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Key Points:

- A deep-learning potential is developed to accurately determine CaSiO₃ perovskite (CaPv)'s tetragonal-to-cubic phase boundary under lower-mantle conditions
- CaPv should exhibit solely a cubic phase throughout the entire lower mantle
- The tetragonal-to-cubic transition in CaPv is not a viable explanation for the mid-mantle seismic scatterers/reflectors or large low-shear-velocity provinces

Supporting Information:

Supporting Information may be found in the online version of this article.

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Deep-Learning-Based Prediction of the Tetragonal \rightarrow Cubic Transition in Davemaoite

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Abstract Davemaoite, that is, CaSiO₃ perovskite (CaPv), is the third most abundant phase in the lower mantle and exhibits a tetragonal-cubic phase transition at high pressures and temperatures. The phase boundary in CaPv has recently been proposed to be close to the cold slab adiabat and cause mid-mantle seismic wave speed anomalies (Thomson et al., 2019, https://doi.org/10.1038/s41586-019-1483-x). This study utilized accurate deep-learning-based simulations and thermodynamic integration techniques to compute free energies at temperatures ranging from 300 to 3,000 K and pressures up to 130 GPa. Our results indicate that CaPv exhibits a single cubic phase throughout lower-mantle conditions. This suggests that the phase diagram proposed by Thomson et al. requires revision, and mid-mantle seismic anomalies are likely attributable to other mechanisms.

Plain Language Summary Davemaoite, also known as calcium silicate perovskite (CaPv), is one of the most abundant minerals in Earth's lower mantle. It can exist in tetragonal and cubic crystal structures, depending on the pressure and temperature conditions. Determining the crystalline phase of CaPv is important for interpreting seismic observations of the lower mantle. A recent study (Thomson et al., 2019, https://doi.org/10.1038/s41586-019-1483-x) suggested that CaPv's tetragonal-to-cubic transition could cause mid-mantle seismic anomalies. However, this phase transition has been a topic of debate. Previous studies have attempted to determine the phase boundary using ab initio methods. The computational cost and challenges associated with handling strong anharmonicity limited these approaches' accuracy and predictive power. In this study, we utilized deep learning and thermodynamic integration techniques to accurately compute the tetragonal to cubic phase boundary of CaPv across the lower mantle pressure range. Our results satisfactorily explain previous experimental measurements and support the notion that CaPv remains in the cubic phase across lower mantle conditions. These findings challenge the previously proposed phase diagram by Thomson et al. and suggest that mid-mantle seismic scatterers/reflectors or large low-shear-velocity provinces in the lower mantle cannot be attributed to this transition in CaPv.

1. Introduction

CaSiO₃ perovskite (CaPv) is the third most abundant phase in a pyrolitic lower mantle and accounts for 24–29 vol% and 5–10 vol% of basaltic and pyrolitic assemblages, respectively (McDonough & Sun, 1995; Valencia-Cardona et al., 2017). Thermodynamic and thermoelastic properties of CaPv phases are crucial for a better understanding of Earth's interior, particularly for understanding potential compositional heterogeneities in the mantle and the D" region where basaltic compositions are expected to be abundant (Gréaux et al., 2019; Hirose et al., 2005; Kesson et al., 1994; Wang et al., 2020). Several experiments and theoretical studies have been carried out to unravel CaPv's structure and thermodynamic properties (Caracas et al., 2005; Komabayashi et al., 2007; Li et al., 2006; Prentice et al., 2019; Shim et al., 2002; Stixrude et al., 1996; Sun et al., 2014; Uchida et al., 2009; Zhang & Wentzcovitch, 2021). With increasing temperature, CaPv undergoes a tetragonal (I4/mcm) to cubic ($Pm\overline{3}m$) phase transition. Recent works have confirmed that cubic CaPv is stabilized by its strong anharmonic fluctuations at high temperatures (Prentice et al., 2019; Sun et al., 2014; Zhang & Wentzcovitch, 2021). Because tetragonal and cubic CaPv have rather different sound velocities (Gréaux et al., 2019; Thomson et al., 2019), their stability field under mantle conditions can be crucial to understanding velocity heterogeneities in the mantle if this transition occurs at mantle conditions.

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So far, the tetragonal-to-cubic phase boundary of CaPv under mantle pressures remains controversial. Stixrude et al. first predicted that the tetragonal-to-cubic CaPv transition occurs at temperatures above 2200 K and pressures of 80 GPa (Stixrude et al., 1996). However, Kurashina et al. conducted an experimental study and observed the phase transition at a much lower temperature of approximately 580 K and 50 GPa (Kurashina et al., 2004). It is important to note that the temperature measurements in Kurashina et al. had a significant uncertainty. Follow-up experiments conducted by Ono et al. (2004) and Murakami et al. (2005) using laser-heated DAC with synchrotron X-rays diffraction suggested the transition of CaPv to a cubic structure above 2000 K, while it maintained a tetragonal structure at room temperature. However, these studies did not provide precise phase boundaries at lower mantle conditions. In 2007, Komabayashi et al. performed X-ray diffraction experiments and determined that the transition temperature of CaPv ranged from 490 to 580 K at pressures between 27 and 72 GPa (Komabayashi et al., 2007), consistent with the findings of Ono et al. and Kurashina et al.. However, a study conducted in 2009 presented conflicting results, suggesting that CaPv remains a non-cubic phase up to 18 GPa and 1600 K (Uchida et al., 2009). Theoretical studies conducted by Adams using ab initio molecular dynamics in a metrically cubic supercell found the transition temperature to cubic CaPv to be between 1000 and 2000 K (Adams & Oganov, 2006). Similar conclusions were reached by Stixrude et al. using Landau mean-field potentials (Stixrude et al., 2007). However, Li et al. conducted AIMD and found that the hydrostatically compressed structure remained tetragonal up to 4000 K (Li et al., 2006). Sun et al. demonstrated that cubic CaPv is stabilized at approximately 600 K and 26 GPa (Sun et al., 2014). Overall, the experimental characterization of the phase boundary is challenging because cubic CaPv is not quenchable to ambient conditions (Komabayashi et al., 2007; Sun et al., 2014; Uchida et al., 2009). Ab initio calculations of the phase boundary of CaPv are also highly nontrivial due to strong anharmonicity in this system (Stixrude et al., 1996; Sun et al., 2014; Thomson et al., 2019). Free energy approaches, such as thermodynamic integration (TI) (Alfè et al., 2000) based on purely ab initio molecular dynamics (AIMD) can be used but is computationally intensive, thus only practical for small systems.

In 2019, Thomson et al. observed the tetragonal-to-cubic phase transition in CaPv at \sim 12 GPa through in situ diffraction and identified the reduction of the seismic velocity along with the phase transition (Thomson et al., 2019). To understand the geophysical consequence of this transition, they combined the experimental measurement and ab initio calculations to determine the phase boundary of CaPv at lower mantle pressures. The slope of the CaPv phase boundary was estimated by ab initio free energy calculations as $dT/dP \sim 15$ K/GPa. Using the calculated dT/dP, they extrapolated the experimental data from 12 GPa to the entire lower mantle pressures and found the CaPv undergoes a cubic–tetragonal transition in cold slab assemblages at pressures greater than 90 GPa. Their phase boundary thus was proposed to explain the seismic anomalies in the mantle, such as the midmantle reflectors and large low-shear-velocity provinces (LLSVPs) in the deep mantle (Thomson et al., 2019). However, their theoretical slope of the phase boundary was obtained via an approximated thermodynamic integration method and the data deviated significantly from Komabayashi et al.'s experimental value of \sim 1.1 \pm 1.3 K/GPa (Komabayashi et al., 2007).

Considering the lack of consensus between these studies, it is evident that further investigations are required to gain a deeper understanding of the phase transition in CaPv, though purely ab initio calculations remain challenging. Recently, interatomic potentials developed with machine learning techniques such as Neural Network Potential (NNP) (Behler & Parrinello, 2007), Gaussian Approximation Potential (GAP) (Bartók et al., 2010), onthe-fly Machine Learning Force Field (MLFF) (Jinnouchi et al., 2019), and Deep Potential for Molecular Dynamics (DPMD) (Zhang, Han, Wang, Saidi, et al., 2018) have significantly extended the timescale and length scale of ab initio simulation. These algorithms can incorporate large amounts of computational or experimental data to construct direct mappings from atomic structures to forces and energies, thus saving significant amounts of computational time required for ab initio calculations (Bartók et al., 2010; Behler, 2016; Behler & Parrinello, 2007; Chmiela et al., 2017; Huan et al., 2017; Liu et al., 2023; Morawietz et al., 2016; Rupp et al., 2012; Schütt et al., 2017; Smith et al., 2017; Thompson et al., 2015). Particularly, the DP method has recently shown its ability to capture higher-order anharmonic force constant (Yang et al., 2022), which can be useful in studying the high-temperature properties of strongly anharmonic materials. By combining with molecular dynamics, DP has proven to be effective in the study of several systems under high-PT conditions, for example, MgSiO₃ (Deng et al., 2023; Luo et al., 2021; Wan et al., 2023; Yang et al., 2022), FeSiO melts (Tang et al., 2023; Zhang et al., 2022), δ-AlOOH (Luo et al., 2023), dense lithium (Wang et al., 2023), high-pressure phases of tin (Chen et al., 2023), solid and fluid H₂O (Zhang et al., 2021) etc.

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In this work, we use the DP method to study phase transitions in CaPv at temperatures ranging from 300 to 3000K and pressures up to 130 GPa. We develop DP potentials with an active learning method and demonstrate its accuracy in predicting energies, forces, and vibrational properties at various PT conditions. By combining the DP and the TI methods, we compute the phase boundary between the tetragonal and cubic phases of CaPv throughout the lower mantle's pressure range and discuss its implication on the seismic anomaly in the lower mantle.

2. Methods

2.1. First-Principles Calculations

Ab initio calculations were performed using the Vienna Ab-initio Simulation Package (VASP) (Kresse & Furthmüller, 1996; Kresse & Hafner, 1993), which implements the projector-augmented wave (PAW) (Blöchl, 1994; Perdew et al., 1996) methodology of density functional theory. Functionals with the local density approximations (LDA) (Perdew & Zunger, 1981) and the generalized gradient approximation (GGA) (Perdew et al., 1996) were studied. PAW potentials with valence electronic configurations $3s^23p^64s^2$, $3s^23p^2$, and $2s^22p^4$ for Ca, Si, and O were used. A plane wave energy cutoff of 550 eV and a $2 \times 2 \times 2$ k-point grid for the 40-atom supercell were used, which was shown to be sufficient to achieve convergence in calculating anharmonic phonon dispersions (Zhang & Wentzcovitch, 2021). Two independent DP models, using LDA and GGA data sets, were developed and are referred to as DP-LDA and DP-GGA, respectively. The smooth edition descriptor se_e2_a proposed by Zhang et al. (Zhang, Han, Wang, Car, & E, 2018; Zhang, Han, Wang, Saidi, et al., 2018) was employed to train these models (see training details in Text S1 in Supporting Information S1).

2.2. Phonon Calculations

The harmonic phonon spectrum was calculated using the finite displacement supercell approach implemented in the Phonopy (Togo & Tanaka, 2015). Anharmonic effects were addressed by the phonon quasiparticle method (Zhang et al., 2019). Temperature-dependent anharmonic phonon dispersions were computed by projecting the atomic velocities onto the harmonic phonon eigenvectors of the temperature-dependent equilibrium structure. In this method, the phonon frequencies and corresponding linewidths can be extracted directly from the MD trajectories, as described by Sun et al. (2014). The DP-based molecular dynamics (DPMD) simulations were used to obtain the mode-projected velocity auto-correlation functions (VAF) (Zhang et al., 2014). The simulations were performed using the NVT ensemble and ran for over 60 ps with the time step of 1 fs and a supercell consisting of 40 atoms.

2.3. Thermodynamic Integration Calculation

To calculate the free energies of the I4/mcm and $Pm\overline{3}m$ phases of CaPv, we used a state-of-the-art TI method developed by Freitas et al. (2016). It provides an efficient method to sample the full TI path from the reference state and target state. Using DPMD simulations, we numerically integrated the work from an initial equilibrium state to the final equilibrium state of interest. At a specific (P_0, T_0) condition, the Gibbs free energy of CaPv is

$$G_{\text{CaPv}}(P_0, T_0) = F_{\text{CaPv}}(V_0, T_0) + P_0 V_0, \tag{1}$$

where V_0 is the volume at (P_0,T_0) , which can be obtained from the equation of state (EOS) of CaPv phases calculated from the NVT (constant number of atoms, volume, and temperature ensemble) MD simulations, shown in Figure 2 and Figure S3 in Supporting Information S1. The Helmholtz free energy F_{CaPv} at (V_0,T_0) condition is calculated via TI method through the NVT-MD simulations, as

$$F_{\text{CaPv}}(V_0, T_0) = F_E(V_0, T_0) + \Delta F(V_0, T_0), \tag{2}$$

where $F_E(V_0, T_0)$ represents the Helmholtz free energy of Einstein reference crystal at (V_0, T_0) and $\Delta F(V_0, T_0)$ is the Helmholtz free energy difference at (V_0, T_0) . The Hamiltonian of the Einstein reference crystal is:

$$H_E = \sum_{i=1}^{N} \left[\frac{\mathbf{p}_i^2}{2m} + \frac{1}{2} m \omega^2 (\mathbf{r}_i - \mathbf{r}_i^0)^2 \right], \tag{3}$$

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where ω is the oscillator frequency and r_i^0 is the equilibrium position of particle i. Its Helmholtz free energy at (V_0, T_0) is given by

$$F_E(V_0, T_0) = 3k_{\rm B}T_0 \ln\left(\frac{\hbar\omega}{k_{\rm B}T}\right). \tag{4}$$

To closely match the characteristic vibrational spectrum of the CaPv system, the value of ω was obtained through NVT-MD simulations at (V_0, T_0) conditions. The mean-squared displacement $<(\Delta r)^2>$ of atoms in the CaPv system was used to determine ω based on the equipartition theorem as $m\omega^2=\frac{3k_BT}{<(\Delta r)^2>}$ (Freitas et al., 2016). This approach differs from the method employed in Thomson et al. (2019), where ω was obtained using harmonic force constants with the artificial elimination of imaginary phonon modes. Since our MD simulations already incorporate the effects of anharmonicity, the determination of ω using the mean square displacement (MSD) method introduced by Freitas et al. (2016) provides a more realistic reference state. The TI method (Freitas et al., 2016) provides a continuous path from the Einstein crystal to CaPv. The forward and backward integration processes were employed to enhance the sampling of the transition pathway. The free energy difference $\Delta F(V_0, T_0)$ was computed by NVT-MD simulation at (V_0, T_0) condition, as

$$\Delta F = \frac{1}{2} (W_{\text{Ein}\to\text{CaPv}}^{irr} - W_{\text{CaPv}\to\text{Ein}}^{irr}), \tag{5}$$

where $W_{\text{Ein}\to\text{CaPv}}^{irr}$ is the irreversible work to transform the Hamiltonian from the Einstein crystal to CaPv, which is noted as

$$W_{\text{Ein}\to\text{CaPv}}^{irr} = \int_0^1 \langle U_{CaPv} - U_{Ein} \rangle_{\lambda} d\lambda, \tag{6}$$

where U_{Ein} and U_{CaPv} are the potential energies for the Einstein crystal and CaPv, respectively. λ is the coupling parameter between the Einstein crystal and CaPv, which generates a new potential energy function in TI as $U = \lambda U_{CaPv} + (1 - \lambda)U_{Ein}$. The "forward" and "backward" terms refer to the direction in which the thermodynamic parameter λ is varied during the switching process. The "forward" process (noted as Ein \rightarrow CaPv) refers to varying the parameter λ from an initial value $\lambda = 0$ (Einstein crystal) to a final value $\lambda = 1$ (CaPv), while the "backward" process (CaPv \rightarrow Ein) refers to the reverse. Averaging the work from the forward and backward processes in Equation 5 eliminates systematic errors arising from irreversible work dissipation during the nonequilibrium switching. During this continuous switching process, the parameter λ varies smoothly from 0 to 1 in 100,000 TI-MD steps. A supercell of 2,560 atoms was used to compute the $\Delta F(V_0, T_0)$ for both tetragonal and cubic phases of CaPv. We noted that at the transition temperatures, the tetragonal phase is metastable and its c/a remains unchanged in the MD simulations.

3. Results and Discussion

3.1. Phonon Dispersion and Equation of States

We collected 3,420 unique configurations that capture a variety of local atomic environments from the ab initio data exploration across temperature ranges of 300 to 3,000 K and pressure ranges of 20–130 GPa (see more details in the Text S1 in Supporting Information S1). We split the data set into 80% for training and 20% for validation. To evaluate the accuracy of the DP, the root mean square errors (RMSEs) of energies, atomic forces, and pressures were compared to DFT calculations for the CaPv system. The results, as shown in Figures S1a–S1c in Supporting Information S1, suggest excellent agreement between DP and DFT calculations, with RMSEs of about 2.0 meV/atom for energies, 0.052 eV/Å for forces and 0.2 GPa for pressures. Similar accuracy was also achieved for DP-GGA, as shown in Figures S1d–S1f in Supporting Information S1. The RMSEs of the training and validating sets are similar, suggesting the neural network was not overfitting. Furthermore, the wide energy distribution displayed in Figures S1a and S1d in Supporting Information S1 indicates the complexity of the configuration spaces involved in exploring the potential energy surface.

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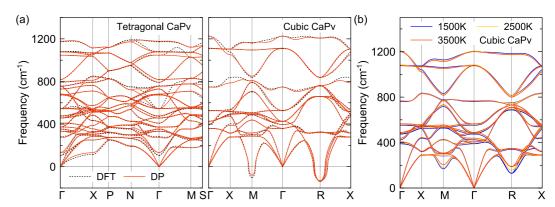


Figure 1. (a) Harmonic phonon dispersions of tetragonal and cubic CaPv at 70 GPa and 0K along high-symmetry lines in the Brillouin zone by DP and DFT with LDA functional. (c) Anharmonic phonon dispersions of cubic CaPv at temperatures of 1500, 2500, and 3500K by DP.

The sensitivity of the phonon dispersion relations to the accuracy of atomic interactions stems from their dependence on the quality of the force constant matrix (dynamical or Hessian matrix). The DP potentials were then applied to determine the interatomic force constants and dynamical matrices via the finite displacement method (Togo & Tanaka, 2015). Figure 1 demonstrates that the DP potential accurately reproduces the harmonic phonon spectra for both tetragonal and cubic CaPv phases. It is noteworthy that the DP method accurately reproduces the soft phonon modes at M(1/2, 1/2, 0) and R(1/2, 1/2, 1/2) in cubic CaPv at 0 K, as shown in Figure 1a. Similar results are also found for DP-PBE potentials, shown in Figure S2 in Supporting Information S1. While soft and unstable modes are present at 0 K in the cubic phase, they can be stabilized at higher temperatures by anharmonic effects (Sun et al., 2014). The temperature-dependent phonon dispersions at 1500, 2500, and 3500K were then calculated using the phonon quasiparticle method (Zhang et al., 2019) with the DP model. As shown in Figure 1b, while most phonon modes showed a weak temperature dependence, significant frequency renormalization was observed at M(1/2, 1/2, 0) and R(1/2, 1/2, 1/2) as the temperature increased, due to strong lattice anharmonicity. In comparison to the harmonic phonon spectrum for cubic CaPv in Figure 1a, the imaginary frequencies at M and R were lifted to positive frequencies, indicating the dynamic stability of the structure. This reproduces the LDA results in Zhang et al. (Zhang & Wentzcovitch, 2021). Similar frequency renormalization is also found with the DP-GGA. The accurate prediction of the anharmonic phonon dispersions demonstrates the ability of our DP to describe both the harmonic lattice dynamics and high-temperature effect, which is crucial for accurately capturing the phase transitions.

We further compare the equation of state (EOS) of CaPv with previous results to validate DP potential across a wide range of *P-T* conditions. Figures 2a and 2b show that the EOSs of cubic CaPv from our DP-LDA and DP-GGA agree well with previous DFT calculations (Kawai & Tsuchiya, 2014; Li et al., 2006; Sagatova et al., 2021) at 300 and 2000 K. The experimental EOS data (Chen et al., 2018; Gréaux et al., 2019; Mao et al., 1989; Ricolleau et al., 2010; Shim et al., 2002; Sun et al., 2016; Thomson et al., 2019; Wang et al., 1996) are mostly between the LDA and GGA results. It is expected because the GGA functional often overestimates the equilibrium volume, while the LDA almost invariably underestimates it. We note that the difference in EOS between the tetragonal and cubic phases of CaPv is very small, as shown in Figure S3 in Supporting Information S1.

3.2. Phase Transition of CaPv

To describe the relative stability between the tetragonal and cubic phases of CaPv, we compute their Gibbs free energy difference $\Delta G(T,p) = G_{tet}(T,P) - G_{cub}(T,P)$ at different P-T conditions. A negative ΔG indicates that the tetragonal phase is more favorable and vice versa. We employ the TI method to compute the G_{tet} and G_{cub} for tetragonal and cubic phases, respectively. The DP-based TI-MD was performed at different temperatures and pressures for the two phases. The energy differences between the CaPv and Einstein crystal reference, denoted as $\Delta U(\lambda) = \langle U_{\text{CaPv}} - U_{ref} \rangle$, were obtained from TI-MD. As shown in Figure 3, the transition paths from the Einstein crystal ($\lambda = 0$) to the CaPv ($\lambda = 1$) were smooth for both tetragonal and cubic phases. The highly nonlinear transition path suggests a significant difference between the two systems. Therefore, one must sample this transition path with a continuously changing λ , which is achieved by the present TI method. Previous studies

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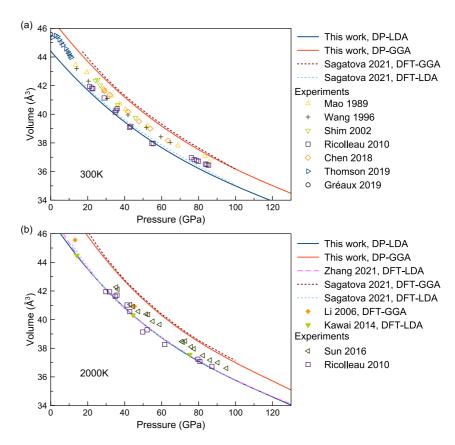


Figure 2. Equation of state of cubic CaPv at (a) 300 K and (b) 2000 K. Solid curves are obtained using DP, and dashed lines are the DFT results (Kawai & Tsuchiya, 2014; Li et al., 2006; Sagatova et al., 2021; Zhang & Wentzcovitch, 2021), and experimental data are taken from Refs.(Chen et al., 2018; Gréaux et al., 2019; Mao et al., 1989; Ricolleau et al., 2010; Shim et al., 2002; Sun et al., 2016; Thomson et al., 2019; Wang et al., 1996).

suggested the size effect can be significant in TI (Sun et al., 2023). To examine this effect, we conducted the TI simulations with different numbers of atoms for both phases in Figure 4a. It shows a simulation size larger than 2,000 atoms can converge the free energy calculation within 0.1 meV/atom. The source of errors in the simulation is discussed in the Text S2 in Supporting Information S1.

We show $\Delta G(T)$ with DP-LDA at 50 GPa in Figure 4b. More $\Delta G(T)$ results at various pressure are shown in the Figure S4 in Supporting Information S1. The tetragonal-cubic phase transition temperatures T_c were obtained from the conditions where $\Delta G(T_c) = 0$. For DP-LDA, the phase boundary exists around 415 K at 25 GPa, 510 K at

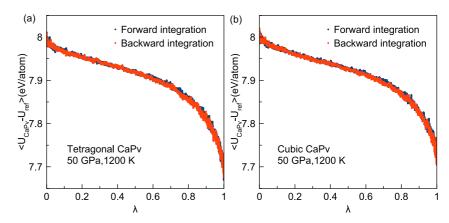


Figure 3. TI calculations at 50 GPa and 1200K. Panels (a–b) show the averaged energy differences between the final system ($\lambda = 1$) and reference system ($\lambda = 0$) in TI-MD simulations for tetragonal and cubic CaPv, respectively.

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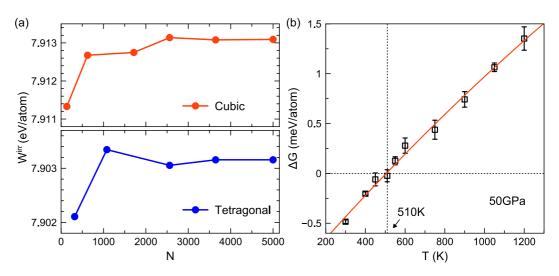


Figure 4. (a) Size effect on the irreversible work with DP-based TI simulations. The circles are W^{irr} measured from the TI with different numbers of atoms, N, in the simulations at 50 GPa and 1200 K. (b) The Gibbs free energy difference between the tetragonal and cubic phase for the CaPv at 50 GPa (See Figure S2 in Supporting Information S1 for more pressures). Negative energy difference indicates that the tetragonal phase is more favorable, and vice versa.

50 GPa, 670 K at 75 GPa, 930 K at 100 GPa, and 1240 K at 125 GPa. We also computed $\Delta G(T)$ with DP-GGA in Figure S5 in Supporting Information S1. For DP-GGA, the phase boundary is around 270 K at 25 GPa, 365 K at 50 GPa, 515K at 75 GPa, 680 K at 100 GPa, and 875 K at 125 GPa. It is worth mentioning that even if the most advanced massively parallel computers are employed, carrying out these simulations using full ab initio calculations is prohibitively time-consuming. With the DP-LDA, we also performed a cooling simulation on cubic CaPv at 125 GPa. As shown in Figure S6 in Supporting Information S1, the cubic phase transformed into the tetragonal phase in the range of 1200–1400 K, consistent with the phase boundary obtained from the free energy calculations.

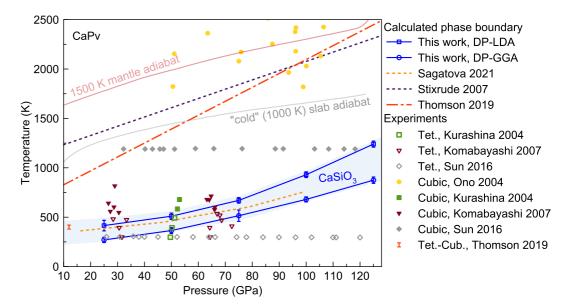


Figure 5. Phase diagram of Ca-perovskite across the mantle pressure range. Previous data includes calculations by Sagatova et al. (2021), Stixrude et al. (2007), Thomson et al. (2019) and experiments by Komabayashi et al. (2007), Kurashina et al. (2004), Ono et al. (2004), Sun et al. (2016), and Thomson et al. (2019). The shaded blue area indicates the uncertainty due to the DFT functional. The brown and gray solid lines depict 1,500 K mantle adiabat and 1,000 K "cold" slab temperature profiles, respectively.

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Figure 5 shows the tetragonal-cubic phase boundary of CaPv obtained from our DP calculations. The DP-LDA results in a higher transition temperature than the DP-GGA by 200-500K. The differences increase with increasing pressure. The tendency of GGA to predict the phase-transition pressure higher than LDA for CaPv is similar to that demonstrated in many other phase-transition studies (Jaffe et al., 2000; Tsuchiya et al., 2004; Yu et al., 2011). Such a tendency can be attributed to the different dependence of the exchange-correlation functional on the electron density in LDA and GGA. Nevertheless, both phase boundaries from LDA and GGA calculations are significantly lower than the earlier calculations from Stixrude et al. (2007) and Thomson et al. (2019) by more than 1000 K at lower mantle pressures. The high computational cost of fully ab initio calculations has forced these studies to rely on approximated free energy calculations. Stixrude et al. (2007) used a Landau potential that relies on a few empirical parameters to fit the ab initio data. This model may not be sufficiently accurate to describe the vanishing free energy difference between the cubic and tetragonal phases near the true critical point. Thomson et al. (2019) used a perturbation method to apply a first-order approximation on the TI as the energy difference between the reference state and CaPv, as $F - F_0 \cong \langle U - U_0 \rangle_0 + \frac{1}{2k_BT} \langle \left[U - U_0 - \langle U - U_0 \rangle_0 \right]^2 \rangle_0$. The accuracy of this equation highly depends on the linearity of the TI path. However, as shown in Figure 3, the TI path from the reference state to CaPv is highly nonlinear, so such an approximation is inaccurate for the CaPv system. Sagatova's DFT result (Sagatova et al., 2021) is similar to ours, where a self-consistent phonon algorithm (SCPH) (Tadano et al., 2014; Tadano & Tsuneyuki, 2015) was used to perform anharmonic phonon calculations.

The difference between LDA and GGA functionals can be treated as the computational uncertainty of the present calculated phase boundary, which provides upper and lower bounds. We consider this region as the confident interval of our calculations due to DFT functionals (blue region in Figure 5). Compared to experimental data, our phase boundary is consistent with all previous measurements (Komabayashi et al., 2007; Kurashina et al., 2004; Ono et al., 2004), including Thomson et al.'s experimental results at 12 GPa (Thomson et al., 2019). The dT/dP slope is ~7 K/GPa, significantly smaller than the calculated results in Thomson et al. (2019).

Our tetragonal-to-cubic boundaries of CaPv lie well below the cold slab geotherm (Shim et al., 2002), where CaPv is supposed to be abundant, or any adiabatic mantle geotherm, suggesting that CaPv should be cubic in all lower mantle environments. Therefore, the tetragonal to cubic transition in CaPv cannot explain the seismic wave speed anomalies in the lower mantle, contrary to the claim of Thomson et al. (2019). The mid-mantle reflectors or scatters may be caused by other mechanisms, for example, the post-stishovite phase transition in pure or aluminous-hydrous silica (Umemoto et al., 2016; Wang et al., 2020) in stagnant subducted slabs (Zhang et al., 2023). Recently, Ko et al. suggested that the dissolution behavior of CaPv in bridgmanite can lead to its disappearance as a separate phase at depths greater than 1,800 km, a new insight into the deep mantle mineralogy (Ko et al., 2022). Irrespective of this dissolution behavior, the problem addressed here is relevant for addressing the origin of seismic scatterers above 1800 km depth.

4. Conclusion

We have implemented DP models for $CaSiO_3$ perovskite using both LDA and GGA functionals. The simulations with the DP model reproduce the harmonic and anharmonic phonon dispersions from DFT calculations. The comparison with experiments suggests that volume versus pressure in EOS is underestimated by the LDA and overestimated by the GGA functionals. Overall, the machine learning approach can describe the strongly anharmonic properties of CaPv with ab initio accuracy. Based on the DP model, we employ the TI method to fully sample the transition path from the reference state of a harmonic crystal to the CaPv phases. The transition path shows strong nonlinearity w.r.t. the integration parameter λ which suggests that TI in this system cannot be approximated as the energy difference between the initial and final states. Therefore, the previously calculated phase boundary in Thomson et al. (2019) is questionable. With the present DP model and TI method, we provide accurate free energy difference between the cubic and tetragonal phases in a large pressure and temperature range close to lower mantle conditions. We determined the tetragonal-to-cubic transition temperatures versus pressure in CaPv and computed the thermodynamic phase boundary. We can satisfactorily explain previous experimental measurements. Based on our phase boundary, the CaPv are cubic at lower mantle conditions. It suggests that the observed seismic velocity anomalies in the mid-mantle and in LLSVPs cannot be explained by the tetragonal-to-cubic phase transition in CaPv and is likely attributable to other mechanisms.

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Data Availability Statement

The authors comply with the AGU's data policy, and the data sets of this paper are available at Zenodo (F. Wu. 2024).

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