

# MH2500 Mini-Quiz

## Question 1

Each game you play is a win with probability  $0 < p < 1$ . You plan to play 5 games, but if you win the fifth game, then you will keep on playing until you lose. Find the expected number of games that you lose.

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## Question 2

Ten balls are to be distributed among 5 urns, with each ball going into urn  $i$  with probability  $p_i$ , where  $\sum_{i=1}^5 p_i = 1$ . Let  $X_i$  denote the number of balls that go into urn  $i$ .

Assume that events corresponding to the locations of different balls are independent. Find  $P(X_1 + X_2 + X_3 = 7)$ .

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## Question 3

Let  $X$  be a discrete random variable such that  $a \leq X \leq b$ . Use the definition of expectation to prove that  $a \leq \mathbb{E}(X) \leq b$ .