
Algorithm 1 EmergeSort with Distinct-Window Constraint

Require: $|items| \geq 2(w + 1) + 1$

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1: procedure EMERGESORT(items, cmp, w) ▷ w = window size
2:   /* — access bookkeeping — */
3:   lastSeen[1...n]  $\leftarrow$  0;   tick  $\leftarrow$  1
4:   function MARKACCESS(i, j)
5:     lastSeen[i], lastSeen[j]  $\leftarrow$  tick;   tick  $\leftarrow$  tick + 1
6:   end function
7:   function ISRECENT(i)
8:     return ( $0 < tick - lastSeen[i] \leq w$ )
9:   end function
10:  function COMPARE(i, j)
11:    MARKACCESS(i, j)
12:    return cmp(items[i], items[j])
13:  end function

14:  /* — initial singleton runs — */
15:  mergeQ  $\leftarrow$  deque of ( $\{2i\}, \{2i+1\}, \emptyset$ ) for  $i = 0 \dots \lfloor n/2 \rfloor - 1$ 
16:  danglingRun  $\leftarrow$  {  $n - 1$  } if n odd else  $\emptyset$ 

17:  while mergeQ  $\neq \emptyset$  do
18:    (L, R, M)  $\leftarrow$  FRONT(mergeQ)
19:    if ISRECENT(L.front)  $\vee$  ISRECENT(R.front) then ▷ enforce distinct-window
20:      pool  $\leftarrow$  { k |  $\neg$ ISRECENT(k) }
21:      choose i, j randomly from pool
22:      COMPARE(i, j) ▷ placeholder comparison
23:      continue
24:    end if
25:    POP_FRONT(mergeQ)
26:    if COMPARE(L.front, R.front)  $\leq 0$  then
27:      PUSH_BACK(M, L.pop_front())
28:    else
29:      PUSH_BACK(M, R.pop_front())
30:    end if
31:    if L  $\neq \emptyset$  and R  $\neq \emptyset$  then
32:      PUSH_BACK(mergeQ, (L, R, M))
33:      continue
34:    end if
35:    M  $\leftarrow$  M  $\cup$  L  $\cup$  R
36:    if danglingRun =  $\emptyset$  then
37:      danglingRun  $\leftarrow$  M
38:    else
39:      PUSH_BACK(mergeQ, (M, danglingRun,  $\emptyset$ ))
40:      danglingRun  $\leftarrow \emptyset$ 
41:    end if
42:  end while
43:  return items[indices in danglingRun]
44: end procedure
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