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# Exploring new phases of $\text{Fe}_{3-x}\text{Co}_x\text{C}$ for rare-earth-free magnets

S Q Wu<sup>1,2</sup>, B Balamurugan<sup>3</sup>, X Zhao<sup>1</sup>, S Yu<sup>1,2</sup>, Manh Cuong Nguyen<sup>1</sup>,  
Y Sun<sup>1</sup>, S R Valloppilly<sup>3</sup>, D J Sellmyer<sup>3</sup>, K M Ho<sup>1</sup> and C Z Wang<sup>1</sup>

<sup>1</sup> Ames Laboratory, US DOE and Iowa State University, Ames, IA 50011, United States of America

<sup>2</sup> Department of Physics, Collaborative Innovation Center for Optoelectronic Semiconductors and Efficient Devices, Xiamen University, Xiamen 361005, People's Republic of China

<sup>3</sup> Nebraska Center for Materials and Nanoscience and Department of Physics and Astronomy, University of Nebraska, Lincoln, NE 68588, United States of America

E-mail: [wangcz@ameslab.gov](mailto:wangcz@ameslab.gov)

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## Abstract

Structures, magnetic moments, and magnetocrystalline anisotropy energies of the  $\text{Fe}_{3-x}\text{Co}_x\text{C}$  intermetallic compounds are systematically investigated using adaptive genetic algorithm (AGA) crystal-structure predictions and first-principles calculations. Besides reproducing the known cementite (*Pnma*) structure of  $\text{Fe}_3\text{C}$ , i.e.  $x = 0$ , the AGA searches also capture several new metastable phases within the room-temperature range. In particular, a bainite (*P6<sub>3</sub>22*) structure exhibits the largest magnetic moment among all low-energy structures, and its energy is only 4 meV/atom higher than the cementite (*Pnma*) phase. The atomic structure of the *Pnma*  $\text{Fe}_2\text{CoC}$  phase, i.e.  $x = 1$ , is also identified, and the calculated x-ray diffraction spectrum, magnetocrystalline anisotropy energy, and saturation magnetization based on the structure from our theoretical study are in good agreement with experiment.

Keywords: structure prediction, magnetic properties, rare-earth free, first-principles calculation

(Some figures may appear in colour only in the online journal)

## 1. Introduction

Fe–Co alloys have been continuously attracting intensive studies due to their potential applications in magnetic devices. In particular, these alloys occupy a prominent position in the search for rare-earth-free permanent magnets because of their high intrinsic magnetic moment [1]. However, the cubic symmetry of the alloys produces negligible magnetocrystalline anisotropy energy (MAE), which is unsuitable for permanent magnets. To overcome this problem, considerable effort has been devoted to stabilize non-cubic crystalline structures in these alloys by non-equilibrium synthesis methods or by adding a third element [2–11]. It was first proposed that through straining the unit cell (i.e. changing the *c/a* ratio), remarkably high MAEs could be achieved [1]. Yet up to now, tetragonal distorted Fe–Co alloys can be produced only for thin films with very few monolayers. Alternatively, doping lighter elements such as B, C, or N into the Fe–Co alloys also has been explored to achieve either the stabilization of the

tetragonal distortion [1–5, 10] or the formation of new crystal phases that possess high intrinsic MAE [7–9]. In this work, we report our study on the structures and magnetic properties of carbon-alloyed Fe–Co, specifically on the compositions of  $\text{Fe}_{3-x}\text{Co}_x\text{C}$  ( $0 \leq x \leq 3$ ).

Recently, Choe *et al* [10] investigated the magnetic properties of the electrolytically extracted cementite  $\text{Fe}_3\text{C}$  (S.G. *Pnma*) phase and found its easy axis of magnetization is the *c*-axis, but this material exhibits only a moderate MAE of about 4 Mergs  $\text{cm}^{-3}$  at 5 K. However, it was reported a high blocking temperature,  $T_B = 790\text{ K}$ , for  $\text{CoFe}_2\text{C}$  nanoparticles, indicating a significantly improved magnetic anisotropy in the  $\text{CoFe}_2\text{C}$  phase [7]. Cobalt carbide nanoparticles also have shown appreciable permanent-magnetic properties [12], but these nanoparticles are composed of  $\text{Co}_3\text{C}$  having cementite (*Pnma*) structure along with  $\text{Co}_2\text{C}$  phase [12, 13]. It is worth noting that crystalline phases prepared by thin-film and nanoparticle synthesis techniques also can be formed with non-equilibrium fabrication methods [14]. In addition,

these methods increase the prospect to obtain new phases/structures, which may exhibit desirable magnetic properties. In this regard, a comprehensive knowledge about not only the ground state but also various metastable crystalline structures in a given chemical composition would be very useful for guiding experimental investigations in the design and discovery of novel magnetic materials.

Using adaptive genetic algorithm (AGA) and first-principles calculations,  $\text{Fe}_{3-x}\text{Co}_x\text{C}$  ( $0 \leq x \leq 3$ ) is studied systematically in this work. Several new metastable phases which can be stable within the room-temperature range are captured. In addition, a bainite ( $P6_322$ ) structure exhibits the largest magnetic moment among all the low-energy structures from our AGA search, and its energy is only 4 meV/atom higher than the cementite ( $Pnma$ ) phase. The atomic structures and MAEs of the  $Pnma$  phase for  $\text{Fe}_2\text{CoC}$  are also determined and a good agreement is found between our experiments and theoretical calculations.

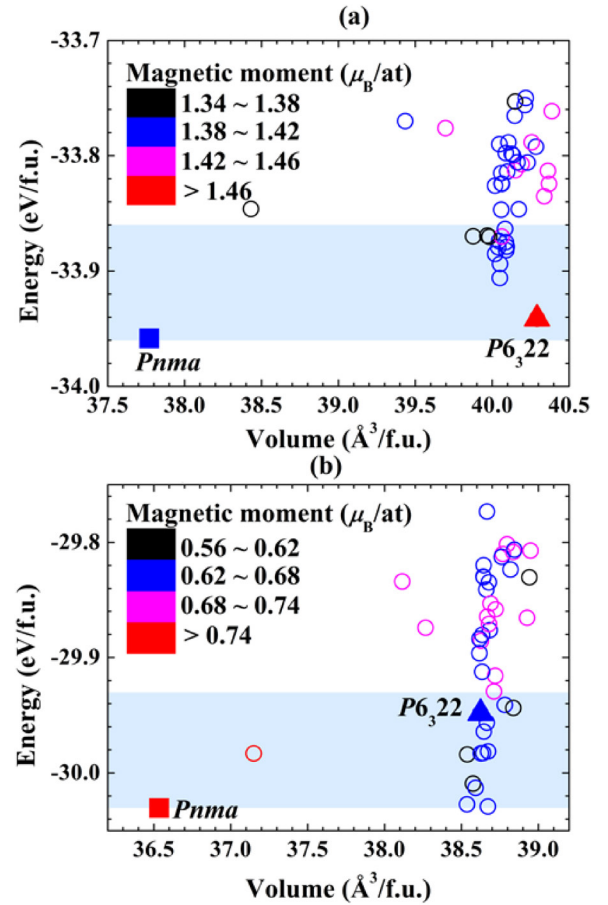
## 2. Methods

In this paper, the low-energy structures of binary and ternary  $\text{Fe}_{3-x}\text{Co}_x\text{C}$  ( $0 \leq x \leq 3$ ) material systems were determined by global search using the AGA method [15]. In the AGA method, the configuration space of the crystal structures is explored by fast genetic algorithm searches using auxiliary classical potentials. The auxiliary classical potential is updated on-the-fly in an iterative process where the parameters of the classical potentials are adjusted by comparing the results of the energies, forces and stresses of the structures from the classical potentials with those of the DFT calculations. The potential fitting is performed using a force-matching method with the stochastic simulated annealing algorithm as implemented in the POTFIT code [16, 17]. In this study, classical potentials in the form based on the embedded-atom method (EAM) are used. The DFT calculations were performed using the Vienna *ab initio* simulation package (VASP) [18, 19], which is based on the spin-polarized density-functional theory, the plane-wave basis and the projector augmented wave (PAW) representation. The exchange-correlation functional is treated within the generalized-gradient approximation (GGA), in the form of Perdew–Burke–Ernzerhof (PBE) [20]. A 400 eV kinetic-energy cutoff was chosen for the plane-wave basis set, and Brillouin-zone integrations were carried out using the Monkhorst–Pack scheme [21] with  $k$ -point mesh resolution of  $2\pi \times 0.03 \text{ \AA}^{-1}$ .

## 3. Results and discussion

### 3.1. Binary $\text{Fe}_3\text{C}$ and $\text{Co}_3\text{C}$

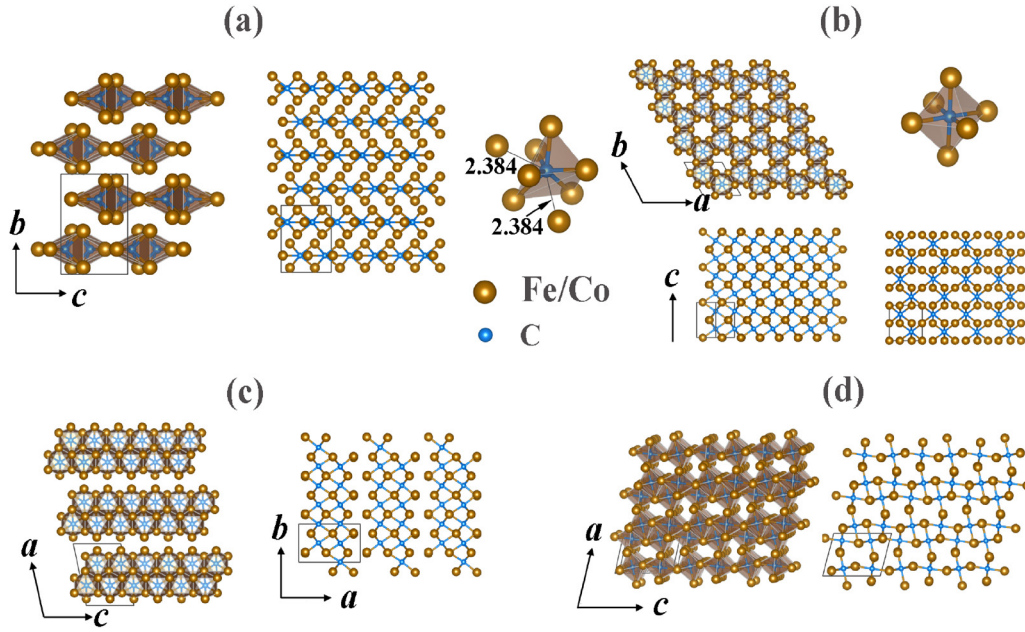
Crystal structures of  $\text{Fe}_3\text{C}$  binary alloy with unit cells containing up to 4 formula units (f.u.) are searched using our AGA method. The energy *versus* volume for the low-energy structures obtained from our AGA search is shown in figure 1(a). Both  $\theta$ - $\text{Fe}_3\text{C}$  (cementite) and  $\varepsilon$ - $\text{Fe}_3\text{C}$  (bainite) phases are found in our optimized structure pool. The orthorhombic



**Figure 1.** Energy versus volume for the low-energy structures of (a)  $\text{Fe}_3\text{C}$  and (b)  $\text{Co}_3\text{C}$  obtained from the AGA searches. The  $\theta$  ( $Pnma$ ) and  $\varepsilon$  ( $P6_322$ ) phases are highlighted with the square and triangle, respectively. The colors used for the symbols are related to the magnitude of the magnetic moment of each structure as indicated by the color bar in the figure.

$\theta$ - $\text{Fe}_3\text{C}$  (S.G.  $Pnma$ ,  $Z = 4$ ) is found to be the lowest-energy structures for  $\text{Fe}_3\text{C}$  system, while  $\varepsilon$ - $\text{Fe}_3\text{C}$  ( $P6_322$ ) is a metastable one with its energy only around 4 meV/atom higher compared to  $\theta$ - $\text{Fe}_3\text{C}$  phase. We note that the volume of the  $\varepsilon$ - $\text{Fe}_3\text{C}$  ( $P6_322$ ) phase ( $40.29 \text{ \AA}^3/\text{f.u.}$ ) is much larger than that of the  $\theta$ - $\text{Fe}_3\text{C}$  ( $Pnma$ ) phase ( $37.77 \text{ \AA}^3/\text{f.u.}$ ). It is also interesting to note that almost all the low-energy structures obtained from the AGA search have a volume similar to that of the  $\varepsilon$ - $\text{Fe}_3\text{C}$  ( $P6_322$ ) phase.

We found that most of the low-energy structures obtained from our AGA search can be viewed as Fe layers derived from a hexagonal close packed (HCP) structure, with C atoms occupying interstitial sites. As shown in figure 2(a), the Fe atoms in the structure of  $\theta$ - $\text{Fe}_3\text{C}$  arrange in pleated layers, which is much distorted from the HCP structure. The calculated lattice constants (5.027, 6.713, 4.477  $\text{\AA}$ ) match well with the experimental values (5.0825(2), 6.733(1), 4.5119(3)  $\text{\AA}$ ) [22] and the previous calculated results (5.0368, 6.7203, 4.4818  $\text{\AA}$ ) [23], (5.058, 6.703, 4.506  $\text{\AA}$ ) [24].  $\varepsilon$ - $\text{Fe}_3\text{C}$  crystallizes in the hexagonal space group  $P6_322$  (S.G. # 182) with two formula units ( $Z = 2$ ) per unit cell, where six Fe atoms and two carbon atoms are in the interstices as shown in figure 2(b) [25, 26]. Besides the two phases mentioned above, more than 10

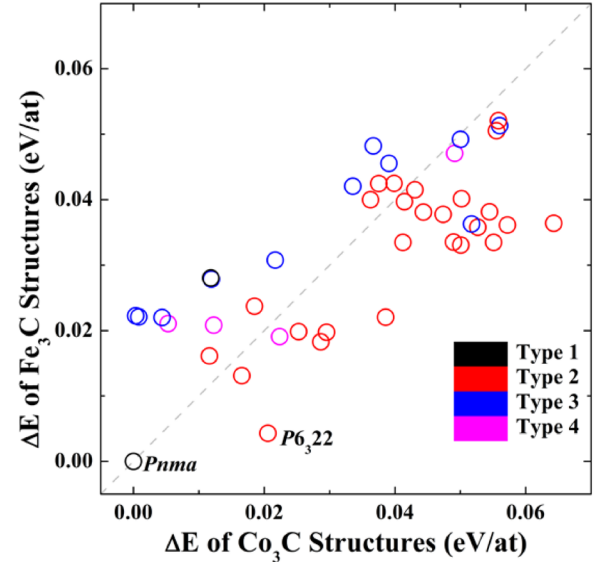


**Figure 2.** Some typical low-energy structures of  $\text{Fe}_3\text{C}$  and  $\text{Co}_3\text{C}$ . (a)  $Pnma$  (type 1), (b)  $P6_322$  (type 2), (c)  $P2_1/c$  (type 3),  $P-1$  (type 4).

metastable phases are found in the room-temperature window (the light-blue shaded region) from the ground-state  $Pnma$  structure as shown in figure 1(a).

As one can see from figure 1, the low-energy structures of  $\text{Fe}_3\text{C}$  and  $\text{Co}_3\text{C}$  obtained from our AGA search are clearly divided into a small volume group and a larger volume group. These low-energy structures can be further classified into four types of structures as shown in figure 2, where one typical structure of each type is shown. Type 1 structures locate in the small-volume region, i.e. with higher atomic density, while all the other three types belong to the large-volume group. The coordination of C atoms in Type 1 structures is  $\text{CFe}_{6+2}$ , i.e. six nearest Fe atoms form a triangular prism with a C atom in the center, while the other two Fe atoms form relatively larger C–Fe bonds with the centered C atom as shown in figure 2(a). In all the other three type structures, Fe atoms form HCP AB stacking layers with C atoms occupy different interstitial sites of the HCP lattice and result in different structure types (Type 2, 3 & 4). In Type 2 structure, the distribution of C atoms is more uniform which leads to relatively high-symmetry structure. Type 3 structures can be considered as ‘layered’ structures, while the Fe lattice of Type 4 structure is more distorted due to inhomogeneous distribution of C atoms. Although the Type 1  $Pnma$  structure is the lowest-energy structure, majority of the low-energy structures belong to Type 2 and Type 3. If we plot the energies of these 4 structural types using different colors as shown in figure 3, we can see that the Type 2 structures are energetically more favorable for the  $\text{Fe}_3\text{C}$  structures than for the  $\text{Co}_3\text{C}$  structures, while the opposite is true for the Type 3 structures.

The magnetic moments of the different  $\text{Fe}_3\text{C}$  and  $\text{Co}_3\text{C}$  structures are shown in figure 1 and table 1. Bainite  $\text{Fe}_3\text{C}$  (S.G.  $P6_322$ ) exhibits the largest magnetic moment ( $1.48 \mu_B/\text{at}$ ) among all the structures in the  $\text{Fe}_3\text{C}$  pool, yet its energy is only 4 meV/atom higher than the cementite ( $Pnma$ ) phase, which has a lower magnetic moment ( $1.38 \mu_B/\text{at}$ ). In the



**Figure 3.** Correlation between the relative energies of  $\text{Fe}_3\text{C}$  and  $\text{Co}_3\text{C}$  structures. The energies of  $Pnma$   $\text{Fe}_3\text{C}$  and  $Pnma$   $\text{Co}_3\text{C}$  are taken as references, respectively.

$\text{Co}_3\text{C}$  system, the most stable phase, i.e. cementite, exhibits the largest magnetic moment ( $0.78 \mu_B/\text{at}$ ) and also the largest MAE of  $8.1 \text{ Mergs cm}^{-3}$  among all the  $\text{Co}_3\text{C}$  structures in the pool. The calculated MAE for  $Pnma$   $\text{Fe}_3\text{C}$  is relatively small ( $0.5 \text{ Mergs cm}^{-3}$ ), which is smaller than the experimental value [10]. The largest MAE among all the  $\text{Fe}_3\text{C}$  structures in the pool is for the  $Pm$  phase with a value of  $12.4 \text{ Mergs cm}^{-3}$ .

### 3.2. Ternary $\text{Fe}_{3-x}\text{Co}_x\text{C}$

As shown above,  $\text{Fe}_3\text{C}$  and  $\text{Co}_3\text{C}$  compounds exhibit different magnetic properties, including magnetic moments and MAEs, even for the counterparts with the same crystal structure. It is interesting to investigate the structures and magnetic



**Table 1.** Structural and magnetic properties of Fe<sub>3</sub>C and Co<sub>3</sub>C.

	Space group (SG)	SG #	Moment $\mu_B/\text{at}$	Theo. MAE ( $\mu\text{eV}/\text{at}$ )	Theo. MAE (Mergs $\text{cm}^{-3}$ )	Expt. MAE (Mergs $\text{cm}^{-3}$ )	Structure type
Fe <sub>3</sub> C (cementite)	<i>Pnma</i>	62	1.38	3	0.5	4.05 <sup>a</sup>	Type 1
Fe <sub>3</sub> C (bainite)	<i>P6<sub>3</sub>22</i>	182	1.48	36	5.7		Type 2
Fe <sub>3</sub> C	<i>Pm</i>	6	1.43	78	12.4		Type 4
Co <sub>3</sub> C	<i>Pnma</i>	62	0.78	46	8.1		Type 1
Co <sub>3</sub> C	<i>P6<sub>3</sub>22</i>	182	0.69	1	0.2		Type 2
Co <sub>3</sub> C	<i>P2<sub>1</sub>/c</i>	14	0.65	40	7.0		Type 3

<sup>a</sup>Ref. [10].

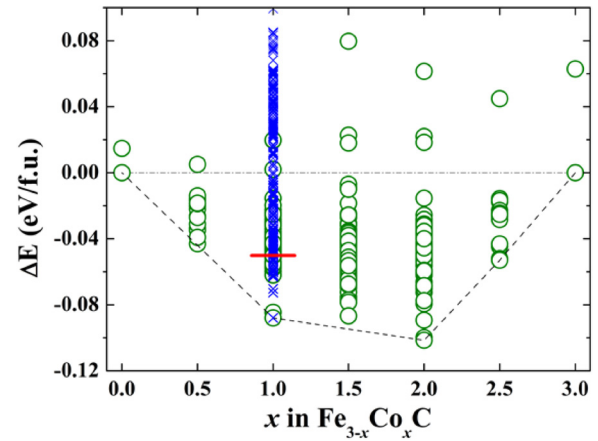
properties of M<sub>3</sub>C compounds with mixed Fe/Co ratios in the M sites. We therefore studied ternary Fe<sub>3-x</sub>Co<sub>x</sub>C using the AGA method (for  $x = 1$ ) and by substitution (for  $x = 0.5, 1.0, 1.5, 2.0, 2.5$ ) based on the several low-energy structures found in the binary systems. A convex hull of formation energies relative to the *Pnma* Co<sub>3</sub>C and *Pnma* Fe<sub>3</sub>C phases for ternary Fe<sub>3-x</sub>Co<sub>x</sub>C is given in figure 4. Both AGA and substitution methods found many structures in the ternary system with negative formation energies.

The magnetic moment and MAE of the lowest-energy structure for each ternary Fe<sub>3-x</sub>Co<sub>x</sub>C composition are shown in table 2. Among all these structures, the ones with  $x$  equal to 1.0, 2.0 and 2.5 are stable against phase decomposition as shown in figure 4. The MAEs for these five structures are all quite small. We also list some structures with relatively high MAEs in table 3. The relative energies of these structures are only about 7 meV/atom to 42 meV/atom higher than that of the corresponding lowest-energy structure at the same composition. Therefore, these metastable structures might be synthesized at high temperature or by non-equilibrium synthesis methods.

### 3.3. Fe<sub>2</sub>CoC

We have fabricated Fe<sub>2</sub>CoC alloys using a conventional arc-melting method followed by a melt-spinning process. High purity elements such as Fe, Co and C were arc-melted to form a homogeneous alloy with Fe<sub>2</sub>CoC composition, which was subsequently made into nanocrystalline ribbons via rapid quenching from the melt using the melt-spinning process. For  $x$  equal to 1.0, i.e. Fe<sub>2</sub>CoC, a structure with the *Pnma* space group is found in our AGA pool. Interestingly, the simulated XRD pattern based on the atomic structure of Fe<sub>2</sub>CoC from our theoretical study is in very good agreement with the measured experimental XRD pattern for the melt-spun Fe<sub>2</sub>CoC alloy as shown in figure 5.

The relative intensity of the peak at  $\sim 53^\circ$  in the experimental XRD pattern suggests the existence of another phase, possibly BCC Fe. The comparison in figure 5 indicates that BCC Fe could be the minority phase in the experimental sample which contributes to the high intensity of the peak at  $\sim 53^\circ$ , although the peak position of simulated XRD pattern of BCC Fe is a little bit larger compared to the experiment one. Besides, the fully relaxed *Pnma* structure shows a double peak at  $\sim 53^\circ$ , corresponding to (220) and (031) faces respectively, compared to the ‘merged’ single peak from experiment. In



**Figure 4.** Convex hull of formation energies in ternary Fe<sub>3-x</sub>Co<sub>x</sub>C. The formation energy is defined relative to the *Pnma* Co<sub>3</sub>C and *Pnma* Fe<sub>3</sub>C phases. Red horizontal line shows the energy of *Pnma* Fe<sub>2</sub>CoC whose simulated XRD pattern matches well with the experimental one.

order to estimate the amount of Fe, we have carried out the Rietveld analysis of the experimental XRD pattern as shown in figure 6(a). Note that melt-spun ribbons often exhibit texture effects [27, 28], and thus a minor (001) and (110) texturing was introduced to obtain a better fitting in figure 6(a). This analysis shows a presence of about 90 wt.% Fe<sub>2</sub>CoC phase and 10 wt.% BCC Fe in the experimental sample.

We also have measured the magnetic properties of the melt-spun Fe<sub>2</sub>CoC alloys using a superconducting quantum interference device (SQUID) magnetometer. Figure 6(b) shows the field-dependent magnetization curves measured at 300 K and 10 K. We have applied the law-approach-to-saturation (LAS) method to estimate the magnetocrystalline anisotropy constant  $K_1$  and saturation magnetization  $M_s$  [29]. In this method, the high-field magnetization curves between 20 and 70 kOe were fitted using the equation  $M = M_s(1 - 4K_1^2/15M_s^2H^2) + \chi H$  as shown in figure 6(c), where  $\chi$  is the high-field magnetic susceptibility [29]. This analysis yields  $K_1 = 10$  Mergs  $\text{cm}^{-3}$  and  $M_s = 1190$  emu  $\text{cm}^{-3}$  ( $\approx 1.23 \mu_B/\text{atom}$ ) at 10 K and  $K_1 = 9.1$  Mergs  $\text{cm}^{-3}$  and  $M_s = 1122$  emu  $\text{cm}^{-3}$  ( $\approx 1.16 \mu_B/\text{atom}$ ) at 300 K.

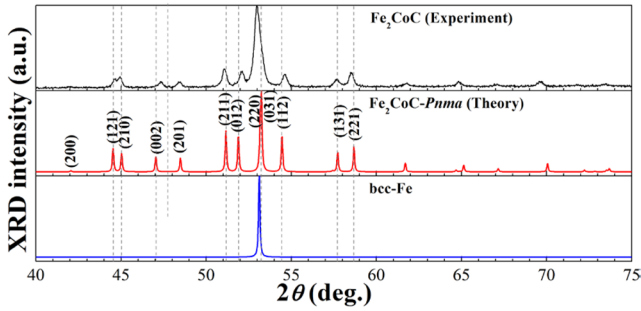
Note that the experimental sample has only a minor Fe fraction of about 10 wt.% ( $\approx 9.9$  vol.% Fe). However, the expanded hysteresis loop measured at 10 K, shown in figure 6(d), indicates a single-phase behavior and suggests a strong exchange coupling between the Fe and Fe<sub>2</sub>CoC phases.

**Table 2.** Magnetic moments and magnetocrystalline anisotropy energies (MAEs) of lowest-energy ternary  $\text{Fe}_{3-x}\text{Co}_x\text{C}$  phases.

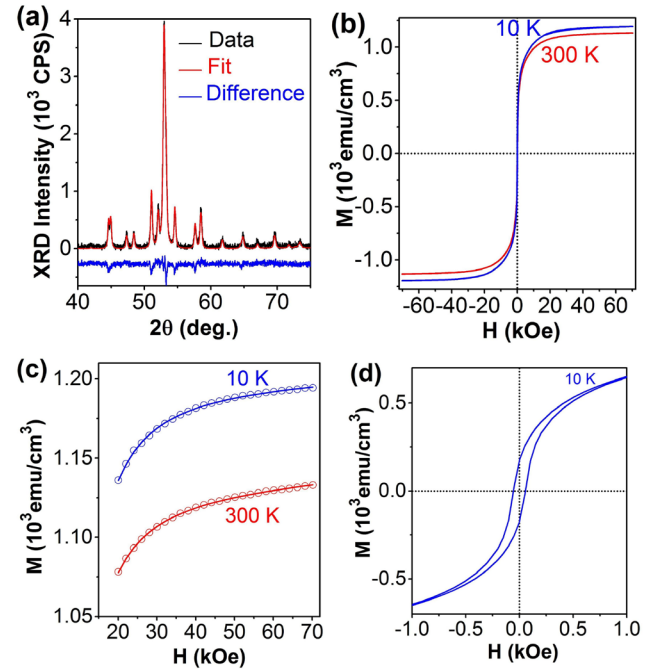
System	Space group (SG)	SG #	$\Delta E$ (meV/f.u.)	Moment ( $\mu_B/\text{at}$ )	Theo. MAE ( $\mu\text{eV}/\text{at}$ )	Theo. MAE (Mergs $\text{cm}^{-3}$ )
$\text{Fe}_{2.5}\text{Co}_{0.5}\text{C}$	$P2_1$	4	-0.043	1.29	15	2.6
$\text{Fe}_2\text{CoC}$	$P2_1/c$	14	-0.088	1.23	9	1.5
$\text{Fe}_{1.5}\text{Co}_{1.5}\text{C}$	$P2_1$	4	-0.087	1.11	5	0.9
$\text{FeCo}_2\text{C}$	$Pna2_1$	33	-0.102	0.96	15	2.6
$\text{Fe}_{0.5}\text{Co}_{2.5}\text{C}$	$P2_1$	4	-0.053	0.89	19	3.3

**Table 3.** Magnetic properties of ternary  $\text{Fe}_{3-x}\text{Co}_x\text{C}$  phases with relatively higher MAEs.

System	Space group (SG)	SG #	$\Delta E$ (meV/f.u.)	Moment $\mu_B/\text{at}$	Theo. MAE ( $\mu\text{eV}/\text{at}$ )	Theo. MAE (Mergs $\text{cm}^{-3}$ )	Expt. MAE (Mergs $\text{cm}^{-3}$ )
$\text{Fe}_{2.5}\text{Co}_{0.5}\text{C}$	$C2$	5	-0.015	1.38	56	9.0	
$\text{Fe}_2\text{CoC}$	$Pnma$	62	-0.050	1.18	38	6.5	9.6
$\text{Fe}_2\text{CoC}$	$C2$	5	0.022	1.29	46	7.4	
$\text{Fe}_{1.5}\text{Co}_{1.5}\text{C}$	$P321$	150	0.080	1.15	85	13.7	
$\text{Fe}_{1.5}\text{Co}_{1.5}\text{C}$	$Pm$	6	0.023	1.11	32	5.5	
$\text{FeCo}_2\text{C}$	$P1$	1	-0.060	1.00	40	6.9	

**Figure 5.** Simulated and experimental XRD patterns. Gray dashed lines indicate the peak positions of  $Pnma$  phase with experimental lattice constants.

For a two-phase exchange-coupled nanocomposite system, the resultant magnetization can be generally written as  $f_h M_s$  (hard) +  $f_s M_s$  (soft).  $f_h$  and  $M_h$  (hard) and  $f_s$  and  $M_s$  (soft) are the volume fractions and saturation magnetizations of the hard and soft phases, respectively. By using the equation for the resultant magnetization, experimental  $M_s$  values determined from the LAS analysis for the melt-spun alloy having  $\text{Fe}_2\text{CoC}$  and Fe phases, and standard  $M_s$  value for Fe (about  $1710 \text{ emu cm}^{-3}$ ) [30], we calculated the  $M_s$  values for the individual  $\text{Fe}_2\text{CoC}$  phase in the ribbon sample as about  $1133 \text{ emu cm}^{-3}$  ( $\approx 1.17 \mu_B/\text{atom}$ ) at 10 K and  $1057 \text{ emu cm}^{-3}$  ( $\approx 1.09 \mu_B/\text{atom}$ ) at 300 K. Similarly, we also estimated the anisotropy constant of the  $\text{Fe}_2\text{CoC}$  phase by taking into account of the minority Fe phase in the melt-spun alloy. Since Fe has a very low anisotropy field (0.6 kOe) [30], the slope of the high-field magnetization curves used for LAS analysis in figure 6(c) mainly originates from the magnetic anisotropy of the hard  $\text{Fe}_2\text{CoC}$  phase, in addition to the high-field magnetic susceptibility. Thus, by considering only the individual magnetization of the  $\text{Fe}_2\text{CoC}$  phase in the melt-spun alloy,  $K_1$  for  $\text{Fe}_2\text{CoC}$  is semiquantitatively estimated as about  $9.6 \text{ Mergs cm}^{-3}$  at 10 K and about  $8.6 \text{ Mergs cm}^{-3}$  at 300 K.

**Figure 6.**  $\text{Fe}_2\text{CoC}$  alloys: (a) experimental XRD pattern and the Rietveld fit. The curve at the bottom is the difference between the measured pattern and the fit. (b) Hysteresis loops measured at 300 K and 10 K. (c) An estimation of magnetic anisotropy constant  $K_1$  and saturation magnetization  $M_s$  from the high-field region of the magnetization curves using the law of approach to saturation method. The open spheres and lines represent the corresponding experimental data and fitting, respectively. (d) The expanded hysteresis loop measured at 10 K.

The experimental magnetic moments obtained for  $\text{Fe}_2\text{CoC}$  are in very good agreement with the theoretical value ( $1.18 \mu_B/\text{atom}$ ). Although the theoretical MAE value ( $6.5 \text{ Mergs cm}^{-3}$ ), as shown in table 3, is somewhat lower than the experimental one for the  $\text{Fe}_2\text{CoC}$  phase ( $9.6 \text{ Mergs cm}^{-3}$ ), the atomic structure matches very well with the experimental one. Previously,

**Table 4.** Structural parameters of *Pnma* Fe<sub>2</sub>CoC.

Fe <sub>2</sub> CoC	Theo.	Expt.
Space group	<i>Pnma</i>	
( <i>a</i> , <i>b</i> , <i>c</i> ) (Å)	(5.0245, 6.7084, 4.4676)	(5.055, 6.756, 4.505)
Fe 8 <i>d</i>	(0.1787, 0.5692, 0.8327)	
Co 4 <i>c</i>	(−0.0354, 0.2500, 0.6568)	
C 4 <i>c</i>	(0.1256, 0.2500, 0.0494)	

Qian *et al* [31] have also reported the magnetic properties of *Pnma* Fe<sub>2</sub>CoC material, and given relatively larger atomic magnetic moment and the MAE comparing with those from our experiments, which could be due to the GGA + U approach used in their work. In addition, our predicted structural parameters together with the experimental lattice parameters of *Pnma* Fe<sub>2</sub>CoC are presented in table 4.

#### 4. Conclusions

In conclusion, stable and metastable structures, and magnetic properties for binary and ternary (Fe, Co)<sub>3</sub>C systems have been studied by combining the AGA method with density-functional theory calculations and experimental synthesis and characterization. The detailed structural properties of M<sub>3</sub>C systems have been analyzed. Besides reproducing the known cementite (*Pnma*) structure of Fe<sub>3</sub>C, the AGA searches also capture several new metastable phases within the room-temperature range. In particular, a bainite (*P6<sub>3</sub>22*) structure exhibits the largest magnetic moment among all the structures in the Fe<sub>3</sub>C pool, yet its energy is only 4 meV/atom higher than that of the cementite (*Pnma*) phase. The relative stabilities among the structures for Co<sub>3</sub>C are quite different from those for Fe<sub>3</sub>C system, but the cementite is still the ground-state phase. Cementite Co<sub>3</sub>C exhibits the largest magnetic moment (0.78  $\mu_B$ /at) and also the largest magnetocrystalline anisotropy energy among all the Co<sub>3</sub>C structures. We also identify the atomic structures of the *Pnma* phase for Fe<sub>2</sub>CoC. The experimental x-ray spectrum for Fe<sub>2</sub>CoC can be understood by combining the *Pnma* Fe<sub>2</sub>CoC that found in our AGA search with a minor BCC Fe phase.

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