

Contacts

2. Phone numbers

Insert (n), Search (n), delete (n)

unsorted array

Searching $\rightarrow \log_2 N + N$

$\log N$

$N + N \log N$

Sorted array
 FIFO
Stack/Queue LIFO

1

N

N

unsorted linked list



N



Sorted list

N

N

N

BST $\Rightarrow \log_2 N$ (Skewed)
 Skewed

++

++

BBst

$\log N_2$

$\log N_2$

$\log N_2$

Count array

$C[300] \Rightarrow T$

$If (C[x])$

$C[x] = 0$

boolean array

1

else

1

false

1

$\hookrightarrow 1$

Direct Access table:

Mobile number \rightarrow 2 digits $\Rightarrow C[90]$

\Rightarrow 10 digits \Rightarrow

10 00, 000 000

999 999 9999

$R \Rightarrow 6000, 00000$

$C[b-a+1]$

$1 = 999 999 9999$

#

Hashing

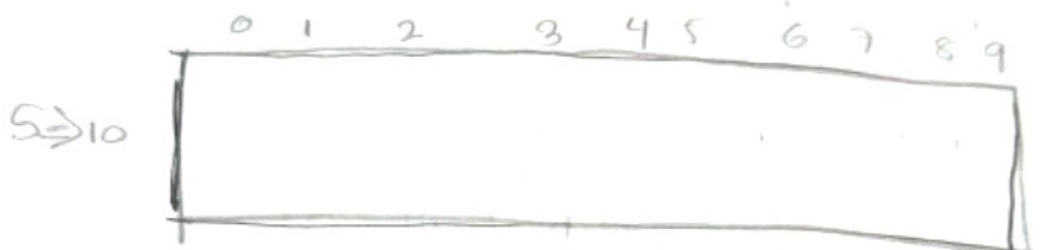
hex: a.i.s

↓
hash function

Phonepe: → Yes bank

< 6-8 years's hours

→ ICICI

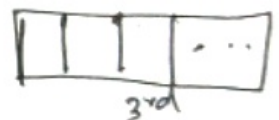


203, 500, 707, 24, 84, 60
└──────────────────┘
mobile numbers ⇒ 6

no is 203

⇒ Size of table is 10

⇒ $203 \div 10 \rightarrow 3$ at Index



Size of table is 10

= $500 \div 10 \Rightarrow$

Collision ⇒ when two different numbers are having
Same hash value

0	203	204	707
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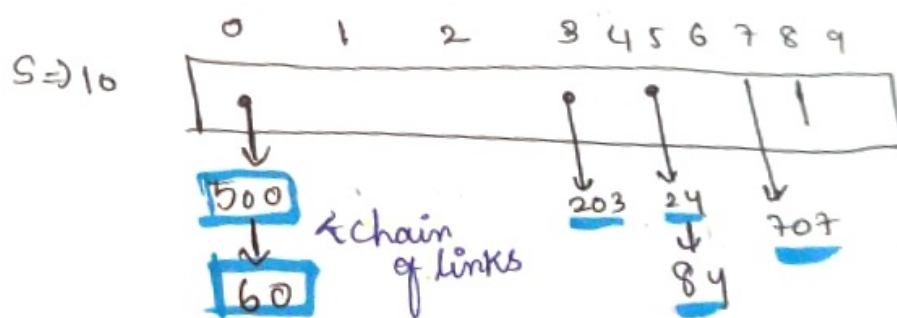
→ Hashing Solve Space related Problem, but collision resolution is Pending

Collision resolution techniques

- 1) Separate chaining
 - Linked List
 - BBST
- 2) Open Addressing
 - Linear Probing
 - Quadratic Probing
 - Double hashing

⇒ 6 → 203, 500, 707, 24, 84, 60

500	203	24	707
0	1	2	3
		4	5
		6	7
		8	9



① Linked List

Insert(n)

4 1
at the head

Search(n)

Delete(n)

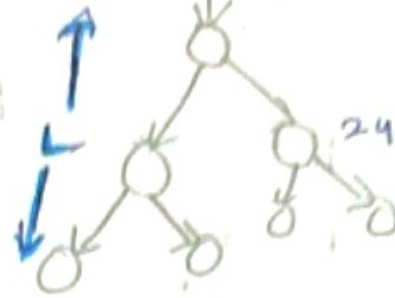
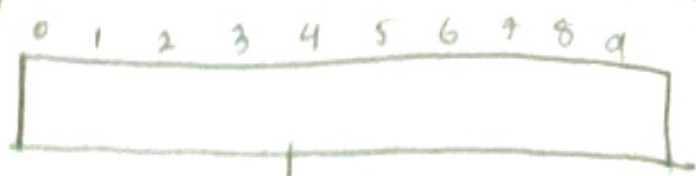
→

2

(balanced binary search)
(2) B.B.S.T

$$H = \log_2 N$$

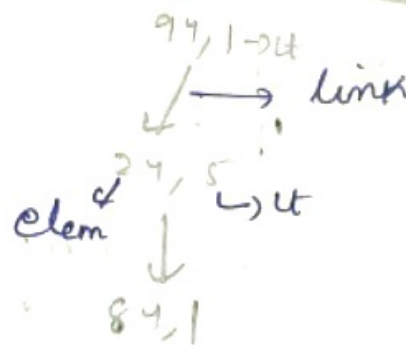
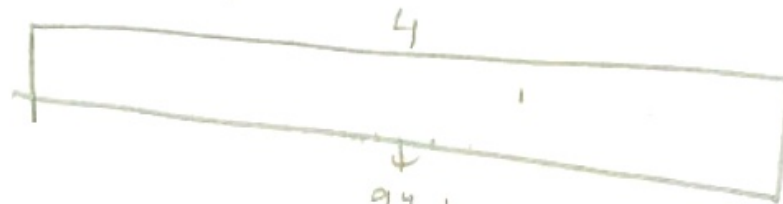
L \rightarrow is height



$24-2$ \rightarrow count (case of duplicate)

Insert $\Rightarrow \log_2 L$, Search $= \log_2 L$, delete $= \log_2 L$

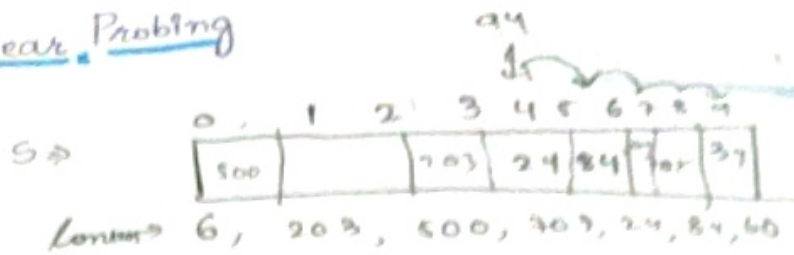
\rightarrow 6 \rightarrow 203, 500, 707, 24, 84, 60, 94, 24, 24, 24
for multiple elements we can take freq and increments
or (duplicates),



\Rightarrow

Insert, delete, Search
L, L, L
(length of link)

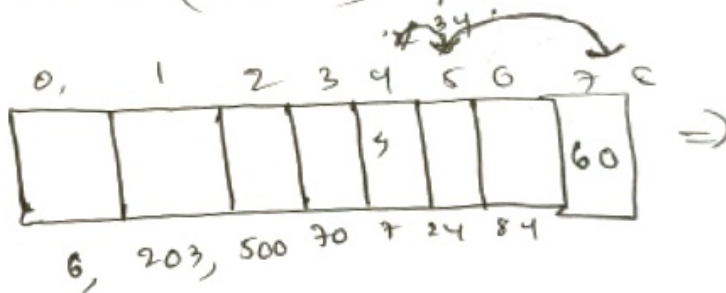
Linear Probing



If occupied it will check for the remaining indices
 If we empty we can put store the value

Quadratic Probing

$$h(x) = (x + i^2) \cdot 10$$



\Rightarrow for $(34 + 0^2) \cdot 10$ already exist
 $(34 + 1^2) \cdot 10 \Rightarrow$ already exist
 $\Rightarrow (34 + 2^2) \cdot 10$
 $\Rightarrow 8^{\text{th}}$ index

Lp Vs Qp

S = 100 → 403, 503, 603, 703, 803, 903

↓
Size of table

Qp: 403 4 7 2 3 4 4
Problem p: 1 2 3 803 7 4
Probes

$$\begin{aligned} & 100 \overline{) 03} \text{ (70} \\ & \quad \underline{700} \\ & \quad \quad 3 \\ & = 704 \checkmark \\ & \quad 705 \checkmark \\ & \quad 706 \checkmark \end{aligned}$$

$$\begin{aligned} & 100 \overline{) 703} \text{ (70} \\ & \quad \underline{700} \\ & \quad \quad 3 \end{aligned}$$

$$\begin{aligned} 703 + (1)^2 &= 704 \\ 703 + (2)^2 &= 707 \\ 703 + (3)^2 &= 712 \end{aligned}$$

$$\begin{aligned} & 100 \overline{) 803} \text{ (80} \\ & \quad \underline{800} \\ & \quad \quad 3 \end{aligned}$$

$$\begin{aligned} & = 803 + 1^2 \\ & 803 + 2^2 = 808 \\ & 803 + 3^2 = \\ & 803 + 4^2 = \end{aligned}$$

$$\begin{aligned} & 100 \overline{) 819} \text{ (80} \\ & \quad \underline{800} \\ & \quad \quad 19 \end{aligned}$$

LP Probes $\rightarrow 0, 1, 2, 3, 4, 4, 5, 6 \rightarrow 28$

QP Probes $\rightarrow 0, 1, 2, 3, 4, 1, 2, 3 \rightarrow 16$
(jumps)

Note:

Quadratic Probing is better when compared to LP.
If cluster is huge it will take time to go in to correct position.



Smaller cluster
less no of steps

Cluster Size & no of Probes

time complexity

Insert

Search

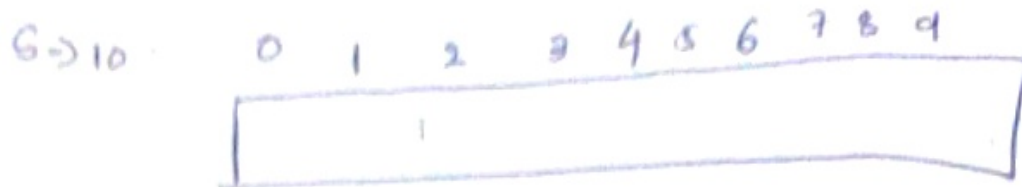
Delete

P = Probes

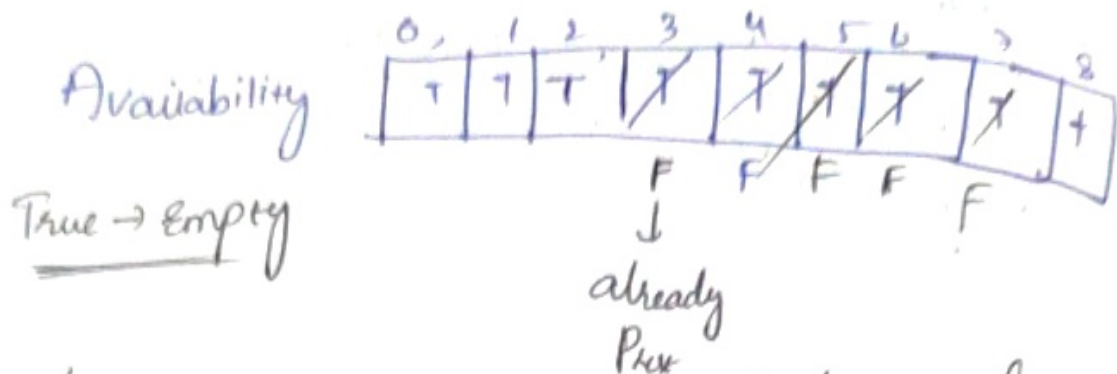
P

P

+



nums → 6, 203, 500, 707, 24, 84



delet → 84 means get the Index and make it is True in Availability array

Search → 34 ⇒ 4 Probe

you → will think 34 is not Present

Problem is we don't differentiate between Empty and delete

- If deleted Keep on Searching
- If Empty Stop Searching **A found!**

3 things

- Empty
- occupied
- Deleted

⇒ taking integer array

- 1) Empty $\rightarrow 0$
- 2) Occupied $\rightarrow 1$
- 3) Deleted $\rightarrow -1$

$\Rightarrow S=10$

500	203	24	84	34	303
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Availability
int

0	1	2	3	4	5	6	7	8	9
1	0	0	-1

deleted

delete $\rightarrow 84 \rightarrow 6$

Search $\rightarrow 34$

3) Double hashing (for cluster)

$$h(x) = h_1(x) + h_2(x)$$

or

$$h_1(x) * h_2(x) \quad \text{some func}$$

$$h_1(x) \Rightarrow \text{linear } (i^2 + x) \% S$$

$$h_2(x) \Rightarrow (x + i^2) \% S, (x + x + i^2) \% S$$

Note:-

$$\{ (x^i) \% S, (x!) \% S, (x^x) \% S \} \text{ bad}$$

$\rightarrow P_{O(n, i)} \rightarrow \log \{ \text{more time complexity} \}$

Good Hash functions

- 1) uniformly distribute the keys over a table
- 2) Easy to compute
- 3)

Final time complexity

<u>Sc</u> → <u>numbers</u>	<u>table size</u>
OA → 100	10 → yes
OA → 100	10 → NO
OA → 100	100 → yes 0%
OA → 100	1000 → yes (90% empty)
OA → 100	10000 → yes (99% empty)

⇒ Higher Size more Search optimization

Internal resizing

double

100 → 200

101 → 200

Class Hashmap {

int ht [100000];

int availability [100000] = 0;

// void insert

int Val = (x+i)/10000;

while loop
i>0,

If (availability[Val] != 1)

ht[Val] = x;

availability[Val] = 1;

}

bool deletion (int n)
void

int y = Search(n);

If (y != -1)

avail[y] = -1;

else

Print("element not found")

int Search(int n) {

=> loop i>0;

int Val = (n+i)/10000;

EMPTY

If (availability[Val] == 0)

return false

found :-

If (availability[Val] == 1 && ht[Val] == n)

Return index

Available array \Rightarrow

0	1	2	3	4	5	6	7	8	9
1	0	0	1	1	1	1	1	0	0

1) Empty $\rightarrow 0$

2) Occupied $\rightarrow 1$

3) Deleted $\rightarrow -1$
arr
S = 10

0	1	2	3	4	5	6	7	8	9
500			203	24	84	34	707		

Elements \rightarrow 6, Elements \rightarrow 203, 500, 307, 24, 84, 34, 707

$i \rightarrow 0, 1, 2, 3, 4, \dots$

$h[i] \rightarrow (x+i) \% S$

$\Rightarrow (203+0) \% 10$

$$= \frac{10 \mid 203}{200} = 3$$

\Rightarrow arr[h[i]] \rightarrow Element

\Rightarrow 500

$\Rightarrow (500+0) \% 10$

$\Rightarrow (500) \% 10$

$\Rightarrow 0 \rightarrow$ Index delete

$= h[0] \Rightarrow 50$

If found.

avail index \square

Index \rightarrow

Search (x)

\rightarrow for $i \rightarrow 0, \dots, n$

int idx = $(x+i) \% 100$

\Rightarrow Empty

if (avail[idx] \neq 0)

return false

If (avail[idx] == 1 and arr[idx] == x)

return true