associated with the same 54 SNP. Therefore, a key issue in multivariate trait analysis is how to 55 maximally maintain statistical power in the presence of many non- 56 associated traits while gaining the power when many or most of the 57 traits are associated with an SNP.

Various methods have been proposed and applied to multivariate 59 trait analysis. Broadly speaking, any existing method for pedigree or 60 longitudinal data analysis is applicable; see a recent nice review by 61 Yang and Wang (2012). The methods can be classified into a few catego-62 ries. The first category is to conduct univariate analysis on each trait, 63 then combine their results (Yang et al., 2010). For example, for any 64 given SNP, one can conduct a single trait–single SNP analysis for each 65 of the multiple traits, then take the minimum p-value from the univar-66 iate analyses with an adjustment for multiple testing. This is like the 67 most commonly adopted approach to single trait–multilocus analysis 68 in GWAS, the so-called UminP approach. The second class is based on dimension reduction on multivariate traits, usually by principal components analysis (PCA) (Lan et al., 2003; Wang and Abbott, 2007) or by 71 principal components of heritability (PCH) (Klei et al., 2008) and related 72

 $http://dx.doi.org/10.1016/j.neuroimage.2014.03.061\\1053-8119/© 2014 Published by Elsevier Inc.$ 

<sup>&</sup>lt;sup>1</sup> Data used in preparation of this article were obtained from the Alzheimer's Disease Neuroimaging Initiative (ADNI) database (adni.loni.usc.edu). As such, the investigators within the ADNI contributed to the design and implementation of ADNI and/or provided data but did not participate in analysis or writing of this report. A complete listing of ADNI investigators can be found at: http://adni.loni.usc.edu/wp-content/uploads/how\_to\_apply/ADNI\_Acknowledgement\_List.pdf.

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methods (Lin et al., 2012; Wang et al., 2008). For PCA, a main issue is that a few top PCs may not capture sufficient association signals (Aschard et al., 2013). For PCH, the sample splitting strategy for population-based studies is not efficient (Yang and Wang, 2012), though the modification of Lin et al. (2012) overcomes this downside. Nevertheless, the interpretation with the use of a few principal components may not be straightforward, and it is debatable whether there exist a few PCs that can genetically capture a large proportion of trait variations. Importantly, it is not clear how robust these methods are in the presence of many non-associated traits, and how many components are needed. Canonical correlation analysis (CCA) also belongs to this class; it seeks the linear combination of all traits yielding the greatest association with a locus (Ferreira and Purcell, 2009). Another special case is simply to take the average (or sum) of multiple traits and then conduct a univariate analysis with this single average (or sum) trait, which is called Average (or Sum) method and has been applied to neuroimaging genetic data recently (Shen et al., 2012). As in the case for single trait-multilocus testing, the Average (or Sum) method suffers from severe power loss in the presence of opposite association directions between the traits and a locus (Pan, 2009), or even worse, as to be shown later, in the presence of some non-associated traits. The third class includes some classical methods for multivariate data, such as MANOVA (Ferreira and Purcell, 2009), which however is not applicable to non-Normal traits, e.g. binary traits. Linear mixed models (LMMs) or generalized least squares for quantitative traits, and generalized linear mixed models (GLMMs) for discrete traits provide a more general alternative (Laird et al., 1982; Fitzmaurice and Laird, 1993; Li et al., 2011; Korte et al., 2012). However, these likelihood-based approaches require one to correctly specify a model, including the correlation structure among the multiple traits, which is often difficult, especially for non-Normal traits. Furthermore, fitting GLMMs is computationally demanding. Alternatively, the generalized estimation equations (GEE) methodology (Liang and Zeger, 1986) is convenient to use, only requiring a correct specification of a marginal mean regression model, not a variance or covariance structure and other higher moments of the traits. In particular, its (generalized) score vector is easy to calculate, in contrast to the intractability in GLMMs. The GEE framework is general and flexible: it can accommodate covariates and various types of traits (Chen et al., 2011; Lange et al., 2003; Liu et al., 2009). Yang and Wang (2012) commented that there may be inflated Type I errors in GEE; we show here that the problem is mainly with the Wald test (Pan, 2001) while the Score test and other score-based tests seemed to work well. Hence, in this paper we adopt the GEE framework, applying some existing tests and developing some new ones, to test for association between a single SNP and multiple, possibly a large number of, quantitative traits.

A challenge in association testing with multiple parameters, such as in multilocus analysis or multivariate trait analysis, is the lack of a uniformly most powerful test. Depending on the unknown truth of the underlying association patterns, any given and fixed test may or may not be powerful. For example, depending on how many of a given set of multiple traits are associated with a locus, different tests may be more powerful: if only few of the traits are associated, then a univariate minimum p-value (UminP) method based on choosing the most significant p-value of the univariate tests on each of the multiple traits, similar to TATES (van der Sluis et al., 2013), would be more powerful; on the other hand, if most or all of the traits are associated with the locus with similar effect sizes, the simple Average method is expected to be more powerful. Our simulation results will confirm these points later. Accordingly, in multilocus association testing, adaptive tests based on weighting multiple loci differently have been proposed (e.g. Lin and Tang, 2011). However, due to the use of fixed weights, these adaptive tests may still suffer from power loss under some situations. Here we propose a class of more highly adaptive tests with a wide range of weights on multiple traits. The goal is that, for a given situation with some unknown association patterns, we can find at least one set of the weights yielding a high-powered test. In our earlier example, if 139 only one trait is associated with a locus, then assigning a large weight 140 to the associated trait while assigning small weights to other traits 141 would be optimal; on the other hand, if all traits are (almost) equally associated with the locus, we would like to assign an equal weight to all 143 the traits. Our proposed class of tests are based on weighting the (generalized) score vector of a marginal generalized linear model (GLM) 145 (McCullagh and Nelder, 1983) in GEE; it maintains the computational 146 simplicity of the Score test and the generality and flexibility of GLMs. 147 Each of our proposed test statistics is a sum of powered score statistics, 148 say SPU( $\gamma$ ), in which an integer  $\gamma$  indexes a set of weights on the multiple traits. Our adaptive SPU (aSPU) test essentially estimates and thus 150 chooses the most powerful SPU test for a given dataset.

Another contribution of this work is to point out connections among 152 the existing and new tests. Although some existing methods, such as 153 classic ones like CCA and MANOVA, recently proposed ones like TATES 154 (van der Sluis et al., 2013), MultiPhen (O'Reilly et al., 2012) and kernel 155 machine regression (KMR) (Maity et al., 2012), and some potentially 156 usable ones like MDMR (McArdle and Anderson, 2001), have been sug- 157 gested for analysis of multivariate traits, their relationships with each 158 other are largely unknown. Here we analytically illuminate on how 159 these existing tests and our proposed tests are related. In particular, 160 when testing on association between multiple quantitative traits and a 161 single SNP in the absence of other covariates, we point out that many 162 existing tests are special cases of the SPU tests. For example, CCA, 163 MANOVA and the GEE-Score test are equivalent, which in turn are 164 closely related to MultiPhen; the Average method coincides with the 165 GEE-SPU(1) test, while TATES is closely related to the GEE-SPU(∞); 166 Under suitable conditions, both MDMR and KMR are the same as the 167 GEE-SPU(2) test. These analytical results will be confirmed in our extensive simulation studies.

Finally we will apply these methods to the NIH Alzheimer's Disease
Neuroimaging Initiative (ADNI) data. We aim to detect associations between SNPs and some multivariate neuroimaging phenotypes in several
related regions of interest (ROIs). As both imaging and genotyping technologies advance, imaging genetics is emerging as a promising yet challenging field. In particular, due to numerous phenotypes measured for the ROIs, there is a high demand on developing and applying powerful association testing for multivariate traits, given limited multivariate methods available (Glahn et al., 2007). Shen et al. (2010) applied the simple Average method and confirmed two associated genes, APOE and TOMM40. We aimed to investigate how our proposed new tests perform as compared to other existing tests. We will demonstrate the advantages and potential usefulness of the GEE-based tests.

Methods 183

Generalized estimating equations

Suppose that for each subject i=1,...,n, we have k traits  $Y_i=(y_{i1},y_{i2},\ 185,...,y_{ik})', x_i=0,1$  or 2 is the genotype score (i.e. count of the minor allele) for an SNP of interest, and  $z_i=(z_{i1},z_{i2},...,z_{iq})$  is a row vector of q 187 covariates. Define the design matrices for the SNP effects and covariates 188 as

$$X_{i} = \begin{pmatrix} x_{i} & 0 & \cdots & 0 \\ 0 & x_{i} & \cdots & 0 \\ \vdots & & & \vdots \\ 0 & \cdots & 0 & x_{i} \end{pmatrix} = x_{i}I, \qquad Z_{i} = \begin{pmatrix} 1 & z_{i} & \mathbf{0} & \mathbf{0} & \dots & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & 1 & z_{i} & \dots & \mathbf{0} \\ & & \vdots & & \vdots & \\ \mathbf{0} & \mathbf{0} & \dots & \mathbf{0} & 1 & z_{i} \end{pmatrix},$$

where **0** is a row vector of all 0's.  $X_i$  is a  $k \times k$  matrix, and  $Z_i$  is a  $k \times 191$  k(q+1) matrix including the intercept term. Define two regression coefficient vectors as  $\beta = (\beta_1,...,\beta_k)'$  for  $X_i$  and  $\varphi = (\varphi_{11},...,\varphi_{1(q+1)}, 192$  ..., $\varphi_{k1},...,\varphi_{k(q+1)})'$  for  $Z_i$ , where the main interest is on  $\beta$ , the SNP effects on the traits. The marginal means,  $E(Y_i|x_i,Z_i) = \mu_i$ , the SNP and 194

195 covariates are modeled through a marginal generalized linear model 196 (GLM):

$$g(\mu_i) = \eta_i = Z_i \varphi + X_i \beta = H_i \theta,$$

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with  $H_i = (Z_i X_i), \theta = (\varphi', \beta')'$  and g(.) as a suitable link function.

The consistent and asymptotically Normal estimates of  $\beta$  and  $\varphi$  are obtained by solving the GEE (Liang and Zeger, 1986):

$$\begin{split} U &= U(\varphi, \beta) = \sum_{i} U_i(\varphi, \beta) = \sum_{i} \nabla \mu_i' V_i^{-1}(Y_i - \mu_i) = 0, \\ \nabla \mu_i &= \partial \mu_i / \partial \theta' = \partial g^{-1}(H_i \theta) / \partial \theta', V_i = \phi A_i^{1/2} R_w(\alpha) A_i^{1/2}, \end{split}$$

where  $g(.)^{-1}$  is the inverse function of g(.),  $\phi$  is a possible dispersion parameter,  $A_i = \text{diag}\{v(\mu_{i1})v(\mu_{i2}),...,v(\mu_{ik})\}$  with  $v(\mu_{im}) = \text{Var}(y_{im}|x_iz_i)\phi$ , and  $R_w = R_w(\alpha)$  is a working correlation matrix that may depend on some unknown parameters  $\alpha$ . Note that  $R_w$  does not have to be correctly specified; for convenience, a working independence model with  $R_w = I$  is often used, as done in this paper unless specified otherwise.

With a canonical link function and a working independence model (i.e.  $R_w = I$ ), it is not difficult to obtain the (generalized) score vector and its consistent covariance estimate:

$$U = (U'_{.1}, U'_{.2})' = \sum_{i=1}^{n} \nabla \mu'_{i} A_{i} (Y_{i} - \mu_{i}) = \sum_{i=1}^{n} (Z_{i}, X_{i})' (Y_{i} - \mu_{i}),$$

$$\widetilde{\Sigma} = \widehat{Cov}(U) = \sum_{i} (Z_{i}, X_{i})' (Y_{i} - \mu_{i}) Y_{i} - \mu_{i})' (Z_{i} X_{i}) = \begin{pmatrix} V_{11} & V_{12} \\ V_{21} & V_{22} \end{pmatrix},$$
(1)

where  $\hat{\mu}_i$  is an estimate of  $\mu_i$ ,  $\Sigma$  is partitioned according to the score vector components  $U_{.1}$  and  $U_{.2}$  for  $\varphi$  and  $\varphi$  respectively.

211 Binary traits

For binary traits (coded as 0 and 1), we use the logit link function, and  $v(\mu_{lm})$   $(\mu_{lm}(1-\mu_m))$ . The (m,l)th element of  $\partial \mu_i/\partial \theta'$  is  $H_{i,ml}\mu_{lm}(1-\mu_{lm})$  with  $H_{i,ml}$  as the (m,l)th element of  $H_i$ . We have the score vector and its covariance estimate as

$$\begin{split} U &= \sum_{i} \left(\frac{\partial \mu_{i}}{\partial \theta'}\right)' A_{i}^{-1/2} R_{w}^{-1} A_{i}^{-1/2} (Y_{i} - \mu_{i}), \\ \widetilde{\Sigma} &= \sum_{i} \left(\frac{\partial \mu_{i}}{\partial \theta'}\right)' A_{i}^{-1/2} R_{w}^{-1} A_{i}^{-1/2} (Y_{i} - \hat{\mu}_{i}) (Y_{i} - \hat{\mu}_{i})' A_{i}^{-1/2} R_{w}^{-1} A_{i}^{-1/2} \left(\frac{\partial \mu_{i}}{\partial \theta'}\right)', \end{split}$$

217 with  $\mu_i$  as an estimate of  $\mu_i$ ,  $A_i = \text{diag}(\mu_{i1}(1 - \mu_{i1}),...,\mu_{im}(1 - \mu_{im}))$ .

Quantitative traits

We use the identity link  $g(\mu_{im}) = \mu_{im}$  and  $v(\mu_{im}) = \phi$ . Then we have

$$U = \sum_{i} H'_{i} R_{w}^{-1} (Y_{i} - \mu_{i}),$$

$$\widetilde{\Sigma} = \sum_{i} H'_{i} R_{w}^{-1} (Y_{i} - \hat{\mu}_{i}) (Y_{i} - \hat{\mu}_{i})' R_{w}^{-1} H_{i}.$$
(2)

220 If we assume a common covariance matrix for *Y<sub>i</sub>*'s across all *i*, then a better covariance estimate is

$$\widetilde{\Sigma} = \sum_{i} H_i' R_w^{-1} \left( \sum_{i} (Y_i - \hat{\mu}_i) (Y_i - \hat{\mu}_i)' / n \right) R_w^{-1} H_i,$$

which is used by default for its better finite-sample performance (Pan, 2001).

223 Existing tests in GEE

Our goal is to detect whether there is any association between any of the traits and the SNP via testing the null hypothesis  $H_0: \beta = (\beta_1, ..., \beta_k)' = 0$  versus  $H_1: \beta \neq 0$ .

To construct score-based tests with covariates  $Z_i$ , we first fit the GEE 227 model under  $H_0$ ,  $g(\mu_i) = Z_i \varphi$ , to obtain  $\hat{\varphi}$  and  $\hat{\mu}_i$ . If we denote for subject 228 i,  $U_{i1}$  as the score vector corresponding to covariates  $Z_i$ , and  $U_{i2}$  as the 229 score vector for the SNP, then the score vector under the null hypothesis, with an assumed independent working correlation structure for the 231 traits, is:

$$\begin{split} U(\hat{\varphi},0) &= \left(U_{.1}', U_{.2}'\right)' = \sum_{i=1}^{n} \left(U_{i1}', U_{i2}'\right)', \\ U_{.1} &= \sum_{i=1}^{n} U_{i1} = \sum_{i=1}^{n} Z_{i}'(Y_{i} - \hat{\mu}_{i}), \\ U_{.2} &= \sum_{i=1}^{n} I^{n}U_{i2} = \sum_{i=1}^{n} X_{i}'(Y_{i} - \hat{\mu}_{i}) = \sum_{i=1}^{n} X_{i}(Y_{i} - \hat{\mu}_{i}). \end{split}$$

The null distribution of the score vector for  $\beta$  is asymptotically Normal 234 under  $H_0$ :

$$U_2 \sim N(0, \Sigma_2) \Sigma_2 = \widehat{\text{Cov}}(U_2) = V_{22} - V_{21} V_{11}^{-1} V_{12}, \tag{3}$$

where 
$$V_{11}$$
,  $V_{12}$ ,  $V_{21}$ ,  $V_{22}$  are defined in Eq. (1).

The Wald test

 $T=\hat{\beta}'\Big(\mathrm{Cov}\Big(\hat{\beta}\Big)\Big)^{-1}\hat{\beta}$ , where  $\hat{\beta}$  is the estimate of  $\beta$  in the GEE marginal model, and  $\mathrm{Cov}\Big(\hat{\beta}\Big)$  is the sandwich estimate. Under  $H_0$ , we have  $_{238}$   $T\sim\chi_k^2$  asymptotically. In spite of its simplicity and popular use, as well  $_{239}$  known (Pan, 2001) and to be shown later, with a relatively large k, the  $_{240}$  Wald test in GEE may become too liberal with inflated Type I errors.

The Score test

 $T = U_2' \Sigma_2^{-1} U_2$ , where  $U_2$  and  $\Sigma_2$  are discussed above; it is asymptot- 243 ically equivalent to the Wald test with the same null distribution  $\chi_k^2$ . 244 Since we only need to fit the model under the null hypothesis, it is computationally simpler than using the Wald test, which requires fitting a 246 full model. More importantly, as to be shown, the Score test controls 247 the Type I error much better than the Wald test. 248

The UminP test 249

 $T=\max_{j=1,\dots,k}U_{.2,j}^2/\sum_{.2,jj}$ , where  $U_{.2,j}$  is the jth element of  $U_{.2}$ , and  $\Sigma_{.2,jj}$  is the jth entry on the diagonal of  $\Sigma_{.2}$ . Although a numerical integration- 251 based method as for single trait-multilocus testing (e.g. Pan, 2009) 252 can be adopted, we use a simulation based method to calculate its p- 253 value. Specifically, we simulate the score vectors  $U_{(b)}=(U_{(b),1}, 254)$   $U_{(b),2},\dots,U_{(b),k}$  from its null distribution  $U_{(b)}\sim N(0,\Sigma_{.2})$  for  $b=1,\dots$  255 B, then calculate the null statistics  $T^{(b)}=\max_{j=1,\dots,k}U_{(b),j}^2/\sum_{.2,jj}$ , and 256 the p-value is  $\sum_{i=1}^{B}I(T^{(b)}>T)/B$ .

With a working independence model  $R_w = I$ , each component  $U_{2,j}$  is 258 equal to the score function for the univariate analysis on the jth trait. 259 Hence, the GEE-UminP test is equivalent to the usual UminP test that 260 combines the univariate analyses on the multiple traits.

For association analysis of rare variants, weighting on the components of the score vector has been recognized as a general and effective approach to synthesizing information contained in the components of the score vector (Lin and Tang, 2011). We borrow this idea and apply quote it to the current context, yielding a weighted score test:

$$T_W = \sum_{i=1}^k w_j U_{.2,j},$$

where the weights *w<sub>j</sub>*'s have to be specified, which is a ke<mark>y and challeng- 269 ing issue</mark>. Various choices of the weights have been proposed for

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analysis of rare variants, all of which are some fixed weights. Our goal is to specify a whole class of weights such that they can cover a wide range of situations: for any given data with unknown true association patterns, we hope that at least one member from the specified class of weights would vield a high-powered test. We reason that, since association information is largely contained in the score vector, the driving force of constructing various score-based tests (as reviewed above), it might be productive to use the score vector to construct the weights. Accordingly, we propose a class of weights  $w_i = U_{2,i}^{\gamma-1}$  for a series of values of  $\gamma = 1, 2, ..., \infty$ , leading to the sum of powered score (*U*) tests, called SPU tests:

$$SPU(\gamma) = \sum_{j=1}^{k} U_{.2,j}^{\gamma}.$$

As  $\gamma = 1$ , the SPU(1) test sums up the information in the multiple traits equally, just as the Average (Sum) test. As the power parameter  $\gamma$  increases, the SPU( $\gamma$ ) test puts higher weights on the traits with larger  $|U_{2,j}|$ , while gradually decreasing the weights on the other traits with smaller  $|U_{2,i}|$ . By statistical theory, we know that a trait associated with the SNP is expected to have a larger  $|U_{.2,j}|$  while a non-associated one has a smaller value. Hence, an increasing value of  $\gamma$  tends to put higher weights on those more strongly associated traits. An extreme situation is that, as  $\gamma \to \infty$  (as an even number), we have

$$SPU(\gamma) \propto \left(\sum_{j=1}^{k} U_{.2,j}^{\gamma}\right)^{1/\gamma} \to \max_{j \in \{1,2,\dots,k\}} \left|U_{.2,j}\right| \equiv SPU(\infty),$$

taking only the largest one. In our experience, an SPU( $\gamma$ ) test with  $\gamma > 8$ often yields results similar to that of the SPU(∞) test. Hence, in all our following experiments, we only used  $\gamma \in \Gamma = \{1, 2, ..., 8, \infty\}$ .

While the SPU(1) is similar to the Average (Sum) test, the SPU(2)test is the same as the SSU test outlined by Yang and Wang (2012), an extension of the SSU test for single trait-multilocus analysis (Pan, 2009) to the current context for multiple traits and a single SNP.

Suppose that the sample size is large enough for the asymptotic null distribution of the score vector to hold, we use a simulation method to estimate the p-value of an SPU test (Lin, 2005; Seaman and Mller-Myhsok, 2005). Suppose that *T* is the test statistic for an SPU( $\gamma$ ) test and  $\hat{\Sigma}_2$  is the covariance matrix of the score vector based on the original data. We draw B samples of the score vector from its null distribution:  $U_2^{(b)} \sim MVN(0, \hat{\Sigma}_2)$ , b = 1,...B, and obtain a null statistic  $T^{(b)} =$  $\sum_{i=1}^k \overline{U_{2,i}^{(b)}}$ . We then calculate p-value  $=\sum_{b=1}^k (|T^{(b)}| > |T|)/B$ .

Since the result of an SPU( $\gamma$ ) test depends on the choice of the power parameter  $\gamma$  while in general it is unknown which value of  $\gamma$  is optimal for a given dataset, it would be convenient to have a test that dataadaptively and automatically chooses the parameter  $\gamma$ . We propose an adaptive SPU (aSPU) test to estimate and thus select the most powerful SPU test for given data. Because it is difficult to characterize the power curve of an SPU test, we use the p-value of a SPU test to approximate its power; this idea has been widely used in practice. Accordingly, the aSPU test statistic is the minimum p-value among all SPU tests:

$$T_{aSPU} = \min_{\gamma \in \Gamma} P_{SPU(\gamma)},$$

where  $P_{SPU(\gamma)}$  is the p-value of the SPU( $\gamma$ ) test.

The p-value of aSPU can be obtained based on simulations. It may appear that a double simulation procedure is needed, but indeed not necessary. As before, first, we simulate B independent copies of the null score vector  $U^{(b)}$  from  $N(0, \hat{\Sigma}_{.2})$  for b = 1, 2,...B. We then calculate the corresponding SPU test statistics  $T_{SPU(\gamma)}^{(b)}$  and their p-values  $p_{\gamma}^{(b)} =$ 

 $\sum\nolimits_{b_1\neq b} I\!\left(T_{SPU(\gamma)}^{(b_1)}\!>\!T_{SPU(\gamma)}^{(b)}\right)\!/(B-1). \text{ Thus, we have } T_{aSPU}^{(b)}=\min\nolimits_{\gamma\;\in\;\Gamma} p_{\gamma}^{(b)},$ 

$$\sum_{b_1 \neq b} I\left(T_{SPU(\gamma)}^{(b_1)} > T_{SPU(\gamma)}^{(b)}\right) / (B-1). \text{ Thus, we have } T_{aSPU}^{(b)} = \min_{\gamma \in \Gamma} p_{\gamma}^{(b)},$$

and the final p-value of the aSPU test is  $P_{aSPU} = \sum_{b=1}^{B} I(T_{aSPU}^{(b)} < 322)$  $T_{aSPU}$ )/B. Note that, in practice we can first use a smaller B, say B =1000, to scan a genome, then gradually and repeatedly increase B for a 324 few SNPs that pass an initial significance criterion (e.g. p-value < 5/B) 325 in the previous step.

The aSPU test aims to data-adaptively approximate the most power- 327 ful SPU test among a set of versatile SPU( $\gamma$ ) tests with various values of 328  $\gamma$ , thus maintaining high power at any given situation. Although we use 329 the minimum p-value to approximate the most powerful SPU test, other 330 combining methods (e.g. Han and Pan, 2010) are also possible and may Q10 be explored. The aSPU test uses adaptive weights on the multiple traits 332 to assess their aggregated effects (while down-weighting the effects of 333

The SPU and aSPU tests assume that the multiple traits are in the 335 same scale; if not, e.g. when the variances of the traits vary a lot, one 336 should first standardize the traits to have an equal sample variance. 337 For example, when some null traits have larger variances than that of 338 associated traits, an SPU test statistic will be dominated by the noises 339 in the score components for the null traits, leading to concealing associ- 340 ation signals and thus reduced power. Alternatively, to account for pos- 341 sibly different scales or variances of the multiple traits, one can use a 342 *variance-weighted SPU test* (SPUw): for any  $\gamma \in \Gamma$ ,

$$SPUw(\gamma) = \sum_{j=1}^{k} \left(U_{.2,j} / \sqrt{\Sigma_{.2,jj}}\right)^{\gamma}.$$

Note that under the working independence model ( $R_w = I$ ) in GEE, the SPUw(∞) test is equal to the UminP test. The adaptive SPUw 346 (aSPUw) test can be accordingly defined as for the aSPU test.

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Properties of the GEE tests

We analyze how the proposed GEE-based tests are related to some 349 existing tests in the absence of covariates while testing for association 350 between a set of quantitative traits and a single SNP. By default (unless 351 specified otherwise), we assume without loss of generality that both  $Y_i$  352 and  $x_i$  have been centered at 0; that is,  $\sum_{i=0}^{n} Y_i = 0$  and  $\sum_{i=0}^{n} x_i = 0$ . 353 For simplicity we also assume that there is no missing data, and each 354 subject has all k traits observed.

We expect that most of our below conclusions can be extended to 356 the case for quantitative traits with covariates  $Z_i$ : we first regress  $Y_i$  on 357  $Z_i$  to obtain residuals  $r_{X,i}$  and regress  $x_i$  on  $Z_i$  to obtain residuals  $r_{X,i}$ ; 358 then we apply the same arguments below to regression of  $r_{Y,i}$  on  $r_{X,i}$  359 (instead of regression of  $Y_i$  on  $x_i$ ).

Fitting a GEE working independence model and an equivalent model In the current context, the GEE model is

$$E(Y_i) = X_i \beta = x_i \beta \tag{4}$$

with  $\beta = (\beta_1, ..., \beta_k)'$ . Note that, due to centering both  $Y_i$  and  $x_i$  at mean 364 0, no intercept term is needed. To test  $H_0$ :  $\beta = 0$ , under the working independence model (i.e.  $R_w = I$ ), we have the score vector and its empirical covariance estimate as 366

$$U = \sum_{i=1}^{n} x_i (Y_i - \overline{Y}) = \sum_{i=1}^{n} x_i Y_i, \qquad \widehat{Cov}(U) = \sum_{i=1}^{n} x_i^2 Y_i Y_i'.$$
 (5)

As an alternative, we fit the below model:

$$E(x_i) = Y_i'b \tag{6}$$

with  $b = (b_1, ..., b_k)'$ . To test  $H_0$ : b = 0, we obtain its score vector and 370 empirical covariance estimate, which are exactly the same as in Eq. (5).

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Note that, due to the possible correlations among the components of  $Y_i$  and possibly non-Normality or non-constant variances of  $x_i$  (the latter of which is true because  $x_i$  is the genotype score), we have to use the empirical covariance estimate of the score vector. In summary, any test based on the score vector of fitting the GEE working independence model (4) can be equally constructed based on fitting a simple linear model (6). For example, a GEE-SPU(2) test based on the GEE model (4) is equivalent to the SSU test based on model (6) (Pan, 2009).

We note that using the GEE score components and their variances to test for  $H_{m,0}$ :  $\beta_m=0$  separately for each trait m is the same as conducting a univariate Score test on each trait m individually. Hence, in addition to UminP, other methods could be applied to combine these univariate tests (Yang and Wang, 2012); in fact, if  $R_w=I$  is used in GEE, all our proposed tests could be regarded in this way.

Finally, we note that the above conclusion holds for other GLMs with a canonical link function, under which the score vector maintains the same form as in Eq. (5) (McCullagh and Nelder, 1983).

GEE-SPU versus GEE-SPUw tests

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In the current context, based on Eq. (5), we have

$$\begin{split} \textit{SPU}(\gamma) &= \sum_{j=1}^k \left(\sum_{i=1}^n x_i y_{ij}\right)^{\gamma}, \\ \textit{SPUw}(\gamma) &= \sum_{j=1}^k \left(\frac{\sum_{i=1}^n x_i y_{ij}}{\sqrt{\widetilde{\Sigma}_{jj}}}\right)^{\gamma} \approx \sum_{j=1}^k \left(\frac{\sum_{i=1}^n x_i^2 y_{ij}}{\sqrt{\sum_{i=1}^n x_i^2 \text{Var}\left(y_{ij}\right)}}\right)^{\gamma} \propto \sum_{j=1}^k \left(\frac{\sum_{i=1}^n x_i y_{ij}}{\sqrt{\text{Var}\left(y_{ij}\right)}}\right)^{\gamma}, \\ \text{Var}\left(y_{ij}\right) &= \text{Var}(x_i)\beta_j^2 + \sigma_1^2 = 2f(1-f)\beta_j^2 + \sigma_1^2, \end{split}$$

where the Hardy — Weinberg equilibrium is assumed in the second equality for  $Var(y_{ij})$ , f is the MAF of the SNP, and  $\sigma_f^2$  is the residual variance of trait j (after removing the effect of the SNP). We also assume that  $Var(y_{ij})$  does not depend on i (but may depend on j).

It is clear that the SPUw tests, but not SPU tests, are invariant to the scales of the traits. Hence, the SPUw and aSPUw tests can automatically account for different scales of the multiple traits, while the SPU and aSPU tests cannot, requiring one to standardize the (residual) variances of the traits if they differ a lot. On the other hand, if  $\sigma_j^2$ 's are all equal, for an associated trait j with  $\beta_j \neq 0$ , due to its larger  $\text{Var}(y_{ij})$ , any SPUw test would but a lower weight on it as compared to the corresponding SPU test, leading to power loss. Dowever, for complex traits with typically small  $|\beta_j|$ , the power loss of the SPUw or aSPUw test is often negligible, resulting in almost equal power between the aSPUw and aSPU tests, as to be confirmed in our numerical examples.

Use of various working correlation structures in GEE

For quantitative traits, it is often reasonable to assume that the marginal covariance matrix  $Cov(Y_i|H_0) = V_0$  does not vary over i. Under this assumption (and thus a equal cluster size  $\dim(Y_i) = k$ ), we can write the working covariance matrix  $V_{w,i} = A_i^{-1/2} R_w A_i^{-1/2} = V_{w,0}$ , invariant to i.

With any working correlation matrix  $R_w$ , the score vector and its covariance estimate are

$$\begin{split} &U(R_w) = \sum_i x_i V_{w,0}^{-1}(Y_i - Y_0), \\ &\hat{\Sigma}(R_w) = \sum_i x_i V_{w,0}^{-1} \left( \sum_i (Y_i - Y_0)(Y_i - Y_0)'/n \right) V_{w,0}^{-1} x_i, \end{split} \tag{7}$$

from which it can be seen that

$$\begin{split} T_{\text{Sco}} &= U(R_{\text{w}})' \hat{\Sigma}(R_{\text{w}})^{-1} U(R_{\text{w}}) \\ &= \left( \sum_{i} x_{i} (Y_{i} - Y_{0})' \right) V_{\text{w,0}}^{-1} \bigg\{ V_{\text{w,0}}^{-1} \sum_{i} x_{i}^{2} \bigg( \sum_{i} (Y_{i} - Y_{0}) (Y_{i} - Y_{0})' / n \bigg) V_{\text{w,0}}^{-1} \bigg\}^{-1} V_{\text{w,0}}^{-1} \bigg( \sum_{i} x_{i} (Y_{i} - Y_{0}) \bigg) \\ &= U(I)' \hat{\Sigma}(I)^{-1} U(I). \end{split}$$

 $=U(I)'\Sigma(I)^{-1}U(I)$ .

That is, the GEE-Score test is invariant to  $R_w$ , the working correlation 415 structure.

Since in general  $U(R_w) \neq U(I)$  and  $\hat{\Sigma}(R_w) \neq \hat{\Sigma}(I)$  for  $R_w \neq I$ , the other The GEE-based tests (except GEE-Score) are not necessarily invariant to  $R_w$ . 418

Surprisingly, as to be shown, the GEE-UminP, GEE-SPUw( $\infty$ ) and 419 GEE-SPU( $\infty$ ) tests may lose power when the true correlation structure 420 is used as  $R_w$ . Here we consider a simple example. Suppose that the 421 first 5 traits are associated with a SNP while all other remaining k-5 422 traits are not; the true covariance matrix  $Cov(Y_i)$  has a compound 423 symmetry structure Cs(r):  $Var(y_{ij}) = 1$  and  $Cov(y_{ij}, y_{il}) = r$  for any 424  $j \neq l$ . The score vector  $U(R_w) = (U_1(R_w), \neg, U_k(R_w))'$  is defined in 425 Eq. (8) and  $\hat{\Sigma}(R_w) \approx \sum_i x_i^2 V_w^{-1} Cov(Y_i) V_w^{-1}$ . Without loss of generality, 426 we also assume  $x_i$  is standardized to have  $\sum_i x_i^2 = 1$ . Under the working 427 independence model  $R_w = l$ , assume that  $E(U_j(l)) = 1$  for  $1 \leq j \leq k_1$ , and 428  $E(U_j(l)) = 0$  for  $5 < j \leq k$ . Hence, with  $R_w = l$ , the component-wise signal 429 magnitude (related to the non-centrality parameter for a univariate 430 Score test on each trait) is

$$\lambda_j = E(U_j(I))^2 / Var(U_j(I)),$$

which is 1 for  $1 \le j \le 5$ , and is 0 otherwise. On the other hand, in the 433 ideal case with  $V_w = \text{Cov}(Y_i)$ , we have

$$E(U(R_w)) = \operatorname{Cov}(Y_i)^{-1} E(U(I)) \hat{\Sigma}(R_w) = \operatorname{Cov}(Y_i)^{-1}.$$

Accordingly, we can calculate its component-wise signal magnitude  $\lambda_i = E(U_i(R_w))^2/\text{Var}(U_i(R_w))$ . Table 1 shows some examples.

It is clear that, compared to using  $R_w = I$ , one may gain or lose with 437 respect to component-wise information contents in the score vector by 438 using a correct correlation matrix as  $R_w$  in GEE, depending on the value 439 of between-trait correlation r and the number of traits k. In particular, 440 with r > 0 and a small k, using a correct correlation matrix may give 441  $\max_j \lambda_j < 1$ , leading to loss of power by the UminP test, as compared 442 to its using the working independence model in GEE; as k increases 443 (while keeping the number of associated traits fixed), it will gain by 444 using the correct correlation matrix as  $R_w$ . This latter point is consistent

**Table 1** Component-wise signal magnitude with various  $R_w$  and k in GEE.

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t1.3	$R_w$	I	$R_0$ : CS( $r =$	0.5)			$R_0$ : CS( $r =$	-0.5)		_
t1.4	k	≥5	5	10	40	400	5	10	40	400
t1.5	E(U <sub>1</sub> )	1	0.3	1.091	1.756	1.975	-1	0.191	0.577	0.658
t1.6	$Var(U_1)$	1	1.667	1.818	1.951	1.995	0.333	0.571	0.649	0.665
t1.7	$\lambda_1$	1	0.067	0.655	1.581	1.955	3.000	0.064	0.513	0.652
t1.8	$E(U_6)$	0	_	-0.909	-0.244	-0.025	-	-0.476	-0.090	-0.008
t1.9	$Var(U_6)$	1	-	1.818	1.951	1.995	-	0.571	0.649	0.665
t1.10	$\lambda_6$	0	_	0.455	0.031	0.0003	-	0.397	0.013	0.0001
t1.11	$\max_{j=1}^{k} \lambda_j$	1	0.067	0.655	1.581	1.955	3.000	0.397	0.513	0.652

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**Q2**t2

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t3.1

**Table 2**Relationships between the existing and new tests.

t2.3	Method	Model or test statistic	Relation to the new tests
t2.4	The Average method (Shen et al., 2011)	$\sum_{i=1}^{k} Y_{ii} = \alpha_0 + \alpha_1 x_i + e_i$ , Applying the Score test on $H_0$ : $\alpha_1 = 0$ .	Average = $GEE-SPU(1)$ .
t2.5	TATES (van der Sluis et al., 2013)	$Y_{ij} = \beta_{0,j} + \beta_{1,j}x_i + e_{ij}$ for $j = 1, 2,, k$ . Testing for $H_0: \beta_{1,1} = = \beta_{1,k} = 0$ with analytical approximations to calculate a p-value.	TATES $\approx$ GEE-UminP $\approx$ GEE-SPUw( $\infty$ ).
t2.6	CCA = MANOVA (Ferreira and Purcell, 2009; Yang and Wang, 2012)	CCA seeks to maximize the correlation between a linear combination of $(Y_{i1},, Y_{ik})$ and $x_i$ . Test statistic: $B = S_{XX}^{-1/2} S_{XY} S_{YY}^{-1} S_{YX} S_{XX}^{-1/2}$	CCA = MANOVA = GEE-Score.
t2.7	MDMR (Zapala and Schork, 2012)	$D_{ij} = d(Y_i, Y_j), A = (-D_{ij}^2/2), G = (I - 11'/n)A(I - 11'/n), H = X(X'X)^{-1}X'.$ Test statistic: $F = tr(HGH)/tr[(I - H)G(I - H)]$	MDMR = GEE-SPU(2) if $d(,)$ is Euclidean.
	KMR (Maity et al., 2012)	Test statistic: $T_{KMR} = (Y - \overline{Y})' V_0^{-1} K V_0^{-1} (Y - \overline{Y})'$	KMR = GEE-SPU(2) if $K = XX'$ and
t2.8			$R_w = Corr(Y_i H_0)$
t2.9	MultiPhen (O'Reilly et al., 2012)	$\pi_j(y) = Pr(x_i = j   Y_i = y), \kappa_j(y) = \sum_{m=0}^{j} \pi_m(y) \text{ for } j = 0, 1, 2, \log \frac{\kappa_j(y)}{1 - \kappa_j(y)} = \alpha_j - y'\beta$ for $j = 0$ and 1. Applying the Score (or likelihood ratio) test on $H_0$ : $\beta = 0$ .	MultiPhen $\approx$ GEE-Score.
t2.10	Generalized Kendall's tau (Zhang et al., 2010)	$u_{ij} = (Y_{i1} - Y_{j1},, Y_{iq} - Y_{jq})', \overline{u}_i = \sum_{j=1}^n u_{ij}/n, \tau = \sum_{i=1}^n x_i \overline{u}_i$ . Test statistic: $T = \tau' V_0^{-1} \tau$ .	GK-tau = $GEE$ -Score.

with the theoretical result of Cai et al. (2013) for a high-dimensional two-sample comparison problem.

Relationships between the new and existing tests

Our proposed tests cover several commonly used methods as special cases in the current context. A summary is given in Table 2, and the details are relegated to the Appendix A.

452 Simulation Set-ups

Unless specified otherwise, by default each simulated dataset consisted of n = 1000 subjects with a varying number (k) of correlated quantitative traits, including the first  $k_1 = 5$  traits associated with the SNPs to be tested under the alternative hypothesis  $H_1$  (while all other  $k - k_1$  traits were not associated). For each subject, we generated a block of p = 11 SNPs in linkage disequilibrium (LD) and the first one was the causal SNP under  $H_1$ . Specifically, for each subject i, we first generated a latent vector  $G_i = (G_{i1}, ... G_{ip})'$  from a multivariate Normal distribution with a first-order auto-regressive (AR-1) covariance structure with parameter p = 0.5:  $Cov(G_{ij}, G_{il}) = \rho^{|j-1|}$ . Second, each latent element  $G_{ii}$  was dichotomized to 0 or 1 with probability  $Prob(G_{ig} = 1)$  as its minor allele frequency (MAF), randomly drawn from a uniform distribution (Pan, 2009). The MAF of the causal (i.e. first) SNP was from U(0.3, 0.4), while the MAFs of the other SNPs were independently drawn from U(0.1, 0.5). In this way, we generated a haplotype for subject i. Similarly, we independently generated another haplotype for

subject *i*; by combining the two haplotypes we obtained the genotype 469 of the subject. We tested on each of the first few SNPs nearest to the causal SNP.

Similarly, we also considered smaller sample sizes n = 500 and n = 472 200, and rare variants (RVs) with MAF = 0.01.

The phenotype for each subject i,  $Y_i = (Y_{i1}, ..., Y_{ik})'$  was simulated 474 from a linear model:

$$Y_i = \beta_0 + x_i \beta + \epsilon_i,$$

where  $\beta_0 = (\beta_{01}, ..., \beta_{0k})'$ ,  $\beta = (\beta_1, ..., \beta_k)'$ ,  $x_i$  is the genotype score of 477 the causal SNP, and  $\epsilon_i$  was independently drawn form a multivariate Normal distribution  $N(0, \sigma^2 R)$ , with  $\sigma = 1$  and R as either an AR-1 correlation matrix with parameter r or a compound symmetry (CS) matrix 479 with parameter r; we considered  $r = \pm 0.3$  or 0.5. In addition, we also 480 considered using a correlation matrix estimated from the ADNI data. 481  $\beta_{0m}$  is the intercept for trait m. Under  $H_0$ , we had  $\beta = 0$ ; under  $H_1$ , we 482 had  $\beta_m \neq 0$  for  $1 \leq m \leq k_1$ , and  $\beta_m = 0$  for  $k_1 < m \leq k$ . The non-zero 483  $\beta_i$ 's were randomly drawn from a uniform distribution U(0.2, 0.3) for 484 weak effects, or from U(0.8, 1) for strong effects. That is, under  $H_1$ , 485 only the first 5 traits were associated with the causal SNP, and we grad- 486 ually increased the number of the non-associated (i.e. null) traits from 0 487 to 5, then 15, up to 35. Under each simulation set-up, 1000 datasets 488 were independently generated and analyzed; we used B = 1000 to obtain p-values for any simulation based method. Unless specified other- 490 wise, by default, the working independence model was used in GEE.

Table 3
Empirical Type I error rates when the multiple traits were correlated with a CS structure with correlation coefficient *r*. An independence working correlation structure was used in GEE.

t3.3										GEE										
t3.4							MDMR					SPU(γ)								
t3.5	r	SNP	#traits	Average	MultiPhen	TATES	$L_1$	L <sub>2</sub>	MANOVA	Wald	Score	UminP	$\gamma = 1$	2	3	4	5	6	00	aSPU
t3.6	0.3	1	5	0.043	0.051	0.048	0.040	0.048	0.051	0.056	0.051	0.046	0.038	0.049	0.050	0.045	0.048	0.049	0.049	0.050
t3.7			10	0.053	0.060	0.055	0.059	0.058	0.060	0.076	0.060	0.053	0.049	0.057	0.051	0.049	0.047	0.052	0.046	0.051
t3.8			20	0.058	0.062	0.046	0.052	0.046	0.064	0.094	0.062	0.046	0.054	0.048	0.046	0.049	0.051	0.049	0.046	0.047
t3.9			30	0.049	0.034	0.047	0.059	0.052	0.036	0.102	0.034	0.042	0.051	0.049	0.051	0.052	0.049	0.045	0.045	0.049
t3.10			40	0.053	0.055	0.059	0.055	0.058	0.061	0.165	0.054	0.059	0.053	0.059	0.061	0.061	0.062	0.064	0.057	0.054
t3.11	0.3	2	5	0.051	0.058	0.059	0.054	0.051	0.059	0.066	0.058	0.056	0.050	0.049	0.051	0.048	0.053	0.050	0.053	0.050
t3.12			10	0.050	0.046	0.043	0.044	0.048	0.047	0.061	0.046	0.047	0.050	0.042	0.047	0.046	0.048	0.046	0.050	0.045
t3.13			20	0.048	0.049	0.048	0.048	0.048	0.049	0.078	0.049	0.048	0.049	0.054	0.053	0.051	0.053	0.055	0.046	0.053
t3.14			30	0.041	0.048	0.045	0.041	0.039	0.050	0.102	0.048	0.045	0.045	0.041	0.042	0.039	0.041	0.042	0.050	0.043
t3.15			40	0.058	0.051	0.044	0.056	0.059	0.053	0.153	0.049	0.051	0.055	0.055	0.055	0.051	0.050	0.046	0.049	0.052
t3.16	0.5	1	5	0.043	0.052	0.050	0.044	0.045	0.051	0.056	0.051	0.045	0.038	0.041	0.046	0.049	0.046	0.047	0.047	0.048
t3.17			10	0.053	0.060	0.045	0.049	0.049	0.060	0.076	0.060	0.048	0.047	0.049	0.054	0.053	0.050	0.048	0.051	0.048
t3.18			20	0.058	0.062	0.048	0.057	0.051	0.064	0.094	0.062	0.055	0.055	0.053	0.049	0.048	0.050	0.047	0.052	0.048
t3.19			30	0.049	0.034	0.045	0.055	0.055	0.036	0.102	0.034	0.055	0.054	0.048	0.050	0.054	0.054	0.053	0.062	0.055
t3.20			40	0.053	0.055	0.048	0.055	0.060	0.061	0.165	0.054	0.051	0.055	0.058	0.060	0.059	0.058	0.056	0.054	0.055
t3.21	0.5	2	5	0.051	0.059	0.054	0.055	0.050	0.059	0.066	0.058	0.049	0.050	0.052	0.050	0.050	0.049	0.045	0.049	0.051
t3.22			10	0.050	0.046	0.045	0.047	0.053	0.047	0.061	0.046	0.047	0.050	0.048	0.045	0.049	0.046	0.046	0.047	0.046
t3.23			20	0.048	0.049	0.046	0.045	0.048	0.049	0.078	0.049	0.048	0.049	0.051	0.050	0.055	0.056	0.054	0.049	0.048
t3.24			30	0.041	0.048	0.043	0.042	0.037	0.050	0.102	0.048	0.046	0.043	0.040	0.040	0.039	0.041	0.042	0.051	0.046
t3.25			40	0.058	0.051	0.040	0.059	0.057	0.053	0.153	0.049	0.046	0.056	0.058	0.057	0.054	0.054	0.054	0.048	0.051

**Table 4** Empirical power when the multiple traits were correlated with a CS structure with correlation coefficient r; the first five traits were associated with a causal SNP with log-ORs  $\beta_i \sim U(0.8, 1)$ , while all others had  $\beta_i = 0$ . An independence working correlation structure was used in GEE.

t4.4										GEE									
t4.5							MDMR					SPU(γ)							,
t4.6	r	SNP	#trait	Average	MultiPhen	TATES	$L_1$	L <sub>2</sub>	MANOVA	Score	UminP	$\gamma = 1$	2	3	4	5	6	00	aSPU
t4.7	0.3	2	5	0.888	0.683	0.823	0.878	0.883	0.683	0.682	0.815	0.889	0.880	0.868	0.862	0.851	0.843	0.812	0.865
t4.8			10	0.567	0.685	0.727	0.786	0.826	0.686	0.684	0.708	0.567	0.830	0.777	0.819	0.796	0.807	0.772	0.795
t4.9			20	0.218	0.613	0.665	0.616	0.729	0.615	0.611	0.657	0.223	0.724	0.667	0.787	0.756	0.792	0.762	0.757
t4.10			30	0.116	0.528	0.607	0.435	0.574	0.531	0.528	0.591	0.117	0.577	0.541	0.725	0.695	0.742	0.738	0.703
t4.11			40	0.084	0.424	0.536	0.262	0.442	0.435	0.424	0.534	0.084	0.432	0.445	0.644	0.609	0.680	0.678	0.639
t4.12	0.3	3	5	0.334	0.178	0.292	0.328	0.330	0.178	0.177	0.281	0.331	0.327	0.321	0.315	0.312	0.305	0.289	0.320
t4.13			10	0.184	0.167	0.203	0.240	0.269	0.167	0.167	0.197	0.182	0.273	0.260	0.282	0.267	0.273	0.244	0.249
t4.14			20	0.092	0.138	0.179	0.149	0.189	0.141	0.137	0.173	0.090	0.188	0.191	0.242	0.246	0.257	0.242	0.229
t4.15			30	0.074	0.121	0.143	0.107	0.120	0.127	0.119	0.146	0.079	0.128	0.141	0.185	0.184	0.203	0.204	0.181
t4.16			40	0.058	0.105	0.132	0.088	0.113	0.109	0.104	0.134	0.062	0.112	0.118	0.161	0.168	0.179	0.188	0.168
t4.17	0.5	2	5	0.829	0.602	0.784	0.821	0.822	0.604	0.601	0.763	0.832	0.821	0.811	0.806	0.800	0.793	0.769	0.806
t4.18			10	0.424	0.725	0.694	0.629	0.729	0.728	0.725	0.685	0.430	0.734	0.714	0.766	0.750	0.765	0.737	0.723
t4.19			20	0.163	0.665	0.624	0.344	0.524	0.666	0.662	0.634	0.161	0.534	0.567	0.697	0.695	0.725	0.722	0.694
t4.20			30	0.093	0.570	0.549	0.186	0.318	0.577	0.570	0.570	0.093	0.319	0.440	0.593	0.609	0.666	0.707	0.653
t4.21			40	0.067	0.484	0.487	0.119	0.203	0.496	0.483	0.508	0.072	0.202	0.333	0.518	0.544	0.612	0.654	0.613
t4.22	0.5	3	5	0.291	0.149	0.270	0.288	0.290	0.150	0.148	0.259	0.290	0.294	0.293	0.285	0.284	0.279	0.263	0.287
t4.23			10	0.129	0.181	0.209	0.171	0.207	0.182	0.180	0.201	0.126	0.203	0.223	0.245	0.249	0.255	0.245	0.223
t4.24			20	0.077	0.138	0.160	0.098	0.130	0.139	0.136	0.168	0.075	0.131	0.158	0.196	0.212	0.220	0.228	0.205
t4.25			30	0.067	0.117	0.129	0.077	0.092	0.121	0.117	0.139	0.065	0.091	0.118	0.144	0.156	0.166	0.195	0.181
t4.26			40	0.055	0.110	0.113	0.071	0.078	0.116	0.109	0.129	0.054	0.079	0.105	0.134	0.148	0.163	0.190	0.166

For comparison, in addition to the GEE-based tests, we also applied some representative existing tests, including the Average method, MultiPhen, TATES, MANOVA (based on the Wilks statistic) and MDMR (based on the  $L_1$ -norm or  $L_2$ -norm as the distance metric).

### ADNI data

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t5.2 t5.3

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Data used in the preparation of this article were obtained from the Alzheimer's Disease Neuroimaging Initiative (ADNI) database (adni.loni.usc.edu). The ADNI was launched in 2003 by the National Institute on Aging (NIA), the National Institute of Biomedical Imaging and Bioengineering (NIBIB), the Food and Drug Administration (FDA), private pharmaceutical companies and non-profit organizations, as a \$60 million, 5-year public-private partnership. The primary goal of ADNI has been to test whether serial magnetic resonance imaging (MRI), positron emission tomography (PET), other biological markers, and clinical and neuropsychological assessment can be combined to measure the progression of mild cognitive impairment (MCI) and early Alzheimer's disease (AD). Determination of sensitive and specific markers of very early AD progression is intended to aid researchers and clinicians to develop new treatments and monitor their effectiveness, as well as lessen the time and cost of clinical trials. The Principal Investigator of this initiative is Michael W. Weiner, MD, VA Medical Center and University of California — San Francisco. ADNI is the result 513 of efforts of many coinvestigators from a broad range of academic insti-514 tutions and private corporations, and subjects have been recruited from 515 over 50 sites across the U.S. and Canada. The initial goal of ADNI was to 516 recruit 800 subjects but ADNI has been followed by ADNI-GO and ADNI-517 2. To date these three protocols have recruited over 1500 adults, ages 55 518 to 90, to participate in the research, consisting of cognitively normal 519 older individuals, people with early or late MCI, and people with early 520 AD. The follow up duration of each group is specified in the protocols 521 for ADNI-1, ADNI-2 and ADNI-GO. Subjects originally recruited for 522 ADNI-1 and ADNI-GO had the option to be followed in ADNI-2. For 523 up-to-date information, see www.adni-info.org.

Results	528
Simulations	520

In Table 3, the multivariate traits had a compound symmetry (CS) 528 correlation structure with parameter r=0.3 or 0.5. All the tests, except 529 the GEE-Wald test, could control the Type I error. As the number of the 530 traits, k, increased, the GEE-Wald test gradually had a severely inflated 531 Type I error; in contrast, the GEE-Score test performed satisfactorily. 532

Empirical power when the multiple traits were correlated with a CS structure with correlation coefficient r = 0.3, and non-zero  $\beta_j \sim U(0.2, 0.3)$ . An independence working correlation structure was used in GEE.

t5.4									GEE									
t5.5						MDMR					$SPU(\gamma)$							
t5.6	SNP	#traits	Average	MultiPhen	TATES	$L_1$	L <sub>2</sub>	MANOVA	Score	UminP	$\gamma = 1$	2	3	4	5	6	00	aSPU
t5.7	1	5	0.664	0.468	0.551	0.653	0.652	0.469	0.468	0.531	0.660	0.658	0.636	0.609	0.597	0.569	0.533	0.632
t5.8		10	0.263	0.574	0.452	0.441	0.506	0.576	0.573	0.437	0.267	0.501	0.460	0.493	0.472	0.481	0.444	0.456
t5.9		20	0.114	0.535	0.335	0.202	0.245	0.536	0.535	0.330	0.114	0.249	0.261	0.330	0.321	0.348	0.345	0.305
t5.10		30	0.084	0.458	0.283	0.126	0.158	0.462	0.456	0.282	0.085	0.162	0.188	0.254	0.262	0.288	0.293	0.257
t5.11		40	0.058	0.412	0.252	0.089	0.103	0.421	0.409	0.250	0.058	0.100	0.128	0.180	0.192	0.236	0.263	0.211
t5.12	2	5	0.226	0.110	0.165	0.209	0.213	0.110	0.108	0.160	0.221	0.214	0.206	0.188	0.188	0.181	0.166	0.211
t5.13		10	0.087	0.142	0.120	0.098	0.117	0.143	0.142	0.115	0.088	0.117	0.116	0.129	0.129	0.128	0.122	0.118
t5.14		20	0.064	0.132	0.085	0.074	0.083	0.135	0.131	0.091	0.064	0.086	0.089	0.099	0.097	0.098	0.095	0.089
t5.15		30	0.058	0.130	0.098	0.063	0.069	0.131	0.129	0.097	0.060	0.071	0.076	0.086	0.092	0.098	0.102	0.087
t5.16		40	0.050	0.091	0.067	0.057	0.056	0.098	0.091	0.066	0.049	0.055	0.057	0.064	0.066	0.070	0.071	0.063

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t7.1

t7.2 t7.3

Table 6 Empirical Type I error rates when the multiple traits were correlated with an AR1 structure with correlation coefficient r. An independence working correlation structure was used in GEE.

6.3										GEE									
6.4							MDMR					SPU(γ)							
6.5	r	SNP	#traits	Average	MultiPhen	TATES	$L_1$	L <sub>2</sub>	MANOVA	Score	UminP	$\gamma = 1$	2	3	4	5	6	00	aSPU
6.6	0.5	1	5	0.037	0.051	0.051	0.049	0.051	0.051	0.041	0.042	0.043	0.033	0.035	0.034	0.037	0.037	0.040	0.036
6.7			10	0.045	0.060	0.053	0.049	0.060	0.060	0.046	0.053	0.041	0.052	0.048	0.051	0.057	0.058	0.051	0.051
6.8			20	0.060	0.059	0.046	0.040	0.059	0.064	0.041	0.044	0.059	0.048	0.055	0.052	0.053	0.047	0.043	0.050
6.9	0.5	2	4	0.048	0.058	0.052	0.060	0.058	0.059	0.041	0.040	0.050	0.045	0.042	0.041	0.041	0.041	0.040	0.040
6.10			10	0.062	0.047	0.044	0.053	0.047	0.047	0.062	0.056	0.063	0.062	0.056	0.057	0.053	0.058	0.064	0.061
6.11			20	0.046	0.047	0.052	0.048	0.047	0.049	0.048	0.052	0.043	0.058	0.053	0.053	0.054	0.051	0.060	0.053
6.12	0.3	1	5	0.037	0.051	0.040	0.047	0.045	0.051	0.041	0.042	0.039	0.034	0.034	0.037	0.037	0.038	0.039	0.036
6.13			10	0.048	0.060	0.049	0.061	0.054	0.060	0.046	0.043	0.047	0.049	0.040	0.044	0.037	0.040	0.040	0.052
6.14			20	0.059	0.062	0.050	0.050	0.048	0.064	0.041	0.058	0.060	0.042	0.062	0.047	0.062	0.055	0.057	0.058
6.15	0.3	2	5	0.049	0.058	0.057	0.056	0.060	0.059	0.041	0.049	0.051	0.050	0.040	0.043	0.046	0.044	0.044	0.042
6.16			10	0.061	0.046	0.054	0.045	0.042	0.047	0.062	0.056	0.061	0.062	0.065	0.063	0.059	0.057	0.057	0.059
6.17			20	0.051	0.049	0.044	0.050	0.047	0.049	0.048	0.062	0.051	0.058	0.051	0.053	0.056	0.059	0.062	0.056

The poor performance of the Wald test and better performance of the Score test for finite-samples in GEE are well known (e.g. Guo et al., 2005); due to its inability to control Type I errors, we will omit the discussion on the GEE-Wald test in the seguel.

Table 9 shows the power performance of the tests when the causal SNP had strong genetic effects on the associated 5 traits. Since the causal SNP and its nearest neighbor were strongly associated with (a subset of) the traits, the power of each test was close to 1 (not shown); hence, we tested on the second and third nearest SNPs next to the causal SNP. First, we can empirically verify our theoretical results derived earlier: i) the equivalence between MANOVA and the GEE-Score test, between MDMR(L2) and the GEE-SPU(2) test, and the Average and GEE-SPU(1) tests; ii) the similar performance between TATES and UminP (or  $SPUw(\infty)$ ), and between MultiPhen and the GEE-Score test. Since the traits had a multivariate Normal distribution, using the  $L_2$ -norm as the distance was more powerful than using the  $L_1$ -norm in MDMR; however, with other trait distributions, it is possible that the latter may edge over the former. Second, we note that the Average test, or equivalently the GEE-SPU(1) test, had the highest power when all  $k = k_1 = 5$  traits were associated with the causal SNP (with similar effect sizes and the same effect direction); however, they quickly lost power as k increased, i.e. more non-associated traits were included. Third, as k increased, an SPU( $\gamma$ ) test with a larger  $\gamma$  had higher power than those with smaller  $\gamma$ . In particular, we highlight the case with k=40: the power of the GEE-SPU(1) or GEE-SPU(2) test could be much lower than GEE-SPU(6) or  $SPU(\infty)$ ; for example for SNP 2 and r = 0.3, the SPU(1), SPU(2) and SPU(6) tests had power as 0.084, 0.432 and 0.680 respectively. We also note that GEE-SPU(6) and SPU( $\infty$ ) gave similar power, implying that using  $\gamma$  up to 6 or 8 (as done here) is good enough. Fourth,

we see that, for any given situation, one of the SPU tests had high power, 562 though its identity changed with the situation. Most importantly, the 563 aSPU test seemed to be able to remain (nearly) most powerful across 564 all situations. (See Table 4.)

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Between an SPU( $\gamma$ ) and SPUw( $\gamma$ ) tests for a fixed  $\gamma$ , the former one 566 was more powerful (not shown). As analyzed in the Methods section, 567 this was presumably due to the larger effect sizes of the associated traits, 568 giving lower weights to associated SNPs in an SPUw( $\gamma$ ) test than in an 569 SPU( $\gamma$ ). Accordingly, the aSPU test was also more powerful than the 570 aSPUw test.

Table 5 shows the results with weaker genetic effects. Now the GEE- 572 Score and related MANOVA and MultiPhen tests were more powerful 573 than the SPU/aSPU tests. Note the puzzling phenomenon: the former 574 tests could have lower power with all k = 5 associated traits than that 575 with some additional non-associated traits; this problem of MANOVA 576 was pointed out by Ferreira and Purcell (2009) and studied by Cole 577 et al. (1984). In addition, due to the smaller effect sizes of the associated 578 SNP, the SPU and SPUw tests, and thus aSPU and aSPUw tests, per- 579 formed similarly (not shown). 580

AR-1

Now we consider the case where the multivariate traits had an AR-1 589 correlation structure. Table 6 shows that all the tests could control the 583 Type I error rates around the nominal level of 0.05 satisfactorily.

For power (Table 7), regardless of the value of r, we reached the 585same conclusions. First, it is clear that the aSPU test was more powerful 586 than the MultiPhen, TATES, Score and UminP test. As more null traits 587 were added, power of all methods generally decreased and the aSPU 588 test still maintained its advantage. The power of MultiPhen was close 589

Empirical power when the multiple traits were correlated with an AR1 structure with correlation coefficient r; the non-zero  $\beta_i \sim U(0.2, 0.3)$ . An independence working correlation structure was used in GEE.

t7.4										GEE									
t7.5							MDMR					SPU(γ)							
t7.6	r	SNP	#traits	Average	MultiPhen	TATES	$L_1$	L <sub>2</sub>	MANOVA	Score	UminP	$\gamma = 1$	2	3	4	5	6	∞	aSPU
t7.7	0.5	1	5	0.661	0.458	0.554	0.629	0.634	0.459	0.458	0.522	0.651	0.630	0.624	0.594	0.582	0.564	0.525	0.624
t7.8			10	0.390	0.371	0.426	0.496	0.527	0.373	0.388	0.447	0.388	0.555	0.534	0.533	0.513	0.513	0.471	0.516
t7.9			20	0.217	0.262	0.332	0.362	0.365	0.263	0.286	0.334	0.214	0.414	0.390	0.427	0.397	0.402	0.343	0.400
t7.10	0.5	2	5	0.223	0.113	0.165	0.202	0.201	0.113	0.113	0.153	0.220	0.206	0.193	0.182	0.178	0.173	0.162	0.208
t7.11			10	0.124	0.107	0.122	0.131	0.129	0.107	0.100	0.112	0.124	0.150	0.137	0.139	0.127	0.129	0.114	0.139
t7.12			20	0.084	0.080	0.105	0.121	0.118	0.081	0.069	0.104	0.090	0.113	0.106	0.122	0.109	0.116	0.103	0.111
t7.13	0.3	1	5	0.780	0.547	0.571	0.698	0.706	0.571	0.546	0.551	0.774	0.706	0.709	0.647	0.637	0.602	0.551	0.737
t7.14			10	0.487	0.442	0.469	0.568	0.596	0.444	0.442	0.443	0.482	0.592	0.569	0.546	0.530	0.511	0.454	0.572
t7.15			20	0.274	0.309	0.366	0.448	0.490	0.312	0.307	0.349	0.277	0.478	0.456	0.467	0.438	0.434	0.368	0.459
t7.16	0.3	2	5	0.245	0.129	0.154	0.177	0.179	0.129	0.127	0.146	0.244	0.180	0.185	0.165	0.164	0.153	0.149	0.190
t7.17			10	0.147	0.120	0.129	0.157	0.156	0.121	0.119	0.122	0.146	0.161	0.146	0.143	0.139	0.136	0.122	0.156
t7.18			20	0.077	0.085	0.093	0.121	0.126	0.087	0.085	0.087	0.078	0.131	0.113	0.115	0.098	0.103	0.091	0.113

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**Table 8** Empirical Type I error rates (for  $\beta=0$ ) and power (for  $\beta\neq0$ ) for 26 traits with the true correlation matrix estimated from the ADNI data; for  $\beta\neq0$ , the first five traits were associated with a causal SNP with log-ORs  $\beta_i\sim U(0.8,1)$  or  $\sim U(0.2,0.3)$ , while all others had  $\beta_i=0$ . An independence working correlation structure was used in GEE.

t8.4							GEE									
t8.5									$SPU(\gamma)$							
t8.6	β	SNP	Average	MultiPhen	TATES	MANOVA	Score	UminP	$\gamma = 1$	2	3	4	5	6	00	aSPU
t8.7	$\beta = 0$	1	0.054	0.037	0.051	0.039	0.037	0.053	0.055	0.048	0.048	0.053	0.053	0.050	0.056	0.056
t8.8	$\beta_j \sim U(0.8,1)$	2	0.116	0.565	0.614	0.574	0.564	0.618	0.113	0.416	0.501	0.659	0.650	0.711	0.716	0.679
t8.9		3	0.064	0.126	0.143	0.132	0.125	0.147	0.060	0.098	0.123	0.162	0.172	0.183	0.220	0.176
t8.10	$\beta_j \sim U(0.2,03)$	1	0.071	0.619	0.302	0.629	0.617	0.317	0.068	0.115	0.151	0.205	0.235	0.272	0.339	0.270
t8.11		2	0.053	0.141	0.079	0.144	0.140	0.085	0.052	0.057	0.059	0.065	0.076	0.080	0.086	0.082

to that of the GEE-Score test, while that of TATES was close to that of the UminP test. For example, when testing the association between SNP 1 and k=5 traits (with no null traits), MultiPhen had a power of 0.458, TATES had 0.554, GEE-Score test had 0.458, UminP had 0.522, while the aSPU test had 0.624, close to 0.661, the highest power given by the Average method, essentially the same as that of SPU(1) test at 0.651. However, as the total number of traits increased to 20 (with 15 null traits), the power of the Averaging method dramatically reduced to 0.217, compared to 0.286 of the GEE-Score test and 0.334 of the UminP, all much lower than 0.400 of the aSPU test. The results also confirmed that if the SNP of interest was physically farther away from the causal SNP, the power any test would be largely reduced. For example, when testing SNP 1 based on 10 traits, the power of the Score test was 0.388 and the aSPU was 0.516; but when testing SNP 2, their power decreased to 0.100 and 0.139 respectively.

It is confirmed that the SPU and SPUw tests, and thus aSPU and aSPUw tests, were always almost equally powered, presumably due to the small effect sizes here (not shown). Given that the majority of common SNPs that are associated with common diseases and other complex traits have only small effect sizes, we conclude that it is unlikely that the aSPU and aSPUw tests would perform much differently in practice; we recommend the use of the aSPU test (after standardizing the correlated traits to the same scale if needed).

When the causal SNP had different effect directions on different traits, and/or when the correlations among the multiple traits were possibly negative, it was confirmed that the Average, SPU(1), SPUw(1) (and more generally, any SPU( $\gamma$ ) or SPUw( $\gamma$ ) test with  $\gamma$  as an odd number) would lose power; the better performance of the GEE-Score (and related tests) over that of aSPU, or vice versa, depended on the situations (not shown), as previously shown for the cases with a CS correlation structure.

#### A more realistic correlation matrix

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t8.3

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t.9.1

t9.2 t9.3 We also considered using a correlation matrix mimicking real data. Specifically, based on the ADNI data, we fitted a null model (with several covariates but no SNP) to a set of 26 neuroimaging traits and thus esti- 624 mated their correlation matrix. These traits appeared to be strongly 625 correlated with the first quartile, median and third quartile of pair- 626 wise correlations at 0.34, 0.47 and 0.59 respectively. We generated simulated data as before except fixing the number of the traits at 26 with 628 their true correlation matrix as the one estimated from the ADNI data. 629 As shown in Table 8, under the null hypothesis, it is clear that the 630 methods could control the Type I error rates satisfactorily (except the 631 GEE Wald test, which was omitted). For power, we randomly picked 632 up the first five traits to be associated with a causal SNP; we considered 633 both strong and weak effects from the causal SNP. The conclusions were 634 the same as before. For example, when the SNP-traits were strongly associated, the aSPU test was more powerful than the Score test. On the 636 other hand, if the causal SNP was weakly associated with the five traits, 637 given that the traits were strongly correlated as for the previous simulation case with a CS structure, the Score test appeared to be more power- 639 ful than the aSPU test. 640

Other cases with smaller sample sizes and association parameters

We considered whether the sample size would change our conclusions. We used a smaller sample size n=500 or n=200 while the multiple traits had a CS(0.3) correlation matrix. As shown in Table 9, we reached the same conclusions. For example, the aSPU test was more powerful than the Score test in these cases.

So far we have always assumed that the association directions be- 647 tween a causal SNP and multiple traits are in the same direction. Next 648 we considered the case where a subset of the traits were positively 649 while another subset were negatively, and weakly associated with the 650 causal SNP. We still used a CS(r) as the correlation matrix for the traits. 651 As shown in Table 10, as expected, the Average method and any  $SPU(\gamma)$  652 test with  $\gamma$  being an odd number were always low powered. Between 653 the Score and aSPU tests, if r=0.3, then the Score test was more powerful; however, if r=-0.3, then the aSPU test was more powerful. 655 Overall, either the Score test or the aSPU test was the winner.

**Table 9** Empirical power when the multiple traits were correlated with a CS(0.3) structure; the first five traits were associated with a causal SNP with log-ORs  $\beta_j \sim U(0.8,1)$ , while all others had  $\beta_j = 0$ . An independence working correlation structure was used in GEE.

t9.4								GEE									
t9.5										$SPU(\gamma)$							
t9.6	n	SNP	#trait	Average	MultiPhen	TATES	MANOVA	Score	UminP	$\gamma = 1$	2	3	4	5	6	00	aSPU
t9.7	500	2	5	0.610	0.369	0.534	0.370	0.366	0.509	0.604	0.598	0.580	0.563	0.557	0.542	0.505	0.577
t9.8			10	0.316	0.389	0.427	0.393	0.386	0.419	0.318	0.528	0.507	0.530	0.514	0.510	0.479	0.495
t9.9			20	0.126	0.273	0.338	0.281	0.269	0.328	0.127	0.386	0.373	0.451	0.446	0.463	0.439	0.405
t9.10			30	0.089	0.209	0.291	0.229	0.208	0.280	0.090	0.261	0.279	0.390	0.380	0.417	0.412	0.370
t9.11			40	0.071	0.188	0.256	0.203	0.186	0.250	0.067	0.191	0.207	0.318	0.299	0.356	0.361	0.333
t9.12	200	2	5	0.306	0.144	0.254	0.146	0.144	0.237	0.312	0.298	0.291	0.285	0.280	0.273	0.249	0.287
t9.13			10	0.160	0.151	0.197	0.163	0.149	0.182	0.155	0.235	0.230	0.247	0.237	0.243	0.225	0.229
t9.14			20	0.087	0.104	0.145	0.117	0.102	0.135	0.087	0.159	0.163	0.198	0.201	0.209	0.199	0.180
t9.15			30	0.066	0.070	0.122	0.089	0.068	0.116	0.066	0.104	0.121	0.155	0.158	0.168	0.163	0.146
t9.16			40	0.054	0.063	0.087	0.091	0.060	0.077	0.053	0.081	0.089	0.123	0.121	0.140	0.139	0.122

t10.1

t10.2

t10.3

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t11.1

t11.2 t11.3

**Table 10** Empirical power when the multiple traits were correlated with a CS(r) structure; the first five traits were associated with a causal SNP with log-ORs  $\beta_j \sim - (-1)^j U(0.2, 0.3)$ , while all others had  $\beta_i = 0$ . An independence working correlation structure was used in GEE.

							GEE											
									SPU(γ)									
1	r	SNP	#trait	Average	MultiPhen	TATES	Score	UminP	$\gamma = 1$	2	3	4	5	6	7	8	00	aSPU
9	SNP 1																	
(	0.3	1	5	0.084	0.926	0.671	0.928	0.626	0.085	0.817	0.442	0.754	0.558	0.712	0.595	0.685	0.631	0.739
			10	0.075	0.854	0.541	0.851	0.512	0.073	0.684	0.356	0.644	0.463	0.598	0.482	0.569	0.529	0.586
			20	0.058	0.713	0.397	0.718	0.392	0.058	0.503	0.237	0.511	0.327	0.477	0.366	0.452	0.416	0.420
		2	5	0.060	0.272	0.173	0.289	0.168	0.063	0.188	0.137	0.179	0.156	0.177	0.163	0.175	0.169	0.140
			10	0.062	0.230	0.120	0.227	0.126	0.062	0.143	0.111	0.145	0.128	0.146	0.133	0.141	0.137	0.115
			20 0.062	0.167	0.100	0.170	0.145	0.084	0.059	0.087	0.078	0.088	0.086	0.083	0.084	0.084	0.087	0.085
	-0.3	1	5	0.152	0.567	0.587	0.571	0.553	0.147	0.730	0.402	0.668	0.479	0.626	0.512	0.599	0.557	0.646
			10	0.115	0.466	0.461	0.490	0.488	0.118	0.640	0.356	0.606	0.435	0.566	0.464	0.552	0.502	0.565
			20	0.078	0.308	0.352	0.329	0.365	0.081	0.511	0.237	0.497	0.316	0.458	0.340	0.435	0.375	0.426
		2	5	0.075	0.117	0.137	0.144	0.165	0.073	0.212	0.135	0.186	0.150	0.168	0.148	0.165	0.159	0.163
			10	0.072	0.121	0.136	0.108	0.121	0.071	0.164	0.119	0.160	0.126	0.143	0.130	0.134	0.129	0.145
			20	0.057	0.091	0.118	0.080	0.076	0.055	0.113	0.069	0.096	0.072	0.092	0.071	0.085	0.074	0.087

Rare variants

As suggested by a reviewer, we considered rare variants with MAF fixed at 0.01 when simulating genotypes, while all other aspects were the same as before. To be consistent with our focus here on single SNP testing, we tested on each RV separately, though testing on multiple RVs was expected to be more powerful. As shown in Table 11, the results were pretty much the same as those for common variants when the causal SNP was strongly associated with five traits. For example, it was confirmed again that the results between the Average and GEE-SPU(1), between TATES and GEE-UminP, and among MultiPhen, MANOVA and GEE-Score tests were almost the same respectively. More importantly, the aSPU test was much more powerful than the previous tests, especially as the number of non-associated traits increased.

# Using other working correlation structures in GEE

It is confirmed that using a non-diagonal correlation structure in GEE may or may not improve the performance of the GEE-based tests. For example, when the true CS correlation structure was used as the working one, the performance of the SPU and aSPU tests improved (Table 12); on the other hand, if  $R_w = \text{CS}$  was used for the case with an AR-1 as the true correlation structure, the power of the SPU and aSPU tests could be lower than that of using  $R_w = I$  (Table 12). On the other hand, in the current context, as shown in the Methods section, the GEE-Score is invariant to the use of  $R_w$ . We also note that the UminP and  $\text{SPU}(\infty)$  (and  $\text{SPUw}(\infty)$ ) tests could have a severe loss of power with the use of a non-diagonal working correlation structure, even if the working correlation structure was the same as the true CS structure, as analyzed in the Methods section.

## Combining the **GEE Score and aSPU tests**

It has been shown that, depending on the correlation structure for 685 multiple traits and association parameters between SNPs and traits, 686 one of the GEE Score test and aSPU test was better than the other, but 687 neither could dominate the other across all situations. In light of this re-688 sult and that in practice it is unknown which test would be more pow-689 erful, it might be productive to combine the two tests. A simple strategy 690 is to take the minimum p-value of the two tests, yielding an aSPU.Sco 691 test with test statistic 692

$$T_{aSPU,Sco} = \min \bigg\{ \min_{\gamma \in \Gamma} P_{SPU(\gamma)}, P_{Sco} \bigg\},$$

where  $P_{Sco}$  is the p-value of the Score test (and  $P_{SPU(\gamma)}$  is the p-value of 694 the SPU( $\gamma$ ) test). To calculate the p-value of the aSPU.Sco test, we do not need another level of resampling; we simply include the Score test 695 along with the SPU tests in the simulation algorithm discussed earlier 696 for the aSPU test.

Table 13 shows the results for the multiple traits with a CS(0.3) correlation matrix. First, it is clear that the new test could maintain a satisfactory Type I error rate. Second, the performance of the new test was
always between the other two tests, often closer to the winner. For ex701
ample, in the case of a causal SNP weakly associated with 5 traits: i) 702
when testing on the five associated traits, the Score test was less
power than the aSPU test with their power as 0.464 and 0.632 respectively, while the power of the new test was 0.612, very close to the
aSPU test; ii) on the other hand, when testing on 10 traits, the power
of the Score test was 0.569, larger than 0.456 of the aSPU test, and the
new test achieved the power of 0.537, again close to the winner.

**Table 11** Empirical Type I error rates (for  $\beta = 0$ ) and power (for  $\beta \neq 0$ ) when the multiple traits were correlated with a CS(0.3) structure; for  $\beta \neq 0$ , the first five traits were associated with a causal RV with log-ORs  $\beta_j \sim U(7.5, 8)$ , while all others had  $\beta_j = 0$ . All the RVs had MAF = 0.01. An independence working correlation structure was used in GEE.

t11.4								GEE											
t11.5								SPU(γ)											
t11.6	β	SNP	#traits	Average	MultiPhen	TATES	MANOVA	Score	UminP	$\gamma = 1$	2	3	4	5	6	7	8	∞	aSPU
t11.7	$\beta = 0$	1	5	0.060	0.052	0.056	0.052	0.052	0.055	0.062	0.052	0.055	0.050	0.050	0.050	0.055	0.057	0.057	0.052
t11.8			10	0.049	0.055	0.047	0.056	0.055	0.042	0.049	0.050	0.051	0.049	0.047	0.048	0.047	0.049	0.043	0.043
t11.9			20	0.040	0.042	0.041	0.042	0.041	0.045	0.042	0.037	0.037	0.040	0.041	0.044	0.046	0.046	0.041	0.042
t11.10			30	0.047	0.048	0.051	0.049	0.047	0.051	0.049	0.054	0.055	0.054	0.059	0.058	0.057	0.056	0.057	0.057
t11.11			40	0.033	0.049	0.045	0.052	0.049	0.048	0.037	0.037	0.037	0.037	0.036	0.040	0.044	0.044	0.048	0.039
t11.12	$\beta \neq 0$	1	5	0.702	0.587	0.677	0.587	0.587	0.679	0.696	0.697	0.698	0.693	0.688	0.684	0.681	0.680	0.674	0.691
t11.13			10	0.596	0.551	0.634	0.552	0.550	0.624	0.594	0.688	0.684	0.698	0.694	0.695	0.690	0.689	0.680	0.679
t11.14			20	0.421	0.513	0.613	0.516	0.513	0.609	0.426	0.678	0.667	0.696	0.692	0.695	0.695	0.696	0.690	0.672
t11.15			30	0.263	0.463	0.579	0.465	0.461	0.575	0.265	0.657	0.649	0.685	0.674	0.692	0.689	0.693	0.680	0.667
t11.16			40	0.163	0.403	0.546	0.409	0.401	0.539	0.160	0.599	0.602	0.669	0.663	0.679	0.679	0.682	0.677	0.648

Table 12
GEE methods with various true and working correlation matrices for non-zero  $\beta_i \sim U(0.2, 0.3)$ .

t12.3	Correlation						SPU(γ)								
t12.4	True	$R_w$	r	SNP	#traits	Score	UminP	$\gamma = 1$	2	3	4	5	6	∞	aSPU
t12.5	CS	CS	0.3	1	5	0.468	0.155	0.662	0.163	0.278	0.164	0.202	0.159	0.152	0.565
t12.6					10	0.594	0.374	0.294	0.595	0.385	0.513	0.375	0.447	0.375	0.536
t12.7					20	0.535	0.352	0.116	0.603	0.394	0.544	0.387	0.476	0.365	0.521
t12.8					30	0.456	0.362	0.084	0.530	0.416	0.512	0.412	0.466	0.374	0.487
t12.9				2	5	0.108	0.065	0.227	0.059	0.101	0.067	0.070	0.068	0.062	0.162
t12.10					10	0.133	0.108	0.102	0.144	0.102	0.138	0.102	0.127	0.113	0.135
t12.11					20	0.131	0.103	0.067	0.155	0.105	0.133	0.097	0.114	0.099	0.112
t12.12					30	0.129	0.123	0.060	0.138	0.109	0.144	0.119	0.133	0.122	0.120
t12.13	AR1	CS	0.5	1	5	0.458	0.158	0.661	0.121	0.293	0.143	0.188	0.146	0.173	0.559
t12.14					10	0.371	0.296	0.345	0.422	0.363	0.369	0.316	0.345	0.307	0.442
t12.15					20	0.261	0.264	0.196	0.337	0.337	0.337	0.317	0.321	0.293	0.368
t12.16					5	0.113	0.062	0.221	0.056	0.096	0.056	0.076	0.060	0.070	0.163
t12.17					10	0.107	0.102	0.116	0.109	0.094	0.107	0.092	0.103	0.096	0.123
t12.18					20	0.080	0.094	0.065	0.124	0.113	0.115	0.099	0.106	0.100	0.121
t12.19	AR1	CS	0.3	1	5	0.546	0.248	0.778	0.297	0.458	0.276	0.338	0.261	0.251	0.699
t12.20					10	0.442	0.323	0.486	0.468	0.482	0.424	0.402	0.387	0.325	0.549
t12.21					20	0.307	0.291	0.273	0.423	0.424	0.399	0.374	0.361	0.312	0.445
t12.22				2	5	0.127	0.081	0.242	0.073	0.123	0.080	0.097	0.081	0.084	0.163
t12.23					10	0.119	0.118	0.147	0.133	0.129	0.130	0.122	0.119	0.108	0.146
t12.24					20	0.085	0.084	0.080	0.126	0.111	0.116	0.095	0.103	0.088	0.125

#### ADNI data

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t13.1

We applied the methods to the ADNI cohort at baseline, which consisted of 680 non-Hispanic Caucasians with both genotype and phenotype data, including 192 healthy controls, 327 subjects with mild cognitive impairment and 161 patients with Alzheimer's disease. We would like to use a few structural MRI-derived multiple traits as intermediate phenotypes to assess their association with genetic variation. We downloaded from the ADNI website 56 cross-sectional FreeSurfer traits related to volumetric and cortical thickness measures at the baseline as processed by the UCSF team (Hartig et al., 2012). For illustration, we only tested 20 SNPs shown by Shen et al. (2010) to be marginally significantly associated with one or more of the FreeSurfer traits. Here we considered only 7 multivariate traits consisting of a varying number of univariate traits as shown in Table 14, which were singled out by Shen et al. (2010) to be more significantly associated with some of the 20 SNPs. The 7 multivariate traits included each of the six multivariate traits in Table 14 at the right side of the brain plus one of them (MeanPar) at the left side of the brain too. The covariates included were sex, handedness, brain volume, education (in years), and age. There were in total 680 subjects.

We first used B=10,000 for any simulation-based method (i.e. GEE-UminP, GEE-SPU and GEE-aSPU tests) to calculate p-values. Then for those SNPs with p-value < 5/B, we gradually increased B to  $10^5$ , then to  $10^6$ , and finally up to  $10^7$  if needed. Other tests used asymptotics to calculate their p-values.

We present the heat maps of  $-\log_{10}$  (p-values) of the new methods in Fig. 1; as a comparison, the results from four existing methods are shown in Fig. 2. In agreement with our theoretical analysis and simulation study, it is confirmed that i) the GEE-Score test, MANOVA and MultiPhen, ii) the GEE-UminP test and TATES, and iii) the GEE-SPU(1)

test and the Average method, yielded similar results. For this dataset, 739 it turns out that the GEE-SPU(2), GEE-aSPU and GEE-aSPUw tests also 740 gave p-values similar to each other, and to those of GEE-SPU(1). Howev- 741 er, the three groups i)-iii) of the tests did give quite different results. 742 Below, taking the GEE-Score, GEE-UminP and GEE-SPU(1) as a repre- 743 sentative for each group, we show their identified marginally signifi- 744 cant SNPs at p-values  $< 10^{-6}$  and  $< 10^{-5}$  respectively. i) The GEE- 745Score test identified an association between rs429358 (in gene ApoE) 746 and RMeanPar (MeanPar at the right side of the brain) with a p-value 747 of  $8.45 \times 10^{-7}$ ; it also gave a p-value of  $8.13 \times 10^{-6}$  for rs7526034 748 and RMeanLatTemp. ii) the GEE-UminP test detected rs7526034 749 marginally associated with RMeanLatTemp and RMeanTemp with p- 750 values of  $3.10 \times 10^{-6}$  and  $7.90 \times 10^{-6}$  respectively; note that neither 751 is significant at the level of p-value  $< 10^{-6}$ . iii) the GEE-SPU(1) test iden- 752 tified rs7526034 to be associated with three traits, RMeanTemp, 753 RMeanLatTemp and RMeanMedTemp, with p-values of  $2.00 \times 10^{-7}$ , 754  $6.00 \times 10^{-7}$  and  $9.00 \times 10^{-7}$  respectively, in addition to a marginal association between rs12839763 and RMeanMedTemp with a p-value of 756  $2.00 \times 10^{-6}$ . As a comparison, the GEE-aSPU test gave results similar 757 to the GEE-SPU(1) test: for the above 4 associations indicated by the 758 SPU(1) test, the aSPU test gave p-values of  $6.00 \times 10^{-7}$ ,  $9.00 \times 10^{-7}$ , 759  $1.80 \times 10^{-6}$ , and  $4.20 \times 10^{-6}$  respectively; in addition, it also gave a 760 p-value of  $9.00 \times 10^{-6}$  to rs2075650 and LMeanPar. In summary, it 761 appears that the three groups of the tests could identify different sets 762 of (marginally) significant associations, though TATES and GEE-UminP 763 did not identify any association with p-value  $< 10^{-6}$ , illustrating a pos- 764 sible loss of power in taking out only most significant univariate 765 associations.

As in the simulation study, the p-values obtained from the Average 767 method and SPU(1) were very close. However, because the former 768 was based on the asymptotic Wald test while the latter was a Score 769

**Table 13** Empirical Type I error rates (for  $\beta = 0$ ) and power (for  $\beta \neq 0$ ) for the multiple traits with a CS(0.3) correlation matrix; for  $\beta \neq 0$ , the first five traits were associated with a causal SNP with log-ORs  $\beta_j \sim U(0.8, 1)$  or  $\sim U(0.2, 0.3)$ , while all others had  $\beta_j = 0$ . An independence working correlation structure was used in GEE.

t13.4		$\beta = 0$			$\beta_j \sim U(0.2,0)$	.3)		$\beta_j \sim U(0.1,1)$		
t13.5	#traits	Score	aSPU	aSPU.Sco	Score	aSPU	aSPU.Sco	Score	aSPU	aSPU.Sco
t13.6	5	0.051	0.050	0.051	0.468	0.632	0.612	0.682	0.865	0.832
t13.7	10	0.060	0.051	0.059	0.573	0.456	0.537	0.684	0.795	0.777
t13.8	20	0.060	0.047	0.048	0.535	0.305	0.463	0.611	0.757	0.741
t13.9	30	0.032	0.049	0.042	0.456	0.257	0.394	0.528	0.703	0.693
t13.10	40	0.054	0.054	0.057	0.409	0.211	0.321	0.424	0.639	0.628

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**Table 14**Multivariate traits. A letter "L" or "R" is to be added to each trait's ID to indicate the left or right side of the brain.

t14.3	Trait ID	Trait description
t14.4	MeanCing	Mean thickness of caudal anterior cingulate, isthmus cingulate, posterior cingulate, and rostral anterior cingulate
t14.5	MeanFront	Mean thickness of caudal midfrontal, rostral midfrontal, superior frontal, lateral orbitofrontal, and medial orbitofrontal gyri and frontal pole
t14.6	MeanLatTemp	Mean thickness of inferior temporal, middle temporal and superior temporal gyri
t14.7	MeanMedTemp	Mean thickness of fusiform, parahippocampal, and lingual gyri, temporal pole and transverse temporal pole
t14.8	MeanPar	Mean thickness of inferior and superior parietal gyri, supramarginal gyrus, and precuneus
t14.9	MeanTemp	Mean thickness of inferior temporal, middle temporal, superior temporal, fusiform, parahippocampal and lingual gyri, temporal pole and transverse temporal pole

test based on simulations, their p-values might be slightly different. For example, for association between rs2075650 and LMeanPar, the Average method gave a p-value of  $9.94 \times 10^{-6}$ , which was essentially the same as  $1.10 \times 10^{-5}$  by the GEE-SPU(1) test.

The similar results between the Average method (or SPU(1)) and SPU(2) or aSPU test were presumably due to the relatively small numbers of univariate traits consisting of the seven multivariate traits. To investigate the robustness of the tests to a larger number of traits, we pooled all seven multivariate traits together to form a combined trait; after removing duplicated ones, a total of 26 univariate traits remained. Since all the methods indicated marginal associations between the rs7526034 and/or rs429358 and several traits, we focused on the two SNPs. As shown in Table 15, in agreement with earlier analyses of the seven individual multivariate traits, i) for SNP rs429358, the GEE-Score test and MultiPhen gave the most significant p-values; ii) for SNP rs7526034, the GEE-SPU(2) and aSPU tests yielded most significant results, followed by those given by TATES and GEE-UminP. However, the Average method and GEE-SPU(1) gave much less significant results, suggesting their non-robustness to a large number of non-associated traits as confirmed in the simulation study. In summary, it seems that the GEE-Score test (or equivalently MultiPhen) and the GEE-aSPU test could give complementary and useful results.

To demonstrate the feasibility of the new tests for GWAS, we conducted a genome-wide scan with a set of 31 FreeSurfer traits. Since the results did not offer additional new insights, to save space, we report the results in Supplementary materials.

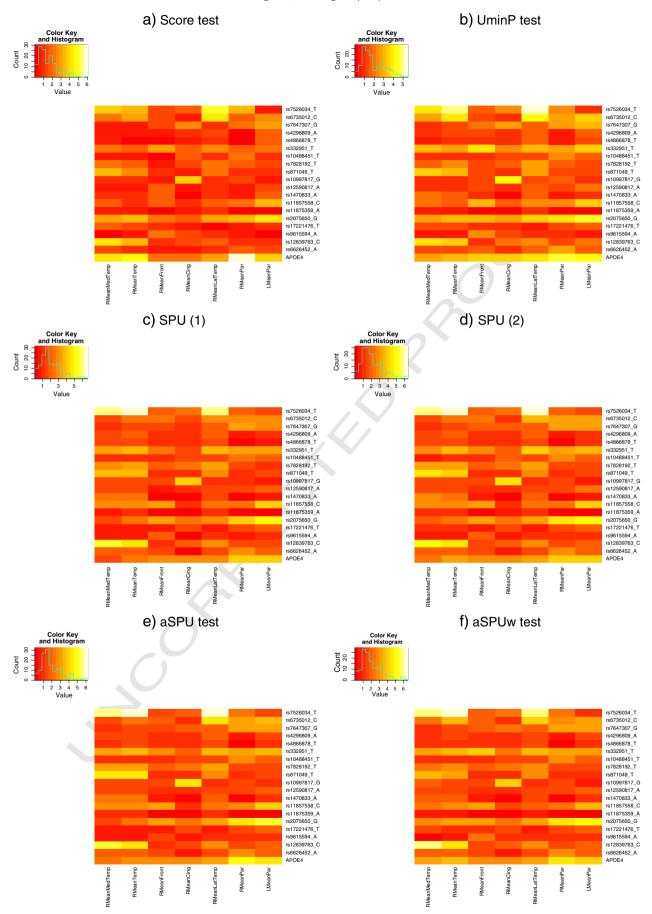
#### Discussion

In this paper we have developed a class of the so-called SPU tests for association analysis of multiple (correlated) traits and a single SNP. We have also proposed an adaptive test called the aSPU test to estimate and thus select the most powerful SPU test for a given dataset. For multivariate trait-single SNP analysis, based on a marginal regression model in GEE that allows the SNP to have different effect sizes and effect directions on different traits, the aSPU test can adapt to the existence and the number of the null (non-associated) traits effectively. With a larger power parameter  $\gamma$ , the SPU( $\gamma$ ) test reduces the influence of null traits and reinforces the associated ones. Thus this test can maintain high power in the presence of a large number of null traits. This property is especially useful for studies where many correlated phenotypes are collected but there are no established guidelines to selecting relevant phenotypes. On the other hand, in the presence of many associated traits, the SPU( $\gamma$ ) test with a smaller  $\gamma$  will be more powerful. In particular, SPU(1) is quite similar to the Average (or Sum) method as used in Shen et al. (2012), while SPU(2) is an extension of the SSU test for single trait-multilocus association analysis to multivariate trait-single locus analysis. As noted, under suitable conditions the SPU(2) test is the same as MDMR or KMR. We have also pointed out how some existing methods, like CCA/MANOVA, TATES and MultiPhen are related to the various GEE-based tests. We emphasize that, many of the existing methods, such as CCA/MANOVA and MultiPhen, may not be applicable to discrete traits or multiple loci, while our proposed GEE-Score and GEE-aSPU tests can with their general modeling and inference framework of GEE. Our proposed tests are potentially useful for a large number of traits, as arising as intermediate phenotypes in neuroimaging studies, which has not been adequately considered in the genetics liter- 824 ature. We also note that our proposed GEE-aSPU test can be equally applied to multiple principal components after PCA or PCH dimension 826 reduction on a large number of traits, though further studies are needed. 827

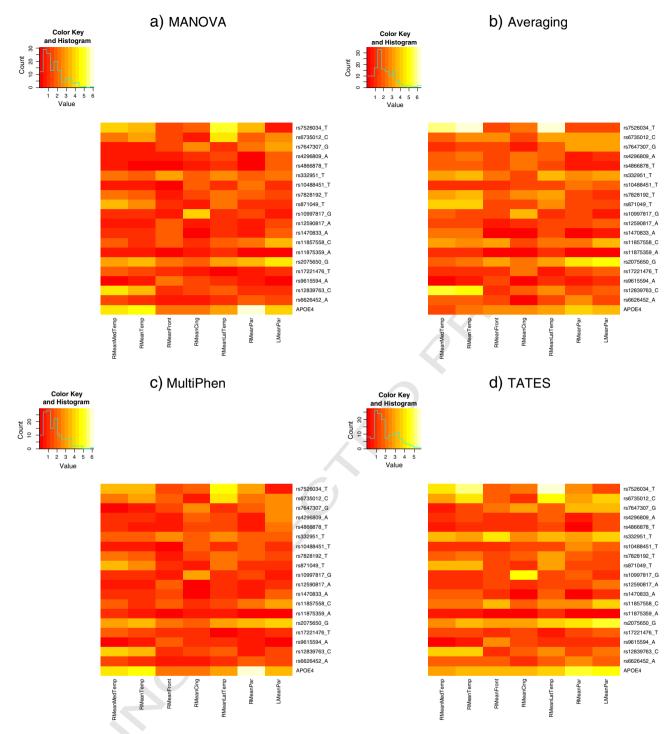
From simulation studies we observed that the relative performance 828 of the GEE-based Score and aSPU tests varied with the degree of the correlations among the traits and with the effect sizes of the causal SNPs. 830 When the traits were somewhat more weakly correlated (e.g. with an 831 AR-1 correlation structure), regardless of the effects size of the causal 832 SNP, the aSPU test was much more powerful than the Score test and 833 UminP test. However, under some situations, e.g. when the traits had 834 a compound symmetry correlation structure, the aSPU test might not 835 be as powerful as the Score test when the effect sizes were small; the 836 opposite conclusion held with larger effect sizes. We note that, the 837 aSPU test largely combines the strengths of the SPU(1) (equivalently 838 the Average method), SPU(2) (closely related to MDMR and KMR), 839 and SPU(∞) (similar to UminP and TATES), but differing from the 840 Score test and MultiPhen while the latter two (and CCA/MANOVA) per-841 form similarly. Since currently we do not have a simple guideline on 842 how to choose between the aSPU and Score tests in practice, we recom- 843 mend the use of both; we have also explored combining the two tests 844 with some promising preliminary results (see Table 13), though more 845 studies are needed.

We have focused on multitrait association testing on a single SNP. A 847 natural extension is to multitrait-multiple SNP testing. For univariate 848 trait analysis, it has been established that testing on multiple SNPs si- 849 multaneously may gain power (Pan, 2009), especially for RVs as evi- 850 denced by the increasing use of the burden tests and variance 851 component tests (Basu and Pan, 2011). Pan et al. (2014) have proposed 852 and studied an analogous aSPU test for RVs, which data-adaptively 853 over-weights (unknown and estimated) associated RVs (while down- 854 weighting non-associated RVs). In contrast, here our proposed aSPU 855 test adaptively over-weights (unknown and estimated) associated 856 traits (while down-weighting non-associated traits). It would be inter-857 esting to see whether combining the two ideas would work for 858 multitrait-multiple SNP association testing, especially in the presence 859 of large numbers of traits and of SNPs. An advantage of the aSPU test 860 is its weighting on, rather than directly selecting, traits (or SNPs), in 861 order to alleviate the effects of non-associated traits (or SNPs) on 862 diminishing the power of a test, expected to be present with many traits 863 (or SNPs); given small effect sizes of common variants (or small MAFs of 864 RVs), weighting tends to outperform selection.

It seems to be a common belief that accounting for correlations among multiple traits would automatically increase power, which however may not be true, or at least not as simple as it may sound. Here are seem arguments. First, using a non-independent working correlation massions among multiple traits; however, as shown in Tables 1 and 12, in these situations a test may or may not have improved power. In particular, the GEE Score test is invariant to the use of the working correlation matrix (with an equal cluster size). Second, as directly shown numerially here (e.g. Table 9), the GEE-SPU(2) test could be more powerful stand the GEE Score test, though the SPU(2) test statistic ignores the correlations among the components of the score vector (due to the correlations among the traits) while the Score test statistic does not. The same sphenomenon is also observed in single trait-multiple SNP analysis (Pan, s79).



**Fig. 1.** The heatmaps of  $-\log_{10}$  (p-values) of the GEE-based tests for seven multivariate traits.



**Fig. 2.** The heatmaps of  $-\log_{10}$  (p-values) of the four existing tests for seven multivariate traits.

2009), in which the SSU test (or equivalently KMR) is known to be often, but not always, more powerful than the Score test. Pan (2009) offers an explanation based on a test's rejection region, which however is hard to visualize for high-dimensional testing while the power also depends on

some unknown association parameters. Certainly this is a topic worth  $\,884$  further investigation.  $\,885$ 

Finally, we have not compared our methods with those based on 886 constructing latent composite traits such as PCA and PCH; a particularly 887

**Table 15** P-values of testing on a pooled set of 26 univariate traits.

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t15.3						GEE						
t15.4	SNPs	Average	MultiPhen	TATES	UminP	Score	SPU(1)	SPU(2)	aSPU			
t15.5 t15.6	rs7526034 rs429358	1.40e-04 1.42e-04	5.82e-04 1.68e-05	1.72e-05 1.23e-04	2.10e-05 1.50e-04	5.86e-04 2.32e-05	7.30e-05 1.10e-04	7.00e-06 7.00e-05	7.00e-06 1.60e-04			

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interesting topic is to investigate how our proposed tests compare with the modified PCH method of Lin et al. (2012) for high-dimensional neuroimaging traits.

#### Q13 Uncited references

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892 Tang and Ferreira, 2012 893 Wu et al., 2011

#### Acknowledgment

This research was supported by NIH grants R01HL65462, R01HL 105397, R01HL116720 and R01GM081535. The authors are grateful to the three reviewers for many helpful and constructive comments.

Data collection and sharing for this project was funded by the Alzheimer's Disease Neuroimaging Initiative (ADNI) (National Institutes of Health Grant U01 AG024904) and DOD ADNI (Department of Defense award number W81XWH-12-2-0012). ADNI is funded by the National Institute on Aging, the National Institute of Biomedical Imaging and Bioengineering, and through generous contributions from the following: Alzheimer's Association; Alzheimer's Drug Discovery Foundation; BioClinica, Inc.; Biogen Idec Inc.; Bristol-Myers Squibb Company; Eisai Inc.; Elan Pharmaceuticals, Inc.; Eli Lilly and Company; F. Hoffmann-La Roche Ltd and its affiliated company Genentech, Inc.; GE Healthcare; Innogenetics, N.V.; IXICO Ltd.; Janssen Alzheimer Immunotherapy Research & Development, LLC.; Johnson & Johnson Pharmaceutical Research & Development LLC.; Medpace, Inc.; Merck & Co., Inc.; Meso Scale Diagnostics, LLC.; NeuroRx Research; Novartis Pharmaceuticals Corporation; Pfizer Inc.; Piramal Imaging; Servier; Synarc Inc.; and Takeda Pharmaceutical Company. The Canadian Institutes of Health Research is providing funds to support ADNI clinical sites in Canada. Private sector contributions are facilitated by the Foundation for the National Institutes of Health (www.fnih.org). The grantee organization is the Northern California Institute for Research and Education, and the study is coordinated by the Alzheimer's Disease Cooperative Study at the University of California, San Diego. ADNI data are disseminated by the Laboratory for Neuro Imaging at the University of California, Los Angeles. This research was also supported by NIH grants P30 AG010129 and K01 AG030514.

# Appendix A. Relationships between the new and existing tests

924 Appendix A.1. The Average (or Sum) test and the GEE-SPU(1) test

A simple dimension reduction method is to take the average (or sum) of the multiple traits and use it as a single trait to assess its association with a single SNP; we call the corresponding method as the Average or Sum method (Shen et al., 2011; van der Sluis et al., 2013). It is easy to see that the score vectors of the two methods in linear regression (or any GLM with a canonical link) are equivalent to each other (up to a constant) as

$$U_A = \sum_i x_i \sum_i Y_{ij},$$

which is equal to the SPU(1) test statistic under  $R_w = I$  in GEE. Hence, the Score test version of the Average or Sum test and GEE-SPU(1) tests (under  $R_w = I$ ) are exactly the same. We implemented the Average test as a Wald test and used its asymptotic distribution to calculate its p-values while we used simulations to calculated the p-values for GEE-SPU(1), which led to some minor differences in their results.

Appendix A.2. TATES, GEE-UminP, GEE-SPUw( $\infty$ ) and GEE-SPU( $\infty$ ) tests

It is easy to verify that the GEE-UminP and GEE-SPUw( $\infty$ ) tests are exactly the same. It is noted that, under the working independence

model, the GEE score vector and its covariance estimate are exactly 941 the same as that for univariate analyses on each of the multiple traits 942 separately. Hence, the GEE-UminP and GEE-SPUw( $\infty$ ) tests are also 943 closely related to univariate analysis-based TATES (van der Sluis et al., 944 2013), but differ in two aspects: first, TATES uses Simes procedure for 945 multiple testing adjustment, while the former two use an "exact" meth- 946 od for such a purpose; second, TATES uses a correlation matrix input by 947 the user to estimate the null distribution of the test statistic, hence is 948 computationally simpler but may be less accurate.

Appendix A.3. CCA, MANOVA and the GEE-Score test

To test for association between multiple traits and a single SNP 951 (without any other covariates), CCA and MANOVA are equivalent 952 (Ferreira and Purcell, 2009; Yang and Wang, 2012). They are based on 953 the largest eigen-value  $\rho^2$  of 954

$$B = S_{XX}^{-1/2} S_{XY} S_{YY}^{-1} S_{YX} S_{XX}^{-1/2},$$

where  $S_{XX} = \widehat{\text{Cov}}(x_i), S_{XY} = \widehat{\text{Cov}}(x_i, Y_i)$  and  $S_{YY} = \widehat{\text{Cov}}(Y_i)$  are sample 956 variance–covariance matrices. In the current context with a single SNP  $x_i$ , since B is a scalar, we have  $\rho^2 = B$ .

With a working independence model  $R_{\rm w}=I$ , the GEE-Score test sta-  $_{958}$  tistic is

$$T_{Sco} = \left(\sum_{i} x_{i} (Y_{i} - \overline{Y})\right)' \left(\sum_{i} x_{i} S_{YY} x_{i}\right)^{-1} \left(\sum_{i} x_{i} (Y_{i} - \overline{Y})\right)$$
$$= nS_{XY} (S_{XX} S_{YY})^{-1} S_{YX} = nB,$$

in which the second equality holds because  $S_{XX}$  is a scalar. Furthermore, 961 as shown earlier, the GEE-Score test is invariant to  $R_w$  in the current context. Hence CCA and MANOVA are equivalent to the GEE-Score test, regardless of the working correlation matrix  $R_w$  being used in GEE. 963

Appendix A.4. MDMR, MANOVA and the GEE-SPU(2) test

MDMR is a nonparametric method as a generalization of Fisher's 965 MANOVA (McArdle and Anderson, 2001); it has been applied to detect 966 association between a single trait and multiple SNPs, named genomic 967 distance-based regression (GDBR) (Wessel and Schork 2006). Schork Q15 and colleagues have outlined its application to analysis of longitudinal 969 or multivariate traits (Zapala and Schork, 2012). We briefly summarize 970 its main steps as the following:

Step 1. Calculate an  $n \times n$  distance matrix for all pairs of subjects 972 by  $D = (D_{ij})$  with  $D_{ij} = d(Y_i, Y_j)$  and d(,) being a distance or semi- 973 distance metric. 974 Step 2. Calculate  $A = (-D_{ij}^2/2)$ . 975

Step 3. Obtain a *centered* similarity matrix G = (I - 11'/n)A(I - 11'/n), 976

Step 3. Obtain a centered similarity matrix  $G = (I - 11^n/n)A(I - 11^n/n)$ , 97 where 1 is an  $n \times 1$  vector of all 1's; 97

Step 4. Denote *X* as the  $n \times 1$  vector of centered genotype scores with 978 elements  $x_i$  (and  $\sum_{i=1}^{n} x_i = 0$ ).

Step 5. Calculate the projection matrix  $H = X(X'X)^{-1}X'$ ; 980 Step 6. Calculate a pseudo F-statistic as 981

$$F = \frac{tr(HGH)}{tr[(I-H)G(I-H)]},$$
(8)

where tr(A) is the trace of matrix A.

To obtain a p-value, we recourse to permutations by shuffling *X* (or, equivalently, shuffling both the rows and columns of *A* simultaneously). 984

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As discussed by McArdle and Anderson (2001), if G is an outer product matrix, say G = ZZ' with an  $n \times k$  matrix Z, the above F-test is simply testing  $H_0$ : B = 0 in a multivariate linear model

$$Z = 1\mu + XB + \epsilon, \tag{9}$$

where 1 is an  $n \times 1$  vector of all 1's,  $\mu$  is a  $1 \times p$  vector of unknown in-989 tercepts, B is a  $1 \times p$  vector of unknown regression coefficients, and  $\epsilon$ is an  $n \times p$  matrix of random errors. Following the same argument in 990 Pan (2011), it can be shown that 991

$$F \propto tr(Z'XX'Z) = tr((Z - \overline{Z})'XX'(Z - \overline{Z})), \tag{10}$$

which is the same as the GEE-SPU(2) test statistic for the multivariate linear model (9) under the working independence model. In particular, if the Euclidean distance (i.e.  $L_2$ -norm) is used as the distance metric d(,), we have Z = Y; thus, MDMR( $L_2$ ), the MDMR implementation with the Euclidean distance, is the same as the GEE-SPU(2) test. Importantly, as to be shown, GEE-SPU(2) loses power in the presence of many null traits, so does MDMR.

Furthermore, MANOVA is based on the same model (9) with Z = Y; however, the (approximate) F statistics in MANOVA are different from Eq. (8). For example, the Wilks statistic is based on

$$\Lambda = \frac{|(I{-}H)G(I{-}H)|}{|(I{-}H)G(I{-}H) + HGH|},$$

1003 with |B| as the determinant of B. For this reason, MANOVA and  $MDMR(L_2)$  will not be the same.

Appendix A.5. KMR and the GEE-SPU(2) test 1004

KMR has been extended to multivariate quantitative traits (Maity et al., 2012; Schifano et al., 2012; Wang et al., 2013). In the current setting, its test statistic is

$$T_{KMR} = (Y - \overline{Y})' V_0^{-1} K V_0^{-1} (Y - \overline{Y}),$$

where  $V_0 = \text{Var}(Y|H_0)$  and K is a kernel function. With a single SNP, it suffices to use a linear kernel with K = XX', thus  $T_{KMR}$  is the same as the GEE-SPU(2) test statistic if the working correlation  $R_w$  is the true correlation structure of  $Y_i$  (i.e.  $R_w = \text{Corr}(Y_i|H_0)$ ). 1011

Since the extended KMR method is based on a mixed-effects model, it is not surprising to see that it requires specifying the correct correlation structure; in contrast, our proposed GEE-SPU(2) and other SPU tests only need a working, not necessarily correct, correlation structure  $R_w$ , maintaining the main advantage of the GEE methodology (while possessing its disadvantage of possible efficiency loss). Furthermore, it is not clear how to extend KMR to multiple discrete (e.g. binary) traits, while our GEE-SPU tests can be easily extended to other types of traits (as long as they can be modeled by GLMs). More importantly, as to be shown, GEE-SPU(2) loses power in the presence of many null traits, suggesting the same drawback of KMR.

Appendix A.6. MultiPhen and the GEE-Score test

MultiPhen (O'Reilly et al., 2012) is based on fitting a proportional odds model (POM). For simplicity, here we assume that  $x_i$ 's are not centered or transformed; otherwise, we just need to modify some notation accordingly. Define  $\pi_j(y) = Pr(x_i = j | Y_i = y)$ , and  $\kappa_j(y) = \sum_{m=0}^{j} \pi_m(y)$ for j = 0, 1 and 2. The POM is

$$\log \frac{\kappa_j(y)}{1 - \kappa_i(y)} = \alpha_j - y'\beta, \tag{11}$$

neuroimaging data, NeuroImage (2014), http://dx.doi.org/10.1016/j.neuroimage.2014.03.061

for j = 0 and 1. To test  $H_0$ :  $\beta = (\beta_1, ..., \beta_k)' = 0$ , MultiPhen applies a likelihood ratio test. We can equally apply an asymptotically equivalent Score test, Following McCullagh (1980), after some algebra, we derive 1031 the negative score vector for the POM as

$$U_{POM} = \frac{-n_1 - n_2}{n} \sum_{i: \mathbf{x} = 0} Y_i + \frac{n_0 - n_2}{n} \sum_{i: \mathbf{x} = 1} Y_i + \frac{n_0 + n_1}{n} \sum_{i: \mathbf{x} = 2} Y_i, \tag{12}$$

where  $n_i = \sum_{i=1}^n I(x_i = i)$  for i = 0, 1 and 2. In contrast, the Score vector for the GEE working independence model (4) can be written as

$$U_{GEE} = \frac{-n_1 - 2n_2}{n} \sum_{i:x_i = 0} Y_i + \frac{n_0 - n_2}{n} \sum_{i:x_i = 1} Y_i + \frac{2n_0 + n_1}{n} \sum_{i:x_i = 2} Y_i.$$
 (13)

Comparing the two score vectors  $U_{POM}$  and  $U_{GEE}$ , we see that they only 1036 differ in their weights on  $Y_i$ 's for  $x_i = 0$  and  $x_i = 2$ . Hence, we would expect that MultiPhen and GEE-Score test give similar results unless the 1037 MAF of  $x_i$  is extreme. The similarity of *empirical* performance between 1038 MultiPhen and MANOVA was observed by other authors (e.g. van der 1039 Sluis et al., 2013), which is shown theoretically here, based on our earlier 1040 result on the equivalence between MANOVA and the GEE-Score test.

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Appendix A.7. Generalized Kendall's tau and the GEE-Score test

Zhang et al. (2010) proposed a nonparametric method to test asso- 1043 ciation between multiple traits and a single SNP. The test statistic is a 1044 U-statistic as a generalized Kendall's tau (denoted as  $GK\tau$ ). Specifically, 1045 define  $u_{ij} = (f(Y_{i1} - Y_{j1}), ..., f(Y_{iq} - Y_{jq}))'$ , where f() is an identity function for quantitative traits or binary traits, or a sign function for ordinal 1047 traits; in the former case, we have  $u_{ij} = Y_i - Y_j$ . Define  $\overline{u}_i = \sum_{i=1}^n u_{ij}/n$ . 1048 Then the *GKT* statistic, after ignoring a constant factor, 2/(n-1), is  $\tau=1049$  $\sum_{i=1}^{n} x_i \overline{u}_i$ , which is asymptotically distributed as  $N(0, V_0)$  under  $H_0$ . The 1050 corresponding GK $\tau$  test is a score or Wald-type test:  $T = \tau' V_0^{-1} \tau \sim \chi_k^2$  1051 under  $H_0$ . With quantitative or binary traits, it is easy to verify  $\overline{u}_i = Y_i - 1052$  $\overline{Y} = Y_i - \sum_{i=1}^n Y_i / n$ ; under this condition we have exactly  $\tau = U$  if a canonical link function and a working independence model are used in 1054 GEE, suggesting the equivalence between the  $GK\tau$  test and the GEE 1055 Score test with Rw = I, which was confirmed by our numerical results 1056 (not shown). It is interesting to note that the nonparametric  $GK\tau$  test coincides with our semi-parametric GEE approach.

This equivalence suggests a natural extension of the  $GK\tau$  test to multiple SNPs (or markers): a new  $GK\tau$  test statistic can be defined in the 1060 same way as the score vector *U* for multiple SNPs in GEE with a canon- 1061 ical link function and a working independence model. This extension Q16 overcomes a conceptual difficulty in generalizing Kendall's tau to two 1063 random vectors with unequal lengths. Furthermore, rather than using 1064 a score- or Wald-type test (which may be low-powered with a high di- 1065 mensionality of kq), we can explore the power of the aSPU test as 1066 discussed before. Finally, our proposed approach differs from the  $GK\tau$  1067 test in the case with covariates. The modified  $GK\tau$  test with covariates 1068 (Zhu et al., 2012) uses a weighting scheme to adjust for covariate effects, 1069 in contrast to our regression approach. 1070

# Appendix B. Supplementary data

Supplementary data to this article can be found online at http://dx. 1072 doi.org/10.1016/j.neuroimage.2014.03.061. 1073

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Please cite this article as: Zhang, Y., et al., Testing for association with multiple traits in generalized estimation equations, with application to

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