

### Instructions:

We will practice modeling optimization problems by loading information from files in this lab. We will also continue modeling problems with integer variables.

To load directly from a `.txt` file containing numbers, we will use the `numpy.loadtxt()` construct. To know more on the numpy methods to load from files, please check <https://numpy.org/doc/stable/reference/routines.io.html>.

To load directly from a file with comma separated values (`.csv` file), we will use `pandas` library. The construct `pandas.read_csv` helps to read contents from a `.csv` file. Please check [https://pandas.pydata.org/pandas-docs/stable/getting\\_started/index.html](https://pandas.pydata.org/pandas-docs/stable/getting_started/index.html) to know more about `pandas` library.

Please follow the instructions given below:

- Please use different notebooks for solving different problems.
- The notebook name for Exercise 1 should be `YOURROLLNUMBER_IE507_Lab4_Ex1.ipynb`.
- Similarly, the notebook name for Exercise 2 should be `YOURROLLNUMBER_IE507_Lab4_Ex2.ipynb`, etc.
- Please post your doubts in MS Teams or Moodle so that TAs can clarify.

For more details on `pyomo`, please consult <https://pyomo.readthedocs.io/en/stable/index.html>.

There are only 2 exercises in this lab. Try to solve all problems on your own. If you have difficulties, ask the Instructors or TAs.

Only the questions marked **[R]** need to be answered in the notebook. You can either print the answers using `print` command in your code or you can write the text in a separate text tab. To add text in your notebook, click **+Text**. Some questions require you to provide proper explanations; for such questions, write proper explanations in a text tab.

After completing this lab's exercises, click File → Download `.ipynb` and save your files to your local laptop/desktop. Create a folder with name `YOURROLLNUMBER_IE507_Lab4` and copy your `.ipynb` files to the folder. Then zip the folder to create `YOURROLLNUMBER_IE507_Lab4.zip`. Then upload only the `.zip` file to Moodle.

The deadline for today's lab submission is **tomorrow, 11 59 PM Indian Standard Time (IST)**.

**Exercise 1: Loading values from a file [8 marks]**

Consider the following optimization problem:

$$\begin{aligned} \max \quad & 0.65x_1 + 0.75x_2 - 5.85x_3 - 8.35x_4 - 12.38x_5 + 30x_6 \\ \text{s.t.} \quad & -0.5x_1 - 3.8x_3 - 0.9x_4 + 0.9x_5 \leq 24.8 \\ & x_1 - x_4 - x_6 \leq 0.8 \\ & -2.9x_2 - 1.9x_3 - 0.9x_6 \leq -71.4 \\ & 4.7x_4 + 8.02x_5 + 6.15x_6 \leq 95 \\ & -0.7x_1 - 1.4x_2 + 7.9x_3 - 2.9x_4 + 0.9x_5 \leq -47 \\ & x_i \geq 0 \quad \forall i \in \{1, 2, \dots, 6\}. \end{aligned} \tag{OP}$$

1. Create a `.txt` file such that:

- The coefficients of the objective function are present in the first line, separated by commas, and the last value represents the scalar (note that the scalar in the objective function is zero in problem (OP)).
- The remaining lines contain the coefficients of the constraints (separated by commas) and the last value in each of the remaining lines represent the right-hand-sides of the constraints.

See the `lab4_practice_coef.txt` file used in practice.

2. Name the file `lab4_ex1_coef.txt`

3. Copy the file to colab environment.

4. Use `numpy.loadtxt` to load `lab4_ex1_coef.txt` into an appropriate `numpy` array.

5. Write code using `pyomo` to create the model for the optimization problem (OP) using the coefficients loaded from `lab4_ex1_coef.txt` file.

6. Use `cbc` solver to solve the optimization problem (OP).

7. [R] Print and explain the solver termination condition and solver status message and provide possible reasons for the messages obtained.

8. If the solver does not give an optimal solution, try to devise a remedy and use it to get an optimal solution.

9. [R] If you have devised a remedy, explain about it and then report the optimal objective function value, the values of variables and the constraint activities.

**Exercise 2: Another Exercise on LP Vs MILP [20 marks]**

The simplest application of MILP is when the variables model discrete objects that can only take whole-number values (e.g. number of drones to manufacture). The Indian Air Force (IAF) has planned to purchase drones from the Hindustan Aeronautics Limited (HAL) for using them in surveillance activities and during crisis situations like floods, fires and earthquakes. The drones are expected to carry cameras and freight. Five different types of drones are available with HAL. Their carrying capacities, costs and parking space requirements are listed below:

Drone Model	Carrying Capacity (kgs)	Cost (in Crores of rupees)	Parking space (sq. m.)
SHREY	11	6.5	5.75
DHARAN	13	8	4.5
SATVA	9	10.5	3.75
ADHYA	15	11.75	4.85
PRAVAT	12	14.5	3.45

The IAF wants to have maximum possible carrying capacity. The budget of IAF is limited to 78 crores of rupees. In addition, parking space for drones is limited to 84 sq. m.

1. Create a `.csv` file containing the data given in the table. Name the file as `lab4_ex3.csv`. Use simple and appropriate names for the headers.
2. Copy the file to colab environment.
3. Use `pandas` to load the `.csv` file contents.
4. [R] Write a mathematical optimization problem to find the number of drones of each type that can be bought in order to maximize the goal. Mention which variables must be integers.
5. Create a model using `pyomo` to solve your optimization problem. Use the loaded contents of `.csv` file to create your model. Use `cbc` solver to solve your optimization problem. In your code, remember to specify which variables are integers.
6. [R] Report the optimal objective function value and the solution.
7. [R] Let us now compare it to a linear program. Suppose we remove the restrictions that the variables in the above problem are integers. Solve this modified problem and report the solution and the objective value.
8. [R] Can the solution of the MILP be obtained by merely rounding the solution of the LP? Why or why not?
9. [R] Suppose now we are interested in finding how the solution changes when the right-hand-sides in our constraints change. Suppose the limit on budget is decreased to 76 crores of rupees and the parking space is increased to 87 units, how will the new LP optimal objective function value and corresponding optimal solution change? How does the new MILP optimal objective function value and corresponding optimal solution change?
10. [R] Now try decreasing limit on budget from 76 crores to 74, 72, 70 and 68 crores of rupees. Correspondingly, increase the parking space to 88, 89, 90 and 91 units. Solve the LP and MILP for each of these four possibilities and comment on the pattern seen in optimal objective function values of the LP and MILP. Also comment on your observations about the optimal solutions obtained.