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Show all necessary work neatly.

Determine whether the methods of integrating factors and separation of variables produce the same solution of the differential equation

$$\frac{dy}{dx} - 4xy = x$$

7. Solve the differential equation either by the method of integrating factors or by separation of variables.

$$\frac{dy}{dx} = (1+y^2)x^2$$

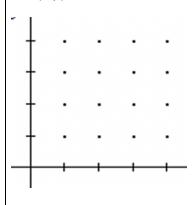
11. Solve the initial value problem.

$$y' - xy = x; y(0) = 3$$

15. Solve the initial value problem.

$$y' = \frac{y^5}{x(1+y^4)}; y(1) = 1$$

21. Sketch the slope field for  $y' = \frac{xy}{8}$  at the 25 gridpoints (x, y), where x = 0,1,...,4 and y = 0,1,...,4.



23. Approximate the solution of the initial value problem using Euler's method. Present your answer as a table.

$$\frac{dy}{dx} = \sqrt{y}; y(0) = 1,0 \le x \le 4; \Delta x = 0.5$$

27. In each part, find the exponential growth model  $y=y_0e^{kt}$  that satisfies the given conditions.

(a)  $y_0 = 2$ , doubling time T = 5.

(c) y(1) = 1; y(10) = 100

(b) y(0) = 5, growth rate 1.5%.

(d) y(1) = 1; doubling time T = 5.

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11. Find the general term of the sequence, starting with n=1, determine whether the sequence converges, and if so find its limit.

(a)  $\frac{3}{2^2 - 1^2}, \frac{4}{3^2 - 2^2}, \frac{5}{4^2 - 3^2}, \dots$ 

(a)  $\frac{1}{2}, -\frac{2}{5}, \frac{3}{7}, -\frac{4}{9}, \dots$ 

13. Show that the sequence is eventually strictly monotone.

(a)  $\{(n-10)^4\}_{n=0}^{\infty}$ 

(b)  $\left\{\frac{100^n}{(2n)!n!}\right\}_{n=1}^{\infty}$