




Exploring the Emergence of Cooperation

Complex Social Systems Group Project
14.10.2020 - Yanninimalhu



Social dilemmas in game theory


Social Dilemmas

incentive to free-ride (T) >
incentives to cooperate (R)

P1 / P2	C	D
C	R, R	S, T
D	T, S	P, P



Enhancing cooperation

Iterated prisoner's dilemma (PD) 

⊙ Imitation

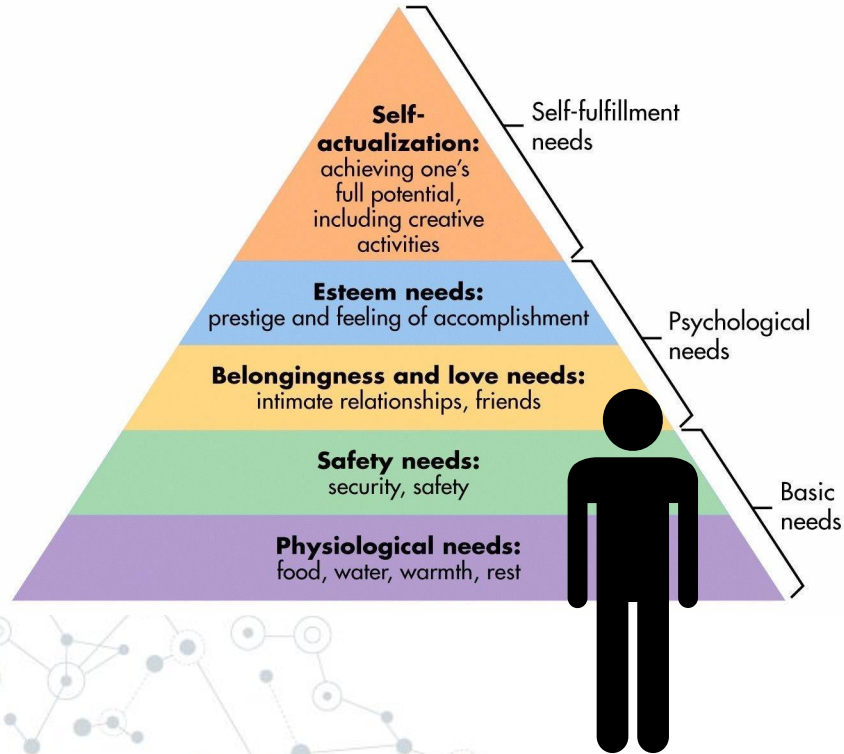
Spatial influences 

⊙ Small-world networks
⊙ Migration

combined

... and many other mechanisms

Maslow's Hierarchy of Needs and Asymmetric Games



		Cooperate	Defect
Cooperate	Cooperate	3,3	-1,2
	Defect	5,-1	0,0



Objectives

• **Explore emergence of cooperation** under



small-world
networks



migration &
imitation



Maslow's
derived
asymmetric
game



Basic Model

Neighborhood of
Player 1

			P2	
	P1			
P3			P4	P5
P6	P7			

We model the world as a grid of cells, some of which are occupied by players.

Players play the prisoner's dilemma game with other players in their neighborhood. Players are either cooperative (C) or defecting (D).

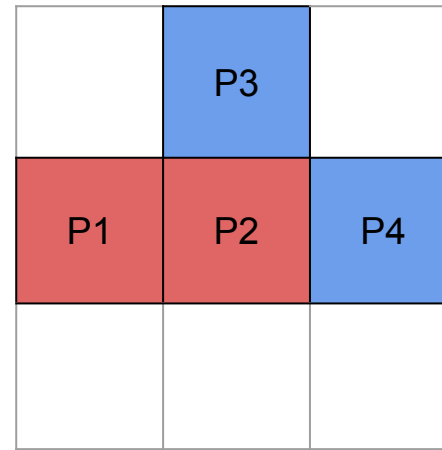
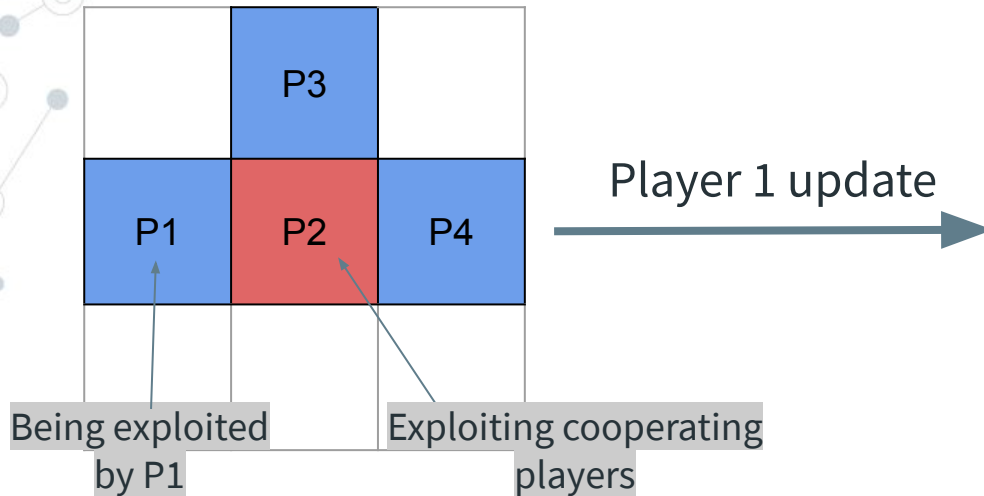
P1 / P2	C	D
C	R, R	S, T
D	T, S	P, P

Basic Model

Imitation

Players update their **strategy** by copying their most successful neighbor

P1 / P2	C	D
C	R, R	S, T
D	T, S	P, P



Basic Model

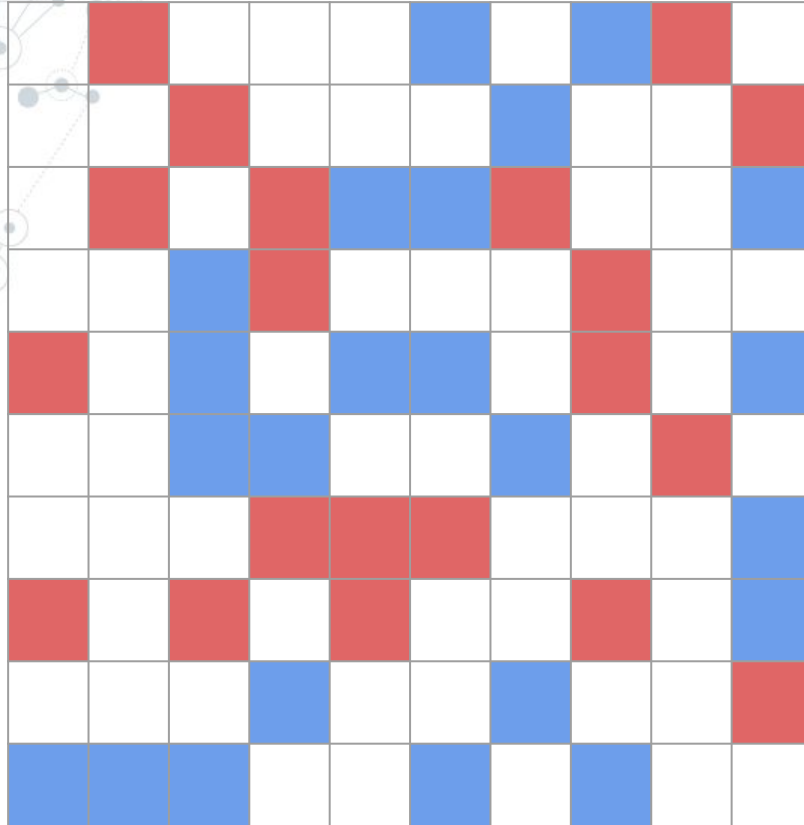
Migration

Players update their **position** by moving to where they would get the best payoff with their current strategy.

P1 / P2	C	D
C	R, R	S, T
D	T, S	P, P



Simulation



P1 / P2	C	D
C	R, R	S, T
D	T, S	P, P

Update all players in a random, sequential order, then iterate.

- Prisoner's Dilemma game
- Migration
- Imitation

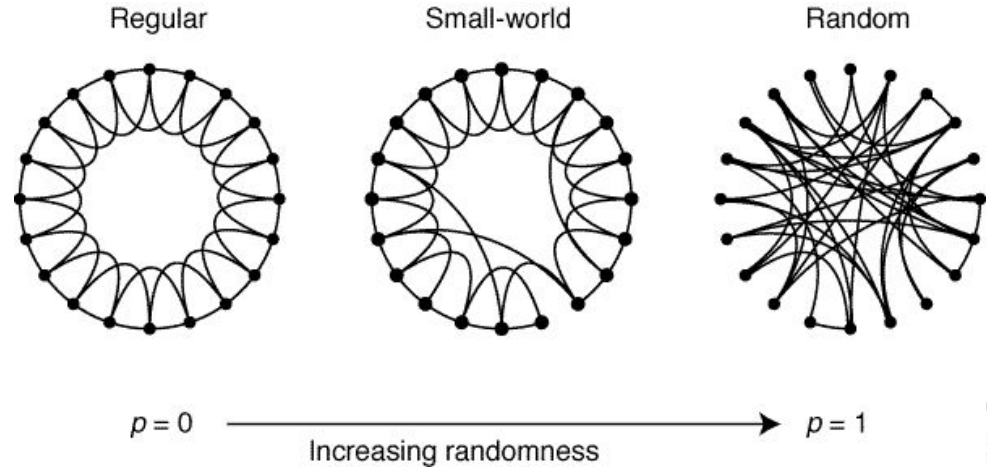
We introduce noise (random strategy mutations) simulate **trial-and-error** behaviour and **unsuccessful imitation**.

Small World Network

We replace the grid with a **small-world network** in which nodes represent players.

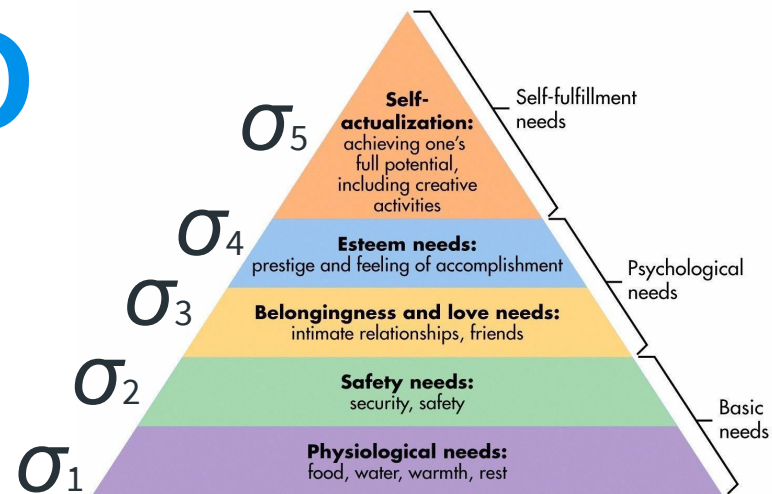
Small-world networks characterized by **small average node distance** and **large clustering coefficients**.

- More realistic modelling of real-world interactions



Asymmetric PD

P1 / P2	C	D
C	$\beta_1 R, \beta_2 R$	$\gamma_1 S, \alpha_2 T$
D	$\alpha_1 T, \gamma_2 S$	$\delta_1 P, \delta_2 P$



Temptation to defect:

$$\alpha \propto 1/(\text{sum all needs})$$

Reward for cooperating:

if physiological needs met: $\beta \propto \text{other needs}$

Sucker's payoff

$\gamma \propto \text{self fulfillment needs}$

Punishment for mutual defection:

$\delta \propto \text{psychological needs}$

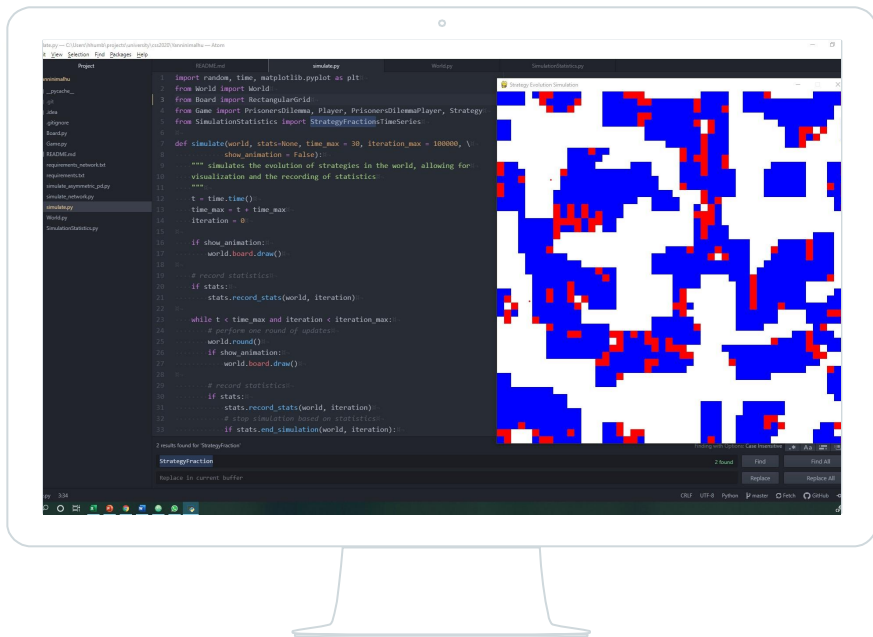
$$\alpha = \frac{2}{1 + \frac{\sum_{i=1}^5 \sigma_i}{\sum_{i=1}^5 i}}$$

$$\gamma = 1 + \sigma_5$$

$$\delta = 1 + \frac{(\sigma_3 + \sigma_4)}{2}$$

$$\beta = 1 + \frac{\sum_{i=1}^5 \sigma_i}{\sum_{i=1}^5 i}$$

Implementation



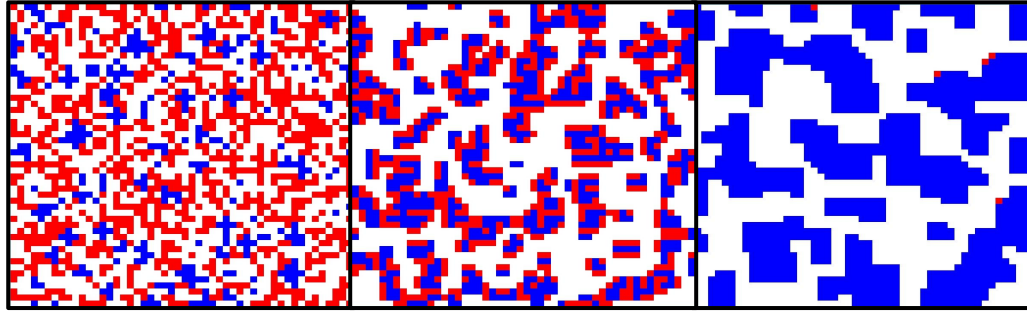
100% Python



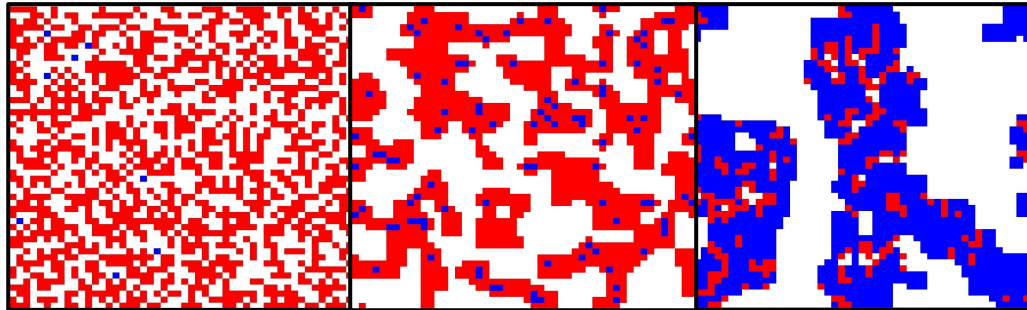
All code was written in Python,
making use of public modules for
animation and network analysis.

Code Validation

No Noise



Noise



Imitation

Migration

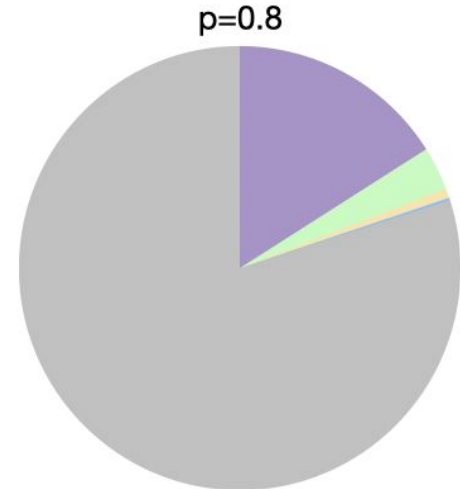
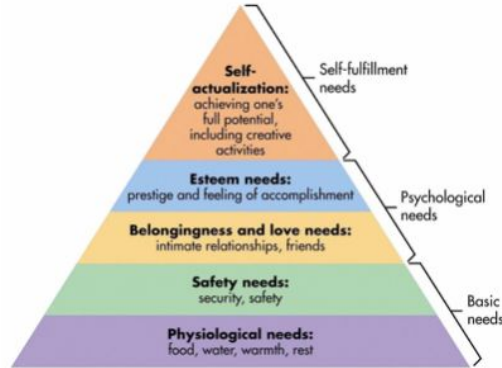
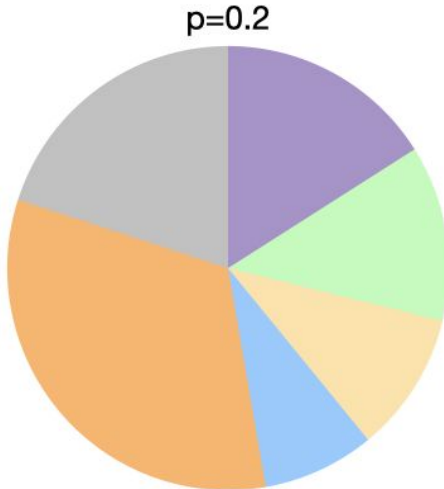
Imitation &
Migration

Cooperative
behaviour robust
to noise!

Results I: Population structure

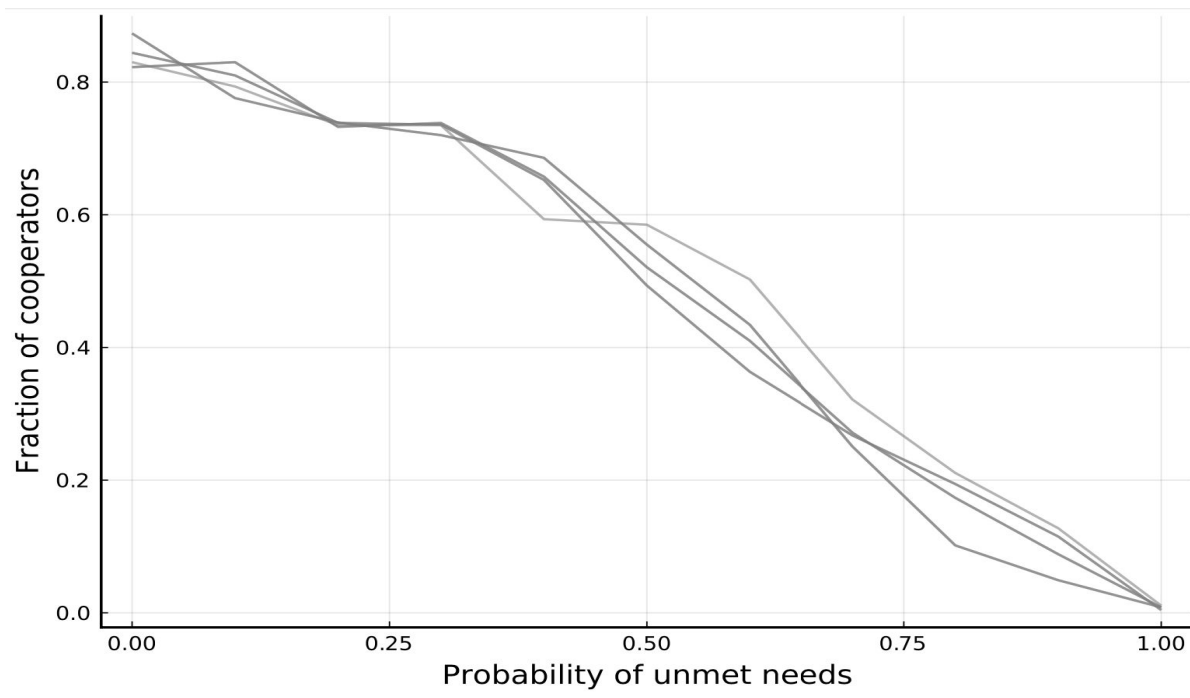
p= probability that need is not met

● Physiological ● Security ● Love ● Esteem ● Self-Actualisation ● None



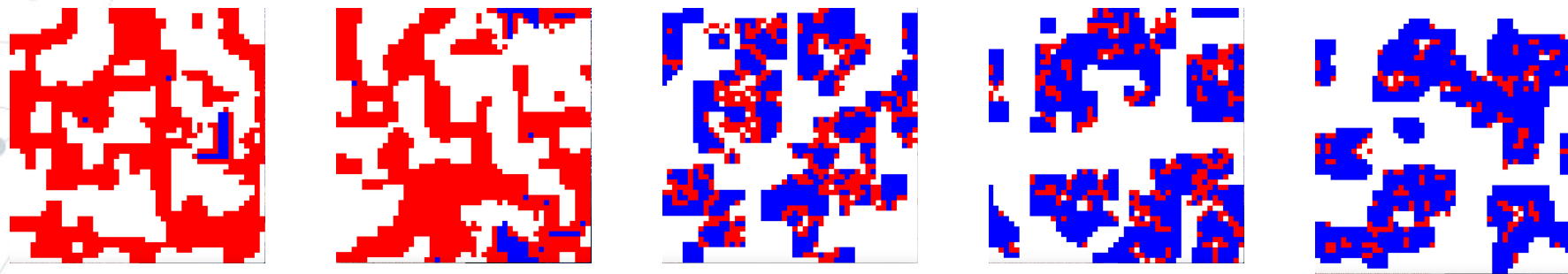
Results I

1. Cooperation is strongly contingent upon the fulfilment of needs



Results I

2. Cooperation cannot exist in societies where basic needs aren't met



Needs

Physio.

Security

Love

Esteem

Self-Act.

Basic needs

Psychological

Results I

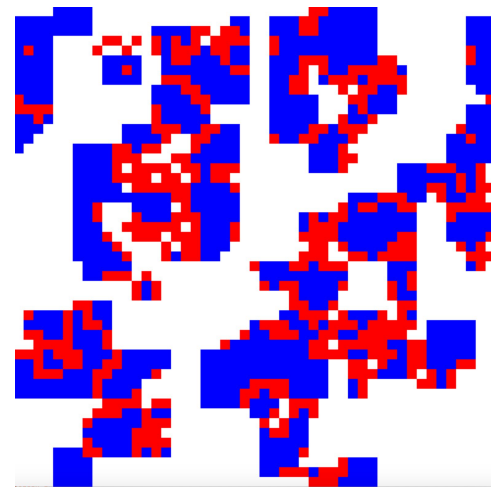
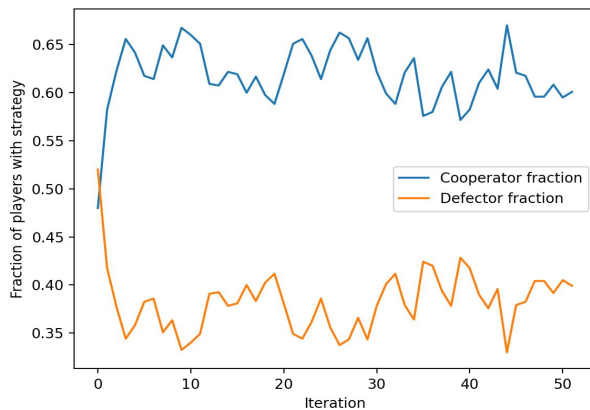
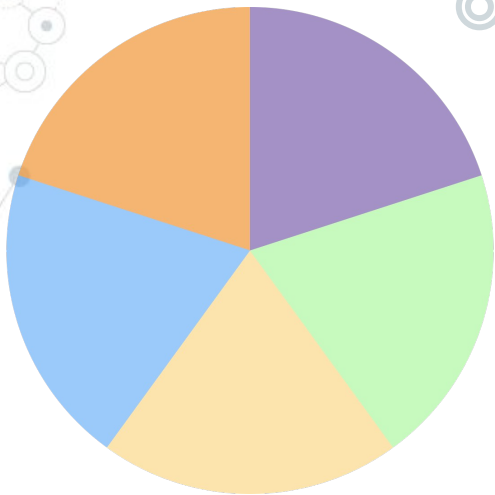
3. Heterogeneous population structures enhance cooperation



Expected fraction ~ 0.5



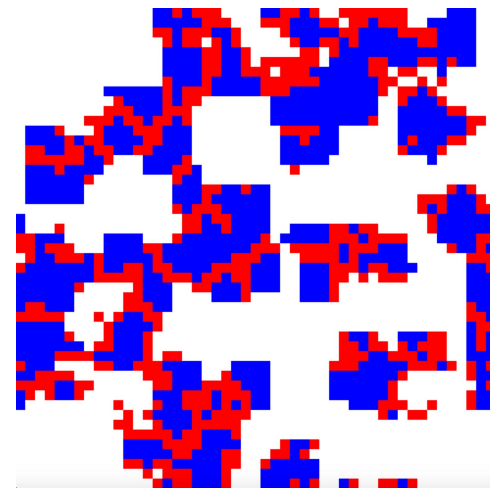
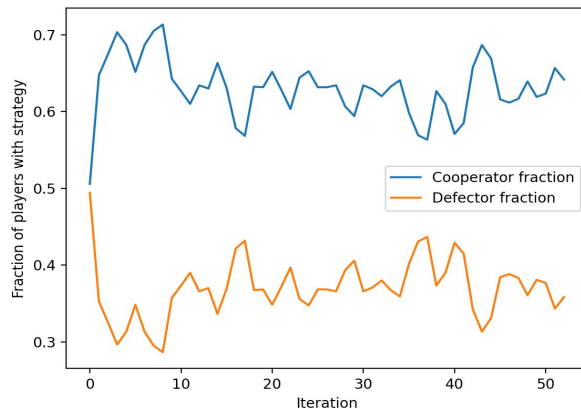
Not just a sum of its parts!



Results I

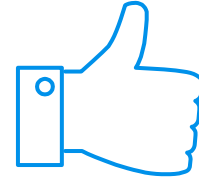
3. Heterogeneous population structures enable cooperation

- Comparable to unrealistic homogenous populations



Conclusions I

Results highlight the
importance of “role-models” in
society





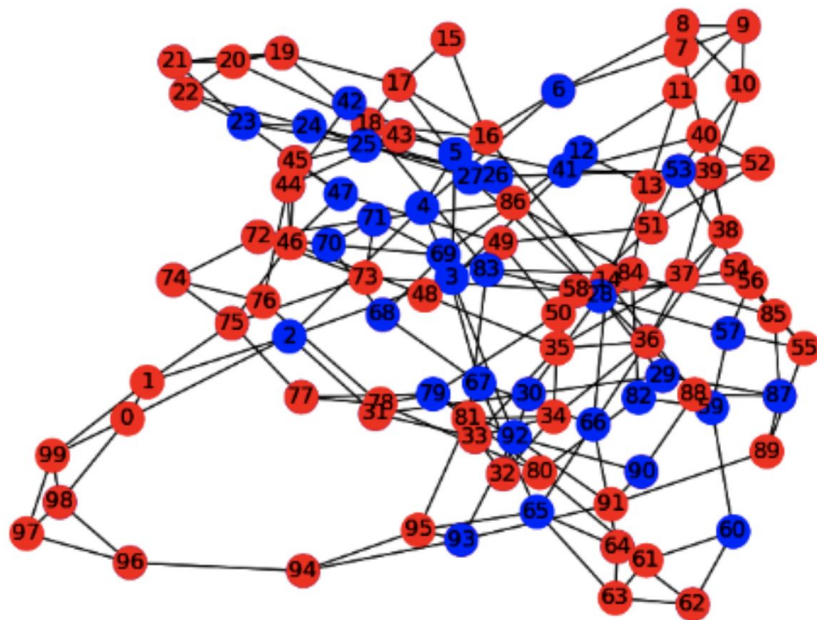
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Socio-political implication:

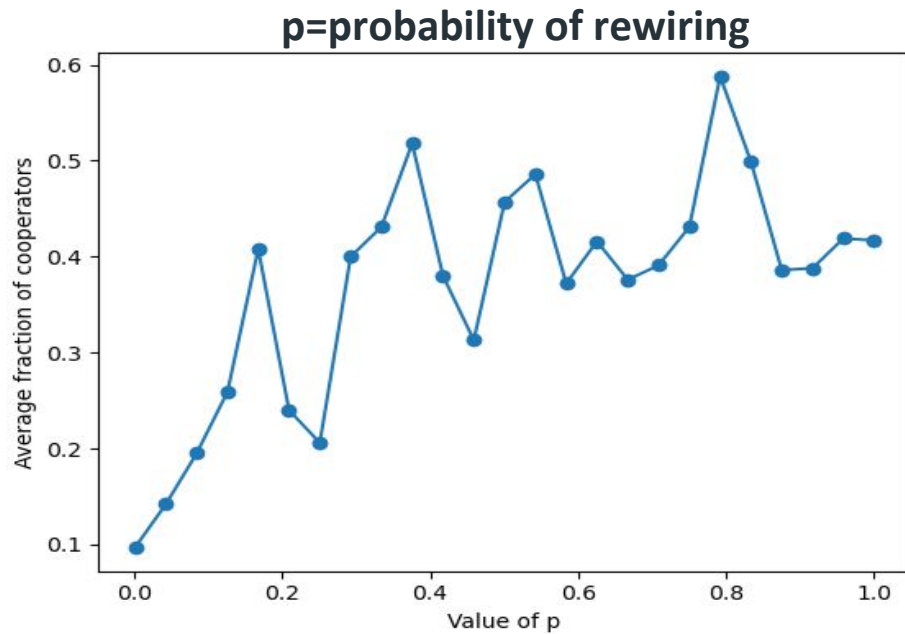
... theories of communism and capitalism do not need to be considered opposites or alternatives, but rather systems that satisfy different stages of humanity's technological development.

Results II: Network topology

100 nodes, mean degree=4 and
probability of rewiring=0.2



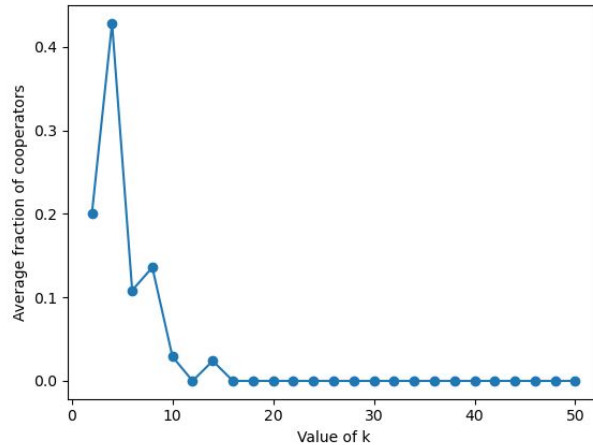
Results II



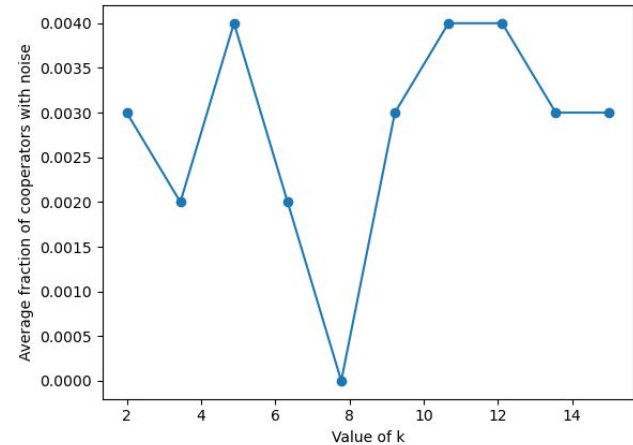
Cooperators vs p

Results II

k =mean degree of the network



(1) Cooperators vs k , noise off



(2) Cooperators vs k , noise on

Conclusions II

- © Hubs promote cooperation
- © Cooperator hubs are good as long as not too accessible






Discussion and extensions

- ◎ Nodes inside are always cooperating
- ◎ Nodes on the “walls” are vulnerable but can be lucky...
- ◎ Hubs are not robust

◎ Possible extensions:

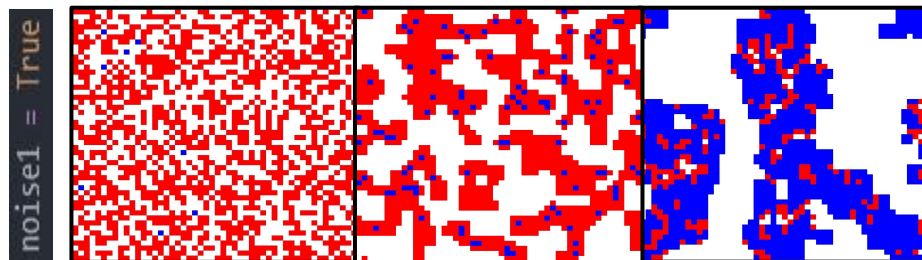
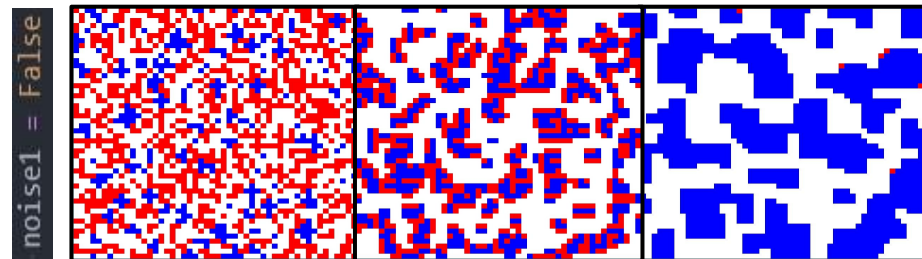
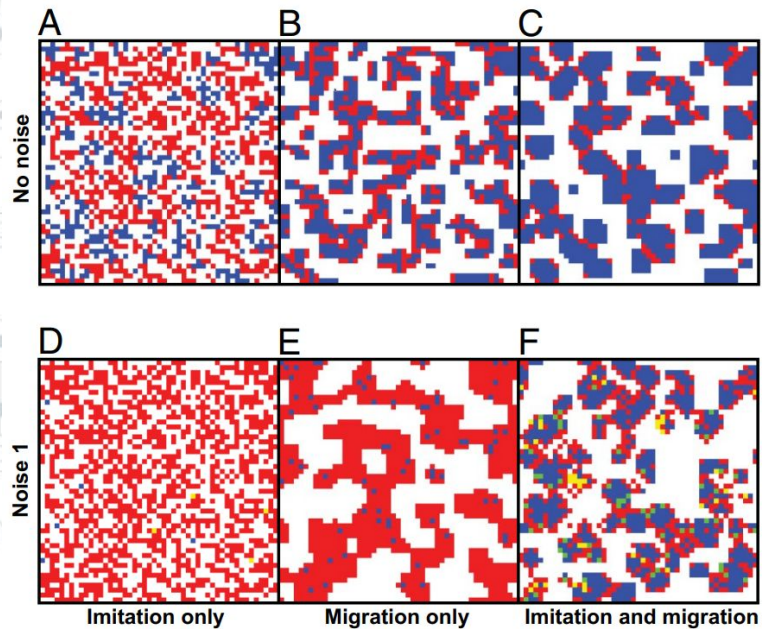
- adaptive networks (structure \Leftrightarrow dynamics)
 - higher order networks (group games)
- 



Thank you!

Any questions?

Appendix



noise1 = True

migration = True

noise1 = True

migration = True