

Network Science

Yadder Aceituno

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The bridges of Königsberg:

Can I have a path that crosses each bridge exactly once? The answer is no.

Computational Social Science:

Interdisciplinary field that uses computational methods to study social systems.

- How to connect nodes - Nodes have attributes - Quantity attached to an edge is a weight

If chatgpt can create synthetic data, how to measure how good is.

A network is a graph. Network science is data driven. Networks are collections of vertices joined by edges. Vertices are nodes. Edges are links. They can be referred to as ties, bonds, connections, interactions.

A graph

$$G = (V, E)$$

where

$$V$$

is the set of vertices and

$$E$$

is the set of edges. Each edge

$$e \in E$$

is a tuple

$$(u, v)$$

where

$$u, v \in V$$

.

$$u$$

and

$$v$$

are the endpoints of the edge and are said to be adjacent.

The maximum number of edges in a graph is

$$|E| = \binom{|V|}{2}$$

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Lecture 2

How do we represent a graph?

- Visual - Adjacency matrix - Edge List (This is most common in projects)

Types of networks:

- Undirected, simple - Directed: also called - Network with self-edges - Multiedges - Weighted graphs - Hypergraphs - Trees - Bipartite networks - Planar networks

There are two types of transformation from Undirected to Directed:

- Co-citation networks - Bibliographic coupling networks

Degree of a node: number of edges incident to it.

Regular graph: all nodes have the same degree.

Vertex degree for directed graph

Forbidden Triad

——- Lecture 5

What do we know so far?

- A network is defined by a collection of nodes and edges - There are different types of networks - There are different network models - Erdős-Rényi Random graph - Barabási-Albert model - Watts-Strogatz model - We have some network metrics for the nodes - Clustering Coefficient - Node Degree - We have some network metrics for the network - Average Path Length - Average Shortest Path Length - Avg Clustering Coefficient - Density - Singleton - Degree Distribution - Diameter: Largest shortest path length - How do we compare nodes? - Clustering Coefficient - Node Degree - Node Betweenness Centrality

Betweenness Centrality: Extent that a node lies on the shortest path between other nodes.

$$X_i = \sum_{s \neq i \neq t} \frac{\sigma_{st}(i)}{\sigma_{st}}$$

Degree Centrality: The importance of a node is a function of the importance of its neighbors.

Katz Centrality:

$$X_i = \sum_{j \in N(i)} X_j$$

Page Rank

Closeness Centrality:

$$X_i = \frac{1}{\sum_{j \in N(i)} d_{ij}}$$

Similarity - Structural equivalence: nodes sharing same neighbors - Regular equivalence: nodes sharing neighbors that are similar