

# CP Problems Analysis

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## 1 Codeforces

### 1327D. Infinite Path

Think of each permutation mapping as a graph. Let  $a \rightarrow b$  be an edge if  $P_a = b$ . It's clear that the minimum value of  $k$  s.t  $C_{P_x^k} = C_x$  for some  $x$  would be the smallest value where the node  $kx$  away from the current node has the same color as the current node for all nonnegative integers  $x$ . As this is the minimum such  $k$ , it follows that  $k|n$ . Thus, we can loop over all divisors of  $n$  and check if it satisfies the condition.

The mistake I made was that I did not remember to check visited for the *current* node, but rather checked it on the *next* node. Thus, the next iteration, it would see that the node was "visited" when it really was not, and break. Thus, all of my answers were just 1.

## 2 USACO

### 2020 US Open - Gold: Haircut

This was actually extremely simple and I don't know why I didn't get it.

When I found inversions with the algorithm, for each index  $i$ , it counted the number of elements  $j < i$  that had  $a_j < a_i$  using a BIT. Then, it subtracted that value from  $i$ .

So we can find the number inversions for all indices  $i$  of a specific value. And that's all we really want. From there we can find the number of inversions solely comprising values  $\leq x \forall x$ .

**Update:** I read my code for *mincross* which had inversion count and I feel terrible for not noticing this – it was literally in the code.

### 2020 US Open - Gold: Exercise

So I made significant progress during the contest but for some reason just didn't implement it. A few key ideas that I came up with were that:

- Each permutation is a "cycle" of different permutations. The number of times before repetition is the lcm of all cycle lengths.

- We need to find  $lcm(a_1, a_2, \dots, a_g)$  for some  $g$  s.t.  $\sum_{i=1}^g a_i = n$ .
- Anything that works for  $j < i$  steps also works for  $i$  steps.

However, I did not know how to find the lcm of all  $a_i$  despite it being clear from the third observation that it was DP.

Let  $dp_{i,j}$  be the running sum with the first  $i$  primes and the first  $j$  indices. Then

$$dp_{i,j} = dp_{i-1,j} + (p_i^a \cdot dp_{i-1,j-p_i^a} \forall a \leq \log_{p_i} j).$$

$dp_{i-1,j}$  is the previous step and the other long expression is the added running sum from the  $i$ th prime  $p_i$ .