

#

## Hashing

$$hash = a \% b$$

↓  
hash function

Phonepe: → Yes bank

< 6-8 Year's hours

→ ICICI

$5 \Rightarrow 10$

0	1	2	3	4	5	6	7	8	9

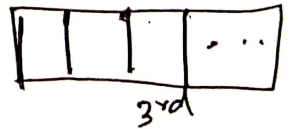
203, 500, 707, 24, 84, 60

mobile numbers  $\Rightarrow 6$

no is 203

$\Rightarrow$  Size of table is 10

$\Rightarrow 203 \% 10 \rightarrow 3$  at Index



Size of table is 10

$$= 500 \% 10 \Rightarrow$$

Collision  $\Rightarrow$  when two different number are having same hash value

0	203	204	707
---	-----	-----	-----

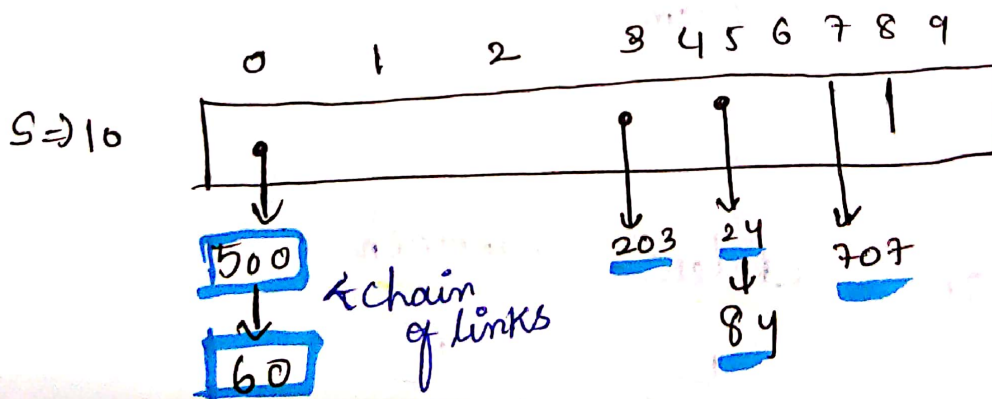
⇒ hashing solve space related Problem, but collision resolution is pending

## Collision resolution techniques

- 1) Seperate chaining → linked list
- 2) open Addressing → BBST
- linear Probing
- Quadratic Probing
- Double hashing

⇒ 6 → 203, 500, 707, 24, 84, 60

16 → collis									
500		203		24				707	
0	1	2	3	4	5	6	7	8	9



### ① linked List

Insert(x)

4 1  
at the head

Search(x)

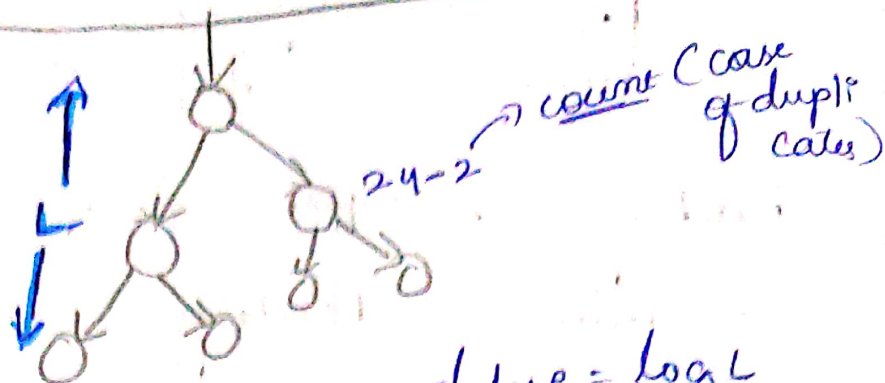
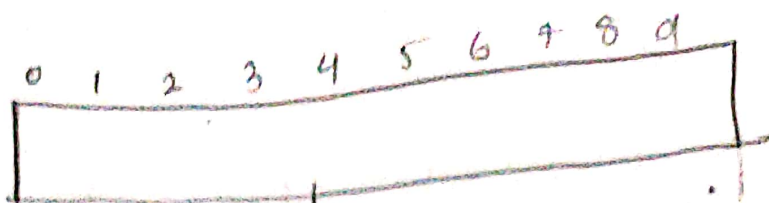
delete(x)  
L

L

(2) B.B.S.T (Balanced binary search)

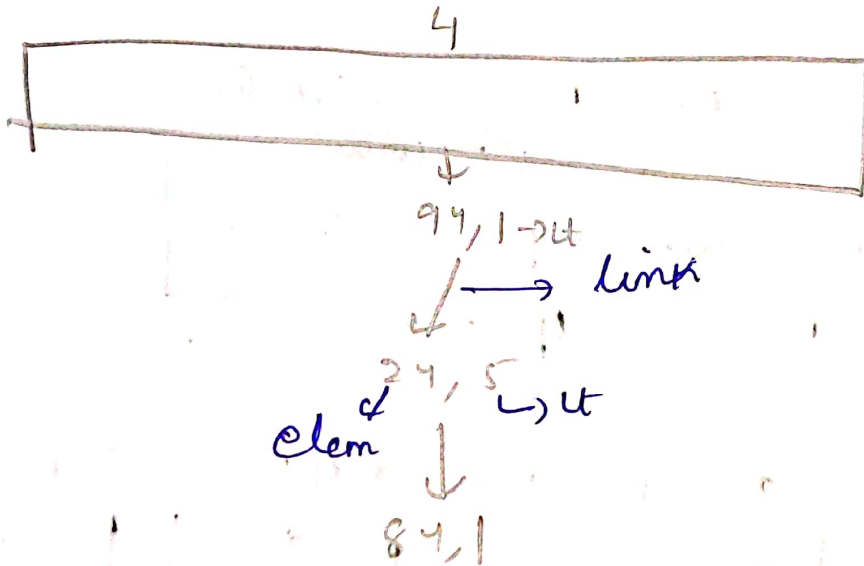
$$H = \log_2 N$$

H  $\rightarrow$  is height



Insert  $\Rightarrow \log_2 L$ , Search  $= \log_2 L$ , delete  $= \log_2 L$

$\rightarrow$  6  $\rightarrow$  203, 500, 707, 24, 84, 60, 94, 24, 24, 24, 24  
for multiple elements we can take freq and increment  
or (duplicates),

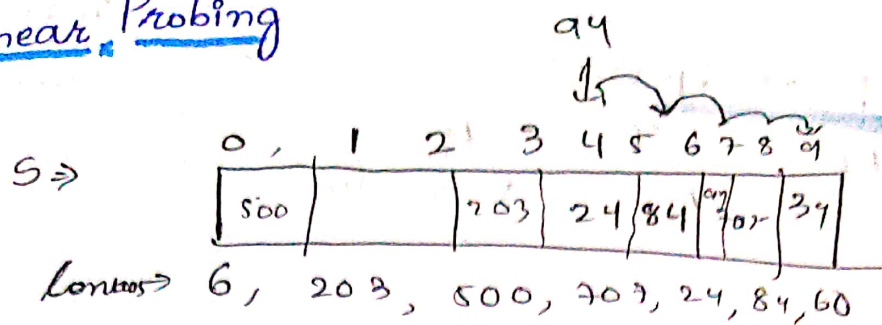


$\Rightarrow$

Insert, delete, Search  
L, L, L  
(Length of link)



## Linear Probing



$$h(x) = (x + i) \% 10 \quad i = 0, 1, 2, \dots$$

$$\Rightarrow (203 + 0) \% 10$$

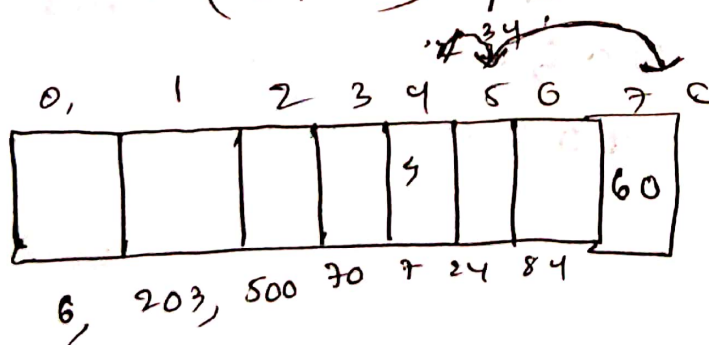
$$\Rightarrow (84 + 0) \% 10 \rightarrow \text{occupied}$$

$$\Rightarrow (84 + 1) \% 10 \rightarrow \text{empty}$$

If occupied it will check for the remaining indexes  
 If we empty we can put store the value.

## Quadratic Probing

$$h(x) = (x + i^2) \% 10$$



$$\Rightarrow \text{for } (34 + 0^2) \% 10$$

already exist

$$(34 + 1^2) \% 10 \Rightarrow$$

already exist

$$\Rightarrow (34 + 2^2) \% 10$$

$\Rightarrow 8^{\text{th}}$  index

Lp Vs Qp probes

$$603 + 0^2 \rightarrow 603$$

$$603 + 1^2 \rightarrow 604$$

$$603 + 2^2 \rightarrow 607$$

Lp:

3

4

5

6

803

904

509, 707

S  $\Rightarrow$  100  $\rightarrow$

403

503

603

703

$\downarrow$

Size of table

Qp:

403

4

7

2

3

7

4

4

6

Problem p: 8

1

2

3

803

Probes

$$100 \overline{) 703} \rightarrow 70$$

$$\underline{700}$$

$$3$$

$\approx$

$$100 \overline{) 03} \rightarrow 70$$

$$\underline{700}$$

$$3$$

$$= 70.4 \checkmark$$

$$70.5 \checkmark$$

$$70.6 \checkmark$$

$$703 + (1)^2 = 704$$

$$703 + (2)^2 = 707$$

$$703 + (3)^2 = 712$$

$$100 \overline{) 803} \rightarrow 80$$

$$\underline{800}$$

$$3$$

$$= 803 + 1^2$$

$$803 + 2^2 = 808$$

$$803 + 3^2 =$$

$$803 + 4^2 =$$

$$10 \overline{) 819} \rightarrow 80$$

$$\underline{800}$$

$$19$$

LP Probes  $\rightarrow 0, 1, 2, 3, 4, 4, 5, 6 \rightarrow 25$

QP Probes  $\rightarrow 0, 1, 2, 3, 4, 1, 2, 3 \rightarrow 16$   
(Jumps)

Note:-

Quadratic Probing is better when compared to LP.

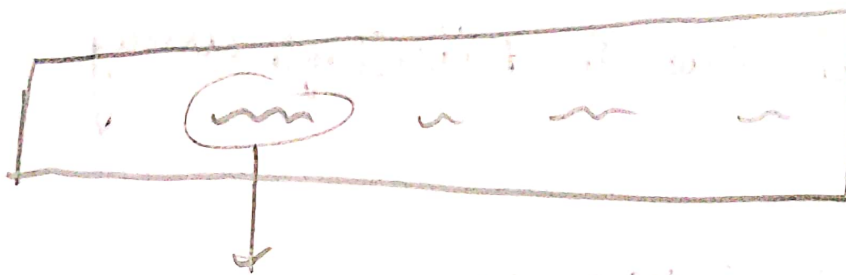
If ~~cluster~~ <sup>cluster</sup> is huge  
 $\Rightarrow$  correct position

cluster Size

LP:



QP



Smaller cluster

less no of steps

cluster Size & no of Probes

time complexity

Insert

Search

Delete

P = Probes

P

P

S → 10:      0    1    2    3    4    5    6    7    8    9

--	--	--	--	--	--	--	--	--	--

runs → 6, 203, 500, 707, 24, 84

Availability

0	1	2	3	4	5	6	7	8
T	T	T	X	X	X	X	X	T

True → Empty

F  
↓  
already  
Present

Delet → 84 means get the Index and make  
it is True in Availability array

Search → 34 ⇒ 4 Probe

You → will think 34 is not Present  
Problem is we don't differentiate between Empty  
and delete

- If deleted Keep on Searching
- If Empty Stop Searching A found

3 things

- Empty
- occupied
- Deleted



⇒ taking Integer array

- 1) Empty  $\rightarrow 0$
- 2) Occupied  $\rightarrow 1$
- 3) Deleted  $\rightarrow -1$

⇒ S=10: 

0	1	2	3	4	5	6	7	8	9
800	203	24	84	34	707				

Availability  
int

0	1	2	3	4	5	6	7	8	9
1	0	0	...		-1				

deleted

delete  $\rightarrow 84 \Rightarrow$

Search  $\rightarrow 34$

### 3) Double hashing (for cluster)

$$h(x) = h_1(x) + h_2(x)$$

or

$$h_1(x) * h_2(x)$$

→ some func

$$h_1(x) \Rightarrow \text{linear } (i^2 + x) \% S$$

$$h_2(x) \Rightarrow (x + i^2) \% S, (x + x + i^2) \% S$$

Note:-  $\{ (x^i) \% S, (x!) \% S, (x^x) \% S \}$  base

→  $Po a(n, i) \rightarrow \log \{ \text{more time complexity} \}$



## Good Hash functions

- 1) uniformly distribute the keys over a table
- 2) Easy to compute
- 3)

### Final time Complexity

<u>Sc</u> → <u>numbers</u>	<u>table Size</u>
OA → 100	10 → Yes
OA → 100	10 → NO
OA → 100	100 → Yes 0%
OA → 100	1000 → Yes (90% empty)
OA → 100	10000 → Yes (99% empty)

⇒ Higher Size more Search optimization

### Interval resizing

double

100 → 200

101 → 200

Class Hashmap {

Int ht [10000];

Int Availability [10000] = 0;

Void Insert

Int Val =  $(x+i^2) / 10000$ ;

while loop  
i > 0

If (Availability [Value] != 1)

ht [Value] = x;

Availability [Value] = 1

}

bool deletion (int n)

Void

int y = Search (n);

If (y != -1)

avail [y] = -1;

else

Print ("element found")

int Search (int n) {

=> loop i > 0; ...

int value =  $(n+i^2) / 10000$

Empty

If (Availability [index] == 0)

return false

found :-

If (Availability [index] == 1 && ht [index] == n)

return index

class Hashmap {

int ht[10000],

int availability[10000] = {0},

void insert(int x) {

{ loop i=0, ----  
int index = (x+i<sup>2</sup>) % 10000;  
if (availability[index] != 1) {  
ht[index] = x;  
availability[index] = 1;  
}

}

void delete(int x) {

int y = search(x),

if (y != -1)

availability[y] = -1;

}

int search(int x) {

→ loop i=0, ----

int index = (x+i<sup>2</sup>) % 10000,

if (availability[index] == 0)

return -1;

if (availability[index] == 1 && ht[index] == x)

return index;

}

}