# Prune Before Converged: Efficiently Training Pruned Transformer Models for Neural Machine Translation

## **Anonymous EMNLP submission**

#### **Abstract**

The Transformer models have been proven effective in machine translation task. To deploy the huge-size Transformer models in realworld applications, pruning methods compress the models by dropping out redundant attention heads. However, most of existing pruning methods only work for well-trained models, leading to massive redundant computations in the training stage. In this work, we propose a structured pruning method to efficiently train Transformer models for neural machine translation. We construct experiments on two widely-used machine translation datasets, and results show that pruning early before convergence significantly saves total training time while keeps comparable performance.

### 1 Introduction

The architecture of Transformer (Vaswani et al., 2017) has shown its tremendous power and achieved great success in machine translation task (Brown et al., 1993; Och, 2003; Sutskever et al., 2014; Bahdanau et al., 2014). The Transformer models, however, have grown increasingly huge (Devlin et al., 2018; Radford et al.; Yang et al., 2019; Raffel et al., 2019; Brown et al., 2020), resulting in substantial computational cost and high inference latency. This prevents them being deployed in resource-limited and real-time applications, such as online services and edge devices.

A mainstream approach to model compression is known as pruning. Unstructured pruning (weight pruning) (Han et al., 2015; Gordon et al., 2020) unrestrictedly removes the redundant parameters in Transformer models, but its pruned sparse matrices usually gain almost no acceleration on common hardware (Wen et al., 2016), and thus cannot effectively speed up the model despite significant model size reduction. On the other hand, Structured pruning (Kovaleva et al., 2019; Voita et al., 2019; Michel et al., 2019) finds that a considerable

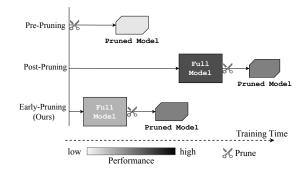


Figure 1: Comparison of different pruning strategies. We propose to prune early in the training stage to save training time while maintain the performance.

number of the attention heads in the well-trained Transformer models are redundant. By pruning these redundant heads, the Transformer models could achieve significant inference speedup while maintaining their performance. 041

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A major drawback of pruning methods is that it can only work for fully-trained models. However, the huge cost in training large Transformer models also greatly limits its utilization in real-world applications. In addition, pruning methods can recover most performance of a large model, which directly training a small model can not (Voita et al., 2019). This raises an interesting question: can we prune the Transformer model early in the training stage?

In this work, we propose a structured pruning method to efficiently train Transformer models for neural machine translation (NMT). Instead of pruning on well-trained models, we propose to prune the model far before converged. We add trainable weights to detect redundant attention heads and feed-forward network (FFN) dimensions and prune them to reduce the model size early.

We evaluate our early pruning approach on datasets of two language pairs. Experiments show that the method of early pruning can keep comparable performance with pruning after convergence, while could save training time by more than 50%.

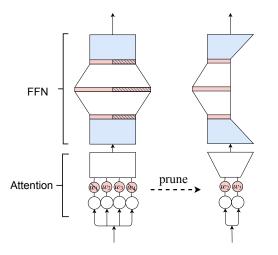


Figure 2: A brief view of a pruned Transformer layer. White circles are attention heads. Red components are additional weights. Blue parts are extra linear projections to keep dimension matched after pruning.

### 2 Related Work

Model compression works are mainly divided into three categories: (1) Knowledge distillation methods, which transfer the knowledge of the original trained "teacher" model to a lite one (Hinton et al., 2015; Jiao et al., 2019; Sanh et al., 2019; Sun et al., 2019, 2020; Jiao et al., 2020; Hou et al., 2020). (2) Quantization methods, which transform model weights in low precision formats to compress the model size (Shen et al., 2019; Zafrir et al., 2019; Han et al., 2016). (3) Pruning methods, which remove the redundant components in models (Voita et al., 2019; Michel et al., 2019; McCarley et al., 2019; Li et al., 2020; Wang et al., 2019; Zhang et al., 2020; Fan et al., 2019). Our work focuses on the pruning methods, while the main difference is that we prune the model far before convergence, saving much redundant computational costs during training.

Lottery Ticket Hypothesis (LTH) (Frankle and Carbin, 2018) shows that training carefully pruned model with re-initialization can recover the performance of full model. You et al. (2019) further shows that such good ticket can be determined early in the training stage. Recently, the existence of winning tickets is also verified in the field of NLP (Yu et al., 2019; Renda et al., 2020). Chen et al. (2020a,b); Prasanna et al. (2020) transfer LTH to Transformer based models. Our work provides a feasible way, i.e., early structured pruning, to find such a lucky ticket for Transformer models in neural machine translation.

#### 3 Our Method

In this section we introduce the details of our early structured pruning method to efficiently train pruned Transformer models. We prune the models far before it converges (e.g., train with a few steps). The pruning strategy can be divided into two steps: (1) Prune the attention layer; (2) Prune the feedforward layer according to the number of pruned attention heads for each layer.

#### 3.1 Attention Layer Pruning

We first detect the importance of attention heads, and then prune unimportant ones. Inspired by Ahmed et al. (2017), we simply add a trainable weight  $w_i$  multiplied on each attention head to measure its importance. Thus, the modified Multi-Head Attention (MHA) can be formulated as:

$$\begin{aligned} \text{MHA}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) &= \text{Concat}(\mathbf{h}_1, \cdots, \mathbf{h}_n) \mathbf{W}^O \\ \mathbf{h}_i &= f(w_i) \cdot \text{Attn}(\mathbf{Q} \mathbf{W}_i^Q, \mathbf{K} \mathbf{W}_i^K, \mathbf{V} \mathbf{W}_i^V) \\ \text{Attn}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) &= \text{Softmax}(\frac{\mathbf{Q} \mathbf{K}^T}{\sqrt{d_k}}) \mathbf{V} \end{aligned}$$

where  $f(\cdot)$  is a ReLU function to avoid negative weight. Trainable head weight  $w_i$  is shown in Figure 2 as red circles. During training, we first initialize each  $w_i$  to 1, and then optimize them using the objective  $\mathcal{L}_{NMT}(\mathbf{w}_i)$  with Transformer's weights fixed, where  $\mathcal{L}_{NMT}$  is the objective of NMT.

We prune attention heads with smaller head weights from encoder, decoder and cross attention by a pre-defined pruning ratio. Thus, the number of pruned heads in each layer may differ, indicating different importance of these layers. Please refer to Appendix A for further details of pruning.

#### 3.2 Feed-Forward Layer Pruning

We suppose that after attention layer pruning, layers with less attention heads also do not require full dimension in its corresponding FFN. Similarly as attention layer, we add weights multiplied on each dimension of FFN layers (including input, intermediate and output layers) to detect redundancy. Different from attention layer pruning, we add two additional prunable linear projections before and after the original FFN to keep the dimension matched with attention module after pruning. The modified

FFN is formulated as:

$$\mathbf{h}_{in} = (\mathbf{x}\mathbf{W}_{entry} + \mathbf{b}_{entry}) \circ f(\mathbf{w}_{in})$$

$$\mathbf{h}_{inter} = f(\mathbf{h}_{in}\mathbf{W}_{1} + \mathbf{b}_{1}) \circ f(\mathbf{w}_{inter})$$

$$\mathbf{h}_{out} = (\mathbf{h}_{inter}\mathbf{W}_{2} + \mathbf{b}_{2}) \circ f(\mathbf{w}_{out})$$

$$\mathbf{o} = \mathbf{h}_{out}\mathbf{W}_{exit} + \mathbf{b}_{exit}$$
(2)

where  $\mathbf{W}_{entry}$ ,  $\mathbf{b}_{entry}$ ,  $\mathbf{W}_{exit}$ ,  $\mathbf{b}_{exit}$  are the parameters of two additional entry and exit projections, as shown in Figure 2 as blue rectangles. " $\circ$ " stands for dimension-wise multiplication.  $\mathbf{w}_{in}$ ,  $\mathbf{w}_{inter}$ ,  $\mathbf{w}_{out}$  are weights on input, intermediate and output layers, as shown in Figure 2 as red rectangles. We call them FFN weights in brief. During training, we first initialize two additional projections as identity functions and FFN weights as 1, and then optimize FFN weights using the objective  $\mathcal{L}_{NMT}(\mathbf{w}_{in}, \mathbf{w}_{inter}, \mathbf{w}_{out})$  similarly.

We prune the dimension for each FFN layer by the ratio of attention heads pruned in that layer. For example, if half attention heads are pruned, half of FFN dimensions should be pruned (shown in Figure 2 as shadowed part of red rectangles). Please refer to Appendix A for further pruning details.

We find that a large proportion of parameters of Transformer models lies in FFN layers, so pruning FFN layers is very crucial for efficient training and inference. As show in Figure 3, by pruning FFN layers along with attention heads, the size of Transformer model can be significantly reduced, and its inference computations (measured by FLOPs) are also greatly saved compared with pruning attention heads alone.

## 4 Experiments

#### 4.1 Setup

We evaluate our proposed method on WMT14 English-German (En-De) and WMT17 Chinese-English (Zh-En) translation tasks. The evaluation metric is case-sensitive BLEU. We implement our method on top of an open-source machine translation toolkit THUMT (Tan et al., 2020). Please refer to Appendix B for detailed experimental settings. **Training Time Comparing** We directly compare training time in the same settings. All runs in our pruning experiments contain three stages: train full

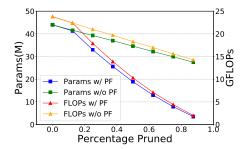


Figure 3: The influence of pruning percentage on model size and FLOPs. "PF" refers to Pruning FFN layers. Parameters and FLOPs are computed theoretically without embedding layer.

model with additional parts (colored component in Figure 2 left) disabled, which is equivalent to a standard Transformer; activate additional parts, train weights and prune the model; train the pruned model. To better observe the convergence time of the final pruned model, we extend the training process of the pruned model to be long enough and observe the training curve of it. We compare following settings with notations:

**Pre-Pruning** Prune the model at the beginning. This is equivalent to training a smaller pruned model from scratch.

**Post-Pruning** Prune the model after convergence. This is conventional practice and serves as the baseline setting here.

**Early-Pruning** Prune the model early in the training stage before convergence. This is what we propose.

## 4.2 Results

Time Efficiency We conduct experiments on both En-De and Zh-En tasks. The results are listed in Table 1. The "Transformer" line represents training a full Transformer model until convergence, which is 100k steps for base model and 200k steps for big model. The pruning ratio is fixed to 30% in all runs, and pruning time step in Early-Prune is step 30k. We compare the training curves of big models on En-De dataset in Figure 4. From the curves, we can observe that Early-Pruning converges in less than 40h, while Post-Pruning costs about 80h to converge. Our method converges earlier by more than 50%. This conclusion remains true on other settings and datasets, please refer to Appendix C.2 for curves of other settings and datasets. According to Table 1, the performance of Post-Pruning and Early-Pruning are comparable in both sizes of model and both language pairs, indicating that

<sup>&</sup>lt;sup>1</sup>In particular, we only prune the decoder FFN layer when heads in cross attention are pruned. Since we don't prune FFN layer when heads in decoder self-attention are pruned, the model size after pruning may differ given same pruning ratio

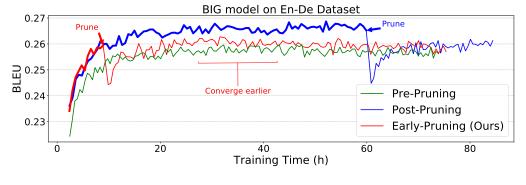


Figure 4: Training curves of big models on En-De dataset. BLEU scores are evaluated on the dev set. We annotate the pruning point on the curve. We train full model before the pruning point (thick line) and train pruned model after it (thin line).

En-	De	Zh-En		
Params	BLEU	Params	BLEU	
98.7M	27.54	93.2M	23.6	
86.0M	26.66	79.9M	22.9	
84.8M	27.15	77.0M	23.3	
83.8M	27.13	78.9M	23.2	
285.4M	29.01	274.5M	23.9	
228.0M	27.60	223.0M	23.4	
223.2M	28.24	227.8M	23.6	
230.0M	28.14	222.9M	23.7	
	98.7M 86.0M 84.8M 83.8M 285.4M 228.0M 223.2M	98.7M 27.54 86.0M 26.66 84.8M 27.15 83.8M 27.13 285.4M 29.01 228.0M 27.60 223.2M 28.24	Params         BLEU         Params           98.7M         27.54         93.2M           86.0M         26.66         79.9M           84.8M         27.15         77.0M           83.8M         27.13         78.9M           285.4M         29.01         274.5M           228.0M         27.60         223.0M           223.2M         28.24         227.8M	

Table 1: Results on WMT14 En-De task and WMT17 Zh-En task.

Pruning Ratio	Post-Pruning	Early-Pruning (Ours)
20%	27.32	27.31
50%	26.65	26.50
80%	24.19	24.33

Table 2: Comparing results when change prune ratio. We prune the model at step 30k. The results are evaluated on WMT14 En-De dataset.

pruning before convergence doesn't harm the final performance of the pruned model. Comparing with Pre-Pruning, our Early-Pruning approach achieves much better performance, proving the necessity of training full model before pruning.

Influence of Pruning Ratio We compare with Post-Pruning with a pruning ratio of 20%, 50% and 80%, as shown in Table 2. From the table, we observe that the performance of Early-Pruning and Post-Pruning are comparable in various pruning ratios, verifying that the effectiveness of our early pruning approach is irrelevant to pruning ratio.

**Influence of Pruning Time Step** We also observe the influence of pruning time step with two differ-

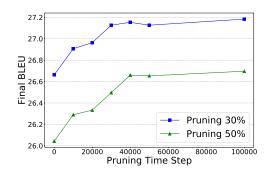


Figure 5: Influence of different pruning time step on final performance.

ent pruning ratios, as shown in Figure 5. There is a trend that the later we prune, the better final performance will be. But the increasing rate of the performance gradually declines, and there is a moment when pruning after it and before it behave differently. We infer from Figure 5 that the critical point is about step 30k for pruning 30% and 40k for pruning 50%. Pruning before it causes significant performance drop, while pruning after it makes slight difference in final performance. Since the critical point is quite a few steps before convergence, it gives evidence that pruning after the critical point before convergence could save training time while hardly harm the final performance.

#### 5 Conclusion

In this work, we present an efficient training method of pruned Transformer models by pruning early in the training stage. With suitable pruning ratio and pruning time step, our method can save more than 50% training time with comparable performance. In the future, we will explore how to apply our model to pre-trained language models, and extend it into other model architectures.

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#### **A** Pruning Details

#### A.1 Attention Heads

When an attention head is decided to be pruned, we simply remove  $W_i^Q, W_i^K, W_i^V$  of the chosen head. The output projection  $W_O$  can be considered a concatenation of  $W_i^O$  matching each head. We prune the  $W_i^O$  of chosen head as well. As shown in Figure 2, the dimension of hidden state is reduced in pruned attention heads, while the dimension of input and output keeps unchanged.

#### A.2 FFN Dimensions

When a dimension in a hidden layer in the FFN is chosen to be pruned, the two linear projections related to the hidden layer are to be pruned. The chosen dimension is directly linked to a corresponding column in the linear projection before the hidden layer and a corresponding row in the linear projection after hidden layer. The linked row and column are pruned to reduce the model size. As shown in Figure 2, we add additional weights on three hidden layers in the FFN, thus four projections  $\mathbf{W}_{entry}$ ,  $\mathbf{W}_1$ ,  $\mathbf{W}_2$ ,  $\mathbf{W}_{exit}$  are pruned. If all heads are pruned in a particular layer, then all dimensions should be pruned. In practice we directly remove the whole layer.

## **B** Experiment Setting

Model setting We perform pruning on base model and big model respectively. Both models contains 6 layers for encoder self-attention, decoder self-attention and cross attention. The hidden size of the base model is 512 and is split into 8 heads, while the hidden size of the big model is 1024 and is split into 16 heads.

Data preparing We conduct our experiments on two language pairs, English-German and Chinese-English. For English-German task, We trained our model on WMT 2014 (Bojar et al., 2014) English-German dataset. The training set contains 4.5 M sentence pairs. We take newstest2013 as validation set and newstest2014 as test For Chinese-English task, we use WMT 2017 (Bojar et al., 2014) Chinese-English dataset while take newsdev2017 as development set and newstest2017 as test set. The Chinese-English training set contains 24.8 M sentence pairs. We use byte-pair encoding (Sennrich et al., 2015) with 32k merges to encode sentences for all language individually. We evaluate our models by case insensitive BLEU score with the script

multi-bleu.perl for En-De task and toolkit sacrebleu (Post, 2018) for Zh-En task.

**Optimization** We trained our base model on 4 NVIDIA V100 GPUs with each batch contains about 16384 tokens on each device. For big model, we use 8 NVIDIA V100 GPUs and set the batch size to 8192. The Adam optimizer is applied for optimization. The learning rate is set to 7E-4 and 5E-4 for base and big model respectively. We train the base model for 100k steps and the big model for 200k steps. We use the standard learning rate decay policy proposed by Vaswani et al. (2017). To train additional weights (head weights and FFN weights), we use an extra Adam optimizer with constant learning rate 1E-4 and train for 2k steps. All other parameters are fixed when we train additional weights. Additional weights are not trained in other circumstances. In decoding phase, we set the beam size to be 4 and the length penalty  $\alpha$  (Wu et al., 2016) to be 0.6 for En-De task and 1.2 for Zh-En task.

## **C** Experiments Details

## C.1 Quick Convergence of Additional Weights

Since we train additional weights to rank the importance of attention heads, an interesting question is how many steps do we need to get a stable pruning decision? As each pruning decision can be noted as a binary mask, with the pruned head marked as 1 and kept one marked as 0. During the process of weight training, inspired by You et al. (2019), we can visualize mask distances between steps to detect whether the weight training converges.

As shown in Figure 6, we find that the mask converge in less than 200 steps of score training, which is negligible compared with the training of model parameters. When we train head weights for the same model several times, the finally converged masks are almost the same, indicating the mask is totally dependent on model parameters and robust to the randomness during training.

#### C.2 Detailed Main Results and Curves

For fair comparison on total training time, we fix the training steps in total. We first train the Post-Pruning setting with enough steps to convergence, and then prune the model and train the pruned model. The process of training pruned model in Early-Pruning is extended to meet the amount requirement of total steps. We also train the model

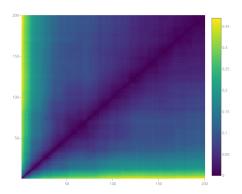


Figure 6: Binary mask distance between steps when training weights at step 30k for base model on En-De dataset. The mask keeps almost unchanged in the last few steps.

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of Pre-Pruning with more steps for fair comparison with previous settings. All results are listed in Table 3. The table shows that although the training time of our method is far beyond convergence, it stills costs less time than Post-Pruning under fair comparison. The training curves of En-De base model, Zh-En base model and Zh-En big model are showed in Figure 8, Figure 9 and Figure 10. In all cases our method converges much earlier than Post-Pruning.

#### **C.3** Compare with Pruning Gradually

A natural idea is that we can prune the model more than one times during training. We try this idea and show the results in Table 5 and notated as "Gradually-Pruning". To compare with our previous experiment, we prune the model from step 30k, and prune 2% of all attention heads and corresponding FFN dimensions every 2k steps for 18 times. The final pruned ratio is nearly 30% then. We train additional weights alone for 200 steps before every pruning time, and these weights are reinitialized to 1 before each time we train them. The experiment shows that pruning gradually performs no better than pruning just once, and only behaves more complicated.

## C.4 Results of Multiple Runs for Different Pruning Moments

The final results evaluated on BLEU score face turbulence in practice. We run each experiment for 3 times to observe the stable trend via averaged values. We list all results in Table 4.

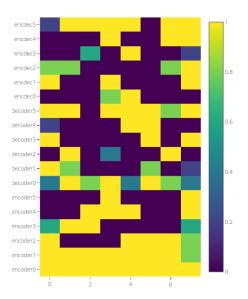


Figure 7: Average pruning decision of 5 independent runs of training weights from same model. Pruning decisions highly focuses on particular heads. Values of most heads in the figure are 0 (never chosen to prune) or 1 (always chosen to prune), indicating the pruning decision of our method is independent of randomness.

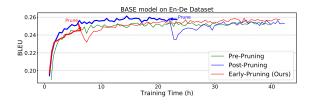


Figure 8: Training curves of base models on En-De dataset.



Figure 9: Training curves of base models on Zh-En dataset.

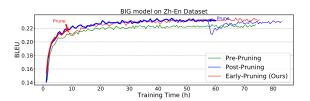


Figure 10: Training curves of big models on Zh-En dataset.

	Steps	Params	En-De BLEU	Time	Params	Zh-En BLEU	Time
BASE model							
Transformer Post-Pruning Early-Pruning Pre-Pruning	100k 100k + 100k 30k + 170k 200k	98.7M 84.8M 83.8M 86.0M	27.54 27.15 27.13 26.66	- 42h3m 39h59m 39h21m	93.2M 77.0M 78.9M 79.9M	23.6 23.3 23.2 22.9	- 40h57m 39h36m 38h30m
BIG model							
Transformer Post-Pruning Early-Pruning Pre-Pruning	200k 200k + 100k 30k + 270k 300k	285.4M 223.2M 230.0M 228.0M	29.01 28.24 28.14 27.60	- 83h29m 73m29m 72h38m	274.5M 227.8M 222.9M 223.0M	23.9 23.6 23.7 23.4	- 81h57m 74h53m 73h30m

Table 3: Results on WMT14 En-De task and WMT17 Zh-En task.

D		Pr	une 30%	)		Pru	ine 50%	
Pruning Step	Run1	Run2	Run3	Avg. BLEU	Run1	Run2	Run3	Avg. BLEU
0k	26.23	27.07	26.69	26.66	25.97	26.13	26.03	26.04
10k	26.88	27.04	26.80	26.91	26.35	26.31	26.21	26.29
20k	27.03	27.00	26.84	26.96	26.20	26.28	26.52	26.29
30k	27.14	27.36	26.88	27.13	26.48	26.43	26.58	26.50
40k	27.22	27.12	27.12	27.15	26.59	26.70	26.69	26.66
50k	27.09	27.04	27.25	27.13	26.67	26.62	26.67	26.65
100k	27.26	27.19	27.10	27.18	26.68	26.70	26.71	26.70

Table 4: All results of 3 runs when change prune step. The pruning ratio is 30% and 50%. The results are evaluated on WMT14 En-De dataset.

Params	BLEU
85.3M	27.13
91.0M	27.12
	85.3M

Table 5: Compare with prune gradually. We prune the model every 2k steps for 18 times from step 30k with 2% of the parameters each time.