

User-User Collaborative Filtering

Reference for UUCF

- An Algorithmic Framework for Collaborative Filtering by Herlocker, Konstan, Borchers, and Riedl (Proc. SIGIR 1999)

The following are screenshots the handwritten notes

$$\begin{array}{l}
 \begin{array}{l}
 \uparrow \quad \uparrow \quad \uparrow \\
 \text{pred. score} \quad \text{user} \quad \text{item}
 \end{array}
 \quad S(u, i) = \frac{\sum_{v \in U} r_{vi}}{|U|} \quad \begin{array}{l} \leftarrow \text{rating} \\ \leftarrow \text{all users} \\ \leftarrow \# \text{ users} \end{array} \\
 \\
 S(u, i) = \bar{r}_u + \frac{\sum_{v \in U} (r_{vi} - \bar{r}_u)}{|U|} \\
 \\
 S(u, i) = \frac{\sum_{v \in U} r_{vi} \cdot w_{uv}}{\sum_{v \in U} w_{uv}} \quad \leftarrow \text{similarity}
 \end{array}$$

$$S(u, i) = \bar{r}_u + \frac{\sum_{v \in U} (r_{vi} - \bar{r}_v) * w_{uv}}{\sum_{v \in U} w_{uv}}$$

$v \neq u$
 (limit size
 min similarity neg. simil.
 Pearson Correl
 $w_{uv} = \frac{\sum_{i \in I} (r_{ui} - \bar{r}_u)(r_{vi} - \bar{r}_v)}{\sigma_u \sigma_v}$

• small overlap
 • binary

$$\frac{\sum_{v \in V}}{\sum_{v \in V}}$$

Common Characteristics

- Collection of Ratings
- Measure of Inter-User Agreement
 - Correlation, Vector Cosine
- Personalized Recommendations/Predictions
 - Weighted Combinations of Others' Ratings
- Tweaks to make things work right ...
 - Neighborhood limitations
 - Normalization
 - Dealing with limited co-ratings

Let's Formalize This ...

- Given a set of items I , and a set of users U , and a sparse matrix of ratings R ,

We compute the prediction $s(u,i)$ as follows:

- For all users $v \neq u$, compute w_{uv}
 - similarity metric (e.g., Pearson correlation)
- Select a neighborhood of users $V \subset U$ with highest w_{uv}
 - may limit neighborhood to top-k neighbors
 - may limit neighborhood to $\text{sim} > \text{sim_threshold}$
 - may use sim or $|\text{sim}|$ (risks of negative correlations)
 - may limit neighborhood to people who rated i (if single-use)
- Compute prediction:

$$s(u, i) = \bar{r}_u + \frac{\sum_{v \in V} (r_{vi} - \bar{r}_v) * w_{uv}}{\sum_{v \in V} w_{uv}}$$

Implementation Issues

- Given $m = |U|$ users and $n = |I|$ items:
 - Computation can be a Bottleneck
 - Correlation between two users is $O(n)$
 - All correlations for a user is $O(mn)$
 - All pairwise correlations is $O(m^2n)$
 - Recommendations at least $O(mn)$
 - Lots of ways to make more practical
 - More persistent neighborhoods ($m \rightarrow k$)
 - Cached or incremental correlations

Core Assumptions/Limitations

- Why does this work?
 - Let's break it down ...
- Assumption: Our past agreement predicts our future agreement
 - Base Assumption #1: Our tastes are either individually stable or move in sync with each other
 - Base Assumption #2: Our system is scoped within a domain of agreement

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