

# GOV 2001/ 1002/ E-200 Section 11

## Choice Modeling and Future Directions in Methods<sup>1</sup>

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<sup>1</sup>These section notes are heavily indebted to past Gov 2001 TFs for slides and R code.

# LOGISTICS

**Reading Assignment-** UPM Chapter 8, Glasgow et. al., 2012

**Final Paper** Due April 27th at 5:00 pm. But with automatic extensions to May 5th at 5:00 pm.

**Final Exam (for E-school students not doing the paper)**

Released on April 27th. You will “check out” the exam on Canvas any time during exam period. After check-out, you will have 1 week to finish. The final deadline is May 14th at 5:00 pm.

**Fill out the RSVP for the party on May 7th!** We only have 4 respondents so far!

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  - ▶ learn how to model choice data
  - ▶ learn how latent space models work.
  - ▶ learn how to generalize from an unrepresentative sample.
  - ▶ learn how to think about learning methods beyond this course!

# OUTLINE

Choice Models

Ideal Point Models

Modern Survey Sampling

Learning more methods



# MODELING CHOICES



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- ▶ Systematic component:

$$\pi_{ij} = \frac{\exp(\eta_{ij})}{\sum_{k=1}^K \exp(\eta_{ik})}$$
$$\eta_{ij} = X_i \beta_j$$

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- How many parameters are we estimating?  $J - 1 \times \text{length of } \beta$ .
- Likelihood  $L(\beta|X, Y)$  :

$$\begin{aligned}
 &\propto \prod_{i=1}^N \prod_{j=1}^J \pi_{ij}^{Y_{ij}} \\
 &\propto \prod_{i=1}^N \prod_{j=1}^J \left[ \frac{\exp(\eta_{ij})}{\sum_{k=1}^J \exp(\eta_{ik})} \right]^{Y_{ij}} \\
 &\propto \prod_{i=1}^N \left[ \prod_{j=1}^{J-1} \left[ \frac{\exp(X_i \beta_j)}{1 + \sum_{k=1}^{J-1} \exp(X_i \beta_k)} \right]^{Y_{ij}} \times \left[ \frac{1}{1 + \sum_{k=1}^{J-1} \exp(X_i \beta_k)} \right]^{Y_{iJ}} \right]
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- ▶ However, has implicit assumption about choice behavior: Independence of Irrelevant Alternatives (IIA).
- ▶ Ratio of choice probability of category 1 to 2 does not depend on any other category:

$$\frac{\pi_{ij}}{\pi_{ik}} = \frac{\frac{\exp(\eta_{i1})}{\sum \exp(\eta_{ik})}}{\frac{\exp(\eta_{i2})}{\sum \exp(\eta_{ik})}} = \frac{\exp(\eta_{i1})}{\exp(\eta_{i2})} = \frac{\exp(X_i\beta_1)}{\exp(X_i\beta_2)}$$

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  - ▶ New probs:  $Pr(\text{Car}) = .5$ ,  
 $Pr(\text{Red Bus}) = Pr(\text{Blue Bus}) = .25$ .  $\frac{Pr(\text{Car})}{Pr(\text{Red Bus})} = \frac{.5}{.25} = 2 \neq 1$

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$Z_j$  are covariates for alternative  $j$  and  $\gamma$  are estimated coefficients.

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European Parliament. Photo by David Iliff. License: CC-BY-SA 3.0

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- ▶ Simple metrics like % agreement miss important variation in agenda.



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- ▶ **Goal:** Infer latent ability/preferences from observed outcomes (test questions/votes).
- ▶ Starting point for poli-sci: Clinton, Jackman, Rivers (2004) “The Statistical Analysis of Roll Call Data” APSR.

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- ▶ Possible to justify this from a “utility maximization” model

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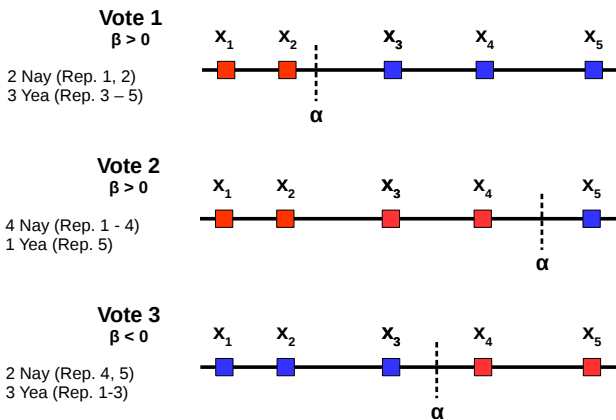
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# IRT EXAMPLE

Figure: Example of latent space model with no voting error



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# IDENTIFICATION

- ▶ We can write the likelihood as the product of  $Y_{ij}$  over  $i$  and  $j$  (assuming independence between votes).
- ▶ What's the issue with ML estimates? Not identified! Likelihood depends only on distances between ideal points. Invariant to scale or rotation!
- ▶ Solutions:
  - ▶ Constrain scale
  - ▶ Fix some legislators' locations
- ▶ Even then, ML estimates are inconsistent. As  $N$  gets large, the number of parameters also grows!
- ▶ More simply - it's just a hard likelihood to maximize!

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  - ▶ MCMC methods repeatedly take draws from these conditionals. Markov chain theory tells us that this converges to drawing from the true posterior!

# WHAT IRT MODELS CAN SHOW US.

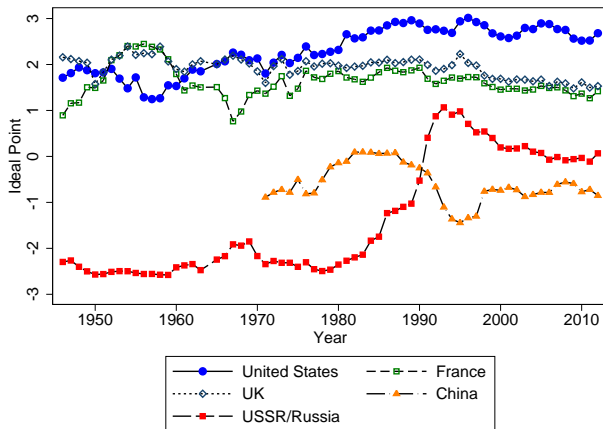


Figure: Dynamic ideal point estimates of P5 countries from UNGA voting - Voeten et. al. (2015)

# OUTLINE

Choice Models

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**Modern Survey Sampling**

Learning more methods

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  - ▶ Post-stratification: Use what we know about population-level covariate distribution to reweight data for predictions.

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- ▶ How? Re-weight our sample to match known population characteristics of Hennepin County.

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  - ▶ Step 4: Calculate weights for your observations such that the (weighted) sample distributions of covariates match the population distributions.

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- ▶ Can also think of it as

$$w_i = \frac{P_h}{p_h}$$

where  $p_h$  is the sample proportion in stratum  $h$ .

- ▶ **Intuition:** Upweight observations that are rare relative to population. Downweight observations that are common.

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  - ▶ Step 4: Repeat across all of the variables in sequence until convergence (no change in weights).

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  - ▶ E.g.: Don't just learn "text analysis," learn how to think about high-dimensional data where  $p \gg n$ .



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    - ▶ More complex examples: instrumental variables, regression discontinuity

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# WHAT METHODS?

- ▶ All of these are elements of almost every methods paper!
  - ▶ I can write down a really complicated model... but it's useless if I can't estimate it!
  - ▶ I can get a really efficient estimate of some regression parameter... but if I want to claim causality, it's useless if I can't also argue that it identifies a causal parameter of interest.
- ▶ **Main Takeaway:** Think first in terms of what you need to better argue from your data, then go out and find what you don't know.

# QUESTIONS

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