

Systems and Networking I

Applied Computer Science and Artificial Intelligence
2023-2024



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Recap from Last Lecture

- Synchronization **primitives**:
 - Locks
 - Semaphores
 - Monitors

Recap from Last Lecture

- Synchronization **primitives**:
 - Locks
 - Semaphores
 - Monitors
- **2** fundamental synchronization problems:
 - Producers-Consumers
 - Readers-Writers

Another Synchronization Problem

- It's lunch time at the Department of Philosophy

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- 5 philosophers sitting at a round table

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Another Synchronization Problem

- It's lunch time at the Department of Philosophy
- 5 philosophers sitting at a round table
- Each philosopher has one chopstick on her/his left and one on her/his right (i.e., 5 chopsticks in total)
- 2 things philosophers are good at 😊:
 - Eating
 - Thinking

The Dining Philosophers

- Thinking means do nothing (just kidding, but you get the idea!)

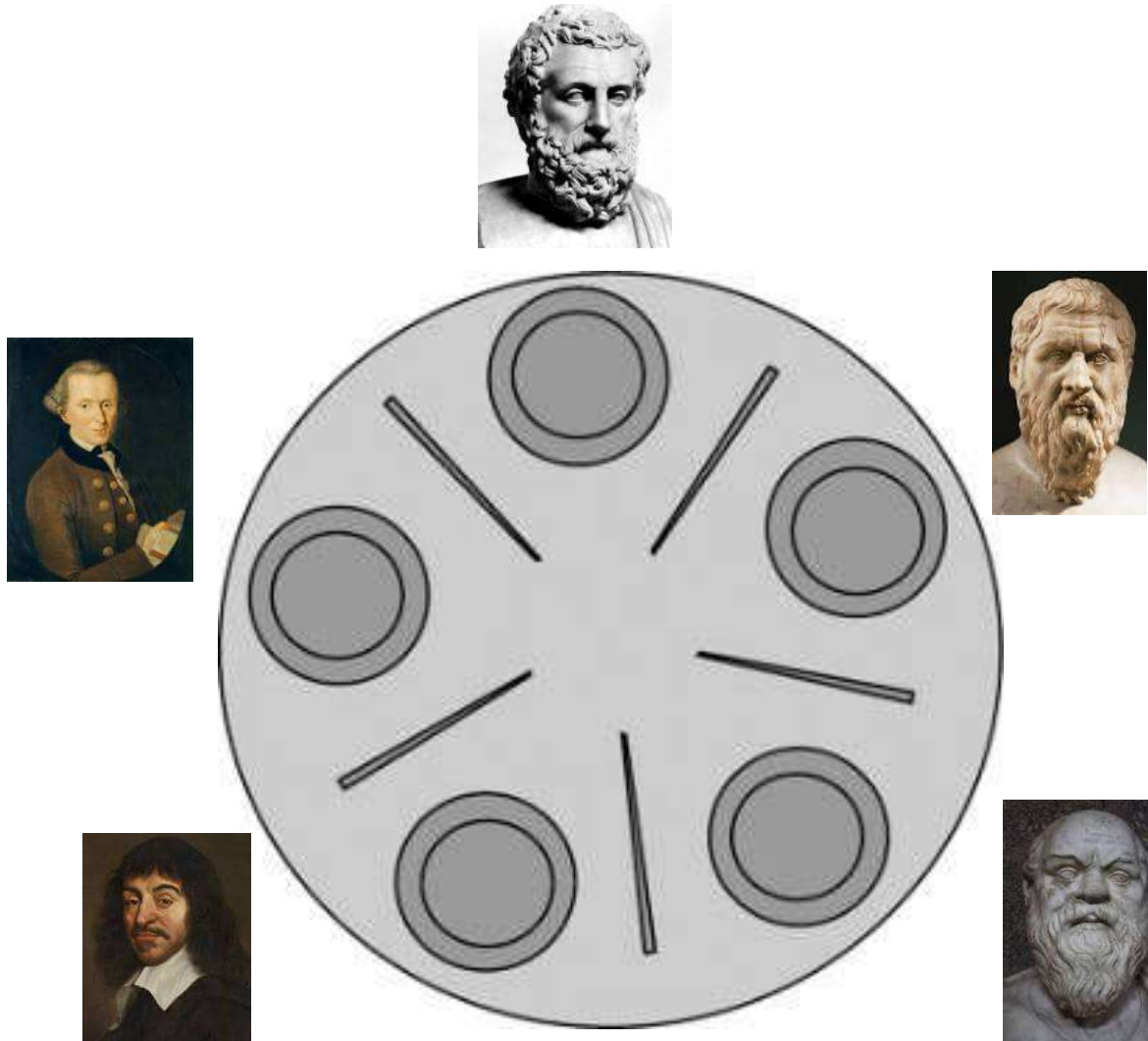
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 - Block if a neighbor has already picked up a chopstick

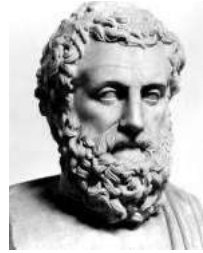
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- Eating means acquiring 2 chopsticks, but how?
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- After eating, put down both chopsticks and go back thinking!

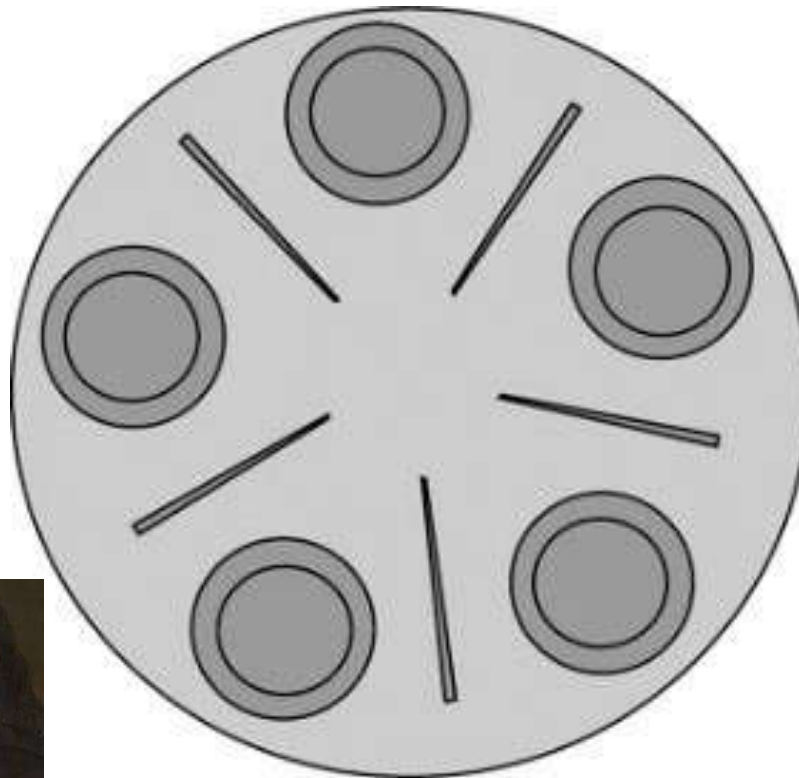
The Dining Philosophers



The Dining Philosophers



How to make them not
starving?



The Dining Philosophers

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Have a "global" lock which allows a single philosopher to pick both chopsticks

Very inefficient! Only **one** philosopher at a time can eat

We still want some concurrency here 😊

The Dining Philosophers: Solution 1

```
Semaphore chopsticks[5];

while(True) {
    chopsticks[i].wait();      // wait on the left chopstick
    chopsticks[(i+1)%5].wait(); // wait on the right chopstick

    eat();

    chopsticks[i].signal();    // signal on the left chopstick
    chopsticks[(i+1)%5].signal(); // signal on the right chopstick

    think();
}
```

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Is this solution correct?

No! Deadlock if all philosophers take the left chopstick

The Dining Philosophers: Solution 2 (monitors)

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Testing if either one of the two neighbors of a given philosopher is currently eating (condition variables)

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Idea: Before picking one chopstick be sure also the second one is available, otherwise wait for the neighbor to finish

Testing if either one of the two neighbors of a given philosopher is currently eating (condition variables)

Never gonna pick a single chopstick!

The Dining Philosophers: Solution 2 (monitors)

```
class Philosopher {
    enum Status {
        THINKING,
        HUNGRY,
        EATING
    }
    Status state;

    public Philosopher() {
        this.state = THINKING;
    }
}
```

```
class DiningPhilosophers {
    Philosopher[5] philosophers;

    public DiningPhilosophers() {
        for(int i=0; i < 5; ++i) {
            this.philosophers[i] = new Philosopher();
        }
    }
    // continue implementation ----->
```

```
void canEat(int i) {
    State state = this.philosophers[i].state;
    State left = this.philosophers[(i-1)%5].state;
    State right = this.philosophers[(i+1)%5].state;
    if(left != EATING && right != EATING && state == HUNGRY) {
        this.philosophers[i].state = EATING;
        this.philosophers[i].notify();
    }
}
```

```
void synchronized pickup(int i) {
    this.philosophers[i].state = HUNGRY;
    canEat(i);
    while(this.philosophers[i].state != EATING) {
        this.philosophers[i].wait();
    }
}
```

```
void synchronized putdown(int i) {
    this.philosophers[i].state = THINKING;
    canEat((i - 1) % 5); // left neighbour
    canEat((i + 1) % 5); // right neighbour
}
```


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 - DB system of a bank: read vs. update account balances

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 - **Producer-Consumer**
 - Audio/Video player embedded in a web browser: shared data buffer + network and render threads
 - **Reader-Writer**
 - DB system of a bank: read vs. update account balances
 - **Dining Philosophers**
 - Lock on multiple resources: e.g., travel reservation (hotel, airline, car rental databases)

Our Journey

- What is deadlock?
- Conditions for deadlock to happen
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What is Deadlock?

“When two trains approach each other at a crossing, both shall come to a full stop and neither shall start up again until the other has gone.”

Kansas legislation early 1900's

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Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

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Thread A

```
printer.wait();  
disk.wait();  
  
// copy from disk to printer  
  
printer.signal();  
disk.signal();
```

Thread B

```
disk.wait();  
printer.wait();  
  
// copy from disk to printer  
  
printer.signal();  
disk.signal();
```

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Thread A

```
printer.wait();  
disk.wait();
```

```
// copy from disk to printer
```

```
printer.signal();  
disk.signal();
```

A starts first



Thread B

```
disk.wait();  
printer.wait();
```

```
// copy from disk to printer
```

```
printer.signal();  
disk.signal();
```

What is Deadlock?

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Thread A

```
printer.wait(); Acquires printer and context switch  
disk.wait();
```



```
// copy from disk to printer
```

```
printer.signal();  
disk.signal();
```

Thread B

```
disk.wait();  
printer.wait();
```

```
// copy from disk to printer
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printer.signal();  
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printer.signal();  
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```

B takes over

Thread B

```
disk.wait();  
printer.wait();  
  
// copy from disk to printer  
  
printer.signal();  
disk.signal();
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Acquires disk and
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What is Deadlock?

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Thread A

```
printer.wait();  
disk.wait();
```

A executes again and blocks

```
// copy from disk to printer
```

```
printer.signal();  
disk.signal();
```

Thread B

```
disk.wait();  
printer.wait();
```

```
// copy from disk to printer
```

```
printer.signal();  
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B executes again and blocks

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A waits B to release the disk

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B waits A to release the printer

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- **Deadlock prevention (offline):** imposes restrictions/rules on how to write deadlock-free programs
- **Deadlock avoidance (online):** runtime support checks resource requests made by threads to avoid deadlocks

Deadlock vs. Starvation

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- Related terms but each one refers to a specific situation
- Starvation occurs when a thread waits indefinitely for some resource but other threads are actually making progress using that resource
- The main difference with deadlock is that the system is not completely stuck!

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Necessary Conditions for Deadlock

- Deadlock *can* happen if *all* the 4 conditions below hold

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 - **Circular Wait** → a set of waiting threads t_1, \dots, t_n where t_i is waiting on $t_{(i+1)\%n}$

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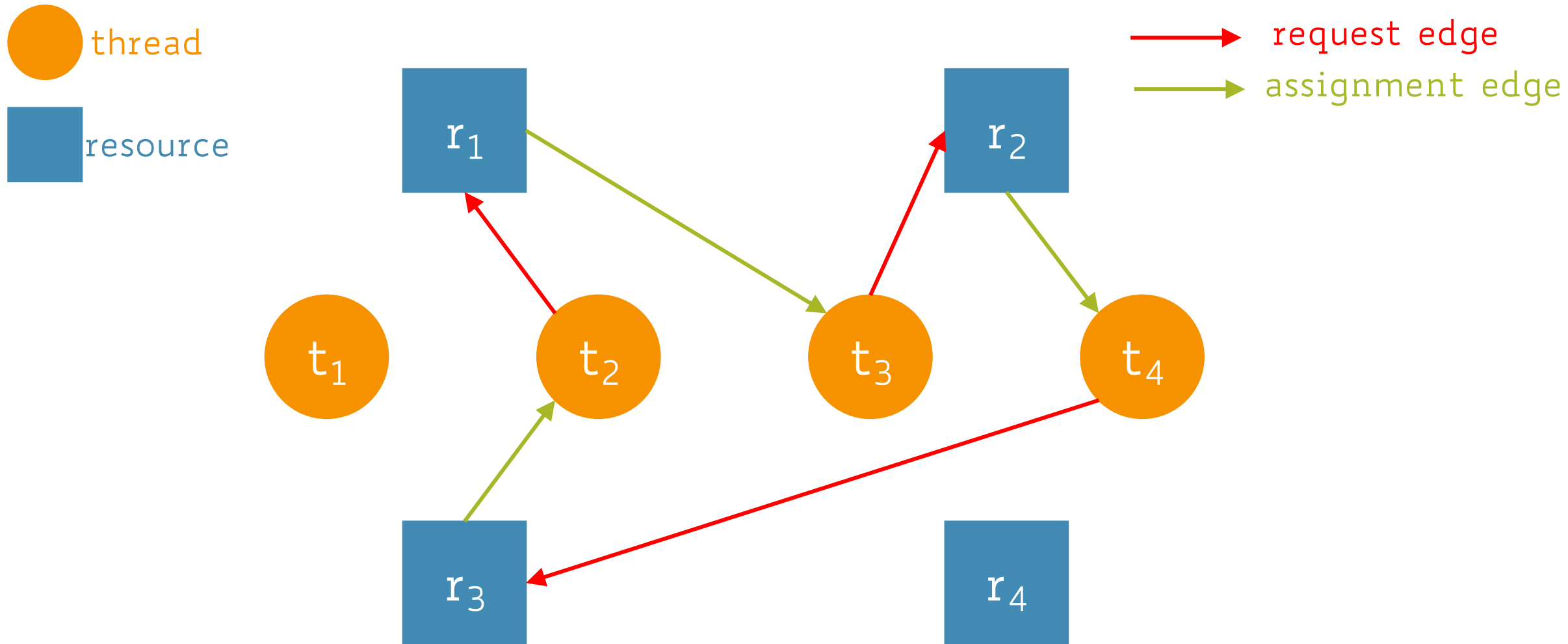
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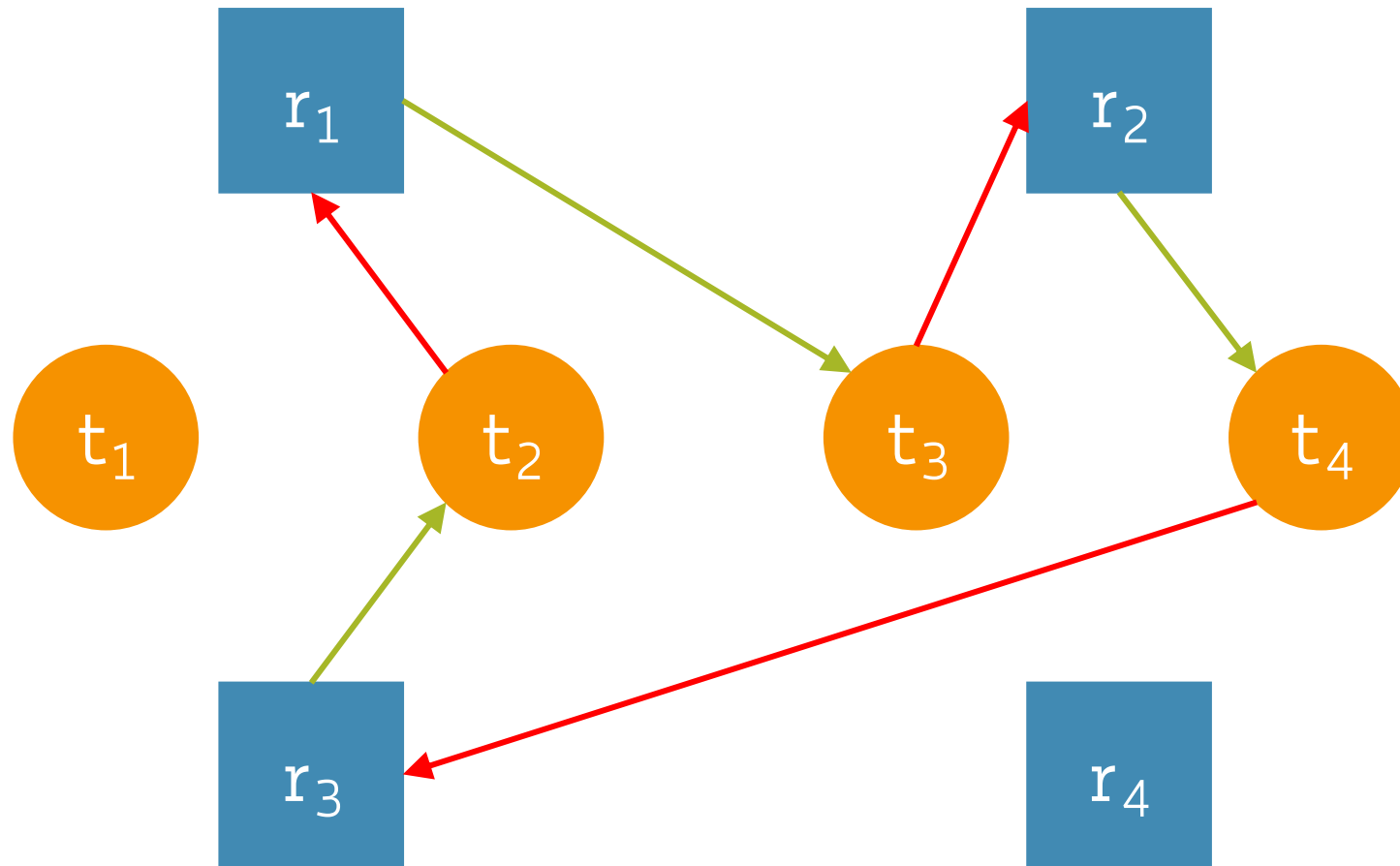
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 - **Assignment Edge** \rightarrow a directed edge (r_j, t_i) indicates that the OS has allocated r_j to t_i

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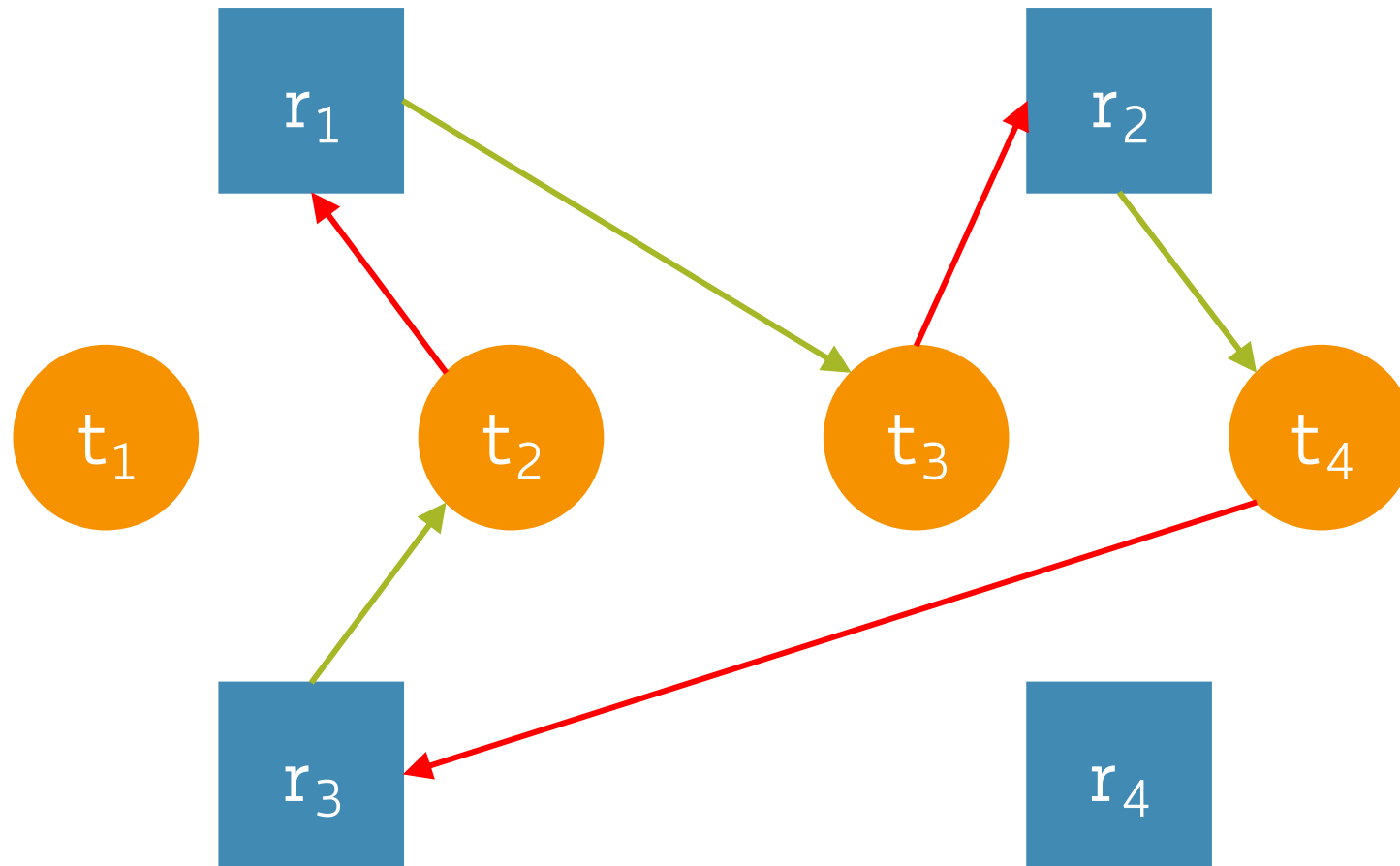


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If the graph has no cycles, no deadlock will ever exist

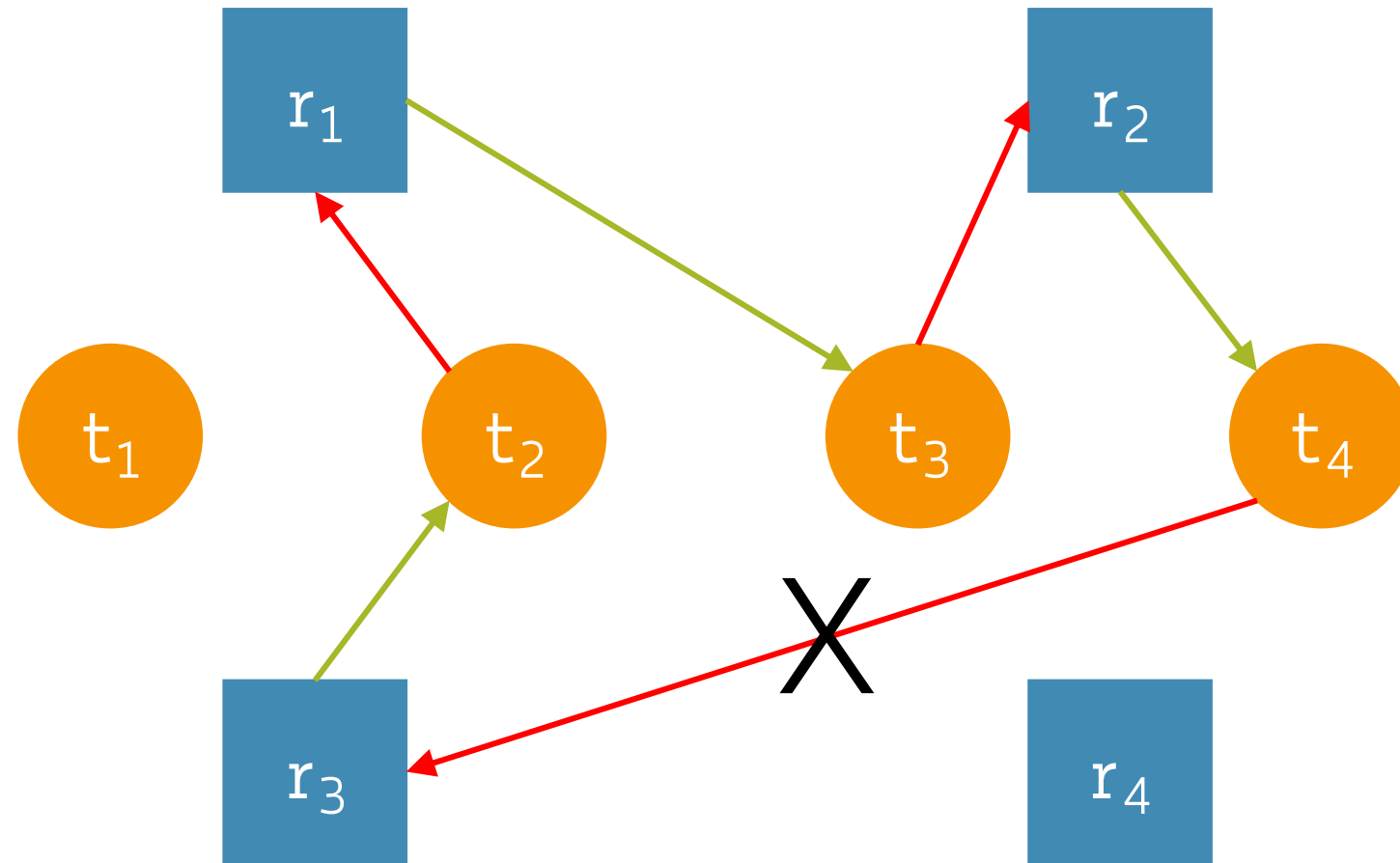
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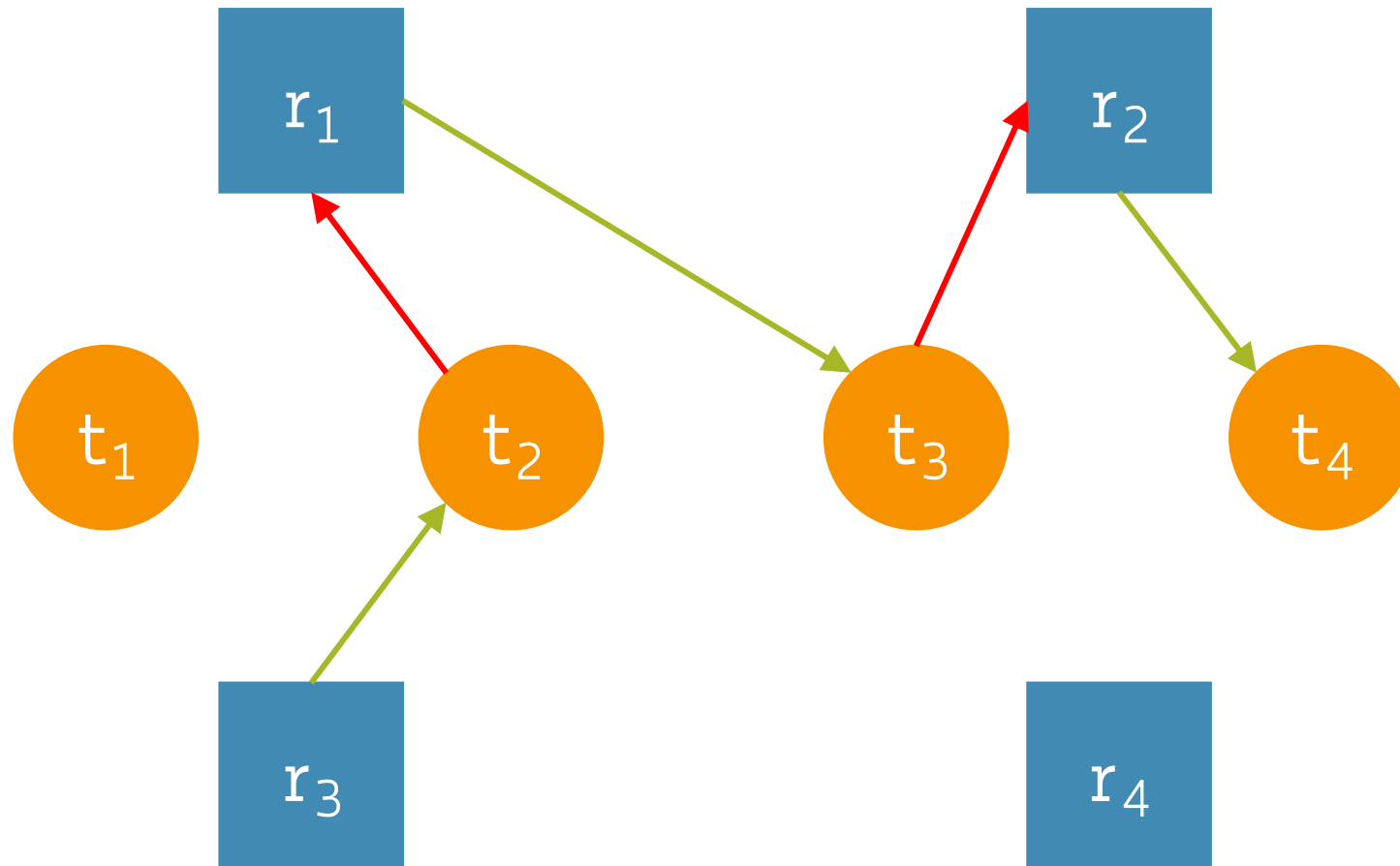
Why?

Deadlock Detection: Resource Allocation Graph



Suppose we remove the edge (t_4, r_3) so as to remove the cycle

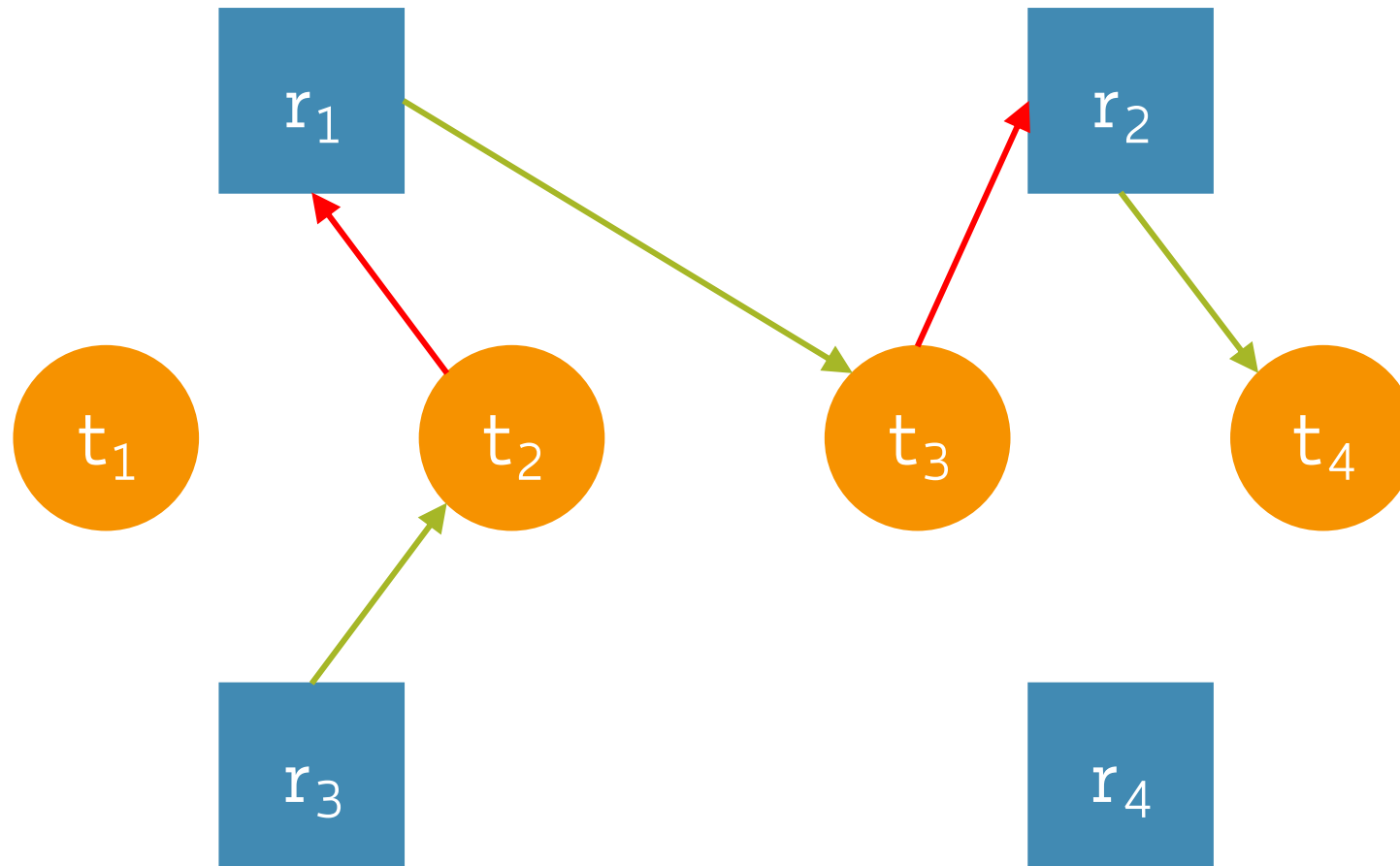
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No deadlock can occur as t_4 is not waiting on anything...

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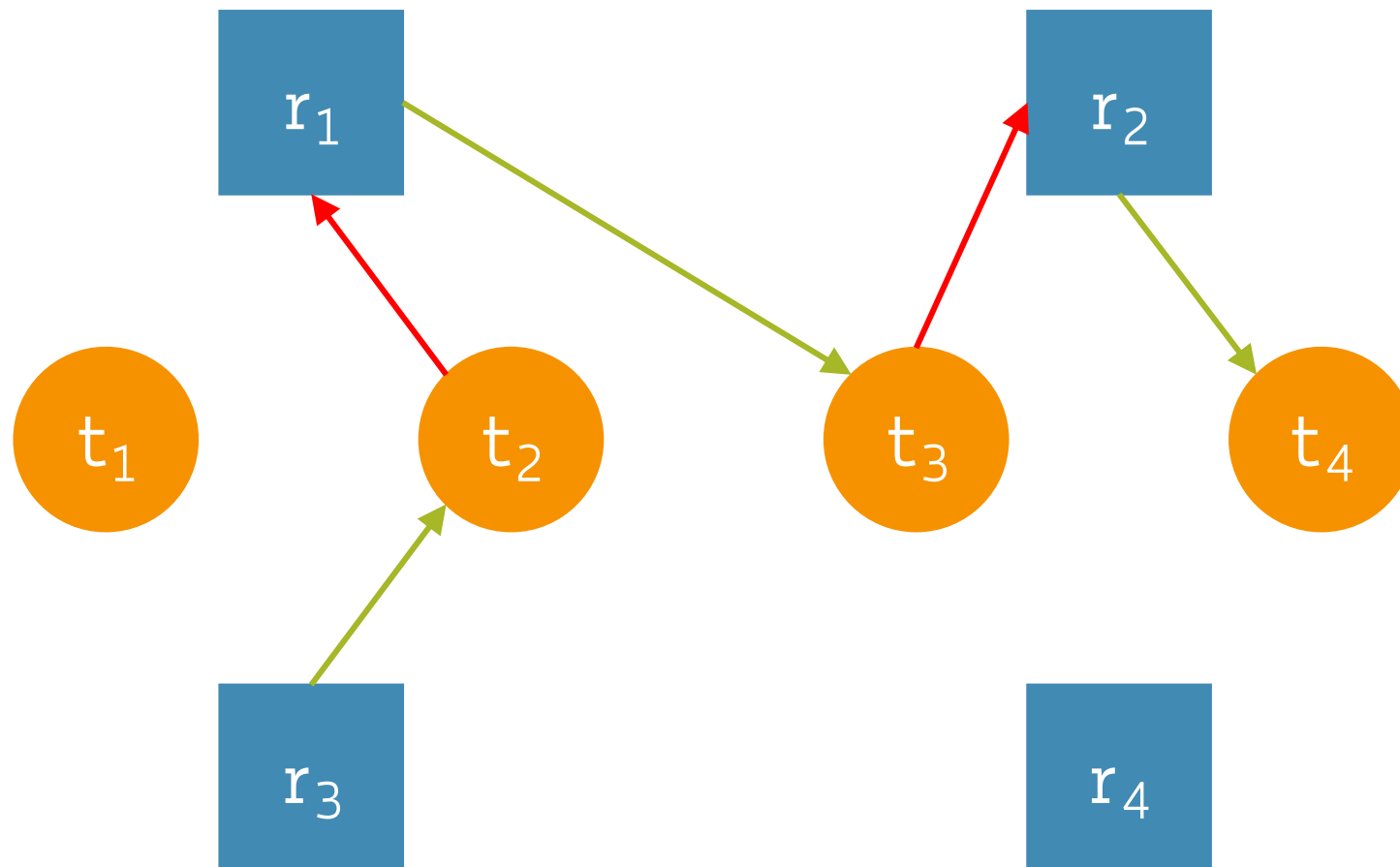


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Therefore, t_4 can run and eventually will release r_2 , which wakes up t_3

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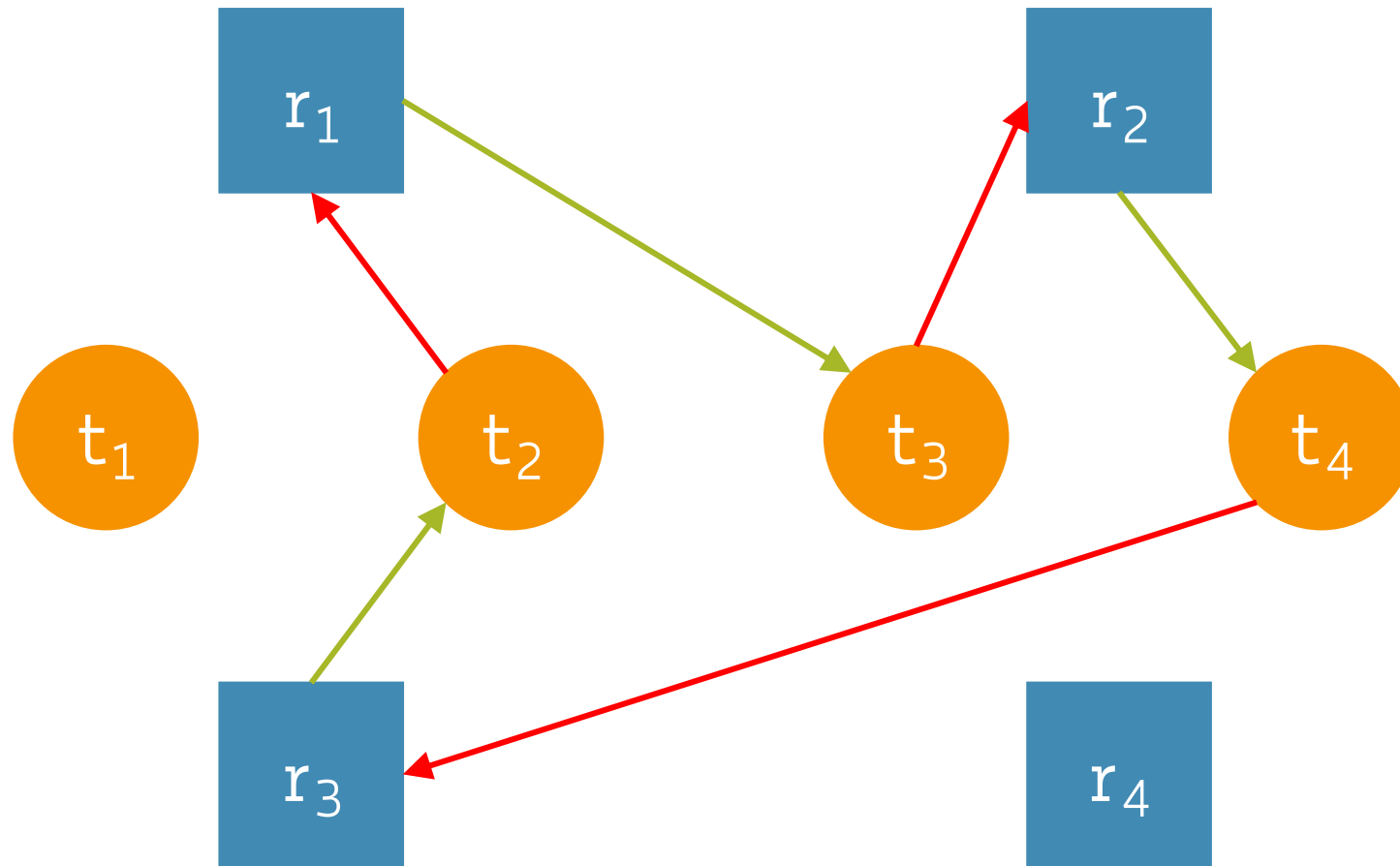
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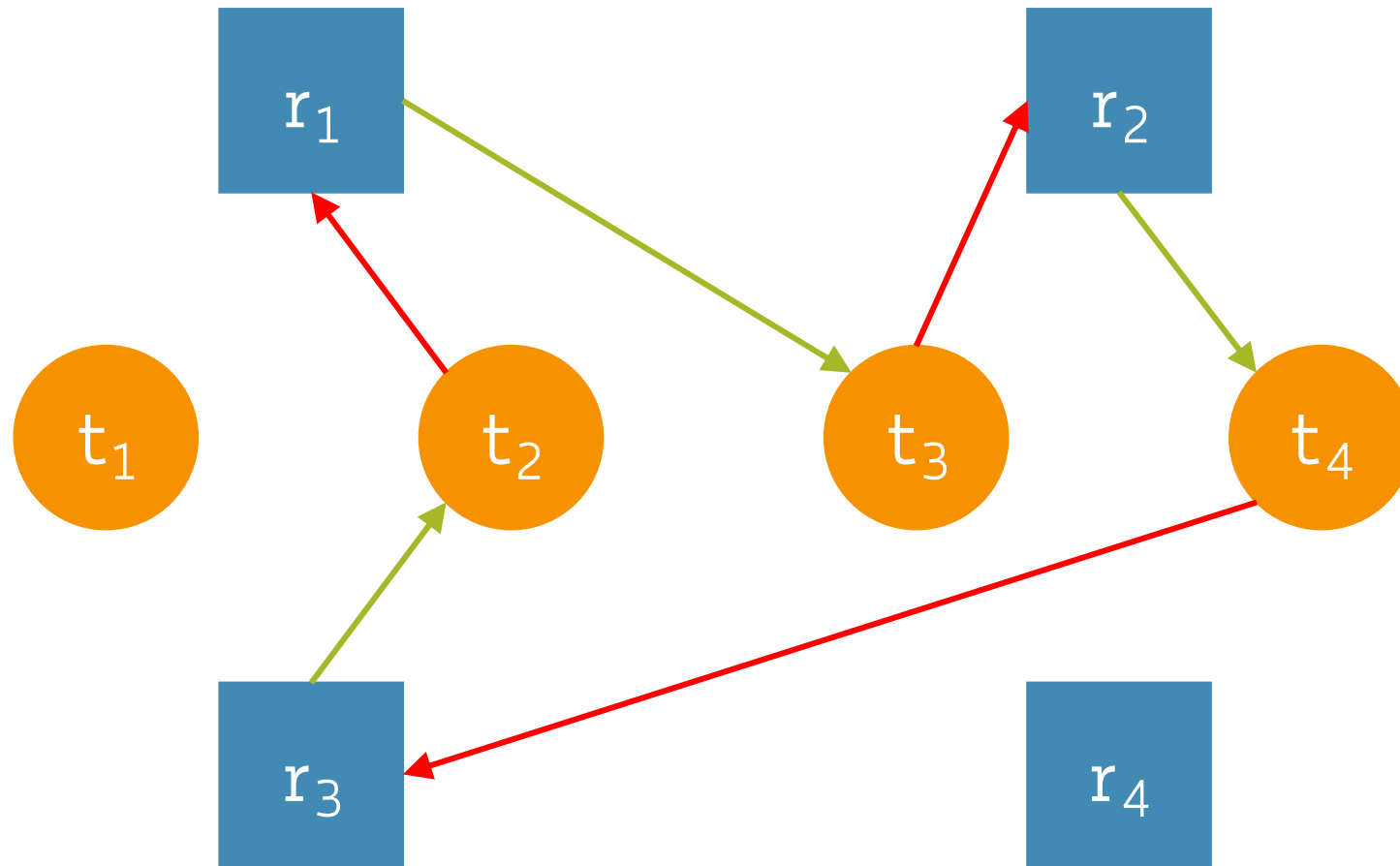
And so on and so forth...

Deadlock Detection: Resource Allocation Graph



If the graph has cycles, deadlock **might** exist

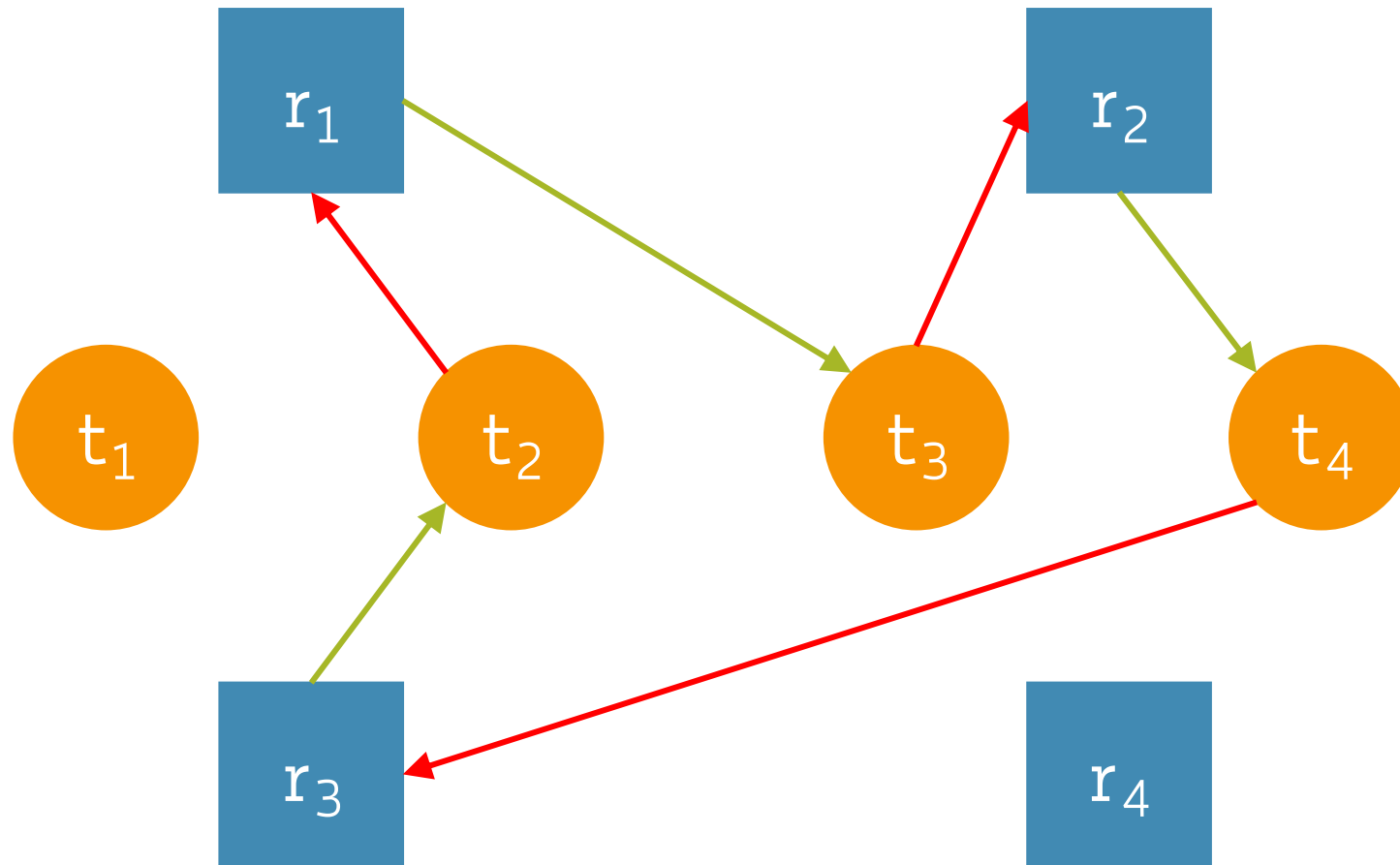
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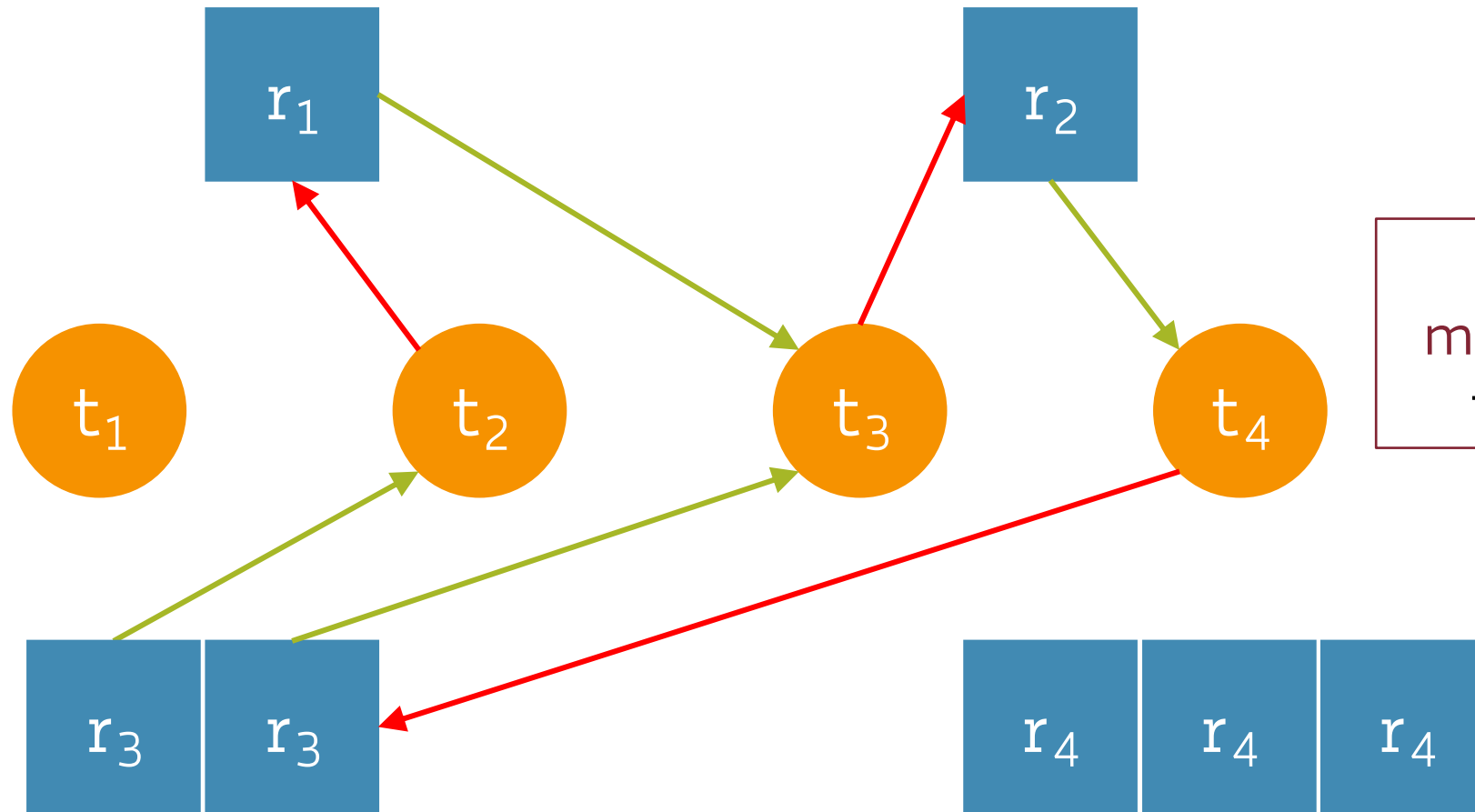
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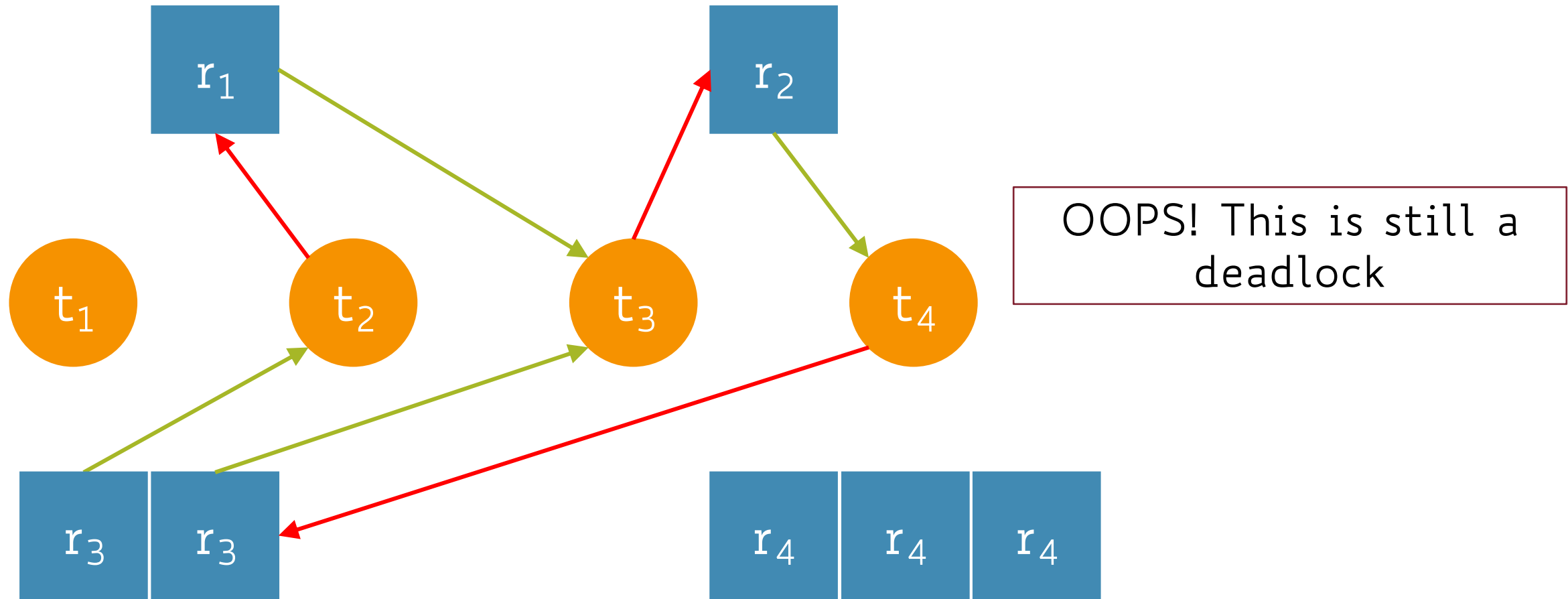
We are assuming the **multiplicity** of each resource is **1** (i.e., one r_1 , one r_2 , etc.)

Deadlock Detection: Resource Allocation Graph

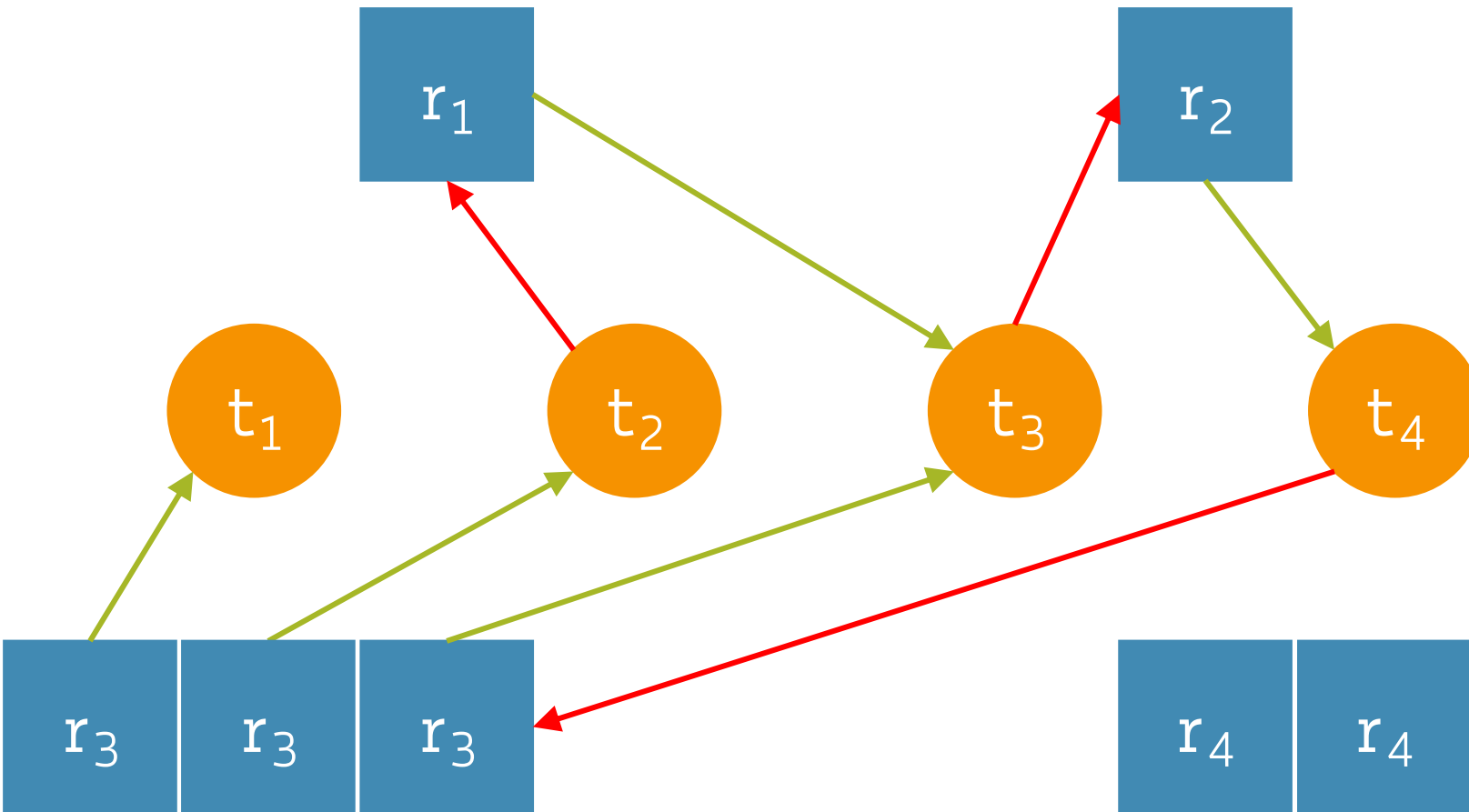


What if there are **multiple** instances of the same resource?

Deadlock Detection: Resource Allocation Graph



Deadlock Detection: Resource Allocation Graph



This works!
If **any** resource involved in the cycle is held by a thread which is not in the cycle (t_1) then we can make progress

Deadlock: Detect and Correct It!

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- We would like to be more precise than that...

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- Detecting cycles on a directed graph $G=(V, E)$ is a quite costly operation
- Known algorithms based on **depth-first search (DFS)** take $O(|V|+|E|)$ time
- $O(|V|+|E|) \sim O(|V|^2)$ as $|E| = O(|V|^2)$ for dense graphs, and $|V| = \text{\#threads} + \text{\#resources}$

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Deadlock: Detect and Correct It!

- When to run such a detection algorithm?
 - Before granting a resource → each granted request will take $O(V^2)$
 - When a request cannot be fulfilled → each failed request will take $O(V^2)$
 - On a regular schedule or when the CPU is under-utilized

Our Journey

- What is deadlock?
- Conditions for deadlock to happen
- Deadlock detection
- **Deadlock prevention**
- Deadlock avoidance

Deadlock Prevention

- Ensure that *at least one* of the 4 necessary conditions doesn't hold
 - **Mutual Exclusion** → make all resources sharable
 - Not all can be shared
 - E.g., disks, printers, etc.

Deadlock Prevention

- Ensure that *at least one* of the 4 necessary conditions doesn't hold
 - **Hold and Wait** → a thread cannot hold one resource when it requests another
 - Enforce requests to be made all at once
 - Hard to predict all the resources a thread will need

Deadlock Prevention

- Ensure that *at least one* of the 4 necessary conditions doesn't hold
 - **No Preemption** → if a thread requests a resource that cannot be allocated to it, the OS preempts (releases) all the resources that the thread is already holding
 - Not all resources can be easily preempted (e.g., printers)

Deadlock Prevention

- Ensure that *at least one* of the 4 necessary conditions doesn't hold
 - **Circular Wait** → impose an ordering (i.e., numbering) on resources and enforce to request them in such order
 - Hard to establish such an order

Our Journey

- What is deadlock?
- Conditions for deadlock to happen
- Deadlock detection
- Deadlock prevention
- Deadlock avoidance

Deadlock Avoidance: Resource Reservation

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m_i = *maximum* number of resources that thread i *might* request

c_i = *current* number of resources that thread i is holding

$C = \sum_{i=1}^n c_i$ = *total* number of resources currently allocated

R = *maximum* number of resources overall available

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$C = \sum_{i=1}^n c_i$ = *total* number of resources currently allocated

R = *maximum* number of resources overall available

Any thread sequence is **safe** if for each thread it holds that:

$$\underbrace{m_i - c_i}_{\text{resources } t_i \text{ might still request}} \leq \underbrace{R - C}_{\text{resources currently available}} + \underbrace{\sum_{j=1}^{i-1} c_j}_{\text{resources currently allocated up to } t_j, j < i}$$

Deadlock Avoidance: Safe State

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- Grant a resource to a thread if the new state is safe, otherwise make it wait even if the resource is available
- This policy ensures no circular-wait condition exists

Deadlock Avoidance: Example

- 3 threads: t_1 , t_2 , and t_3 are competing for 12 tape drives (resources)

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Thread	m_i	c_i	$m_i - c_i$
t_1	4	3	1
t_2	8	4	4
t_3	12	4	8

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Is the current state safe?

Deadlock Avoidance: Example

Thread	m_i	c_i	$m_i - c_i$
t_1	4	3	1
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The current state is safe: there exists a sequence of threads (t_1, t_2, t_3) where each one gets the maximum number of resources without waiting

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t_1 can complete using the current allocation and the 1 drive left

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t_2 can use the current allocation, plus t_1 's resources and 1 drive left (4 drives)

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The current state is safe: there exists a sequence of threads (t_1, t_2, t_3) where each one gets the maximum number of resources without waiting

t_1 can complete using the current allocation and the 1 drive left

t_2 can use the current allocation, plus t_1 's resources and 1 drive left (4 drives)

t_3 can use the current allocation, plus t_1 's & t_2 's resources and 1 drive left (8 drives)

Deadlock Avoidance: Example

Thread	m_i	c_i	$m_i - c_i$
t_1	4	3	1
t_2	8	4	4
t_3	12	5	7

Suppose t_3 requests one more drive, then now there are **no more available drives**

Deadlock Avoidance: Example

Thread	m_i	c_i	$m_i - c_i$
t_1	4	3	1
t_2	8	4	4
t_3	12	5	7

Suppose t_3 requests one more drive, then now there are **no more available drives**

Theoretically, **everything might still work** (e.g., t_1 may never request another drive)

Deadlock Avoidance: Example

Thread	m_i	c_i	$m_i - c_i$
t_1	4	3	1
t_2	8	4	4
t_3	12	5	7

Suppose t_3 requests one more drive, then now there are **no more available drives**

Theoretically, **everything might still work** (e.g., t_1 may never request another drive)

However, t_3 must wait because allocating that extra drive would lead to an unsafe state, which in turn might lead to deadlock

Deadlock Avoidance: Resource Allocation Graph

- An extension of the original resource allocation graph

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- Edges can now be of **3 types**:
 - **Request Edge** \rightarrow a directed edge (t_i, r_j) indicates that t_i has requested r_j , but not yet acquired
 - **Claim (dotted) Edge** \rightarrow a directed edge (t_i, r_j) indicates that t_i might request r_j in the future
 - **Assignment Edge** \rightarrow a directed edge (r_j, t_i) indicates that the OS has allocated r_j to t_i

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 - **Assignment Edge** \rightarrow a directed edge (r_j, t_i) indicates that the OS has allocated r_j to t_i
- Satisfying a request means converting a **claim** into an **assignment** edge

Deadlock Avoidance: Resource Allocation Graph

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- If the allocation results in an unsafe state, this will be denied even if the resource is actually available

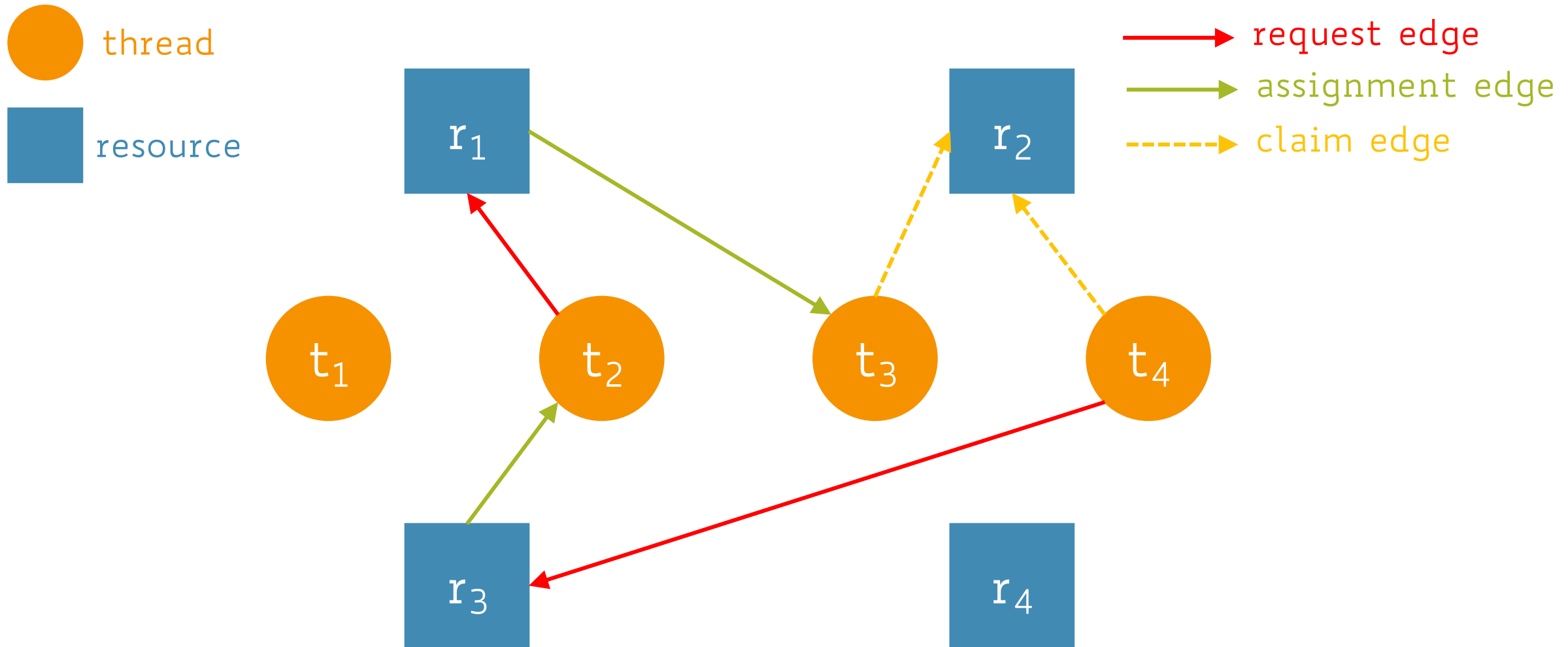
Deadlock Avoidance: Resource Allocation Graph

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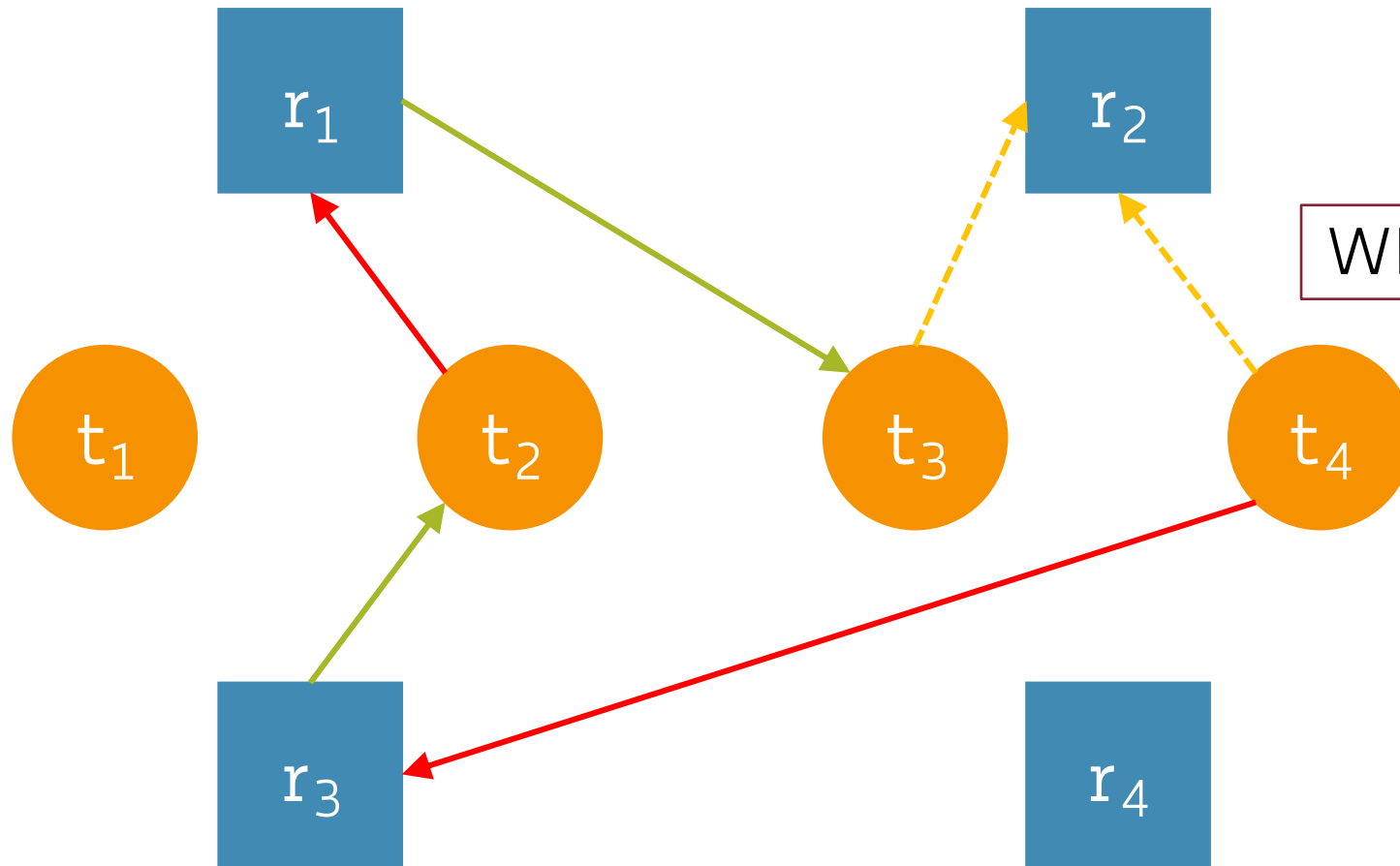
Deadlock Avoidance: Resource Allocation Graph

- A cycle in this extended RAG indicates an unsafe state
- If the allocation results in an unsafe state, this will be denied even if the resource is actually available
- In other words, the claim edge is converted into a request edge and the thread will wait
- NOTE: This solution does not work when there are multiple instances of the *same* resource

Deadlock Avoidance: Resource Allocation Graph

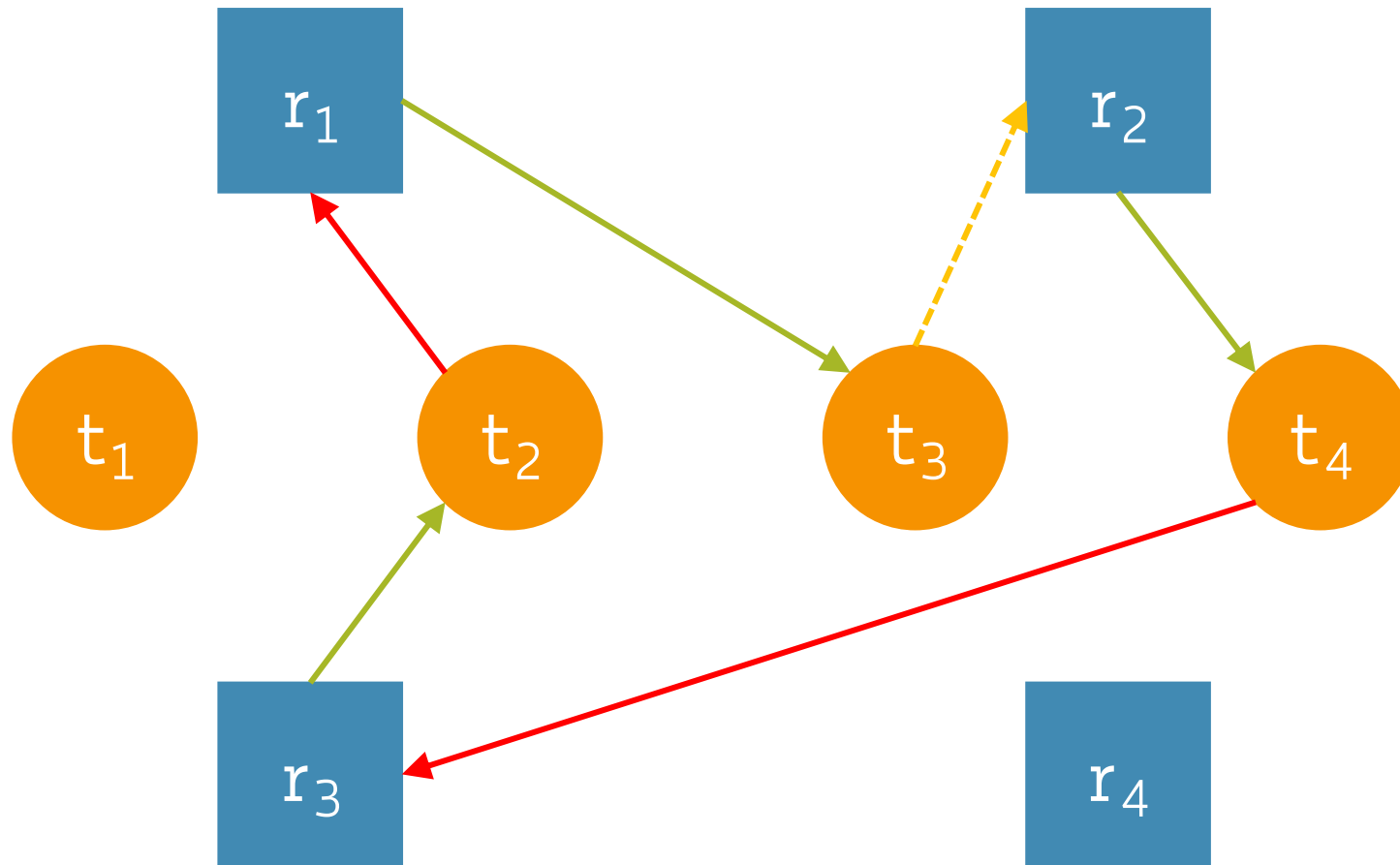


Deadlock Avoidance: Resource Allocation Graph



What happens if t_4 is given r_2 ?

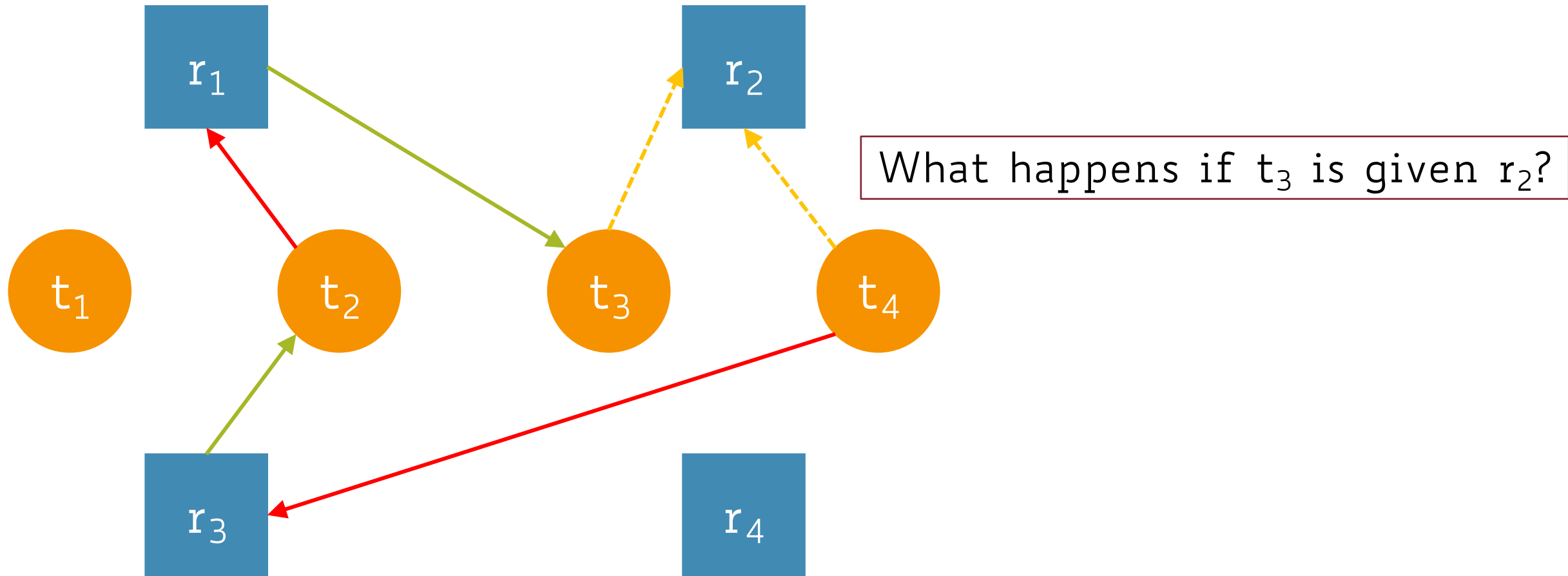
Deadlock Avoidance: Resource Allocation Graph



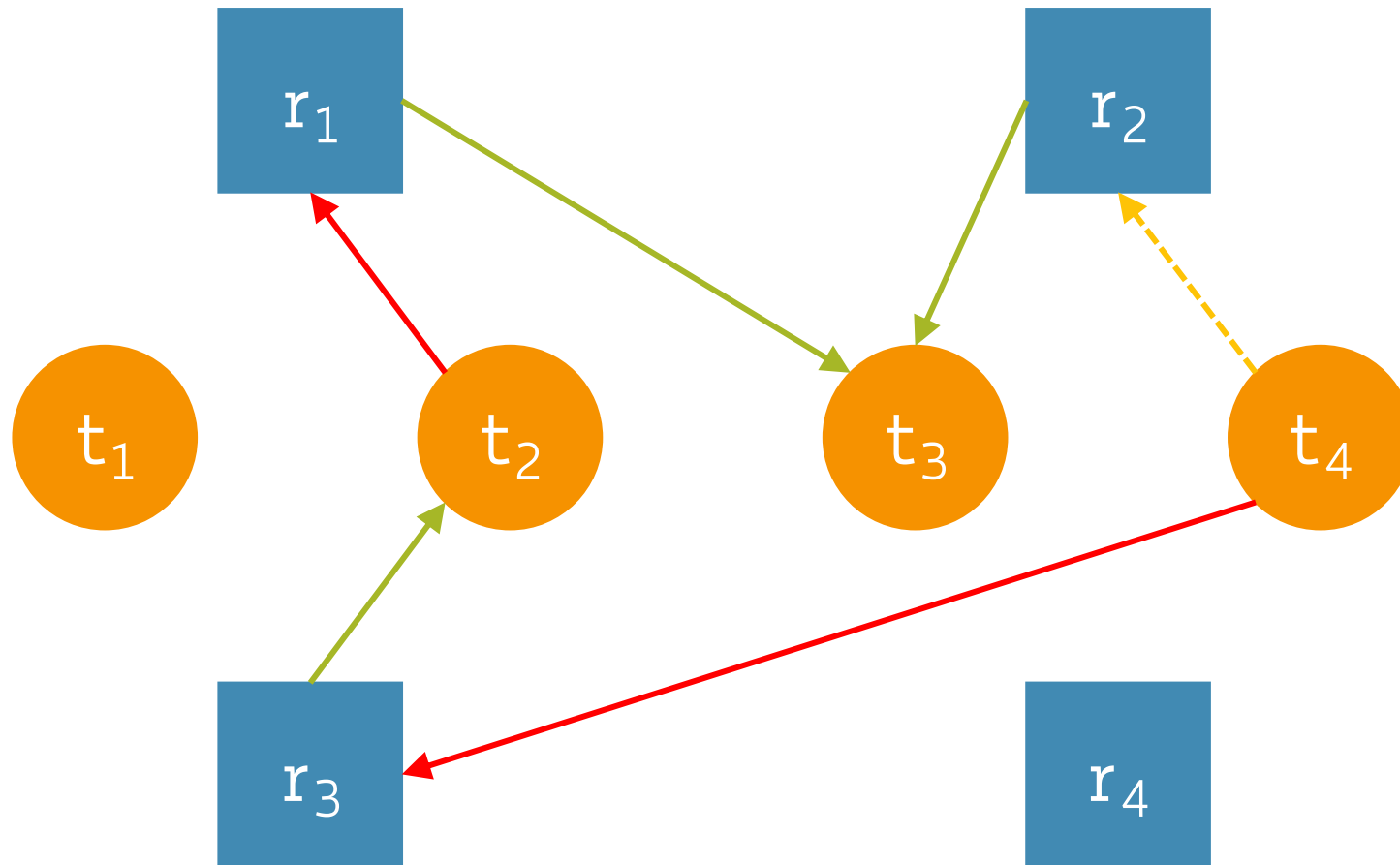
We are introducing a potential cycle (t_3 requests r_2), which in turn might cause deadlock

unsafe state

Deadlock Avoidance: Resource Allocation Graph



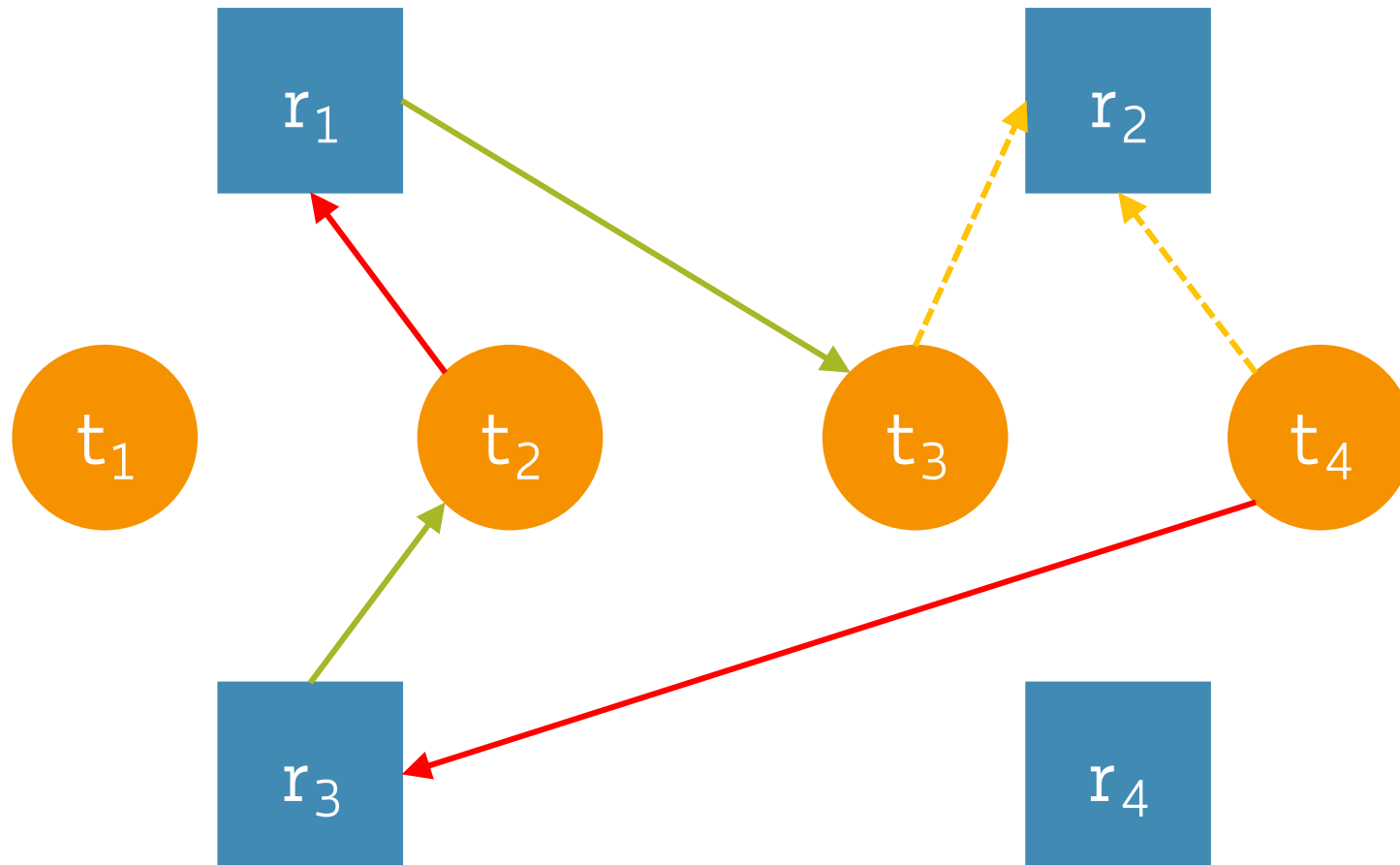
Deadlock Avoidance: Resource Allocation Graph



We are **not** introducing any potential cycle (t_4 requests r_2)

safe state

Deadlock Avoidance: Resource Allocation Graph



Start from a safe state

Invariant

Accept a request iff
we move from a safe
state to another

Banker's Algorithm

- Handles multiple instances of the same resource
- Forces threads to provide information on what resource they might need, in advance
- The resources requested must not exceed the total available in the system
- The algorithm allocates resources to a requesting thread if the allocation leaves the system in a safe state, otherwise the thread waits

Banker's Algorithm: Data Structures

- n = number of threads; m = number of resource types
- $\text{available}[1..m]$: m -dimensional vector
 - $\text{available}[j] = k$ means there are k resources of type j available
- $\text{max}[1..n, 1..m]$: $n \times m$ matrix
 - $\text{max}[i, j] = k$ means thread i may require at most k resources of type j
- $\text{allocation}[1..n, 1..m]$: $n \times m$ matrix
 - $\text{allocation}[i, j] = k$ means thread i has allocated k resources of type j
- $\text{need}[1..n, 1..m]$: $n \times m$ matrix
 - $\text{need}[i, j] = \text{max}[i, j] - \text{allocation}[i, j] = k$ means thread i may need k more resources of type j to complete its task

Banker's Algorithm: Idea

- The algorithm is divided in **2 tasks**:
 - **isSafeState** → given the current status of allocation of resources, tests if this is a safe state
 - **resourceRequest** → given a thread and its resource request decides if such a request can be satisfied

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 - **resourceRequest** → given a thread and its resource request decides if such a request can be satisfied
- A request can be satisfied iff this leads to a safe state!
- In other words, the second task uses the output of the first one in order to make a decision

Banker's Algorithm: isSafeState

1. Let work and finish be vectors of length m and n, respectively

Initialize: $\text{work} = \text{available}$; $\text{finish}[i] = \text{false}$; for all i

2. Find an i such that:

$\text{finish}[i] = \text{false} \ \&\& \ \text{need}[i] \leq \text{work}$

If no such i exists, go to step 4.

3. Assume thread i executes:

$\text{work} = \text{work} + \text{allocation}[i]$; $\text{finish}[i] = \text{true}$; go to step 2.

4. If $\text{finish}[i] == \text{true}$ for all i, the system is in a safe state

Banker's Algorithm: requestResource

Input: i (thread) and request an m -dimensional vector of requests

1. If $\text{request} > \text{need}[i]$ raise an error as thread i is attempting to request more resources than it claimed, otherwise go to step 2.
2. If $\text{request} > \text{available}$ thread i must wait since resources are not available, otherwise go to step 3.
3. Even if resources are available, test if this allocation will lead to a safe state by simulating it
 $\text{available} -= \text{request}$; $\text{allocation}[i] += \text{request}$; $\text{need}[i] -= \text{request}$;
 $\text{isSafeState}()$? OK : $\text{rollback}()$ and $\text{wait}()$

Banker's Algorithm: Example

A snapshot of the current state of the system

		RESOURCES								
		MAX			ALLOCATION			AVAILABLE		
		A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1			
	T ₁	1	7	5	1	0	0			
	T ₂	2	3	5	1	3	5			
	T ₃	0	6	5	0	6	3			
	Total				2	9	9	1	5	2

Banker's Algorithm: Example

Q1: How many resources of type A, B, and C are there overall?

		RESOURCES								
		MAX			ALLOCATION			AVAILABLE		
		A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1			
	T ₁	1	7	5	1	0	0			
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	T ₃	0	6	5	0	6	3			
Total					2	9	9	1	5	2

$$\begin{aligned} A &= 2 + 1 = 3 \\ B &= 9 + 5 = 14 \\ C &= 9 + 2 = 11 \end{aligned}$$

Banker's Algorithm: Example

Q2: What is the content of the NEED matrix?

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1						
	T ₁	1	7	5	1	0	0						
	T ₂	2	3	5	1	3	5						
	T ₃	0	6	5	0	6	3						
	Total				2	9	9	1	5	2			

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Q2: What is the content of the NEED matrix?

$$\text{NEED}[i, j] = \text{MAX}[i, j] - \text{ALLOCATION}[i, j]$$

		RESOURCES									NEED		
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C			
T H R E A D S	T ₀	0	0	1	0	0	1						
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T H R E A D S	T ₀	0	0	1	0	0	1				0-0 = 0		
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T H R E A D S	T ₀	0	0	1	0	0	1				0	$0 - 0 = 0$	
	T ₁	1	7	5	1	0	0						
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		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	$1-1=0$
	T ₁	1	7	5	1	0	0						
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	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

Q3: Is the system in a safe state? Why?

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

Let's start with T_0

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

Eventually, T_0 finishes and releases all its resources

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

T_1 can't execute as it still might NEED (0, 7, 5) and AVAILABLE = (1, 5, 3)

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	8	1	5	3			

Banker's Algorithm: Example

T_2 can execute as it still might NEED (1, 0, 0) and **AVAILABLE** = (1, 5, 3)

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	8	1	5	3			

Banker's Algorithm: Example

T_2 can execute as it still might NEED (1, 0, 0) and **AVAILABLE** = (1, 5, 3)

		RESOURCES									NEED		
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	2	3	5				0	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				3	9	8	0	5	3			

Banker's Algorithm: Example

T_2 eventually finishes and releases all its resources

		RESOURCES												
		MAX			ALLOCATION			AVAILABLE						
		A	B	C	A	B	C	A	B	C	A	B	C	
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-	
	T ₁	1	7	5	1	0	0				0	7	5	
	T ₂	2	3	5	-	-	-				-	-	-	
	T ₃	0	6	5	0	6	3				0	0	2	
Total					1	6	3	2			8	8		

Banker's Algorithm: Example

T_3 can execute as it still might NEED (0, 0, 2) and **AVAILABLE** = (2, 8, 8)

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	0	6	3				0	0	2
	Total				1	6	3	2	8	8			

Banker's Algorithm: Example

T_3 can execute as it still might NEED (0, 0, 2) and **AVAILABLE** = (2, 3, 6)

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	0	6	5				0	0	0
	Total				1	6	5	2	8	6			

Banker's Algorithm: Example

T_3 eventually finishes and releases all its resources

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	-	-	-				-	-	-
	Total				1	0	0	2	14	11			

Banker's Algorithm: Example

T_1 can now execute since NEED (0, 7, 5) and AVAILABLE = (2, 14, 11)

		RESOURCES									NEED		
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	7	5				0	0	0
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	-	-	-				-	-	-
Total					1	7	5	2	7	6			

Banker's Algorithm: Example

We have found a sequence of execution T_0, T_2, T_3, T_1 which leads to safe state!

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	-	-	-				-	-	-
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	-	-	-				-	-	-
	Total				-	-	-	3	14	11			

Banker's Algorithm: Example

Q4: If T_1 issues a REQUEST (0, 5, 2), can this be granted immediately?

		RESOURCES									NEED		
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C			
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

We have to ask ourselves: 1. if the request can be satisfied;
2. if it will lead to a safe state

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

To answer 1. check if: a. REQUEST \leq NEED and b. REQUEST \leq AVAILABLE

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

1.a. REQUEST \leq NEED?

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

1.a. REQUEST \leq NEED? YES! $(0, 5, 2) \leq (0, 7, 5)$

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

1.b. REQUEST \leq AVAILABLE?

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

1.b. REQUEST \leq AVAILABLE? YES! $(0, 5, 2) \leq (1, 5, 2)$

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C			
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

To answer 2. we simulate the request is granted and see if we are still in a safe state

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	0	0				0	7	5
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Banker's Algorithm: Example

To answer 2. we simulate the request is granted and see if we are still in a safe state

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE			NEED		
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	5	2				0	2	3
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
Total					2	14	11	1	0	0			

Banker's Algorithm: Example

Let's start with T_0

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	0	0	1				0	0	0
	T ₁	1	7	5	1	5	2				0	2	3
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	14	11	1	0	0			

Banker's Algorithm: Example

Eventually, T_0 finishes and releases all its resources

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	5	2				0	2	3
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	14	10	1	0	1			

Banker's Algorithm: Example

T_1 can't execute as it still might NEED (0, 2, 3) and AVAILABLE = (1, 0, 1)

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	5	2				0	2	3
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	14	10	1	0	1			

Banker's Algorithm: Example

T_2 can execute as it still might NEED (1, 0, 0) and **AVAILABLE** = (1, 0, 1)

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	5	2				0	2	3
	T ₂	2	3	5	1	3	5				1	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	14	10	1	0	1			

Banker's Algorithm: Example

T_2 can execute as it still might NEED (1, 0, 0) and **AVAILABLE** = (1, 0, 1)

		RESOURCES									NEED		
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C			
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	5	2				0	2	3
	T ₂	2	3	5	2	3	5				0	0	0
	T ₃	0	6	5	0	6	3				0	0	2
	Total				3	14	10	0	0	1			

Banker's Algorithm: Example

T_2 eventually finishes and releases all its resources

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	5	2				0	2	3
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	0	6	3				0	0	2
	Total				1	11	5				2	3	6

Banker's Algorithm: Example

T_3 can execute as it still might NEED (0, 0, 2) and **AVAILABLE** = (2, 3, 6)

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	5	2				0	2	3
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	0	6	3				0	0	2
	Total				1	11	5	2	3	6			

Banker's Algorithm: Example

T_3 can execute as it still might NEED (0, 0, 2) and **AVAILABLE** = (2, 3, 6)

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	5	2				0	2	3
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	0	6	5				0	0	0
	Total				1	11	7	2	3	4			

Banker's Algorithm: Example

T_3 eventually finishes and releases all its resources

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	5	2				0	2	3
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	-	-	-				-	-	-
	Total				1	5	2	2			9	9	

Banker's Algorithm: Example

T_1 can now execute since $NEED(0, 2, 3)$ and $AVAILABLE = (2, 9, 9)$

		RESOURCES									NEED		
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C			
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	1	7	5				0	0	0
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	-	-	-				-	-	-
	Total				1	7	5	2	7	6			

Banker's Algorithm: Example

We have found a sequence of execution T_0, T_2, T_3, T_1 which leads to safe state!

		RESOURCES											
		MAX			ALLOCATION			AVAILABLE					
		A	B	C	A	B	C	A	B	C	A	B	C
T H R E A D S	T ₀	0	0	1	-	-	-				-	-	-
	T ₁	1	7	5	-	-	-				-	-	-
	T ₂	2	3	5	-	-	-				-	-	-
	T ₃	0	6	5	-	-	-				-	-	-
	Total				-	-	-	3	14	11			

Summary

- **Deadlock** → a situation in which a set of threads/processes cannot proceed because each one requires resources held by another

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- **Detection and Recovery** → recognize deadlock after it has occurred and break it
- **Prevention** → design resource allocation strategies which guarantee at least one of the 4 necessary deadlock conditions never holds

Summary

- **Deadlock** → a situation in which a set of threads/processes cannot proceed because each one requires resources held by another
- **Detection and Recovery** → recognize deadlock after it has occurred and break it
- **Prevention** → design resource allocation strategies which guarantee at least one of the 4 necessary deadlock conditions never holds
- **Avoidance** → runtime checks to avoid deadlock online

Summary

In practice, most OSs don't do anything and leave it all to applications

