## CS302 Assignment 3

- 1. (15 points) Determine, for the typical algorithms that you use to perform calculations by hand, the running time to do the following (also explain the reasoning behind your answers)
  - (a) Subtract two n-digit integers
  - (b) Compute  $a^n$  where a is a 3-digit number
  - (c) Divide an n-digit number with a 1-digit number that is greater than 1. (i.e. n-digit number / 1-digit number)

2. (10 points) Show for any constant k > 0 the following always must be true  $O(\log^k n) = O(n)$ . You can use the natural log, its derivative is

$$\left(\frac{\partial}{\partial n}\right) \ln^k(n) = \frac{k \ln^{k-1}(n)}{n}$$

3. (5 points) Prove or disprove  $2^n = \Theta(3^n)$ 

4. (15 points) Rearrange the following functions from smallest asymptotic growth rate to the largest asymptotic growth, if any functions have the same asymptotic growth rate, please indicate that (use < to denote the function on the right has a larger growth rate and use = to denote same growth rate, for example  $n < n^2$  and 3n = 4n)

$$1.0001^n, \ 2^{64}, \ 4\log_2 n, \ n\sqrt{n}, \ \frac{n}{2^{64}}, \ 2n^{1.5} - n\log_2 n, \ 4000n + 22, \ n\log_2 n, \ \frac{n^2}{2} + 20n - 4, \ \log_{10} n$$

5.	(15 points)	Perform ins	ertion sort on th	the following list, show the steps of the inner loop and show when							
	an iteration	n of the outer	r loop finishes.	5, 3, 10, 2, 9, 1	5, 3, 10, 2, 9, 1						

6.	(15 points)	Perform	mergesort	on the	following	list,	$\operatorname{draw}$	the recursive	tree t	o shows	how t	the	problem
is broken up and how the merge is done.													

1, 30, 29, 31, 11, 25, 32, 21, 35, 23, 13, 2, 4, 6, 5, 10

7. (15 points) Perform quicksort on the following list, show the pivot and show how the left and right pointers are moving and how the elements are swapped after in each step, choose the leftmost element of each sublist as the pivot.

10, 23, 7, 6, 2, 5, 13, 8, 19, 11