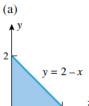
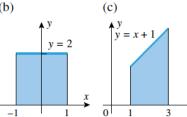
1. In each part, use a definite integral to find the area of the

region, and check your answer using an appropriate formula from geometry.







In Exercises 3–6, find the area under the curve y = f(x) over the stated interval.

5. $f(x) = 3\sqrt{x}$; [1,4]

In Exercises 7–19, evaluate the integrals using Part 1 of the Fundamental Theorem of Calculus.

10. $\int_{-1}^{2} 4x(1-x^2) \, dx$

 $\int_{-\pi/2}^{\pi/2} \sin\theta \, d\theta$

 $\int_{1/2}^{1} \frac{1}{2x} dx$

 $\int_{1}^{4} \left(\frac{1}{\sqrt{t}} - 3\sqrt{t} \right) dt$

(a) $\int_{-1}^{2} \sqrt{2 + |x|} \, dx$

 $\int_0^{\frac{\pi}{2}} \left| \frac{1}{2} - \cos x \right| dx$

| 35. Use a calculating utility to find the midpoint approximation of the integral using $n=20$ subintervals, and then find the exact value of the integral Part 1 of the Fundamental Theorem of Calculus. $\int_1^3 \frac{1}{x^2} dx$ | 40. Find the area that is above the x -axis but below the curve $y=x-x^2$. Make a sketch of the region. |
|---|---|
| 43. Sketch the curve and find the total area between the curve and the given interval on the x -axis. $y = x^2 - x$; $[0,2]$ | 45. Sketch the curve and find the total area between the curve and the given interval on the x -axis. $y=2\sqrt{x+1}-3$; $[0,3]$ |
| 49. Find the area enclosed by the graphs of $y=\frac{1}{\sqrt{1-x^2}}, y=$ (a) Show that the exact area is $\sin^{-1}0.8$. | 0, x = 0, and x = 0.8. |
| | |