Advanced Quantitative Research Methodology, Lecture Notes: Model Dependence in Counterfactual Inference¹

Gary King

March 26, 2016

 King, Gary and Langche Zeng. "The Dangers of Extreme Counterfactuals," Political Analysis, 14, 2, (2007): 131-159.

- King, Gary and Langche Zeng. "The Dangers of Extreme Counterfactuals," Political Analysis, 14, 2, (2007): 131-159.
- King, Gary and Langche Zeng. "When Can History be Our Guide?
 The Pitfalls of Counterfactual Inference," International Studies
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http://j.mp/causalinference

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- Counterfactuals are some part of most social science research

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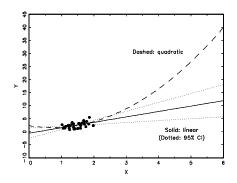
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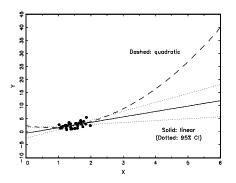
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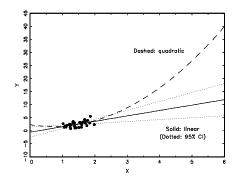
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 - Is this a true test of an ex ante hypothesis or merely a demonstration that it is *possible* to find results consistent with your favorite hypothesis?

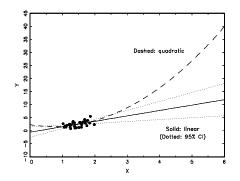




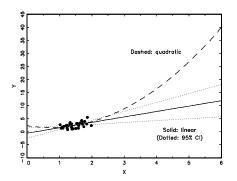
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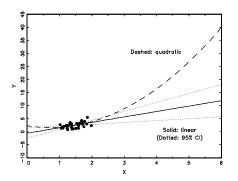
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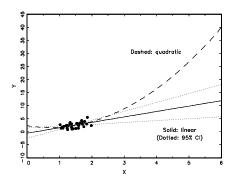
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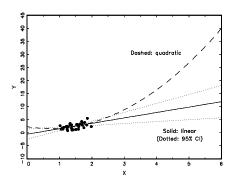
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- Same for what if questions, predictions, and causal inferences

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Result

The maximum degree of model dependence: solely a function of the distance from the counterfactual to the data

A (Hypothethical) Research Design

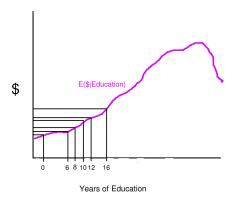
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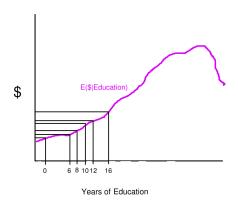
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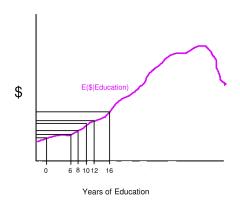
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- We find a coefficient of $\hat{\beta}=\$1,000$, big t-statistics, narrow confidence intervals, and pass every test for auto-correlation, fit, normality, linearity, homoskedasticity, etc.

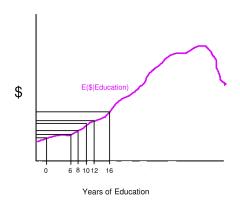




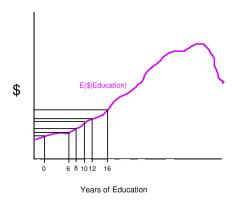
 A Factual Question: How much salary would someone receive with 12 years of education (a high school degree)?

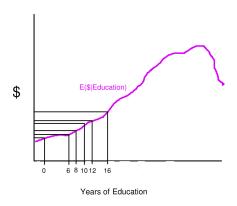


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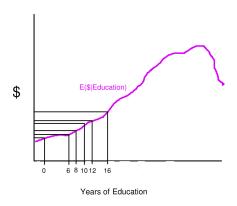


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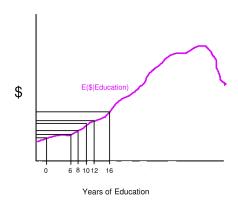




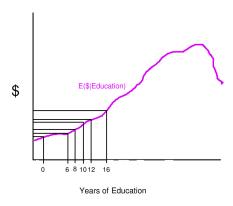
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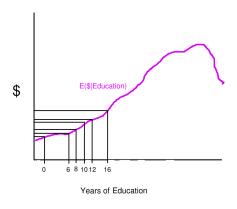


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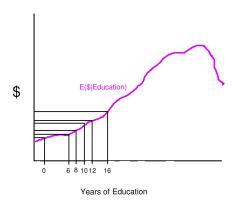


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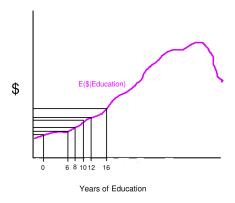


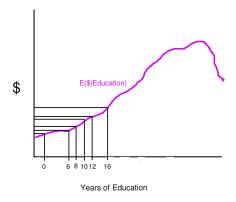
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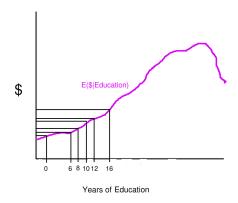
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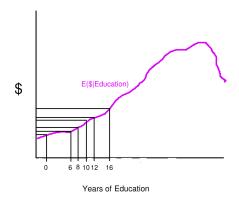




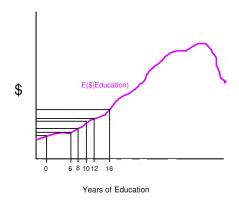
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- What's changed? How would we recognize it when the example is less extreme or multidimensional?

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- (If X were continuous, we would be reducing ∞ to 2, also by assumption)

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- The difference: an enormous assumption based on convenience, not evidence or theory.

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- The curse of dimensionality introduces huge assumptions, often recognized.

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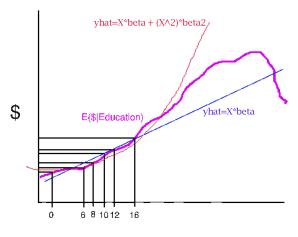
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 - No need to specify models (or a class of models), estimators, or dependent variables.
 - Results of one run apply to the class of all models, all estimators, and all dependent variables.

Interpolation vs Extrapolation in one Dimension



Years of Education

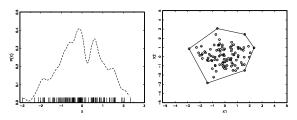
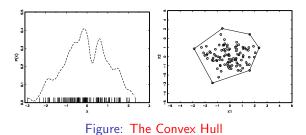


Figure: The Convex Hull



Interpolation: Inside the convex hull

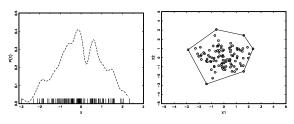
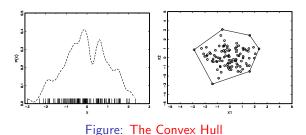


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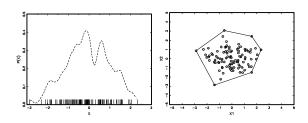


Figure: The Convex Hull

- Interpolation: Inside the convex hull
- Extrapolation: Outside the convex hull
- Works mathematically for any number of X variables
- Software to determine whether a point is in the hull (which is all we need) without calculating the hull (which would take forever), so its fast; see http://GKing.harvard.edu/whatif

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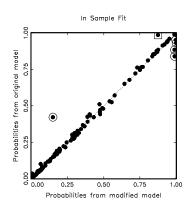
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- Thus, without estimating any models, we know inferences will be model dependent; for illustration, let's find an example....

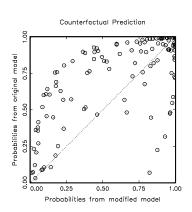
Doyle and Sambanis, Logit Model

	Original Model			Modified Model		
Variables	Coeff	SE	P-val	Coeff	SE	P-val
Wartype	-1.742	.609	.004	-1.666	.606	.006
Logdead	445	.126	.000	437	.125	.000
Wardur	.006	.006	.258	.006	.006	.342
Factnum	-1.259	.703	.073	-1.045	.899	.245
Factnum2	.062	.065	.346	.032	.104	.756
Trnsfcap	.004	.002	.010	.004	.002	.017
Develop	.001	.000	.065	.001	.000	.068
Exp	-6.016	3.071	.050	-6.215	3.065	.043
Decade	299	.169	.077	-0.284	.169	.093
Treaty	2.124	.821	.010	2.126	.802	.008
UNOP4	3.135	1.091	.004	.262	1.392	.851
Wardur*UNOP4	<u> </u>	_	_	.037	.011	.001
Constant	8.609	2.157	0.000	7.978	2.350	.000
N		122			122	

Log-likelihood -45.649 -44.902
Pseudo *R*² .423 .433

Doyle and Sambanis: Model Dependence





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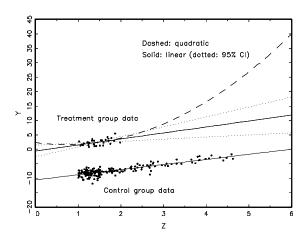
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- Δ_e Extrapolation bias (check this with data!)

Interpolation vs Extrapolation Bias



Causal Effect of Multidimensional UN Peacekeeping Operations

