Sorting

↳ Permutations → arrangements

↳ arranging data in a particular permutation (this depends on requirement) is called as Sorting

Q ⇒ Given n integer values, arrange them in increasing order.

Ex → [15, -1, 3, 8, 2, 6] ← n — array → n!

Brute force → we can generate all possible Permutations and filter out your reqd ans.

[3, 2, 1] ↪

3 2 1
3 1 2
2 1 3
2 3 1
1 2 3
1 3 2

O(K) → to generate one perm

O(K×n!) ≈ O(n!)

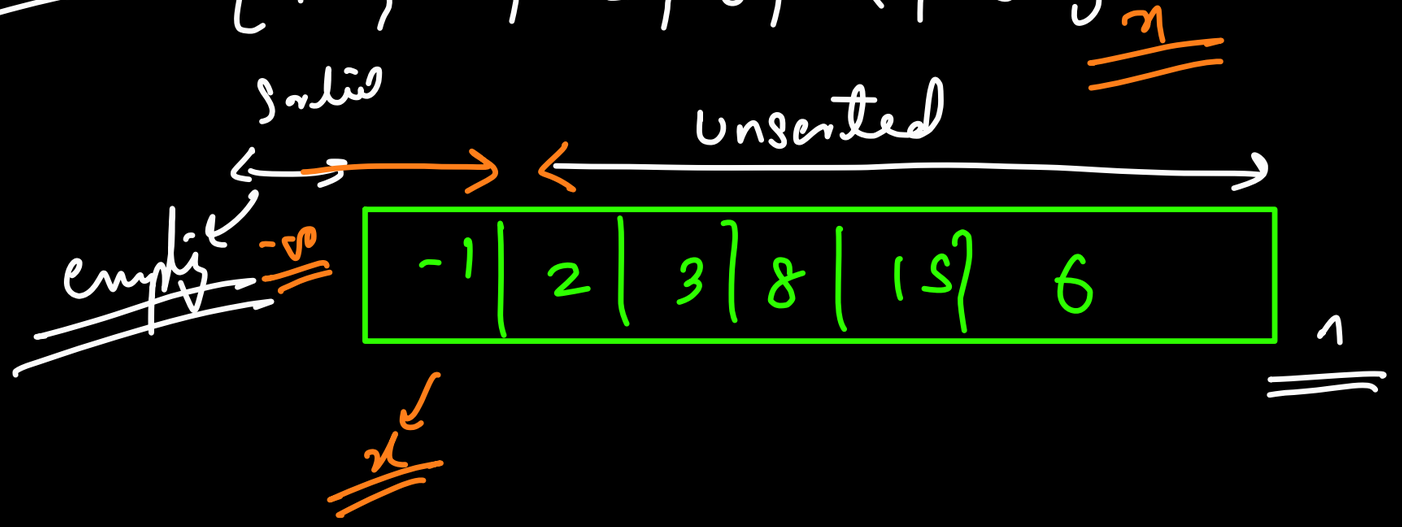
↳ Bubble Sort
↳ Selection Sort
↳ Insertion Sort
↳ Counting sort
↳ merge sort
↳ quick sort

Selection Sort

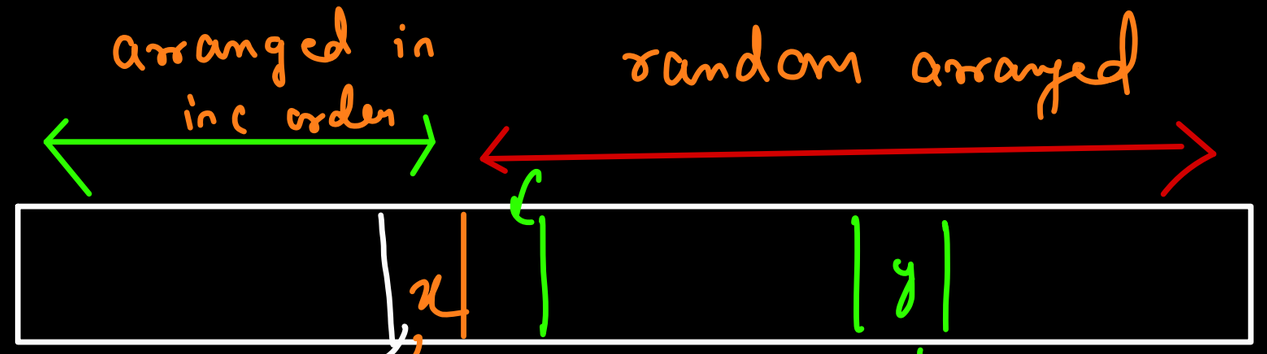
Q ⇒ Given n integer values, arrange them in increasing order.

Ex → [15, -1, 3, 8, 2, 6] ← array

n



In the unsorted region how to get min elem. ??



x is the largest element of sorted area

x is the last element of sorted area

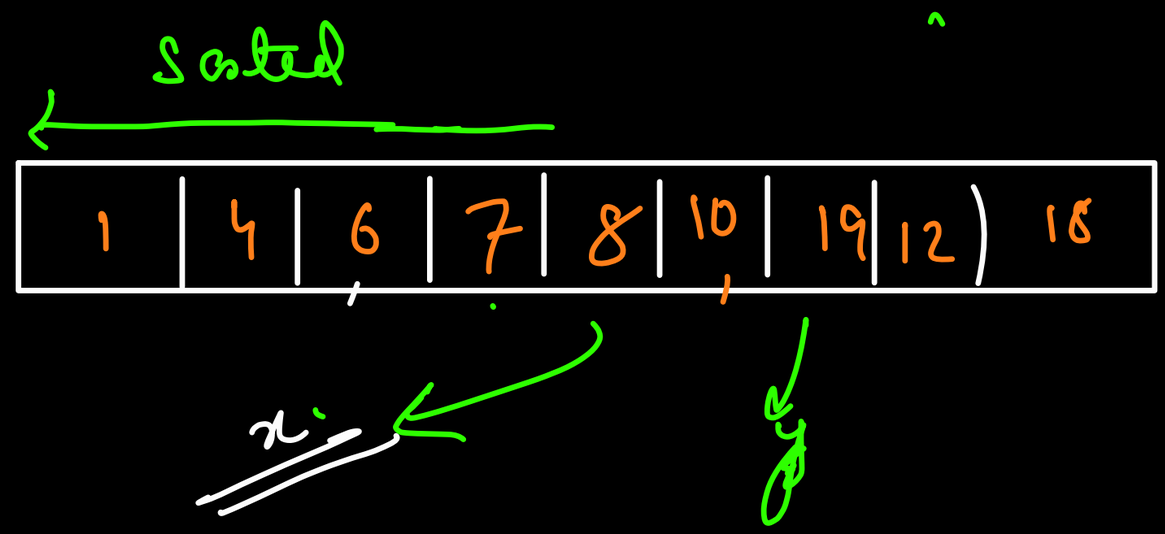
y is the min element of unsorted region.

Condition 1 → Array is divided into 2 parts where first half is perfectly sorted & the second half is unsorted.

Condition 2 → the last element of sorted region (x) is less than or equal to the minimum element of the unsorted region:

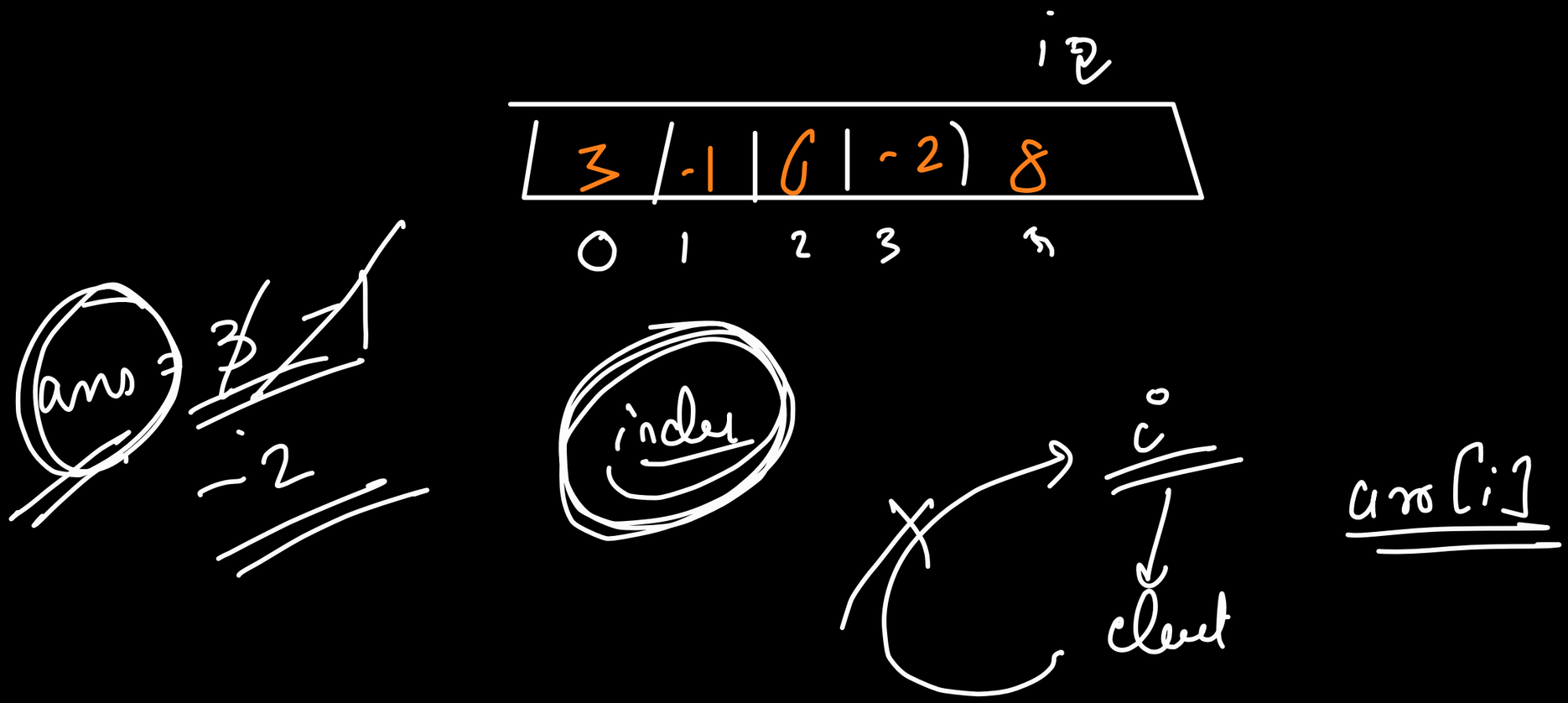
$$x <= y$$

Q → how can we expand the sorted region:



⇒ if $x <= y$ and x is the largest element of Sorted region & y is the Smallest element of unsorted region & $x <= y$.

then we can arrange y just after x.



i

→ unsorted
→ sorted

-1	1	2	3	15	6	10
0	1	2	3	4	5	6

n = 7

i

n

j

min_index = 4

i = 0

[i, n-1]

unsorted region

i → sorted

Swap → min_index , i

j ∈ [i+1, n-1]

↳ thus j goes from i to n-1 & get the min,

In every iteration, we will scan the whole unsorted region & get the index of min element

```
function getMinIndex(arr, i) {
    // this function returns the index of the minimum element in the range [i, n-1]
    let minIndex = i; // we assume first element of the range as the minimum element candidate
    for(let j = i + 1; j < arr.length; j++) {
        // we go in the reminaing array form [i+1, n-1]
        if(arr[j] < arr[minIndex]) {
            // if the current element at the index j is less than our current minimum candidatw
            minIndex = j;
        }
    }
    return minIndex;
}

function selectionSort(arr) { // we assume array is integer array
    for(let i = 0; i < arr.length; i++) {
        // [i, n-1] -> unsorted region
        let minIndex = getMinIndex(arr, i);
        // swap the ith element with min index
        if(i != minIndex) {
            let temp = arr[i];
            arr[i] = arr[minIndex];
            arr[minIndex] = temp;
        }
    }
}

let arr = [1,2,3,4,5];
selectionSort(arr);
console.log(arr);
```

```javascript
function getMinIndex(arr, i) {
    // this function returns the index of the minimum element in the range [i, n-1]
    let minIndex = i; // we assume first element of the range as the minimum element candidate
    for(let j = i + 1; j < arr.length; j++) {
        // we go in the reminaing array form [i+1, n-1]
        if(arr[j] < arr[minIndex]) {
            // if the current element at the index j is less than our current minimum candidatw
            minIndex = j;
        }
    }
    return minIndex;
}

function selectionSort(arr) { // we assume array is integer array
    for(let i = 0; i < arr.length; i++) {
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        let minIndex = getMinIndex(arr, i);
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        if(i != minIndex) {
            let temp = arr[i];
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        }
    }
}

let arr = [1,2,3,4,5];
selectionSort(arr);
console.log(arr);
```

$$(n-1) + (n-2) + (n-3) \ldots\ldots\ldots + 2 + 1$$

$$\Downarrow$$

$$\frac{n(n-1)}{2} \rightarrow \frac{n^2}{2} - \frac{n}{2}$$

$\frac{n^2}{2}$ → x

$\frac{n}{2}$ → x

lower degree term

$$O(n^2)$$

Space → O(1)

Worst time → $O(n^2)$

Best time → $O(n^2)$

Avg → $O(n^2)$

Comparison

is Inplace ??

↓

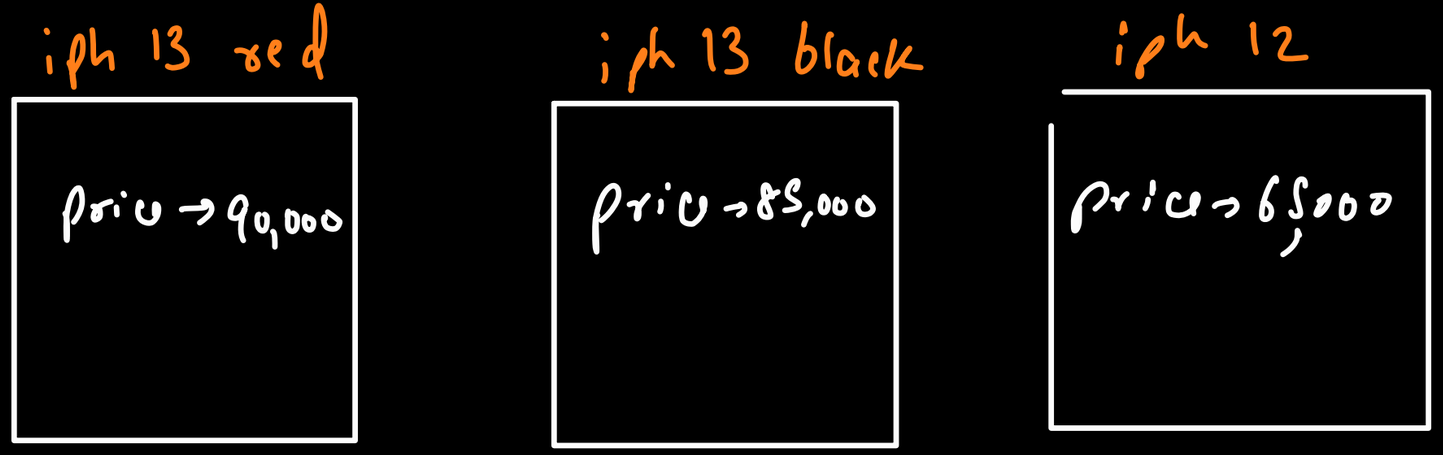
Yes

In selection sort Swapping happens → at max approx n times → O(n)

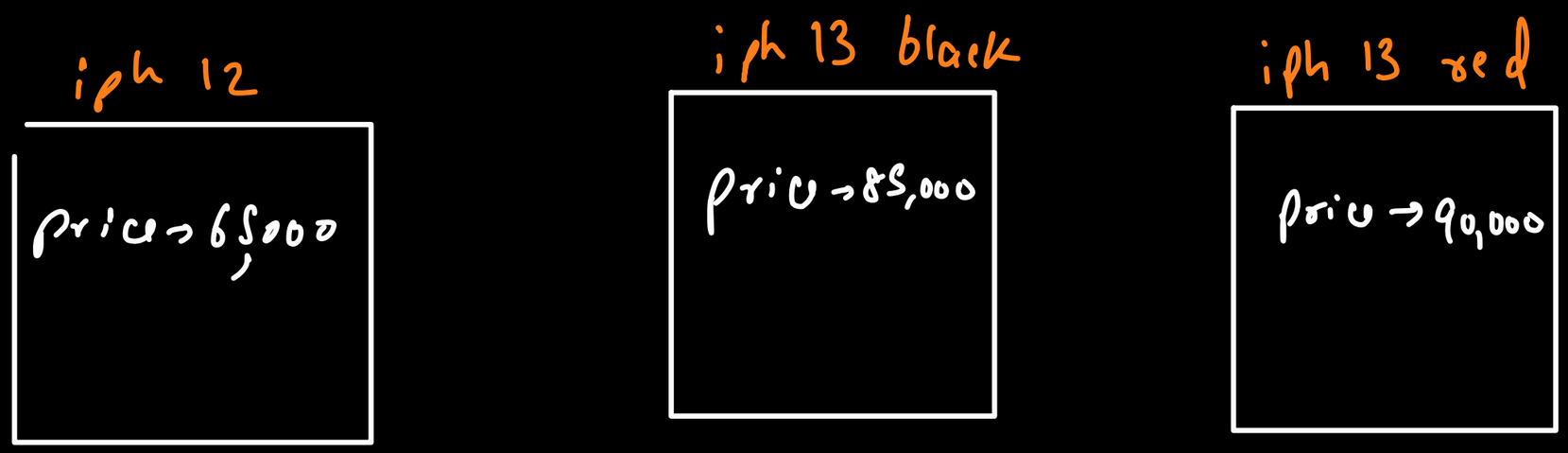
Comparisons → $O(n^2)$

Inplace → An algo is considered inplace if they donot depend on extra data structure for modifying data & implementing the algo.

Stability of the sorting algo



→ Sort it based on price in inc order



Rank → 4.7 | 4.6 | 4.5

input

iph 13 red
price → 90,000

iph 13 black
price - 90000

iph 12
price → 65000

1st possibility →

4.5
iph 12
price → 65000

4.7
iph 13 red
price → 90,000

4.6
iph 13 black
price → 90000

→ stable sort arrayment

2nd possibility

iph 12
price → 65000

iph 13 black
price → 90000

iph 13 red
price → 90,000

→ unstable sort

1) You went to amazon

2) You first sort the products by rating

3) Reordered the products based on price

Stable sort → after a stable sort the data which has the same value retains the same relative order as it was before sorting

HW → Is selection sort stable ??